

Blackman $\rightarrow 0.42 - 0.5 \cos\left(\frac{2\pi n}{m-1}\right) + 0.08 \cos\left(\frac{4\pi n}{m-1}\right)$

Hamming $\rightarrow 0.54 - 0.46 \cos\left(\frac{2\pi n}{m-1}\right)$

$|H(\omega)|^2 = H(\omega) H^*(\omega)$

$H(z) = b_0(1 - z_1 z^{-1})(1 - z_2 z^{-1})$

1 complex multiplication = 2 real multiplications per butterfly

DSP-2018
QuizSet-3A
Date: 22/11/2018
Time : 50 minutes
Marks: 20

Rate
no. of butterfly $\rightarrow \frac{N}{2}$
 $\rightarrow \frac{N}{2}$
 $\rightarrow 2\left(\frac{N}{2}\right)$

Question 1: Do the following.

- 1) State True or False: Fourier transform of any sequence is same as it's Z transform evaluated on the unit circle. [1]
- 2) A transfer function with a double zero located at same frequency is linear phase system. [1]
- 3) Write down the window function for hamming window. [1]
- 4) State True or False: The phase of the LTI system should be constant to guarantee linear phase of the system. [1]
- 5) Any sequence $x(n)$ is related to it's odd and even sequence as $x(n) = \frac{x_e(n) + x_o(n)}{2}$. [1]
- 6) If $|H(\omega)|^2 = H(\omega) \cdot H^*(\omega)$ and also $H(\omega) = H(z)|_{z=e^{j\omega}}$ then $|H(\omega)|^2 = H(z) \cdot H^*(z^{-1})$ is true. [1]

[P.T.O.]

DSP- 2018
Lab exam #5

1406C126

DSP-2018
QuizSet-2B
Date: 31/10/2018
Time : 60 minutes
Marks: 30

Question 1: Do the following.

- 1) Mention the number of complex multiplications needed for N point DFT using Radix-2 algorithms. [1]
- 2) Mention the number of real additions required by Radix-2 and Radix-4 butterfly respectively. [1]
- 3) Write down the expression for Forward DCT. [1]
- 4) State True or False: In radix-2 Decimation in time the input signal is applied in Bit reverse order and output is in natural order. [1]
- 5) For a circularly even symmetric sequence $x(n)$ having length $N = 4$, the sample $x\left(\frac{N-1}{2}\right)$ is equal to _____. [1]
- 6) In split radix, the even frequency components are calculated using _____ algorithm. [P.T.O]

DSP- 2018
Problem Set #1B
Roll No:

Time :50 Minutes

Weightage : 20 Marks[4 Marks each]

- 1) For a signal $x_a(n) = \cos(\frac{\pi}{3}n)$
calculate the magnitude and phase spectrum. Comment on symmetries of both the spectrums.
- 2) Write down the Analysis and synthesis expression for Discrete time aperiodic signal.
The corresponding spectrum is _____ and _____.
- 3) Use DFT expression and write down the IDFT Matrix for $N = 4$ point.(No Zero padding)
- 4) For $N = 128$, calculate the no. of complex multiplications and additions required using
 - Using Direct method.
 - Using division $L = 64$, $M = 2$, where $N = L \cdot M$.
 - Can the multiplications reduces further compared to above step if we further divide the above $L = L_1 \cdot L_2$, where $L_1 = 32$, $L_2 = 2$ and keep same $M = 2$. Write down the no. of Complex multiplications required for this case.
- 5) Derive the symmetry property(Magnitude only) of fourier transform if discrete signal $x(n)$ is real.

The LNM-IIT, Jaipur, Rajasthan

16vec126

Instructions to students
1. This question paper is printed on both side of the paper.
2. Use of calculator is not permitted.
3. Organize your answers clearly.
4. Master algebra.

- 1) Take random integer sequences $x(n)$ of length N . (Make separate files for each part)
 - a) Generate 2-point FFT using DIF-radix-2 for $N = 2$. [2]
 - b) Generate 4-Point FFT using DIF-radix-2 for the above sequence with $N = 4$. [2]
 - c) Generate 8-Point FFT using DIF-radix-2 for the sequence with $N = 8$. [4]
 - d) Calculate the complexity in terms of complex multiplications using some count variable for step a and b. [2]
 - e) Use simulink to simulate 4 point FFT of sequence $[6, 6, -6, -6]$. [2]

- 1) A signal $x(t) = 2 \sin(2\pi 6000t)$,
is sampled at $F_{s1} = 6e6$ to generate the ideal signal $x(n)$.
- a) Generate a discrete time signal by sampling the above signal $x(t)$ with sampling rate $F_{s2} = 24000$ Hz and display first 5 cycles. [2]
- b) Generate a discrete time signal by sampling the above signal $x(t)$ with sampling rates $F_{s3} = 8000$ and display first 3 cycles. Display spectrum using inbuilt fft for current and above step. [2]
- c) Generate a discrete time signal by sampling the above signal $x(t)$ with sampling rates $F_{s3} = 12000$, $F_{s4} = 600000$ Hz. Use linear interpolation to make all signals of equal length as ideal $x(n)$. [4]
- d) Find and plot MSE for both the above cases. [2]
- e) Use simulink to generate nearest neighbourhood interpolation to make the sampled signal at $F_{s2} = 24000$ of same length as $x(n)$. [2]

1) Convolution : (Make separate files for each code:).

