

# **CSCI3170 Introduction to Database Systems**

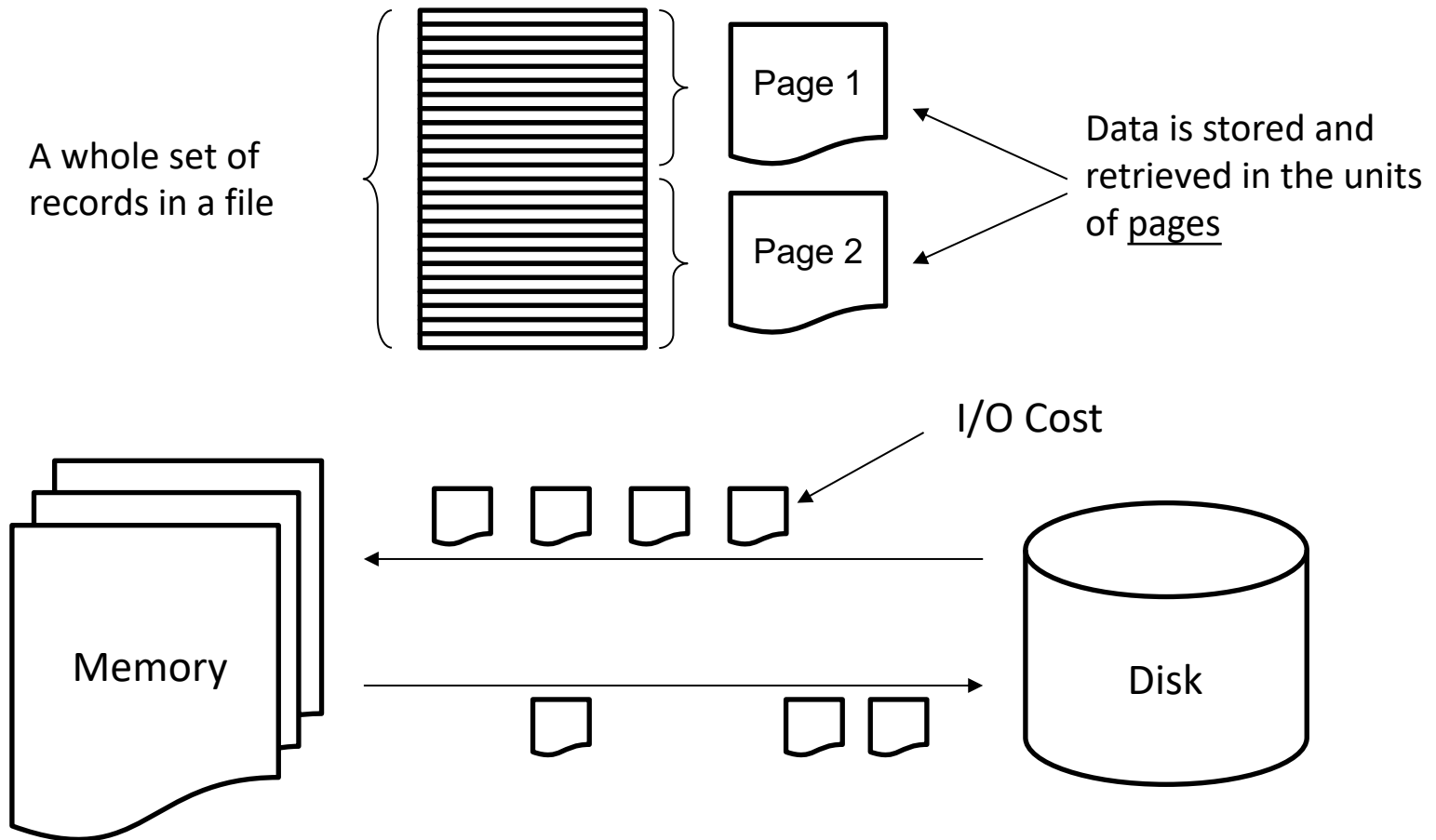
**Tutorial 9 – Storage and Indexes (2)**

# Outline

- Overview of Storage and Indexes
- Tree-structured Indexing
  - B+ Tree
- Hash-based Indexes
  - Static Hashing
  - Dynamic Hashing

# Storage

- Files and pages



# Record and Index

- Record
  - Record ID =  $\langle \text{Page ID} \rangle + \langle \text{Offset} \rangle$ 
    - E.g. Record ID:  $\langle 3 \rangle + \langle 10 \rangle$  = The 10<sup>th</sup> record in the 3<sup>rd</sup> page
- Index
  - Given a search key K, index can be used to speed up the selection of a set of particular pages.
  - A index file contains a collection of data entries.
  - The data entry of search key K is denoted as  $K^*$ .
    - $K^* = \langle K, \text{Record ID (rid)} \rangle$

# Index Classification (1)

- Primary and Secondary
  - Primary
    - Search key contains primary key.
  - Secondary
    - Otherwise

# Index Classification (2)

- Dense and Sparse
  - Dense
    - $K^*$  appear for ALL search key
  - Sparse
    - Otherwise

# Index Classification (3)

- Clustered and Unclustered
  - Clustered
    - Data entries and records are sorted by K.
    - Order of records are equal/close to the order of data entries in index.
    - Support range search.
  - Unclustered
    - Otherwise

