

Coursera Statistical Inference Project Part 1

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Synopsis

This is the project for the statistical inference coursera data science specialization class. This project consists of two parts :

- A simulation exercise.
- Basic inferential data analysis.

Task

The exponential distribution can be simulated in R with `rexp(n, lambda)` where `lambda` is the rate parameter. The mean of exponential distribution is $1/\lambda$ and the standard deviation is also $1/\lambda$. Set $\lambda = 0.2$ for all of the simulations. In this simulation, you will investigate the distribution of averages of 40 exponential(0.2)s. Note that you will need to do a thousand or so simulated averages of 40 exponentials.

```
# set seed for reproducibility
set.seed(31)

# set lambda to 0.2
lambda <- 0.2

# 40 samples
n <- 40

# 1000 simulations
simulations <- 1000

# simulate
simulated_exponentials <- replicate(simulations, rexp(n, lambda))

# calculate mean of exponentials
means_exponentials <- apply(simulated_exponentials, 2, mean)
```

Illustrate via simulation and associated explanatory text the properties of the distribution of the mean of 40 exponential(0.2)s. You should:

Question 1

Show where the distribution is centered at and compare it to the theoretical center of the distribution.

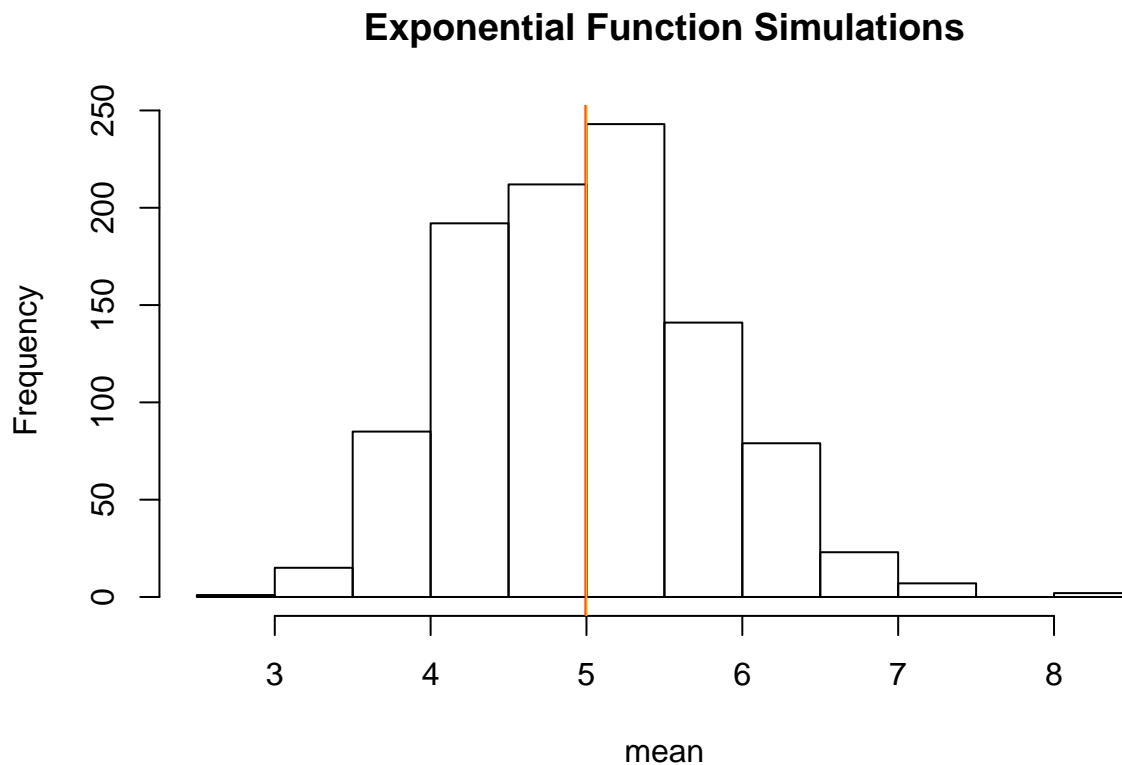
```
# distribution mean
analytical_mean <- mean(means_exponentials)
analytical_mean
```

```
## [1] 4.993867
```

```
# analytical mean  
theory_mean <- 1/lambda  
theory_mean
```

```
## [1] 5
```

```
# visualization  
hist(means_exponentials, xlab = "mean", main = "Exponential Function Simulations")  
abline(v = analytical_mean, col = "red")  
abline(v = theory_mean, col = "orange")
```



