

$$= \frac{1}{2} \sum_{i=1}^N \log (P(y^{(i)} | x^{(i)}, \theta))$$

$$= \frac{1}{2} \sum_{i=1}^N \log \left(\frac{P(x^{(i)} | y^{(i)}, \theta) P(y^{(i)})}{P(x^{(i)})} \right)$$

Derivation

$$= \frac{1}{2} \sum_{i=1}^N \log \left(\frac{P(x^{(i)} | y^{(i)}, \theta) P(y^{(i)})}{\sum_{k=1}^K P(x^{(i)} | y=k, \theta) P(y=k)} \right)$$

$$= \frac{1}{2} \sum_{i=1}^N \log (P(x^{(i)} | y^{(i)}, \theta)) + \log \left(\frac{1}{K} \right) - \log \left(\frac{1}{K} \times \sum_{k=1}^K P(x^{(i)} | y=k, \theta) \right)$$