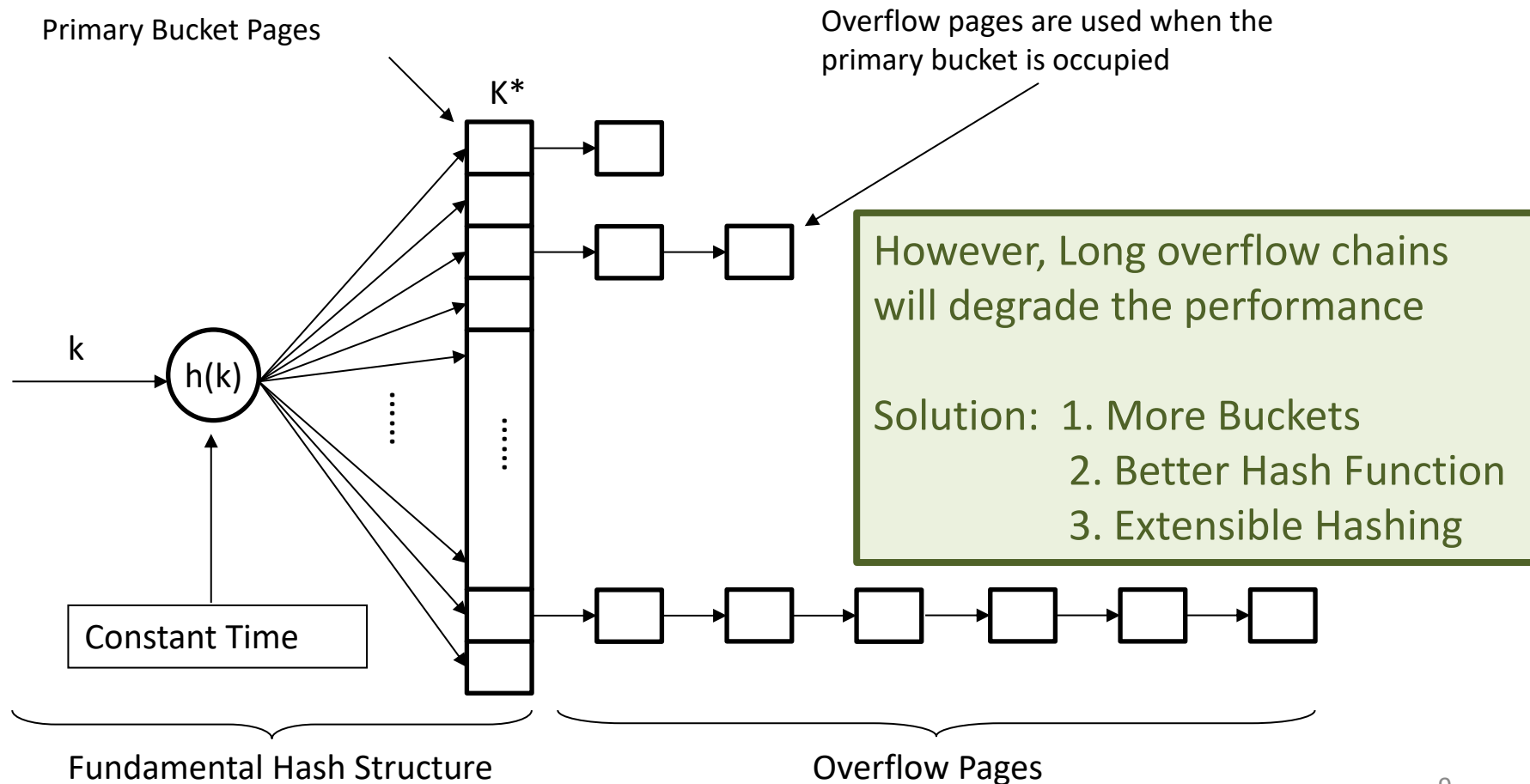
# Hashing

- Properties
  - Data entries are kept in bucket.
  - Hashing function  $h(k)$  = address of the bucket.
  - $h(k)$  should distribute  $K^*$  uniformly.
  - Best for equality selection.
  - Not support range search.
  - Constant time retrieval.



# Static Hashing

No. of primary pages fixed, allocated sequentially, never de-allocated; overflow pages if needed.

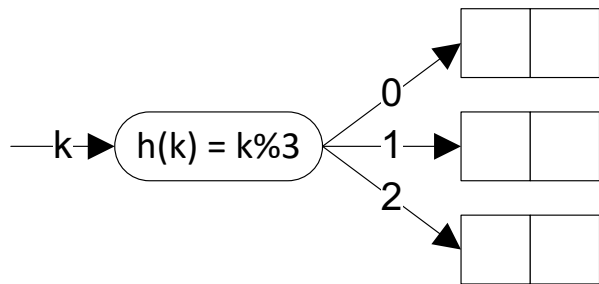


# Static Hashing: an example

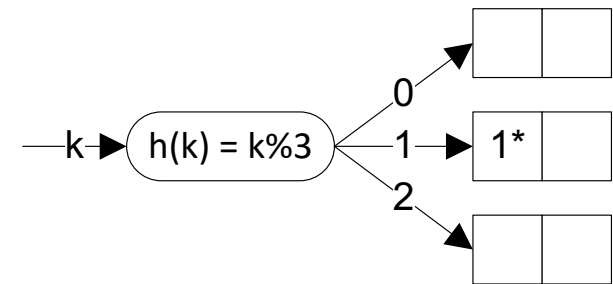
- Suppose the hash function is  $h(x) = x \bmod 3$  and a bucket can hold at most 2 data entries. Below show a static hash structure after inserting 1, 4, 5, 7, 8, 2.

