**Time Complexity**

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(a):

(b):

(c):

(d):

(e):

**Fibonacci**

Prove: .

By trial and error: It appears that for all

To prove: For all positive integers

By induction on . Base case:

Step, assume: Indeed, true that for all

To prove:

LHS:

Suffices to prove:

(by dividing the above by )

It is indeed true that

**Multiplication**

Graphical user interface, text, application

Description automatically generated

Suppose instead of both and being n-bit, is n-bit and is m-bit. What is the worst-case time efficiency of ?

Proposed:

Time Efficiency:

So, final answer: