

Weight Block Sparsity: Training, Compilers, and Accelerators

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ABSTRACT

We present the main ideas about a vertical system where convolution and matrix multiplication weights can be trained to exploit an 8x8 block sparsity, compilers recognize such a sparsity for both data compaction and computation splitting into threads. If we take a Resnet50, we can reduce the weight by half with little accuracy loss. We can achieve speeds similar to an hypothetical Resnet25. We shall present performance estimates by accurate and complete code generation for a small and efficient set of AIE2 (Xilinx/AMD Versal FPGAs) using Resnet50, Inception V3, and VGG16.

KEYWORDS

Sparsity, AI, Performance, FPGA, and Tools

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1 INTRODUCTION

We shall start presenting what we mean for block sparsity and for a vertical solution. Block sparsity is an intuitive concept but it is also a little misunderstood. Take a matrix multiplication as in Equation 1

$$\begin{pmatrix} C_0 & C_1 \\ C_2 & C_3 \end{pmatrix} = \begin{pmatrix} A_0 & A_1 \\ A_2 & A_3 \end{pmatrix} \begin{pmatrix} 0 & B_1 \\ B_2 & 0 \end{pmatrix} \quad (1)$$

This is simply the computation

$$C_0 = A_1 B_2; C_1 = A_0 B_1; C_2 = A_3 B_2; C_3 = A_2 B_1 \quad (2)$$

and in general with proper γ_i (i.e., a mask):

$$C_i = \sum_{k=0}^1 A_{2i+k} (\gamma_{2k+i} B_{2k+i}) \quad (3)$$

Where the matrix B is constant, diagonal, and each submatrix B_2 and B_1 can split further down and may have even smaller zero blocks. In this work, we chose the basic block of $B_i = 8 \times 8$. It is a great starting point for architectures based on AMD AIE2 products and we support others. For example,

$$B = \sum_i \gamma_i B_i, \quad \gamma_i \in \{0, 1\} \quad (4)$$

This is a well known data structure in the sparse computation field: We can use Compress Block Row or Column format (CBR). There are standard Matrix Sparse-Matrix Multiplication interfaces

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and algorithms for CPU and GPUs using this data format (where only one operand is sparse or both) [3, 14].

We explore training techniques (PyTorch and the Keras). The most successful so far is the simplest: we take a pre-trained model, we compute a Γ per layer using a function to determine the blocks more likely to be zeros (Norm) and then we train the model till convergence or accuracy achieved. We take the sparse model and we quantize to 8-bit integer computations by using the Vitis-AI quantizer. The final model is a Xilinx IR quantized model. See Section 3. We have a custom compiler that takes the XIR model and an abstraction of a connected set of AIE2. See Section 4. Given the HW and per layer, the compiler computes the maximum sub-volume computation per core. By heuristics and following a schedule, it computes a memory allocation in mem-tile for input, outputs, and weights. It formats the weights so that to exploit spatial distribution to Mem-tiles and cores into a single compacted tensor. We generate all the explicit communications between DDR, MemTile, and cores. Knowing the subproblem sizes per core and the computation throughput and with a clear specification of what is executed in parallel: we can estimate the execution time per layer and of the entire network with an accuracy closer to a simulation. We shall use this in order to write time estimates for all parts of the computation: we shall show estimates for three CNN models, a eight different AIE designs; see Section 5.

In the following Section 2, we shall start with a quantitative measure about the advantages of block sparsity in general.

2 BLOCK-SPARSE MATRIX-MATRIX MULTIPLICATION

As thought experiment, consider Γ and Ω two appropriate 0,1 matrices so that for square matrices in $\mathbb{R}^{N \times N}$

$$C = (\Gamma A) * (\Omega B)^t \quad (5)$$

More precisely, consider non-zero blocks of size $k \times k$ so that

$$C_{i*N+j} = \sum_k (\gamma_{i*N+k} A_{i*N+k}) (\omega_{j*N+k} B_{j*N+k}) \quad (6)$$

Thanks to the sparsity and if we store only non-zeros, then γ_{i*N+k} and ω_{j*N+k} are at the very least contiguous. There will be a meaningful product to compute if and only if $\gamma_{i*N+k} = 1$ and $\omega_{j*N+k} = 1$. We merge-sort these vectors. See how the Sparse Sparse Matrix multiplication using Coordinate Block Structure (COO) is applied for example in in Figure 1. We shall provide software to reproduce this. Now, the quantitative part, assume we want to achieve a fixed sparsity (i.e., density) of 50% for a square matrix of size N and we choose the block size $k \times k$. The larger k is, the smaller the overhead will be. The relative performance of the k^3 multiplication is better as k get larger because spatial and temporal locality and optimized code for a constant/parameterized k .