$$h(1) = 1$$

Insert 1



After insert 1

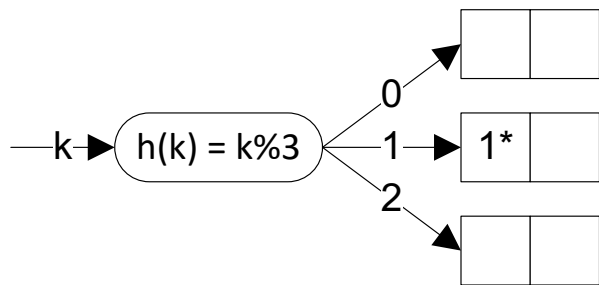


# Static Hashing: an example

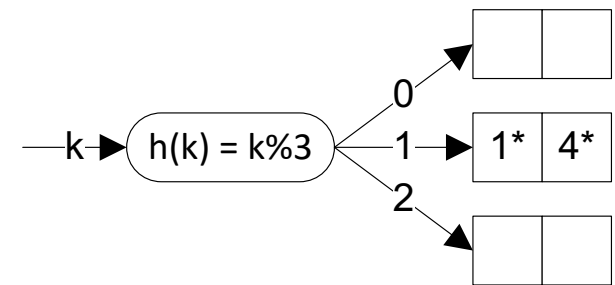
- Suppose the hash function is  $h(x) = x \bmod 3$  and a bucket can hold at most 2 data entries. Below show a static hash structure after inserting 1, 4, 5, 7, 8, 2.

$$h(4) = 1$$

Insert 4



After insert 4

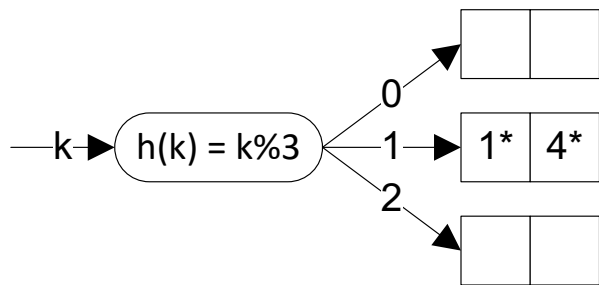


# Static Hashing: an example

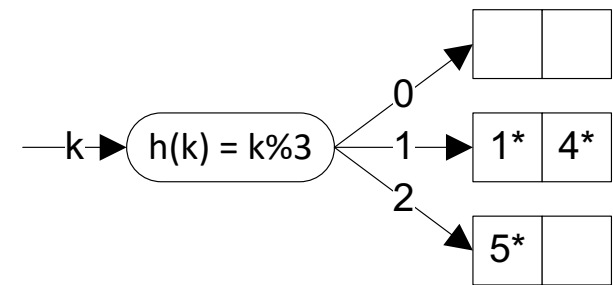
- Suppose the hash function is  $h(x) = x \bmod 3$  and a bucket can hold at most 2 data entries. Below show a static hash structure after inserting 1, 4, 5, 7, 8, 2.

$$h(5) = 2$$

Insert 5



After insert 5

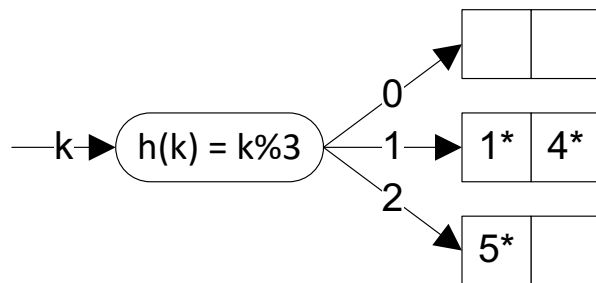


# Static Hashing: an example

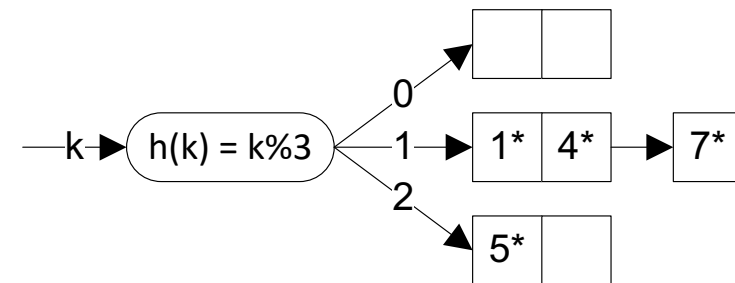
- Suppose the hash function is  $h(x) = x \bmod 3$  and a bucket can hold at most 2 data entries. Below show a static hash structure after inserting 1, 4, 5, 7, 8, 2.

