# Equity and Currency markets review: Section 8

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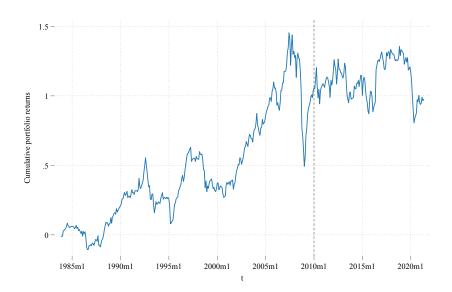
2.

- a.  $P_{new} = P_5 P_1$ .  $P_5$  currencies with  $\uparrow$  interest rates (largest forward discounts).  $P_1$  currencies with low interest rates.
- b. Negative relationship between carry trade returns and equity volatility.
- c. Recall  $P_{new}$  is a portfolio of 15 developed countries: Australia, Belgium, Canada, Denmark, euro area, France, Germany, Italy, Japan, Netherlands, New Zealand, Norway, Sweden, Switzerland, and the United Kingdom.

This particular  $P_{new}$  strategy has not performed well 2010 even though average equity volatility about the same pre vs. post-2010. Interest rates in developed countries fell since pre-Great Recession (e.g.

Australia

https://tradingeconomics.com/australia/interest-rate).



3.

1. PPP spot rate

$$S_t^{PPP} = \frac{cpi_t^{c1}}{cpi_t^{c2}}$$

2. Real exchange rate

$$q_t = \frac{\frac{1+\pi^{c1}}{1+\pi^{c2}}}{1+e_t} = \frac{\frac{1+\frac{cpi_{t+1}^{c1}-cpi_t^{c1}}{cpi_t^{c1}}}{1+\frac{cpi_{t+1}^{c2}-cpi_t^{c2}}{cpi_t^{c2}}}}{1+\frac{S_{t+1}-S_t}{S_{\star}}}$$

3. Did you observe mean reversion to 1?

### Exam

- 24 hour take-home exam.
- Start: Wednesday, October 6 at 7am PT.
- End: Thursday, October 7 at 7am PT.
- THIS IS A HARD DEADLINE.
- Submit your exam early. Email exam to me if you have submission issues.
- Submission issues are not a valid excuse for late exam submission.
- Exam should take around 5 hours.
- Equity and currency: review materials and homework make sure you understand the assignments.



### Mean-variance preferences

- We want to maximize active returns while minimizing risk.
- $U_P = \alpha_P \lambda \cdot \omega_P^2 = h'_{PA} \cdot \alpha \lambda \cdot h'_{PA} \cdot V \cdot h_{PA}$ 
  - Recall that we pretend we are institutional *equity* managers and ignore  $\beta \neq 1$ .
  - $(\beta_P 1) \cdot E[r_B] \lambda' \cdot (\beta_P 1)^2 \cdot \sigma_B^2$  cancels out.
- Solving the maximization problem yields the optimal holdings:

$$\frac{\partial U}{\partial h'_{PA}} = \alpha - 2\lambda V h_{PA} = 0$$

$$\Rightarrow h^*_{PA} = \frac{\alpha}{2\lambda V}$$

- We can also add other constraints such as requiring fully-invested portfolios (see Pset 1.6).
- Fully-invested minimum variance portfolio:  $h_C = \frac{V^{-1}e}{e^{\top}V^{-1}e}$ .



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#### Covariance matrices

• 
$$V = Cov(r, r)$$
,  $\hat{\sigma}_{ij} = \frac{1}{T-1} \sum_{t=1}^{T} \left[ r_i(t) - \bar{r}_i \right] \cdot \left[ r_j(t) - \bar{r}_j \right]$ 

$$V = \begin{pmatrix} \sigma_1^2 & \sigma_{12} & \cdots & \sigma_{1N} \\ \sigma_{21} & \sigma_2^2 & \cdots & \sigma_{2N} \\ \vdots & & \ddots & \vdots \\ \sigma_{N1} & & & \sigma_N^2 \end{pmatrix}$$

Estimating V with exponential smoothing

$$V_{ij} = \frac{\sum_{t=1}^{T} \left[ r_i(t) - \overline{r}_i \right] \cdot \left[ r_j(t) - \overline{r}_j \right] \cdot e^{-\gamma(T-t)}}{\sum_{t=1}^{T} e^{-\gamma(T-t)}}$$

•  $\sigma_P^2 = h_P^\top \cdot V \cdot h_P$ 



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### The Fundamental Law of Active Management

- FLoAM IR depends on "skill" and breadth (independent bets per period).
- Ex ante:  $IR = IC\sqrt{BR}$ .
- With transfer costs:  $IR = IC\sqrt{BR}TC$ .
- Multiple ICs:  $IR_P^2 = \sum_{i \in P} BR_i \cdot IC_i^2$ .

