

Curriculum vitæ

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RESEARCH INTERESTS

Category theory and everything about it.

CURRENT POSITION

2020 | -

- 1 | **Postdoctoral fellow**
Tallinna Tehnikaülikooli Küberneetika Instituut | Tallinn EE

Jan 2020 | now 🇪🇪

PAST POSITIONS

2016 | 2020

- 1 | **Postdoctoral fellow**
Centro de Matemática da Universidade de Coimbra | Coimbra

Jul 2019 | Dec 2019 🇵🇹

- 2 | **Postdoctoral fellow**
Max-Planck-Institut für Mathematik | Bonn

Sep 2018 | Feb 2019 🇩🇪

- 3 | **Postdoctoral fellow**
Masarykova univerzita | Brno

Mar 2017 | Apr 2018 🇨🇪

- 4 | **Postdoctoral fellow and Assistant Professor**
University of Western Ontario | London

Sep 2016 | Nov 2016 🇨🇦

EDUCATION

2008 | 2016

- 1 | **Ph.D. in Mathematics**
SISSA | Trieste
thesis: *t-structures on stable ∞ -categories* : 2005.14295

Oct 2012 | Jun 2016 🇮🇹

- 2 | **M.Sc. in Mathematics**
Università degli studi di Padova
thesis: *Orlov reconstruction theorem*

Oct 2010 | Jul 2012 🇮🇹

- 3 | **B.Sc. in Mathematics**
Università degli studi di Padova
thesis: *Monads and Beck's theorem*

Jan 2008 | Jun 2010 🇮🇹

PUBLICATIONS

- 1 | **A Categorical Semantics for Bounded Petri Nets** w/F. Genovese, D. Palombi |
2101.09100 | Applied Category Theory 2021
We provide a categorical semantics for bounded Petri nets, both in the collective- and individual-token philosophy. In both cases, we describe the process of bounding a net internally, by just constructing new categories of executions of a net using comonads, and externally, using lax-monoidal-lax functors. Our external semantics is non-local, meaning that tokens are endowed with properties that say something about the global state of the net. We then prove, in both cases, that the internal and external constructions are equivalent, by using machinery built on top of the Grothendieck construction. The individual-token case is harder, as it requires a more explicit reliance on abstract methods.

- 2 | **Coends of higher arity** w/T. de Oliveira Santos |
2011.13881 | Applied Categorical Structures
We specialise a recently introduced notion of generalised dinaturality for functors $T : (\mathcal{C}^{\text{op}})^p \times \mathcal{C}^q \rightarrow \mathcal{D}$ to the case where the domain (resp., codomain) is constant, obtaining notions of ends (resp., coends) of higher arity, dubbed herein (p, q) -ends (resp., (p, q) -coends). While higher arity co/ends are particular instances of "totally symmetrised" (ordinary) co/ends, they serve an important technical role in the study of a number of new categorical phenomena, which may be broadly classified as two new variants of category theory. The first of these, weighted category theory, consists of the study of weighted variants of the classical notions and construction found in ordinary category theory, besides that of a limit. This leads to a host of varied and rich notions, such as weighted Kan extensions, weighted adjunctions, and weighted ends. The second, diagonal category theory, proceeds in a different (albeit related) direction, in which one replaces universality with respect to natural transformations with universality with respect to dinatural transformations, mimicking the passage from limits to ends. In doing so, one again encounters a number of new interesting notions, among which one similarly finds diagonal Kan extensions, diagonal adjunctions, and diagonal ends.

- 3 | **A Categorical Semantics for Hierarchical Petri Nets** w/F. Genovese, J. Herold, D. Palombi |
2102.00096 | Proc. of GCM, 2021 Springer.
We show how a particular flavor of hierarchical nets, where the firing of a transition in the parent net must correspond to an execution in some child net, can be modelled utilizing a functorial semantics from a free category - representing the parent net - to the category of sets and spans between them. This semantics can be internalized via Grothendieck construction, resulting in the category of executions of a Petri net representing the semantics of the overall hierarchical net. We conclude the paper by giving an engineering-oriented overview of how our model of hierarchical nets can be implemented in a transaction-based smart contract environment.

