Homework One

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Problem 1.

Solution Cipher text: LFDPHLVDZLFRQTXHUHG We can easily get the character frequency of the cipher text:

$$H: 3, L: 3, D: 2, F: 2, L: 2, P: 1, V: 1, Z: 1, R: 1, Q: 1, T: 1, X: 1, U: 1, G: 1$$

Since the two most frequent characters of the ciphertext are "H" and "L", we infer that "H" and "L" represents "E" and "I" in the plaintext correspondingly, Therefore, the shift method is

$$C = (M+3) \mod 26$$

We can get the plaintext:

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Problem 2.

Solution (a) ciphertext: FSKWPYTJUMB

- (b) plaintext: csfivetwoeightfive
- (c) h

Problem 3.

Solution a) Encryption : $ciphertext = plaintext \oplus key$

Plaintext:

H(00111), E(00100), L(01011), L(01011), O(01110)

KEY:

X(10111), M(01100), C(00010), K(01010), L(01011)

Ciphertext:

Q(10000), I(01000), J(01001), B(00001), F(00101)

(b) Decryption: $plaintext = ciphertext \oplus key$

Ciphertext:

Q(10000), I(01000), J(01001), B(00001), F(00101)

KEY:

$$T(10011), Q(10000), U(10100), R(10001), I(01000)$$

Plaintext:

$$D(00011), Y(11000), D(11101), Q(10000), N(01101)$$

(c) We can get

$$M_1 \oplus KEY = C_1, M_2 \oplus KEY = C_2$$

Therefore,

$$(M_1 \oplus KEY) + (M_2 \oplus KEY) = M_1 \oplus M_2 = C_1 \oplus C_2$$

Problem 4.

Solution e can compute L_0,R_0 :

1.
$$L_2 = R_3 + f(K, L_3), R_2 = L_3$$

2.
$$L_1 = R_2 + f(K, L_2), R_1 = L_2$$

3.
$$L_0 = R_1 + f(K, L_1), R_0 = L_1$$

Problem 5.

Solution a) The number of keys we have to try on average is

$$2^{56} \times 2^{56} \div 2 = 2^{111}$$

(b)If $K_1 = K_2$, 3DES will covert to DES

Problem 6.

Solution onvert the plaintext into binary form:

$$P = P_0 P_1 P_2 P_3 P_4 P_5 = I(1000) A(0000) M(1100) B(0001) O(1110) B(0001)$$

Then

$$C_0 = E(K, P_0 \oplus IV) = P_0 \oplus IV + 1 = 1011(L)$$

$$C_1 = E(K, P_1 \oplus C_0) = C_0 \oplus P_1 + 1 = 1100(M)$$

$$C_2 = E(K, P_2 \oplus C_1) = C_1 \oplus P_2 + 1 = 0001(B)$$

$$C_3 = E(K, P_3 \oplus C_2) = C_2 \oplus P_3 + 1 = 0001(B)$$

$$C_4 = E(K, P_4 \oplus C_3) = C_3 \oplus P_4 + 1 = 0000(A)$$

$$C_5 = E(K, P_5 \oplus C_4) = C_4 \oplus P_5 + 1 = 0010(C)$$

Therefore, the ciphertext is

$$C = LMBBAC$$