This is the one thing you should remember from our equity class if you can only remember one thing!

In general, a factor model represents excess returns as

- $\bullet$  r = Xb + u
  - $X_{N \times K}$  stock exposures to the factors.
  - $b_{K\times 1}$  vector of factor returns.
  - $u_{K\times 1}$  specific return vector.

With asset covariance matrix

- $V = Cov(r, r) = XFX^{T} + \Delta$ 
  - $F_{K \times K}$  The covariance of factors
  - $\Delta_{N \times N}$  Diagonal covariance matrix of "specific risk".



#### More on factor models

• Fundamental models – "Calculate X, estimate b"

• 
$$b = \underbrace{(X^{\mathsf{T}}X)^{-1}X^{\mathsf{T}}}_{H^{\mathsf{T}}} r$$

- *H* is the factor-mimicking portfolio.
- The columns of *H* correspond to portfolio weights for each factor.
- What if we had b and were interested X?

$$r_n(t) = \sum_{k=1}^K b_k(t) \cdot X_{nk} + \varepsilon_n(t)$$



- We estimate covariance matrix using observed historical data.
- But we can use the estimated covariance matrix for (hopefully) good beta forecasts.
- Barr's better betas:

$$\beta_P = \frac{h_P^\top \cdot V \cdot h_B}{\sigma_B^2} = h_P^\top \cdot \beta$$
$$\beta = \frac{V \cdot h_B}{\sigma_B^2}$$
$$\sigma_B^2 = h_B^\top \cdot V \cdot h_B$$

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#### Valuation

Dividend discount model – there is uncertainty

$$\rho(0) = \sum_{t} \frac{E[d(t)]}{(1+y)^{t}}$$
 (1)

Constant-growth dividend discount model – assume a growth rate

$$d(t) = d(1) \cdot (1+g)^{t-1} \tag{2}$$

• Eq. (1) + Eq. (2)  $\Rightarrow$ 

$$p(0) = \frac{d(1)}{y - g}$$

• Constant dividends and discount rate imply total return is

$$y = \frac{p(1) - p(0) + d(1)}{p(0)}$$



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### More valuation equations

$$e(t) = d(t) + I(t)$$

• 
$$d(t) = \kappa \cdot e(t)$$

• 
$$\Rightarrow I(t) = (1 - \kappa) \cdot e(t)$$

• 
$$e(t+1) = e(t) + ROE \cdot I(t) = (1 + ROE \cdot (1 - \kappa)) \cdot e(t)$$

• 
$$\Rightarrow$$
  $g = ROE \cdot (1 - \kappa)$ 

• 
$$y = i_f + \beta f_B + \alpha$$

• 
$$+CGDDM \Rightarrow g = \alpha + \beta f_B + i_f - \frac{d}{P}$$

• Observe 
$$p_{mkt}$$
 and estimate:  $p_{model}(t) = \frac{\kappa \cdot e(t+1)}{y-g}$ 

• Multiples: 
$$m_{mkt} = \frac{p_{mkt}}{e}$$
,  $m_{model} = \frac{\kappa}{y-g}$ 

• Relative mispricing: 
$$rmp = \frac{p_{model}}{p_{mkt}} - 1 = \frac{m_{model}}{m_{mkt}} - 1$$



### Market impact model

• Price impact proportional to volatility &  $\sqrt{\text{volume}}$ 

$$\bullet \ \frac{\Delta p}{p} = c \cdot \sigma \cdot \sqrt{\frac{V}{\bar{V}_{daily}}}$$

Overall cost:

• Cost = commission 
$$+ \frac{\mathsf{spread}}{p} + c \cdot \sigma \cdot \sqrt{\frac{V_{trade}}{\bar{V}_{daily}}}$$

• Cost-aware portfolio construction:

$$U = h_{PA}^{\mathsf{T}} \cdot \alpha - \lambda h_{PA}^{\mathsf{T}} \cdot V \cdot h_{PA} - \frac{Cost\{h_i, h\}}{\tau_h}$$

• where  $\tau_h$  is the transactions cost amortization horizon



### $\alpha$ dynamics

Information decay at equilibrium

$$\alpha(t) = e^{-\gamma \cdot \Delta t} \cdot \alpha(t - \Delta t) + \tilde{s}(t) \cdot \sqrt{\Delta t}$$

- ullet  $\gamma$  guides turnover or decay rate of old information.
- ullet  $\gamma$  is closely related to half life of alpha information.

$$e^{-\gamma \cdot \Delta t} \equiv \frac{1}{2}^{\Delta t/HL}$$

• In equilibrium,  $BR = \gamma \cdot N$ .