- 4 | **Nets with Mana: A Framework for Chemical Reaction Modelling** w/F. Genovese, D. Palombi |
2101.06234 | *Graph Transformation*, Proc. of ICGT, 2021 Springer.
We use categorical methods to define a new flavor of Petri nets which could be useful in modelling chemical reactions.

- 5 | **Functorial semantics for partial theories** w/I. Di Liberti, et al. |
2011.06644 | Proc. ACM Program. Lang. 5, POPL, 2021. | doi:10.1145/3434338
We provide a Lawvere-style definition for partial theories, extending the classical notion of equational theory by allowing partially defined operations. As in the classical case, our definition is syntactic: we use an appropriate class of string diagrams as terms. This allows for equational reasoning about the class of models defined by a partial theory. We demonstrate the expressivity of such equational theories by considering a number of examples, including partial combinatory algebras and cartesian closed categories. Moreover, despite the increase in expressivity of the syntax we retain a well-behaved notion of semantics: we show that our categories of models are precisely locally finitely presentable categories, and that free models exist.

- 6 | **Triangulated factorization systems and t-structures** w/S. Virili |
1705.08565v3 | *Journal of Algebra* | doi:10.1016/j.jalgebra.2019.12.021
We define triangulated factorization systems on triangulated categories, and prove that a suitable subclass thereof (the normal triangulated torsion theories) corresponds bijectively to t-structures on the same category. This result will then be placed in the framework of derivators regarding a triangulated category as the base of a stable derivator.

- 7 | **Categorical notions of fibration** w/E. Riehl |
1806.06129 | *Expos. Math.* (2019) | doi:10.1016/j.exmath.2019.02.004
Fibrations over a category B , introduced to category theory by Grothendieck, encode pseudo-functors $B^{\circ} \rightsquigarrow \mathbf{Cat}$, while the special case of discrete fibrations encode presheaves $B^{\circ} \rightarrow \mathbf{Set}$. A two-sided discrete variation encodes functors $B^{\circ} \times A \rightarrow \mathbf{Set}$, which are also known as profunctors from A to B . By work of Street, all of these fibration notions can be defined internally to an arbitrary 2-category or bicategory. While the two-sided discrete fibrations model profunctors internally to \mathbf{Cat} , unexpectedly, the dual two-sided codiscrete cofibrations are necessary to model V -profunctors internally to $V\text{-}\mathbf{Cat}$.