In Figure 1, we present two scatter plots: on the abscissa the effective multiplication-and-addition number, on the ordinate the performance in GFLOPS, when the sparse matrix with dense block is 1x1 and 8x8. Given the same problem, we may use more threads

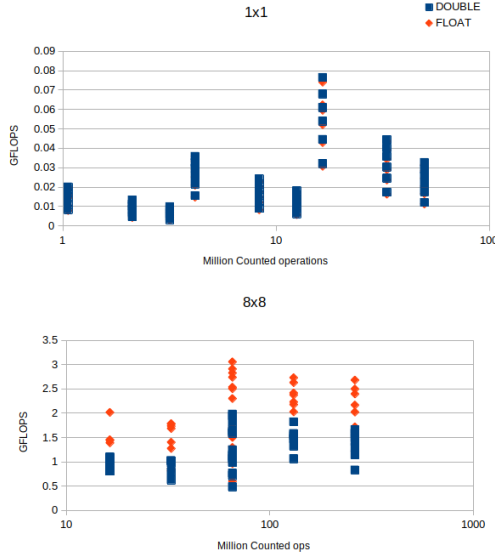


Figure 1: Block 1x1 and 8x8 performance

and thus the Jenga effect. With the same number of effective operations, the block permits and exploits higher GFLOPS per effective operation (Float is 2x faster than Double precision and this can be emphasized further [8, 13] and [12]).

3 BLOCK SPARSITY: TRAINING AND QUANTIZATION

In Convolutional Neural Networks, the two main operations are convolutions/correlations and fully connected layers (matrix multiplication). The block sparsity we are seeking to deploy is not naturally recurring and we must train the network for it.

First, let us clarify block sparsity for convolution weights, then we clarify our training process. A convolution has a weight tensor in four dimension: $\mathbf{W} \in \mathbb{R}^{c_{out} \times h \times k \times c_{in}}$. In the hyperplane of the h and k , we can simplify the weight as $\tilde{\mathbf{W}} \in \mathbb{R}^{c_{out} \times c_{in}}$ and block sparsity can be simply described by a mask $\Gamma \mathbf{W}$. Although, we speak of a 8×8 of non zeros, this is in practice a $8 \times h \times k \times 8$ block. For the matrix multiply $h = k = 1$, there is no difference from the previous discussions.

3.1 Keras

We shall provide a repository using Keras [5] where we implements the contents of this section.

We target convolutions only and without quantization. The idea of the framework is simple: we take any model and we create a copy where we enhance the convolution with a (non-trainable) Γ . A convolution will have three parameters (saving the model into a different format). The forward computation is modified so that the weights used for convolution are $\Gamma \mathbf{W}$. We assume the backward computation (i.e., gradient) is done automatically from the forward definition. There is no need to change the bias. For example, we take Resnet50 from the keras application repository, we start with a $\Gamma = 1$, and we trained one epoch using imagenet repository [6].

The goal is to choose Γ so that we achieve the required sparsity and to have the minimum loss in accuracy. Using this repository, we can test different ways to train but we skip for lack of space (incremental, Fisher measure, Hessian, diagonal Hessian, penalty losses).

3.2 Γ chosen once and full training ahead: PyTorch

Take a convolution with $\Gamma = 1$ and weights \mathbf{W} . For each γ_i , this will be representative of a block $\mathbf{W}_i \in \mathbb{R}^{8 \times h \times w \times 8} \sim \mathbb{R}^{8 \times 8}$. We can choose the \mathbf{W}_i using a measure of importance:

- $L_2 = \sqrt{\sum_k w_k^2}$ with w_k elements of \mathbf{W}_i ,
- $L_1 = \sum_k |w_k|$,
- Variance $\sigma^2 = \frac{1}{64} \sum_k (w_k - \mu)^2$ with $\mu = \frac{1}{64} \sum w_k$ or $\frac{1}{N} \sum w_k$ (the whole tensor). In signal processing σ^2 is the power of the signal.