### Covered Interest Parity

$$(1+i_{\S})=\frac{F}{S}(1+i_{*})$$

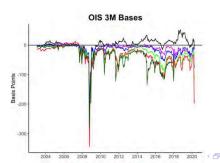
- Interest rate difference should equal the difference between forward and spot exchange rates.
- $F_{0,1}$  = Today's 1-period forward rate in \$/\*.
- Approximate version:  $i_{\$} i_{*} = \frac{F_{0,1} S_{0}}{S_{0}} \left(1 + i_{*}\right) \approx \frac{F_{0,1} S_{0}}{S_{0}}.$
- % forward discount on the \$ is approximately  $\frac{F_{0,1}-S_0}{S_0}$ .
  - If  $> 0 \Rightarrow \$$  at forward discount.
  - If  $< 0 \Rightarrow$ \$ at forward premium.
- This is an arbitrage condition.



When CIP holds (ignoring any adjustments),

$$B_{t} = \overbrace{i_{t}^{\$}}^{\text{cash}} - \underbrace{\left[\frac{F_{t}}{S_{t}}(1 + i_{t}^{*}) - 1\right]}_{\text{synthetic}} = 0$$

 $\bullet$   $B_t$  is the cross-currency basis.



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- Gordon Liao (2020) "Credit migration and covered interest rate parity"
  - Credit spread is lower in Europe ⇒ ↑ demand to borrow in €
  - $\uparrow \in$  borrowing  $\Rightarrow \uparrow$  demand for currency hedge
  - ⇒ ↑ balance sheet of forward contract issuers
  - ⇒ more costly to swap to \$.
- Other potential candidates that affect cross-currency basis:
  - Demand for credit borrowing (corporate demand for currencies).
  - Demand for swaps.

### Purchasing Power Parity

- $P_{\$}$  = US prices in USD.
- $P_*$  = Country \* prices in \* currency.
- Absolute version of PPP

$$S = \frac{P_\$}{P_*}$$

- $S_{t+1} S_t > 0$ 
  - $\Rightarrow$  \$ depreciation (because you need more \$ to pay for a unit of \*)
- Condition relies on Law of One Price.
  - Applied internationally to a standard consumption basket.



Relative PPP and the real exchange rate

$$e = \frac{\pi_{\$} - \pi_{*}}{1 + \pi_{*}} \approx \pi_{\$} - \pi_{*}$$

- $\bullet$  e > 0
  - ⇒ \$ depreciation (because you need more \$ to pay for a unit of \*)
  - $\Rightarrow$  positive inflation difference  $(\pi_{\$} \pi_{*})$  to keep exchange rate constant on PPP
- In expectation,

$$E\left[\pi_{\$}-\pi_{*}\right]\approx\frac{E_{t}\left[S_{t+1}\right]-S_{t}}{S_{t}}.$$

• We define the real exchange rate as

$$q = \frac{1 + \pi_{\$}}{(1 + e)(1 + \pi_{*})} = \frac{\frac{1 + \pi_{\$}}{1 + \pi_{*}}}{1 + e}.$$



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### Uncovered Interest Parity

- If there exists an interest rate difference in an efficient market, the currency that has a higher interest rate is expected to give it back.
- Approximately,

$$i_{\$}-i_{*}\approx \frac{E_{t}\left[S_{t+1}\right]-S_{t}}{S_{t}}=E[e].$$

- If the interest rate difference is negative,  $S_{t+1}$  is expected to decrease meaning that it takes fewer \$ to buy \* or the \$ is expected to appreciate.
- This is an equilibrium condition.
  - Relies on the assumption that capital markets are efficient.
  - If not true, interest rates may be set inefficiently.



### Reasons to peg to a currency?

- It becomes a nominal anchor.
- If country has high inflation, pegging currency slows down inflation.
  - As long as you can keep the peg!

### Impossible trinity

- Fixed exchange rate
- Free/flexible monetary policy
- Free capital flow (no controls)

### Signals of a currency crisis.

- Deviations in real exchange rate.
- Long, consistent trade deficits signal a looming currency crisis.
  - Current account and capital account have to balance.
- Borrowing from foreign entities with short maturities.
- Borrowing to finance public budget deficits.
- Difficult to predict the timing.

#### Triffen dilemma

- Triffen paradox: countries with reserve currencies run a balance of payments deficit
  - $\Rightarrow$  long-term balance of payments deficit lowers confidence in reserve currency
  - ⇒ downfall of reserve currency
- Modern Triffin dilemma: Demand for US dollar assets will outstrip US fiscal capacity.
  - Farhi, Gourinchas, Rey (2011); Obstfeld (2013); Farhi and Maggiori (2018).

#### Order flow matters

- Transactions are buys or sells.
- Aggregating player transactions gives big picture view of the market.
  - Implicit information.
- Learning through order flow is important.
- Aggregate order flows are highly correlated with changes in exchange rates.
  - They also explain a lot of these changes (something macro fundamentals tend to fail to do) – Evans-Lyons model.

### The end