- 8 | **Hearts and towers in stable infinity-categories** w/D. Fiorenza, G. Marchetti |
 1501.04658 | *Journal of Homotopy and Related Structures* 2019 | doi:10.1007/s40062-019-00237-0
 We exploit the equivalence between t-structures and normal torsion theories on a stable ∞ -category to show how a few classical topics in the theory of triangulated categories, i.e., the characterization of bounded t-structures in terms of their hearts, their associated cohomology functors, semiorthogonal decompositions, and the theory of tiltings, as well as the more recent notion of Bridgeland's slicings, are all particular instances of a single construction, namely, the tower of a morphism associated with a J -slicing of a stable ∞ -category \mathbf{C} , where J is a totally ordered set equipped with a monotone \mathbb{Z} -action.
- 9 | **A standard theorem on adjunctions in two variables**
 1902.06074 | *Preprints of the MPIM*, 2018 (67)
 We record an explicit proof of the theorem that lifts a two-variable adjunction to the arrow categories of its domains.
- 10 | **A Fubini rule for ∞ -coends**
 1902.06086 | *Preprints of the MPIM*, 2018 (68)
 We prove a Fubini rule for ∞ -co/ends of ∞ -functors $F : \mathbf{C}^{\text{op}} \times \mathbf{C} \rightarrow \mathbf{D}$. This allows to lay down "integration rules", similar to those in classical co/end calculus, also in the setting of ∞ -categories.
- 11 | **Homotopical Algebra is not concrete** w/I. Di Liberti |
 1704.00303 | *Journal of Homotopy and Related Structures* (2017): 1-15 | doi:10.1007/s40062-018-0197-3
 We generalize Freyd's well-known result that "homotopy is not concrete", offering a general method to show that under certain assumptions on a model category M , its homotopy category $\text{ho}(M)$ cannot be concrete. This result is part of an attempt to understand more deeply the relation between set theory and abstract homotopy theory.
- 12 | **Sober Ontic Structural Realism and Yoneda lemma**
 abstract at the *Triennial conference of the SILFS*, Bologna
 A note on why the Yoneda lemma prevents to take too strong a position towards the non-existence of relata (*radical* ontic structural realism posits that only relations exist).
- 13 | **Coend calculus**
 1501.02503 | LMS Lecture Note Series 468. Cambridge University Press. 2021. ISBN 9781108778657.
 A survey of the most striking and useful applications of *coend calculus*. This is a revised version of 1501.02503v4. After having given a series of preliminary definitions, we characterize co/ends as particular co/limits; then we derive a number of results directly from this characterization. The last sections discuss the most interesting examples where co/end calculus serves as a powerful abstract way to do explicit computations in diverse fields like Algebra, Algebraic Topology and Category Theory. The appendices serve to sketch a number of results in theories heavily relying on co/end calculus.
- 14 | **t-structures are normal torsion theories** w/D. Fiorenza |
 1408.7003 | *Applied Categorical Structures* 24.2 (2016): 181-208 | doi:10.1007/s10485-015-9393-z
 We characterize t-structures in stable ∞ -categories as suitable quasicategorical factorization systems. More precisely we show that a t-structure \mathbf{t} on a stable ∞ -category \mathbf{C} is equivalent to a normal torsion theory \mathbb{T} on \mathbf{C} , i.e. to a factorization system $\mathbb{T} = (E, M)$ where both classes satisfy the 3-for-2 cancellation property, and a certain compatibility with pullbacks/pushouts.

PREPRINTS

- 1 | **Escrows are optics** w/F. Genovese, D. Palombi |
 2105.10028
 We provide a categorical interpretation for *escrows*, i.e. trading protocols in trustless environment, where the exchange between two agents is mediated by a third party where the buyer locks the money until they receive the goods they want from the seller. A simplified escrow system can be modeled as a certain kind of *optic* in a monoidal category \mathcal{M} (e.g., the category of sets with cartesian product); escrows can be regarded as morphisms of a category $\mathcal{E}(\mathcal{M})$, with the same objects of \mathcal{M} , and where the hom-objects are $\langle X, Y \rangle = \mathbf{Opt}_{\mathcal{M}}([X], [Y])$. When X is a comonoid and Y is a monoid in \mathcal{M} , $\mathcal{E}(\mathcal{M})(X, Y)$ is a monoid in **Set** (or in the base of enrichment chosen to model one's specific problem), acting on the set of optics $[B] \rightarrow [X]$. Moreover, we define a map

$$\triangleleft : \langle Y, X \rangle \times \mathbf{Opt}([X], [B]) \rightarrow \mathbf{Opt}([X], [Y \otimes B])$$

having action-like properties. This has the following interpretation: the object B acts as an intermediary in a transaction between X and Y , modeled by an escrow in $\langle Y, X \rangle$.

2 | Differential 2-rigs

w/F. Genovese |

2103.00938

We explore the notion of a category with coproducts \cup and a monoidal structure \otimes distributing over it, endowed with an endo-functor ∂ which is 'linear and Leibniz'. Such ∂ can be legitimately called a *derivation* on \mathcal{C} , and the pair (\mathcal{C}, ∂) appears as the categorification of a differential ri(n)g: a *differential 2-rig*. We explore a number of possible special examples: when \mathcal{C} is semicartesian (i.e., its \otimes -monoidal unit is the terminal object), derivations are better behaved in some respect; interesting examples arise when $\mathcal{C} = [\mathcal{A}, \mathbf{Set}]$ is a presheaf topos endowed with a convolution product: among these, the operation of Brzozowski's derivative in formal language theory; we retrieve the 'chain rule' in a category of 'non-symmetric species' $[\mathbf{Fin}, \mathbf{Set}]$, obtained when a substitution product $F \diamond G$ is interpreted as composition $T_F \circ T_G$ of the associated finitary functors, regarded as formal power series. Derivations on a 2-rig are tightly related to *tensorial strengths*; this draws a connection between the present theory and applicative structures in functional programming. Moreover, given a derivation on \mathcal{C} , the derivative of the \otimes -monoidal unit ∂I is a *self-similar* object, i.e. a solution to the equation $X \cong X \cup X$; we explore the many consequences of this apparently innocuous observation. This has connection with the category-theoretic analysis of dynamical systems.