$$h(7) = 1$$

Insert 7



After insert 7

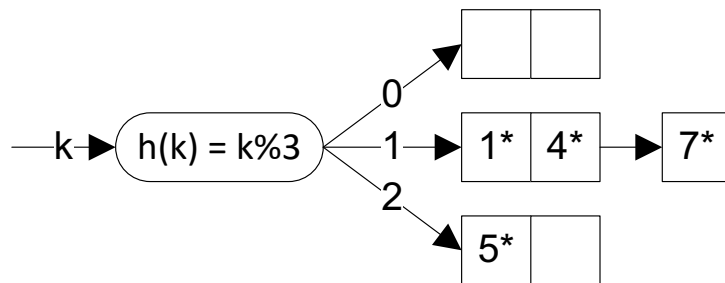


# Static Hashing: an example

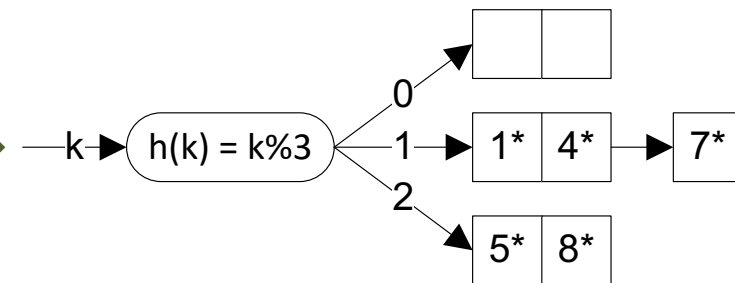
- Suppose the hash function is  $h(x) = x \bmod 3$  and a bucket can hold at most 2 data entries. Below show a static hash structure after inserting 1, 4, 5, 7, 8, 2.

$$h(8) = 2$$

Insert 8



After insert 8

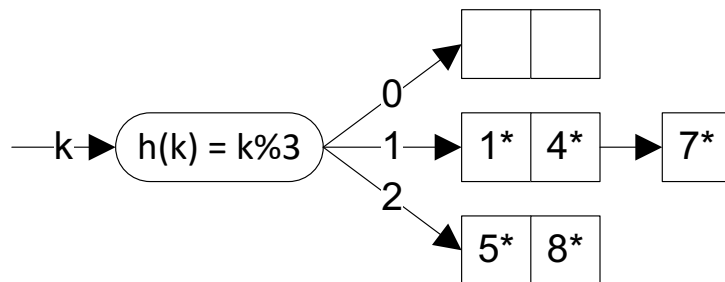


# Static Hashing: an example

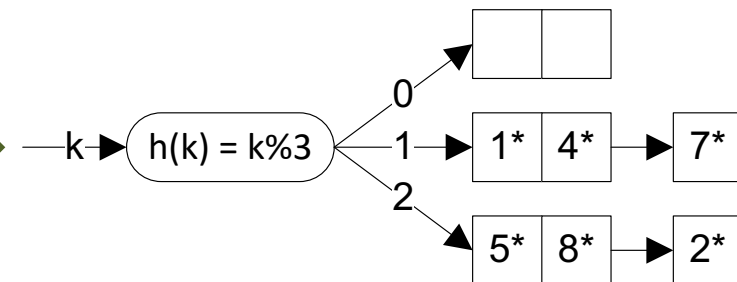
- Suppose the hash function is  $h(x) = x \bmod 3$  and a bucket can hold at most 2 data entries. Below show a static hash structure after inserting 1, 4, 5, 7, 8, 2.