We can then sort them in ascending order and for example choose the first 50% to set to zero. Then we start re-training. We do this for the whole network or for one convolution at a time.

In Table 1, we show the results by using one-time masks and full training: VGG-16, ResNet-50, Inceptionv3 on ImageNet20 (20 classes) and ImageNet1k (1000 classes). We use three samples per class for the validation accuracy for ImageNet1k data set; instead, we use 50 samples per class for ImageNet20. Fine-tuning sparse networks on the original ImageNet data-set [6] is expensive. To reduce the training time, we chose 20 classes (from the original 1000 classes) with the least number of images per class in the training data-set and this choice will affect the accuracy because there are fewer samples for re-training.

Table 1: Accuracies of the sparsity models

Model	Dataset	Baseline Acc.(%)	Sparsity		
			block	ratio (%)	Acc.(%)
Inception-v3	ImageNet1k	77.2	8x8	50	75.5
ResNet-50	ImageNet1k	76.7	8x8	50	74.6
VGG-16	ImageNet1k	70.6	8x8	50	69.7
ResNet-50	ImageNet20	96.1	8x8	25	95.1
ResNet-50	ImageNet20	96.1	8x8	50	92.0
ResNet-50	ImageNet20	96.1	8x8	75	87.1
ResNet-50	ImageNet20	96.1	1x1	25	96.0
ResNet-50	ImageNet20	96.1	1x1	50	95.6
ResNet-50	ImageNet20	96.1	1x1	75	93.5
VGG-16	ImageNet20	92.0	8x8	50	89.6
VGG-16	ImageNet20	92.0	1x1	50	92.3
VGG-16	ImageNet20	92.0	1x1	75	91.7

Classification accuracy on ImageNet1k drops by only 1 - 2% after applying 50% sparsity with a 8×8 block (this is without any quantization). We experiment with different block shapes such as 16×4 and 4×16 on ResNet-50, but the accuracy is slightly worse compared to block of 8×8 . Fine-grained sparsity (1×1 block) does not sacrifice any accuracy (i.e., almost any). We use the sparsified

models, we quantize them using Vitis AI, and we shall use it for time estimates (i.e., Section 5).

4 THE COMPILER AND ITS CODE GENERATION FOR AIE

Within our Xilinx/AMD effort, we can take a PyTorch/Keras model, quantize it using Vitis AI, and create an intermediate representation that we call Xilinx Intermediate Representation (XIR). This is a graph where each node is an operation that reads tensors and writes one tensor. A convolution has one quantized input: we use the tensor layout format BHWC, the tensors are represented in INT8 with a position where the fraction starts (power of two scale). It computes a tensor using the same layout as the input and with a proper scale. The weights and bias are properties of the convolutions, as such they can be tailored; the layout of the weight tensor is $COUT \times h \times w \times CIN$, which is similar to the caffe layout [11] (different from [1]). For this project, we are at the third generation of a compiler for custom architectures.

The main difference is the ability to represent a parameterized block sparsity (block size and overall sparsity ratios) and the capability to split these tensors when we split the computation. All weights are statically prepared into DDR and we move them explicitly towards the inner levels. Inputs and outputs have designated space in DDR. DDR can and it will be used for tensors spills. The memory allocation to Mem-Tile is basically coloring algorithms and some heuristics. In this architecture, we do not allow *streaming* of neither data or weights (because they share space in Mem-Tile). In a previous architecture, we could.

4.1 AIE Hardware abstraction



Figure 2: 4x4 AIE representation

For this presentation, see Figure 2, we work with a mesh of 4x4 AIE2 cores connected by 4 horizontal and 4 vertical interconnections (we shall presents estimates for square 2x2, .. $i \times i$.. 8x8 and

rectangular shapes are in the works). Each core has 8 banks memories for a total 64KB. About 6 banks are used as input/output/weight buffers and 2 banks are used as temporary space for kernels. Each core can request and send data to its direct neighbors (if aware of connection and control). Double buffering as ping/pong is commonly used for inputs and outputs.

There are four mem-tiles: each 512KB and each can either be connected to one columns and its direct neighbor column, or it can be connected to a row and its neighbor. The total amount of space is 2MB. Memtile is a circular buffer to exploit more flexible allocation, implicitly a 2×2 architecture will have one memtile per column and a total of two (1MB).