3 | Rosen's no-go theorem for regular categories

2012.11648

The famous biologist Robert Rosen argued for an intrinsic difference between biological and artificial life, supporting the claim that 'living systems are not mechanisms'. This result, understood as the claim that life-like mechanisms are non-computable, can be phrased as the non-existence of an equivalence between a category of 'static'/analytic elements and a category of 'variable'/synthetic elements. The property of a system of being synthetic, understood as being the gluing of 'variable families' of *analytica*, must imply that the latter class of objects does not retain sufficient information in order to describe said variability; we contribute to this thesis with an argument rooted in elementary category theory. Seen as such, Rosen's 'proof' that no living system can be a mechanism arises from a tension between two contrapuntal needs: on one side, the necessity to consider (synthetically) variable families of systems; on the other, the necessity to describe a syntheticum via an universally chosen analyticum.

4 | Functorial Erkennen

w/D. Dentamaro |

<http://philsci-archive.pitt.edu/18519/>

We outline a 'formal theory of scientific theories' rooted in the theory of profunctors; the category-theoretic asset stresses the fact that the scope of scientific knowledge is to build 'meaningful connections' (i.e. well-behaved adjunctions) between a linguistic object (a 'theoretical category' \mathcal{T}) and the world \mathcal{W} said language ought to describe. Such a world is often unfathomable, and thus we can only resort to a smaller fragment of it in our analysis: this is the 'observational category' $\mathcal{O} \subseteq \mathcal{W}$. From this we build the category $[\mathcal{O}^{\text{op}}, \mathbf{Set}]$ of all possible displacements of observational terms \mathcal{O} . The self-duality of the bicategory of profunctors accounts for the fact that theoretical and observational terms can exchange their rôle without substantial changes in the resulting predictive-descriptive theory; this provides evidence for the idea that their separation is a mere linguistic convention; to every profunctor \mathfrak{R} linking \mathcal{T} and \mathcal{O} one can associate an object $\mathcal{O} \mathrel{\mathfrak{R}} \mathcal{T}$ obtained *glueing* together the two categories and accounting for the mutual relations subsumed by \mathfrak{R} . Under mild assumptions, such an arrangement of functors, profunctors, and gluings provides a categorical interpretation for the 'Ramseyfication' operation, in a very explicit sense: in a scientific theory, if a computation entails a certain behaviour for the system the theory describes, then saturating its theoretical variables with actual observed terms, we obtain the entailment *in the world*.

5 | Categorical Ontology I

w/D. Dentamaro |

<http://philsci-archive.pitt.edu/17136/>

The present paper approaches ontology and metaontology through mathematics, and more precisely through category theory. We exploit the theory of *elementary toposes* to claim that a satisfying "theory of existence", and more at large ontology itself, can both be obtained through category theory. In this perspective, an *ontology* is a mathematical object: it is a category, the universe of discourse in which our mathematics (intended at large, as a theory of knowledge) can be deployed. The *internal language* that all categories possess prescribes the modes of existence for the objects of a fixed ontology/category. This approach resembles, but is more general than, fuzzy logics, as most choices of E and thus of Ω_E yield nonclassical, many-valued logics. Framed this way, ontology suddenly becomes more mathematical: a solid corpus of techniques can be used to backup philosophical intuition with a useful, modular language, suitable for a practical foundation. As both a test-bench for our theory, and a literary *divertissement*, we propose a possible category-theoretic solution of Borges' famous paradoxes of Tlön's "nine copper coins", and of other seemingly paradoxical construction in his literary work. We then delve into the topic with some vistas on our future works.