- a) Generate the circular convolution matrix and hence circular convolution output $y(n)$ for two random integer sequences $x(n)$ and $h(n)$ with lengths 6 and 5 respectively. [2]
- b) Generate DFT matrix of appropriate size using myDFT function. [2]
- c) Prove circular convolution in time domain is Fourier transform pair with DFT multiplication of $x(n)$ and $h(n)$. [4]
- d) Show linear convolution and circular convolution matches by appropriate method. [2]
- e) Use simulink to circularly convolve two sequences taken from command window. [2]

The LNM-IIT, Jaipur, Rajasthan

The LNM Institute of Information Technology, Jaipur
Mid-Term Examination, Spring Semester (2018-19)
Digital Signal Processing (ECE 326)

Time: 90 Min.

M.M.: 35

Instructions to students

1. This question paper is printed on both side of the paper and have 4 questions. All questions are compulsory. Marks are indicated in parentheses.
2. Use of electronic calculators only is permitted. No extra resources viz. graph papers, log-tables, trigonometric tables would be required.
3. Organize your work, in a reasonably neat and coherent way. Work scattered all over the page or across the answer script without a clear ordering will receive very less marks.
4. Mysterious or unsupported answers will not receive full marks. A correct answer, unsupported by calculations, explanation, or algebraic work will receive no marks; an incorrect answer supported by substantially correct calculations and explanations might still receive partial marks.

1 a).

A continuous-time signal $x(t)$ is composed of a linear combination of frequencies F_1, F_2, F_3 and F_4 (all are in Hz). The signal $x(t)$ is sampled at a 8 kHz rate and the sampled signals are passed through a lowpass filter with cutoff frequency of 3.5 kHz, generating a continuous-time signal $y(t)$ composed of three sinusoidal signals of frequencies 150 Hz, 400 Hz, 925 Hz respectively. The possible values of

$$F_1 = \underline{\hspace{2cm}} F_2 = \underline{\hspace{2cm}}, F_3 = \underline{\hspace{2cm}}, \text{ and } F_4 = \underline{\hspace{2cm}}. \quad [4]$$

- b). If a 3-bit ADC channel accepts analog input ranging from -2.5 to 2.5 volts, then [5]

- (i). Find the number of quantization levels.
- (ii). Calculate the step size of the quantizer.
- (iii). Determine the quantization level when the analog voltage is -1.2 volts.
- (iv). Write the binary code produced by the ADC.

2. Determine the total response $y[n]$, $n \geq 0$ of the discrete-time system described by the second order difference equation $y[n] = 0.7y[n-1] - 0.1y[n-2] + 2x[n] - x[n-2]$, when the input sequence is $4^n u[n]$. [4]
(Hint: Using traditional method i.e. homogenous solution and particular solution)

- 3 a). The system function of a causal discrete-time LTI system H is given by $H(z) = \frac{(1-\frac{3}{2}z^{-1})(1+\frac{1}{3}z^{-1})(1+\frac{5}{3}z^{-1})}{(1-z^{-1})^2(1-\frac{1}{4}z^{-1})}$.
Give the pole-zero plot for $H(z)$ and specify the ROC. Is the system BIBO stable (YES/NO)? [4]

- b). If the input to a causal discrete-time LTI system is $x[n] = (0.5)^n u[n] - (1/4)(0.5)^{n-1} u[n-1]$ with $u[n]$ is the unit step sequence, then the output is [6]

$$y[n] = \left(\frac{1}{3}\right)^n u[n]$$

- i). Determine the system function $H(z)$ of the system.
- ii). Determine the impulse response $h[n]$ of the system.

iii). Find the step response $y[n]$ of the system.

[6]

c). Given a discrete time system H with system function

$$H(z) = \left(-\frac{2}{5}\right) \frac{\left(1 - \frac{1}{2}z^{-1}\right)^2 \left(1 - \frac{1}{4}z^{-1}\right)}{\left(1 + \frac{1}{3}z^{-1}\right) \left(1 - \frac{2}{3}z^{-1}\right) \left(1 + \frac{3}{5}z^{-1}\right)}$$

i). Find the difference equation that characterizes this system.

ii). Give the Direct form I and Direct form II realization of the system.

[6]

4. Given a discrete-time periodic signal $x[n] = \{\dots, 1, 0, 1, 2, \frac{3}{1}, 2, 1, 0, 1, \dots\}$

- Determine and sketch the magnitude and phase spectra of $x[n]$ upto five discrete-time Fourier series coefficients.
- Calculate the power using from discrete-time Fourier series coefficients.