$$h(2) = 2$$

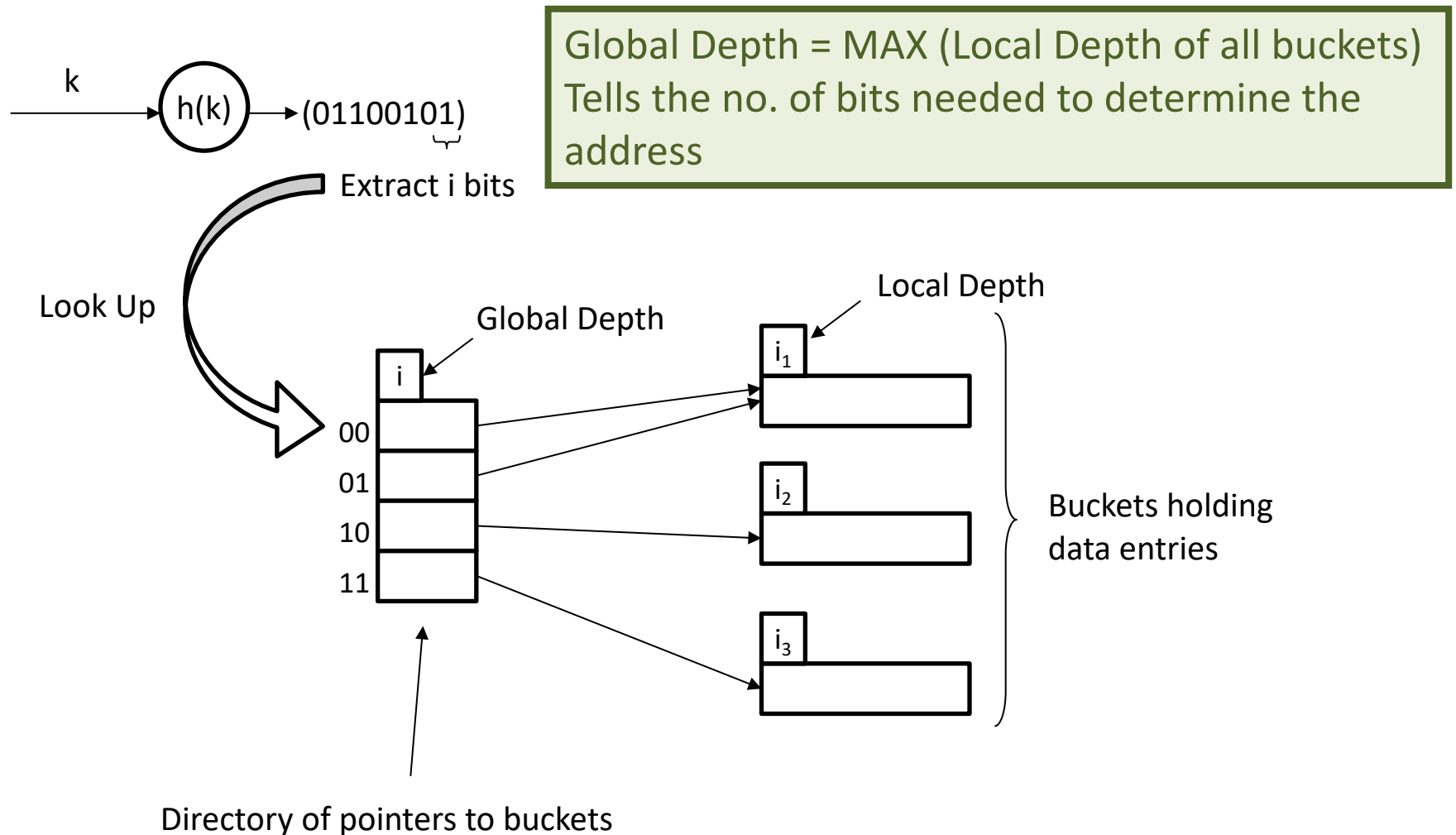
Insert 2



After insert 2



# Extensible Hashing

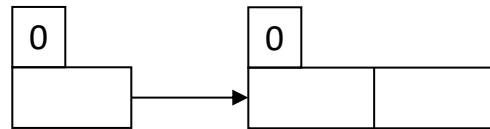




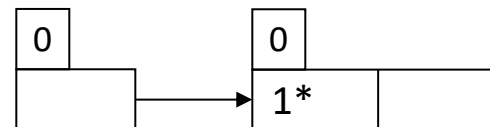
# Insertion of Extensible Hashing

- Suppose the hash function is  $h(x) = x \bmod 8$  and each bucket can hold at most 2 data entries. Below show an extendable hash structure after inserting 1, 4, 5, 7, 8, 2.

Initial:



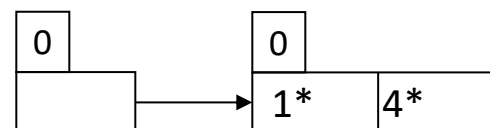
After insert 1:



(ok)

$$h(1) = 001$$

After insert 4:

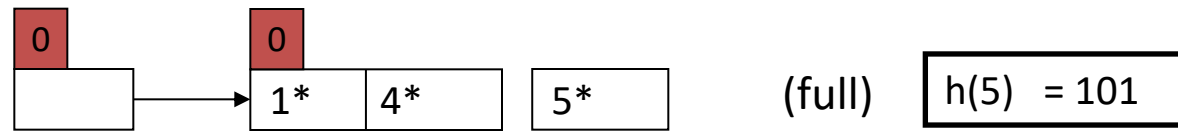


(ok)

$$\begin{aligned} h(1) &= 001 \\ h(4) &= 100 \end{aligned}$$

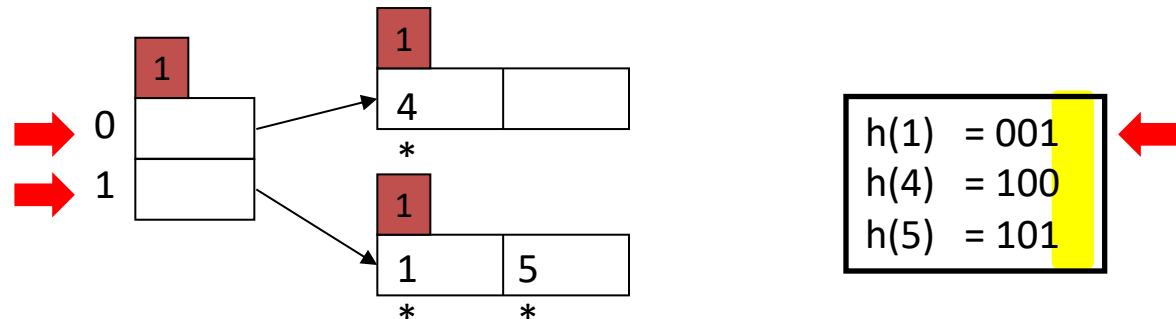
# Insertion of Extensible Hashing

Insert 5:



If bucket with local depth = global depth, then double the directory and split the bucket.