6 | Profunctor optics, a categorical update

w/B. Clarke, et al. |

2001.07488

Profunctor optics are bidirectional data accessors that capture data transformation patterns such as accessing subfields or iterating over containers. They are modular, meaning that we can construct accessors for complex structures by combining simpler ones. Profunctor optics have been studied only using **Sets** as the enriching category and in the non-mixed case. However, functional programming languages are arguably better described by enriched categories and we have found that some structures in the literature are actually mixed optics. Our work generalizes a classic result by Pastro and Street on Tambara theory and uses it to describe mixed V -enriched profunctor optics and to endow them with V -category structure. We provide some original families of optics and derivations, including an elementary one for traversals that solves an open problem posed by Milewski. Finally, we discuss a Haskell implementation.

7 | On the unicity of formal category theories

w/I. Di Liberti |

1901.01594v1

We prove an equivalence between cocomplete Yoneda structures and certain proarrow equipments on a 2-category \mathbf{K} . In order to do this, we recognize the presheaf construction of a cocomplete Yoneda structure as a relative, lax idempotent monad sending each admissible 1-cell $f : A \rightarrow B$ to an adjunction $\mathbb{P}_! f \dashv \mathbb{P}^* f$. Each cocomplete Yoneda structure on \mathbf{K} arises in this way from a relative lax idempotent monad "with enough adjoint 1-cells", whose domain generates the ideal of admissibles, and the Kleisli category of such a monad equips its domain with proarrows. We call these structures "yosegi". Quite often, the presheaf construction associated to a yosegi generates an ambidextrous Yoneda structure; in such a setting there exists a fully formal version of Isbell duality.

8 | Accessibility and presentability in 2-categories

w/I. Di Liberti |

1804.08710v4

We outline a definition of accessible and presentable objects in a 2-category \mathbf{K} endowed with a Yoneda structure; this perspective suggests a unified treatment of many "Gabriel-Ulmer like" theorems (like the classical Gabriel-Ulmer representation for locally presentable categories, Giraud theorem, and Gabriel-Popescu theorem), asserting how presentable objects arise as reflections of generating ones. In a 2-category with a Yoneda structure, two non-equivalent definitions of presentability for $A \in \mathbf{K}$ can in principle be given: in the most interesting, it is generally false that all presheaf objects $\mathbb{P}A$ are presentable; this leads to the definition of a Gabriel-Ulmer structure, i.e. a Yoneda structure rich enough to concoct Gabriel-Ulmer duality and to make this asymmetry disappear. We end the paper with a roundup of examples, involving classical (set-based and enriched), low dimensional and higher dimensional category theory.

9 | Localization theory for derivators

1802.08193v1

We outline the theory of reflections for prederivators, derivators and stable derivators. In order to parallel the classical theory valid for categories, we outline how reflections can be equivalently described as categories of fractions, reflective factorization systems, and categories of algebras for idempotent monads. This is a further development of the theory of monads and factorization systems for derivators.

10 | Recollements in stable ∞ -categories

w/D. Fiorenza |

1507.03913v2

We develop the theory of recollements in a stable ∞ -categorical setting. In the axiomatization of Beilinson, Bernstein and Deligne, recollement situations provide a generalization of Grothendieck's "six functors" between derived categories. The adjointness relations between functors in a recollement $\mathbf{D}^0, \mathbf{D}, \mathbf{D}^1$ induce a "recollée" t-structure $\mathbf{t}_0 \boxplus \mathbf{t}_1$ on \mathbf{D} , given t-structures $\mathbf{t}_0, \mathbf{t}_1$ on $\mathbf{D}^0, \mathbf{D}^1$. Such a classical result, well-known in the setting of triangulated categories, is recasted in the setting of stable ∞ -categories and the properties of the associated (∞ -categorical) factorization systems are investigated. In the geometric case of a stratified space, various recollements arise, which "interact well" with the combinatorics of the intersections of strata to give a well-defined, associative \boxplus operation. From this we deduce a generalized associative property for n -fold gluing $\mathbf{t}_0 \boxplus \dots \boxplus \mathbf{t}_n$, valid in any stable ∞ -category.