The analytics mean is 4.993867 the theoretical mean 5. The center of distribution of averages of 40 exponentials is very close to the theoretical center of the distribution.

Question 2

Show how variable it is and compare it to the theoretical variance of the distribution.

```
# standard deviation of distribution  
standard_deviation_dist <- sd(means_exponentials)  
standard_deviation_dist
```

```
## [1] 0.7931608
```

```
# standard deviation from analytical expression  
standard_deviation_theory <- (1/lambda)/sqrt(n)  
standard_deviation_theory
```

```
## [1] 0.7905694
```

```
# variance of distribution  
variance_dist <- standard_deviation_dist^2  
variance_dist
```

```
## [1] 0.6291041
```

```
# variance from analytical expression  
variance_theory <- ((1/lambda)*(1/sqrt(n)))^2  
variance_theory
```

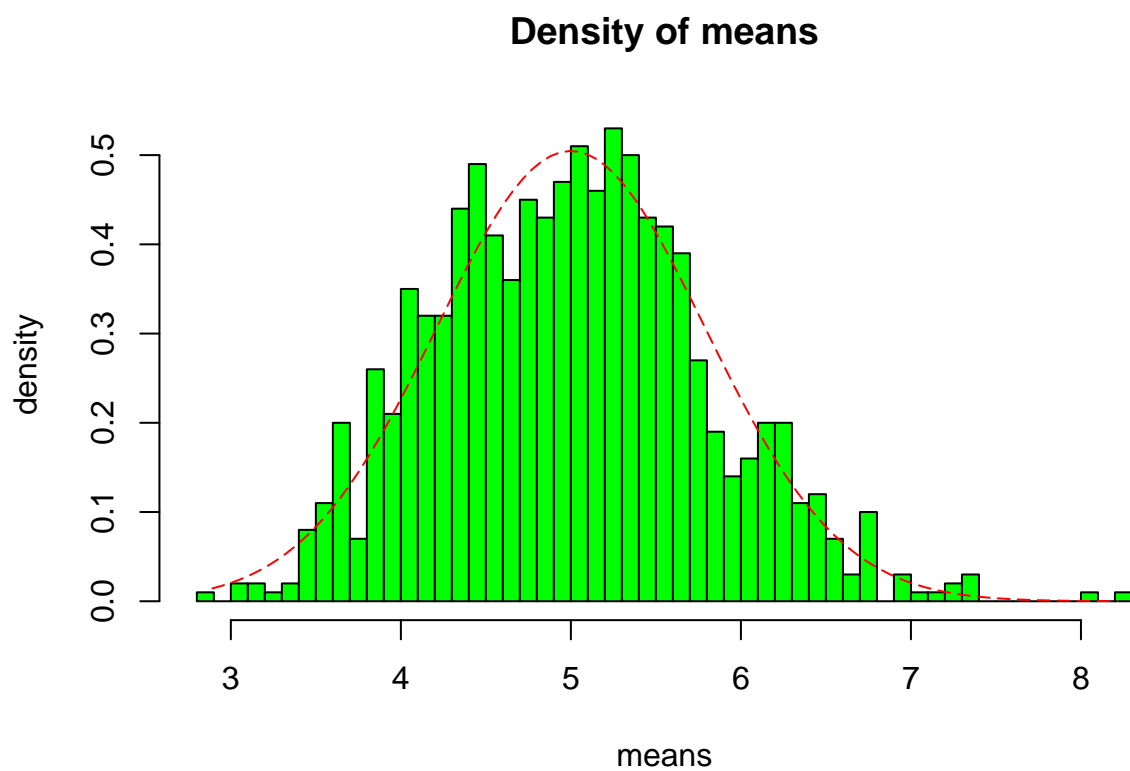
```
## [1] 0.625
```

Standard Deviation of the distribution is 0.7931608 with the theoretical SD calculated as 0.7905694. The Theoretical variance is calculated as 0.625. The actual variance of the distribution is 0.6291041