Digital Signal Processing (ECE326)

End Term Examination

Date: 3/12/2018

Time : 180 minutes

[Marks: 50]

1) State True or False:

- a) In radix-2 Decimation in frequency algorithm, the input signal is applied in bit reverse order and output is natural order. [1]
- b) A discrete time aperiodic signal has continuous spectrum. [1]
- c) A comb filter produces multiple notches in the magnitude spectrum at random discrete frequencies. [1]
- d) The group delay of the LTI system $H(w) = e^{-j2w}$ guarantees linear phase of the system. [1]
- e) A system having impulse response $h(n) = (\frac{9}{8})^n u(n)$ fullfills the condition of absolute summability and hence the stability of the system. [1]

2) Mention the following.

- a) Mention the analysis and synthesis expression for continuous time periodic signal. [1]
- b) Let a sequence is given by $x(n) = \{2, 5, -3, 6, 7, 8, 1, -9\}$, Determine $x((-3))_N$. [1]
- c) State whether system given below is minimum phase, maximum phase or mixed phase. [1]

$$H(z) = (0.25) \left(\frac{z^{-1} + 2.5}{1 + 0.5z^{-1}} \right) \left(\frac{3.6z^{-1} + 4}{4 + z^{-1}} \right)$$

- d) Mention the paley-wiener criteria and its use for LTI system. [1]
- e) Write down the window function for hamming window. [1]

3) Do the following.

- a) Mention where the poles and/or zeros lies for Digital resonator, Notch filter, Comb Filter. [2]
- b) Mention the fourier transform pair for two sequences $x_1(n)$, $x_2(n)$ having multiplication in time domain. [2]
- c) Calculate and write IDFT matrix for $N = 3$ point. [2]
- d) Calculate No. of complex multiplications and complex additions required for N point DFT using Divide and conquer approach, where $L = 384$, $M = 4$. [2]
- e) Calculate the number of samples required of a signal $x(t) = 2 \cos(2\pi 6000t)$ for spectrum resolution of 0.3 KHz. [2]

4) Do two of the following.

- a) Derive the forward DCT expression for a discrete signal $x(n)$. [6]
Also mention the underlying DFT property for this derivation.

[P.T.O.]

b) Sampling & Quantization:

i) Derive SQNR expression for a sinusoidal periodic signal $x(t) = A \cos(2\pi ft)$. [3]

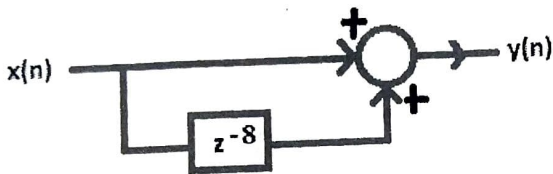
ii) Determine the resolution Δ , quantization noise and SQNR value for signal $x(t) = 1.5 \cos(2\pi(200)t)$ when 16 level quantizer is used to encode this signal. [3]

c) Calculate the complex multiplications required for $N=16$ using Radix-2 and Radix-4 algorithm. [3]

• If decimation is performed only once. [3]

• If decimation is performed $\log_r N$ times (Here r is radix). [4]

5) Let a system shown in the figure is excited with a composite signal $x(t) = \cos(2\pi(600)t) + \cos(2\pi(150)t)$ sampled at $F_s = 2400$ Hz. Calculate its response and conclude which frequency gets blocked by this system. [4]



6) Do any one of the following:

a) Filtering:

• Write down expression for $H_r(w)$ for a linear phase FIR filter which fulfills the condition $h(n) = -h(M-1-n)$, $0 \leq n \leq M-1$, where M is even. [2]

• Using above step and provided $|H_r(w = \frac{\pi}{3})| = 1$ and $|H_r(w = \pi)| = \frac{1}{\sqrt{2}}$ for $M = 4$, calculate impulse response $h(n)$ of the FIR filter. [3]

• Let two signals, the first signal $x_1(n) = \sum_{k=-\infty}^{\infty} \delta(n-k)$ and another signal $x_2(t) = \cos(2\pi(3600)t)$ which is sampled at $F_s = 21.6$ KHz is given at the input of this filter. Mention which one will get blocked at the output. why?. [1]

b) Let a transfer function is given by

$$H(z) = \frac{b_0}{1 - 1.5 \cos\left(\frac{\pi}{8}\right) z^{-1} + 0.5625 z^{-2}}$$

• Mention the type of the system and its characteristic. [1]

• Calculate value of b_0 . [2]

• Plot magnitude response at $(0, \pm \frac{\pi}{8}, \pm \pi)$. [3]

7) Perform the following.

a) Radix:

i) Derive odd frequency components for Radix-4 DIF-FFT. [2]

ii) Draw split-radix butterfly structure. [2]

iii) Calculate DFT of sequence $x(n) = \{1, 1, -1, -1, 1, 1, -1, -1\}$ using above structure. [4]

WELL DONE