TALKS

1 | Functorial semantics of partial theories

Apr 2021

Invited Speaker | Seminari di logica Torino-Udine








2 | Coends of higher arity

Dec 2020

Organiser and speaker | ItaCa - Italian Category theorists conference

3 The art of \int	Dec 2019
Invited speaker ItaCa - Italian Category theorists conference	
4 Axiomatic cohesion of toposes	Dec 2019
Invited speaker Università "La Sapienza" - Rome	
5 On the unicity of the formal theory of categories	Dec 2018
Lectures on 1901.01594 ULB - Bruxelles	
6 Accessibility and Presentability in 2-categories	Nov 2018
Talk on 1804.08710 Università degli studi di Torino	
7 Homotopical algebra is not concrete	Sep 2017
Contributed talk <i>British Topology Meeting</i> Leicester	
8 The formal category theory of derivators	Sep 2017
Invited speaker <i>Some trends in Algebra</i> Prague	
9 Sober Ontic Structural Realism	Jun 2017
Invited speaker <i>SILFS</i> Bologna	
10 Model categories	May 2017
Invited speaker <i>A categorical day in Turin</i> Torino	
11 t-derivators	Feb 2017
Invited speaker <i>Young researchers in homotopy theory</i> , Bonn	
12 Coend calculus	May 2016
Lectures on 1501.02503 Leeds	

TEACHING & ORGANIZATIONAL ACTIVITIES

- 1 |  **ITI9200 - Introduction to Category Theory** Jan 2021 | May 2021
Introduction to Category Theory and its Applications (*Sissejuhatus kategooriateooriasse ja selle rakendustesse*). Part of the MSc in Software Engineering at TalTech. Here you find the [course webpage](#) on [tallcats.io](#).
- 2 |  **ITI9200 - Introduction to Category Theory** Jan 2020 | May 2020
Introduction to Category Theory and its Applications (*Sissejuhatus kategooriateooriasse ja selle rakendustesse*). Part of the MSc in Software Engineering at TalTech.
- 3 |  **Organiser of ItaCa Fest** June 2020 | now
An online webinar aimed to gather the community of [ItaCa](#).
- 4 |  **appointee for Adjoint school 2019** Mar 2019 | Jun 2019
A webinar and online applied Category Theory reading course. The project name is *Traversal optics and profunctors*. Led to the development of [arXiv:2001.07488](#).
- 5 |  **2-categories** Padova - IT
A short course on 2-dimensional category theory. Tentative program: monoidal and enriched categories, the calculus of coends and Kan extensions, 2-categories, the bicategory of profunctors, the 2-category of derivators, 2-dimensional limits, the formal theory of monads, formal category theory.
- 6 |  **PSSL 103 - Brno** MU Brno - CZ
I have been one of the organizers of 103rd Peripathetic Seminar on Sheaves and Logic.
- 7 |  **Formal category theory** MU Brno - CZ
A series of lectures having the scope to breach in Riehl-Verity's theory of ∞ -cosmoi.

- 8 | 🎓 **Elements of Finite Mathematics** UWO London - CA
Techniques of counting, probability, discrete and continuous random variables.
- 9 | 🎓 **Homotopical Algebra** MU Brno - CZ
A bottom-up introduction to the language of Homotopical Algebra
- 10 | 🗓 **appointee for Kan Extension Seminar I** Jan 2014 | Jul 2014
A webinar and online Category Theory reading course.
- 11 | 🎓 **supervisor and coadvisor B.Sc. in Mathematics** *student: Giovanni Ronchi*
Adjoint Functors | amslaurea.unibo.it

OTHER ACTIVITIES

- 1 | **Sparse skills**
I like the art of crafting books and drawing maps; this is not unrelated to my love for Mathematics. I am a pretty decent TeXnic (I maintain this CV as a github repo [here](#)). I know bits of Haskell, Python, and Wolfram. I like artificial languages (mi ŝatus verki vortaron al matematiko, kun terminoj el teoria kategorioj); again, this is not unrelated to my love for Mathematics.
- 2 | **Reviewer for**
zbMath, AMS Math. Rev.

Foto Loregia