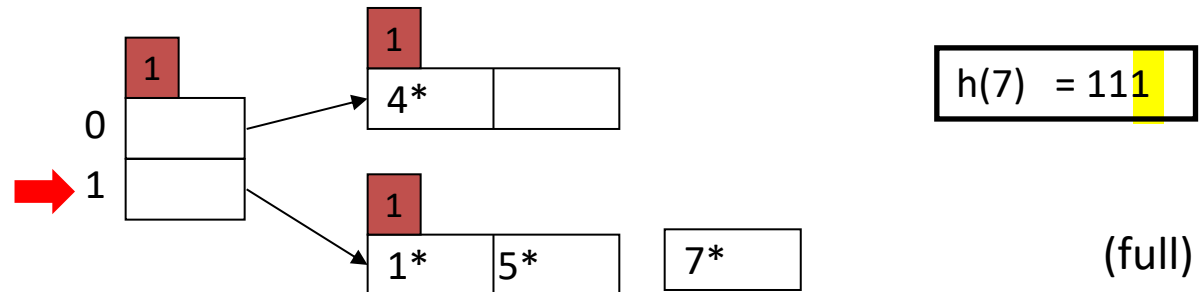
After insert 5:



Increase the global depth and local depth of the new buckets by 1.

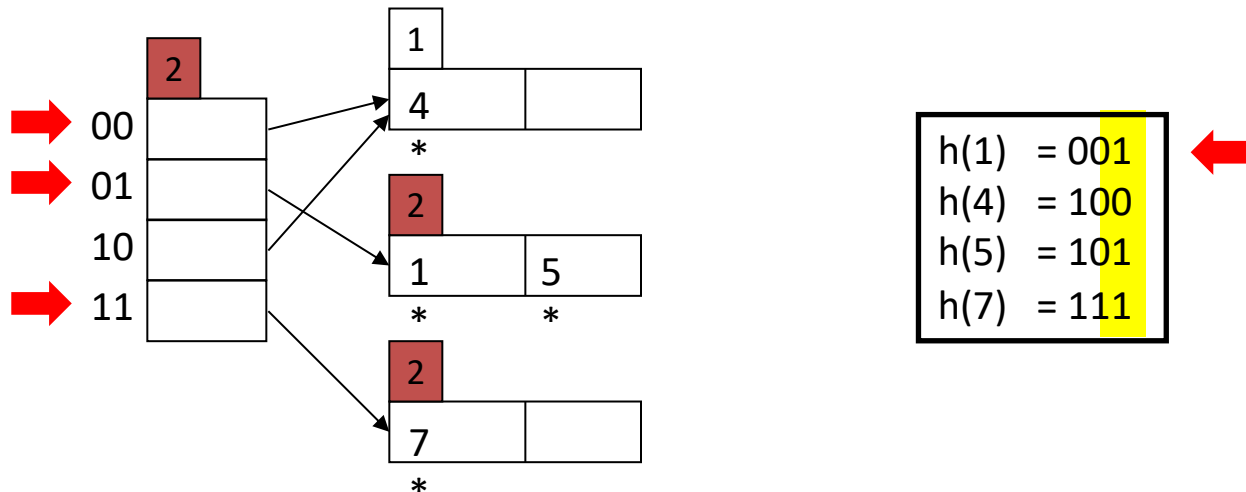
# Insertion of Extensible Hashing

Insert 7:



If bucket with local depth = global depth, then double the directory and split the bucket.

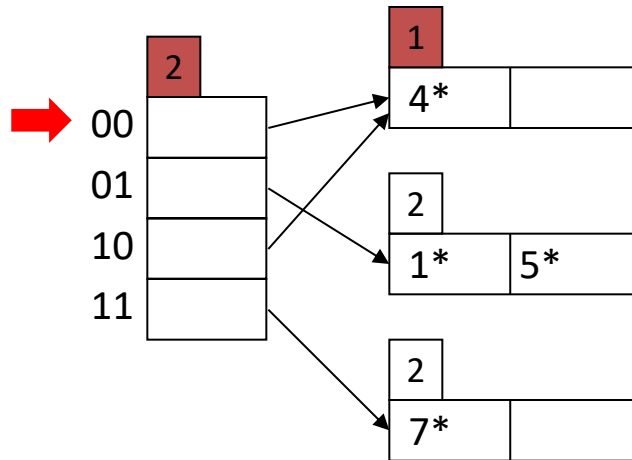
After insert 7:



Increase the global depth and local depth of the new buckets by 1.

