

Part 1

Q1

$$\pi_{\text{find, arrives}} (\sigma_{\text{to} = \text{"HK"}} (\text{Flight}))$$

Q2

$$\pi_{\text{eid}} \left(\pi_{\text{aid}} \left(\sigma_{\text{cruisingrange} \geq 8000} (\text{Aircraft}) \right) \bowtie \text{Certified} \right)$$

Q3

The query cannot be expressed in standard relational algebra because there is no aggregate function in relational algebra. We cannot use relational algebra to sum queries.

Q4 $\pi_{\text{aid}} (\text{Aircraft}) - \pi_{\text{aid}} \left($

$$\text{Aircraft} \bowtie_{\text{Aircraft.cruisingrange} < A.cruisingrange} \rho(A, \text{aircraft}) \right)$$

Q5

$$\rho \left(\text{NY-to-LA}, \left(\sigma_{\text{from} = \text{"New York"} \wedge \text{to} = \text{"Los Angeles"}} (\text{Flight}) \right) \right)$$

$$\rho \left(\text{Non-stop}, \text{Aircraft} \bowtie_{\text{Aircraft.cruisingrange} > \text{NY-to-LA.distance}} \text{NY-to-LA} \right)$$

$$\rho (\text{Airbus}, \sigma_{\text{manufacturer} = \text{"Airbus"}} (\text{Aircraft}))$$

$$\rho (\text{EID}, \pi_{\text{eid}} (\pi_{\text{aid}} (\text{Non-stop}) \bowtie \text{Certified}) - \pi_{\text{eid}} (\pi_{\text{aid}} (\text{Airbus}) \bowtie \text{Certified}))$$

$$\pi_{\text{salary}} (\text{EID} \bowtie \text{Employee})$$

Part 2

Q1 The query cannot be expressed into relational algebra because there is no aggregate function in relational algebra. We cannot use relational algebra to sum queries.

Q2

$\rho(\text{Eagle}, \sigma_{\text{predator} = \text{"eagle"}}(\text{Foodchain}))$

$\rho(\text{Leopard}, \sigma_{\text{predator} = \text{"leopard"}}(\text{Foodchain}))$

$\rho(\text{Tiger}, \sigma_{\text{predator} = \text{"tiger"}}(\text{Foodchain}))$

$\rho(\text{Food}, (\pi_{\text{food}}(\text{Eagle}) \bowtie \pi_{\text{food}}(\text{Leopard})) \cup (\pi_{\text{food}}(\text{Eagle}) \bowtie \pi_{\text{food}}(\text{Leopard})))$

$\pi_{\text{category}}(\text{Creature} \bowtie_{\text{creature.name} = \text{Food.food}} \text{Food})$

Q3

$\rho(\text{Food}, \pi_{\text{name}}(\sigma_{\text{category} = \text{"Amphibia"} \wedge \text{status} = \text{"critically Endangered"}}(\text{Creature})))$

$\rho(\text{Predator}, \pi_{\text{predator}}(\text{FoodChain} \bowtie_{\text{FoodChain.food} = \text{Food.food}} \text{Food}))$

$\rho(\text{Predator}(\text{predator} \rightarrow \text{food}), \text{Predator})$

$\pi_{\text{predator, food}}(\text{FoodChain}) / \text{Predator}$

Q4

$$\pi_{\text{name, status}} \left(\text{Creature} - \left(\pi_{\text{predator}} \left(\sigma_{\text{predator} = \text{food}} (\text{FoodChain}) \right) \times \text{Creature} \right) \right)$$

Q5 We cannot directly compute exactly three, but we can compute at least three. So the idea of this question is to compute queries of food with at least 3 predators and at least 4 predators. Then we take a set difference.

FC stands for FoodChain

$$\rho(\text{FC1}, (\text{predator} \rightarrow \text{predator1}, \text{food} \rightarrow \text{food1}), \pi_{\text{predator, food}}(\text{FoodChain}))$$

$$\rho(\text{FC2}, (\text{predator} \rightarrow \text{predator2}, \text{food} \rightarrow \text{food2}), \pi_{\text{predator, food}}(\text{FoodChain}))$$

$$\rho(\text{FC3}, (\text{predator} \rightarrow \text{predator3}, \text{food} \rightarrow \text{food3}), \pi_{\text{predator, food}}(\text{FoodChain}))$$

$$\rho(\text{FC4}, (\text{predator} \rightarrow \text{predator4}, \text{food} \rightarrow \text{food4}), \pi_{\text{predator, food}}(\text{FoodChain}))$$

$\rho(\text{At Least 4},$

$$\sigma_{\text{food1} = \text{food2} \wedge \text{food2} = \text{food3} \wedge \text{food3} = \text{food4} \wedge (\text{predator1} \neq \text{predator2} \vee \text{predator2} \neq \text{predator3} \vee \text{predator3} \neq \text{predator4})} (\text{FC1} \times \text{FC2} \times \text{FC3} \times \text{FC4})$$

$\rho(\text{At Least 3},$

$$\sigma_{\text{food1} = \text{food2} \wedge \text{food2} = \text{food3} \wedge (\text{predator1} \neq \text{predator2} \vee \text{predator2} \neq \text{predator3})} (\text{FC1} \times \text{FC2} \times \text{FC3})$$

$$\pi_{\text{food}}(\text{AtLeast 3}) - \pi_{\text{food}}(\text{AtLeast 4})$$