Question3

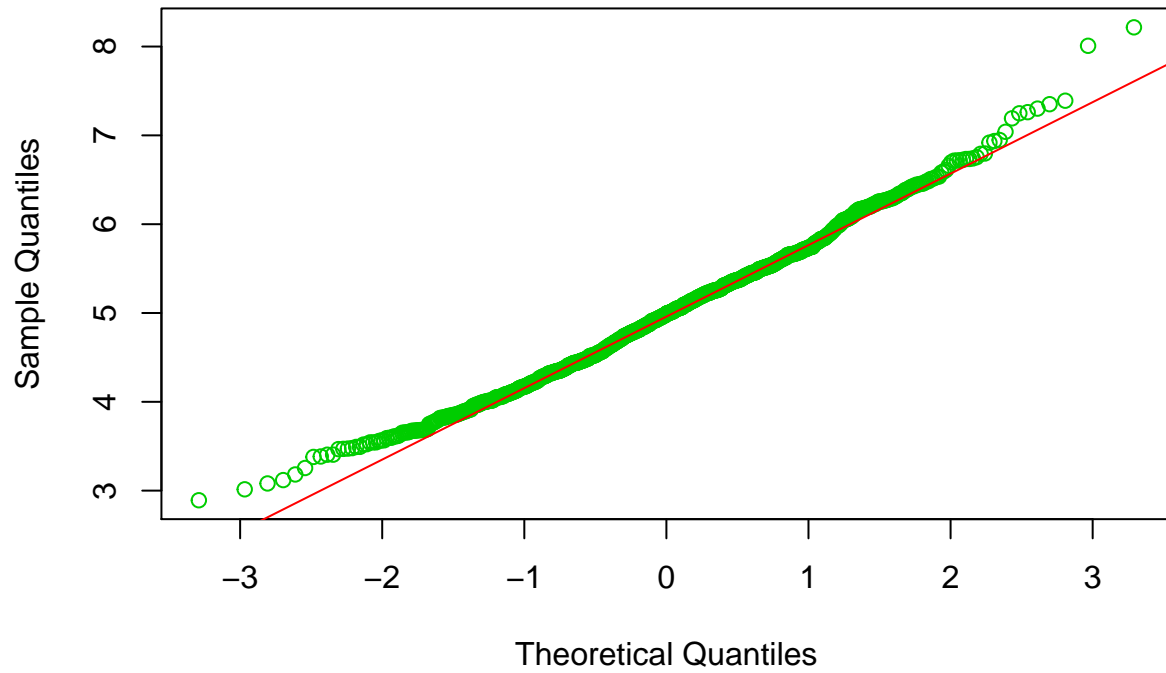
Show that the distribution is approximately normal.

```
xfit <- seq(min(means_exponentials), max(means_exponentials), length=100)  
yfit <- dnorm(xfit, mean=1/lambda, sd=(1/lambda/sqrt(n)))  
hist(means_exponentials,breaks=n,prob=T,col="green",xlab = "means",main="Density of means",ylab="density")  
lines(xfit, yfit, pch=22, col="red", lty=5)
```



```
# compare the distribution of averages of 40 exponentials to a normal distribution  
qqnorm(means_exponentials,col=3)  
qqline(means_exponentials, col = 2)
```

Normal Q-Q Plot



Due to the central limit theorem (CLT), the distribution of averages of 40 exponentials is very close to a normal distribution.