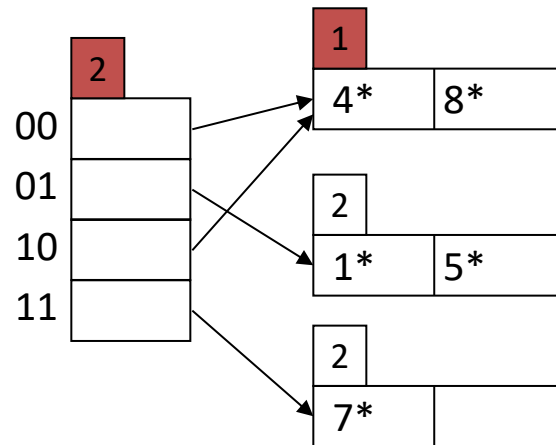
# Insertion of Extensible Hashing

Insert 8:



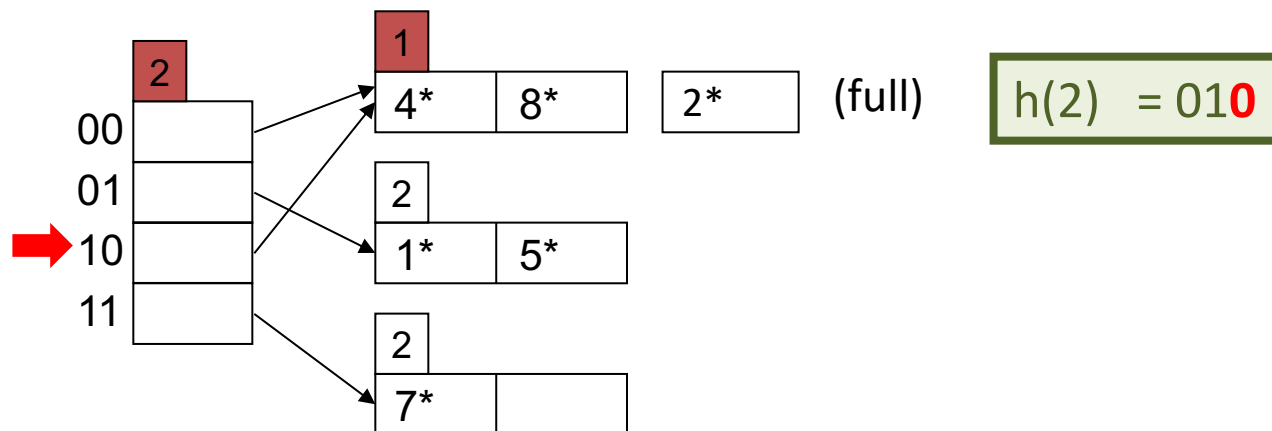
$$h(8) = 00\mathbf{0}$$

After insert 8:



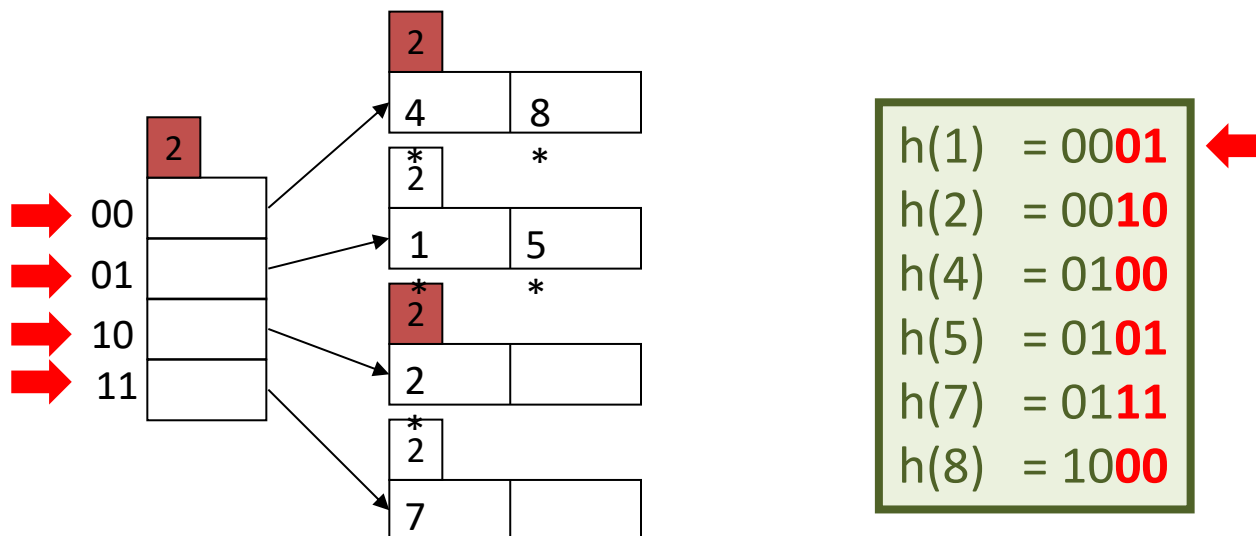
# Insertion of Extensible Hashing

Insert 2:



If bucket with local depth < global depth, then split the bucket and update the pointers.

