

Big O is a set, i.e. a category.  $10n = O(n)$  is a shortcut for  $10n \in O(n)$ . We know that  $10n$  is in the category of functions shaped like  $n$ .

Likewise,  $10n^3 + 75n^2 - 5200n + 1000007$  is in the category of functions shaped like  $n^3$ , so it is  $O(n^3)$ .

Formally:

$$O(g(n)) = \{f(n) | \exists c, n_0 > 0 \wedge f(n) \leq c \bullet g(n), \forall n > n_0\}$$