After insert 2:

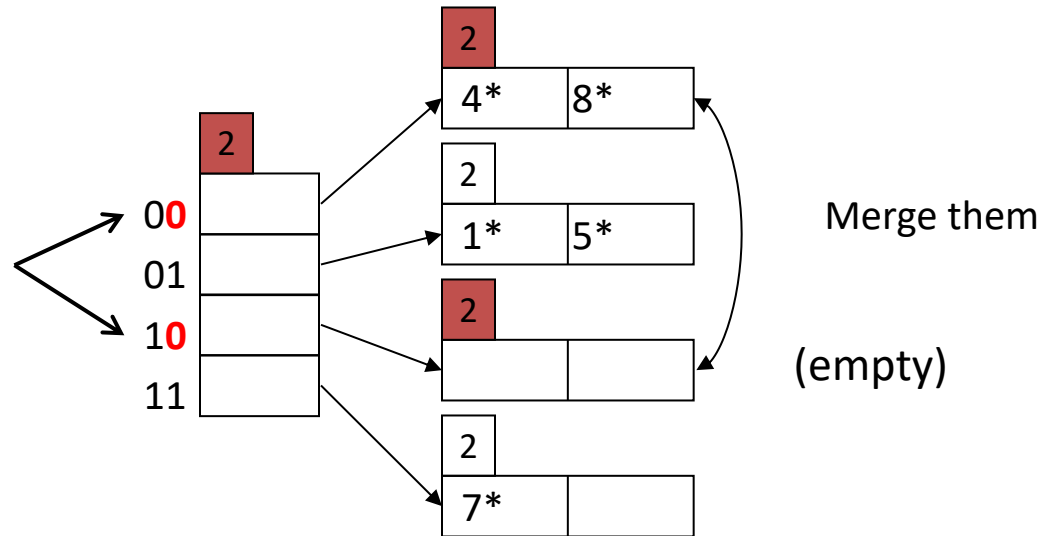


Increase the local depth of the new buckets by 1.

# Deletion of Extensible Hashing

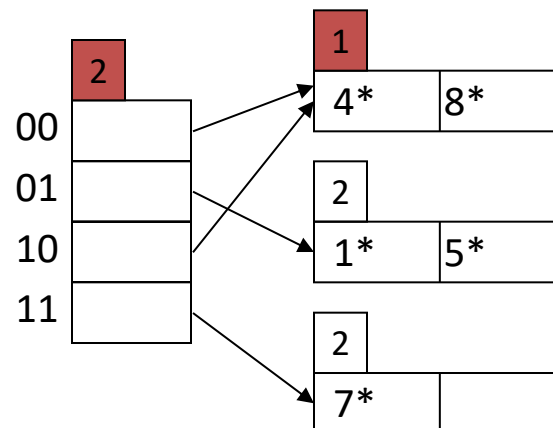
Delete 2:

Look at the last  
(global depth-1) bits



If the removal makes the bucket empty, then remove the bucket and update the pointer.

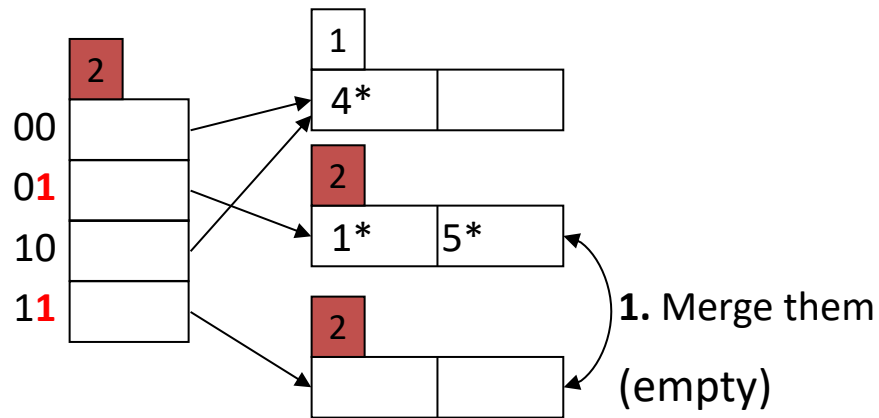
After delete 2:



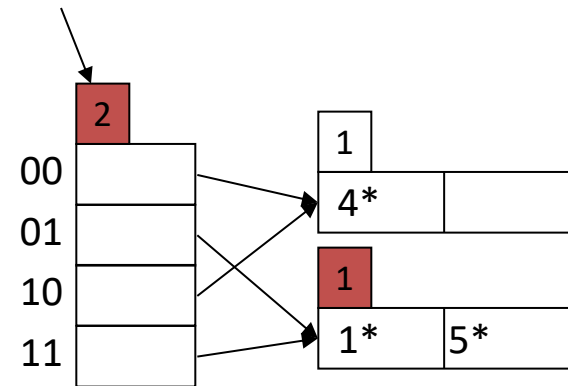
Decrease the local depth of the new bucket by 1.

# Deletion of Extensible Hashing

Delete 7:

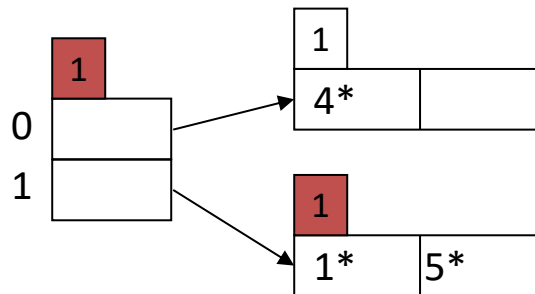


2. Halve the directory



If the merge makes  $\max(\text{local depth of all buckets}) < \text{global depth}$ , then halve the size of directory.

After delete 7:



Decrease the global depth of the new bucket by 1.