A Memtile can broad-cast data per column or per row. We can dedicate a memtile for weights, one for activations, or we can share. We shall show mostly shared configurations. To maximize the computation parallelism, every core will write data per column into memtile: there are different designs that can be used. We shall explore the case where Inputs/Outputs/Weights are evenly distributed across mem-tiles although the distribution is different per tensor.

4.2 Sub Volume, Data compression and Data Movement

The computation is split by column (cores columns): each output tensor is split evenly by width, so each memtile will store different columns by width, each core will compute different output channels, and the computation streams computing the height of the tensor by using core input and output ping/pong. As often as possible, we store the weights in the core and we reuse them as much as possible (unless we need to stream the weight instead). The set of cores is a cohort and we always choose symmetric computations. This means that we do not merge two operations like convolution and max-pool and give three columns to convolution and one column to max-pool.

If we have the inputs, output, and weights in memtile, what is the largest computation we can do in the AIE? The minimum computation is at least one output channel and one row (by height). If this is not possible, we try to reduce the size of the width (e.g., shaping the tensor in memtile by using DDR spills) and we can manage to split the input channels and to split the weights accordingly and prepare for accumulation. We call W-Split the distribution of tensor by columns in the AIE mesh. We can COUT-split, this will require the partial transfer of weights (but we can stream by height). We can CIN-split when we need to split by input channel, this is the last resort because it is also the most expensive (accumulation of the outputs).

At this stage, the subvolume describes the smallest shape of the weights we need to manage. We compress the weight accordingly to such a subvolume so that any data movement will always be a multiple of the subvolume and can be a single load. Such a compress data will have the same properties whether it is sparse or dense. Of course, sparse data is smaller and we compute fewer operations.

4.3 Schedule and memory allocation

During the scheduling of each layer, we evaluate what can fit in mem tile. Here, activation and weight tensors share the space. It

means that an input tensor is distributed among the memtiles identified by one starting address and a final address and so the weights. At each step the memory allocation will check if we can allocate. If we cannot, we evict all tensors into DDR and then split/time the computation.

At the end of this stage, every tensor will be associated to an address in memtile or DDR (or both). If there are only DDR addresses, the compiler will take the basic computation and, by heuristics, will split the computation (thus the output tensor) by width, output channel, height, and input channel (non necessarily in this order). Every computation will have its data movements for the first two levels of the memory hierarchy. The heuristics have a simple objective: find the largest problem fitting the memory level.

We use an implementation that takes a recursive approach in tiling: For clarity, Σ is a sum or reduction and $\dot{\Sigma}$ is a parallel loop and a W-split can be written as

$$Y = \text{Conv}(X, W) = \sum_w \text{Conv}(X_w, W) \quad (7)$$

The split is pre-computed as function of the foot print, before and after each convolution there will be an explicit data movement. At this stage each input, output, and weights will have addresses associated with each sub-computation. Then the code generation of each $\text{Conv}(X_w, W)$ is independent and, recursively and as needed, there will be specific splits of the computation accordingly. This is a tree (i.e, a root with w children instead of a loop with w iterations, we do not have support for loops at this level). If the convolution has strides and large kernel, each sub-convolution may have overlap data but defined addresses and data movement if necessary. For example, computing the output by rows and the weights are reused.

Note scheduling and memory allocation among layers is a hard problem and often barely addressed by other systems. We addressed as first requirements.

4.4 Code Generation

The compiler recursively creates a list of operations smaller and smaller that can actually be executed Mem-Tile to Mem-Tile. In practice, there is a further decomposition using only AIE cores but it is completely determined by the subvolume computation. Here, we shall show how we produce the execution time estimates as in Figure 3. This is the computation of a convolution with top/bottom padding by height:

$$Y_{\text{height}} = \text{Conv}(X_{h=0}) + \sum_{h=1}^9 \text{Conv}(X_w) + \text{Conv}(X_{h=10}) \quad (8)$$

An important feature of the current system is the concept of **iteration** between mem-tile and core: Using locks and chaining them (locks like in semaphores): We can write a single instruction from the prospective of a single core (as a SIMD instruction) but driving all cores at once (ASM-like code) for multiple iterations ($\sum_{h=1}^i \text{Conv}(X_w)$):

```
LOADFM Lock k_0 mem-tile addr core addr iter i
CONV iteration i
WRITEFM Lock k_1 mem-tile addr core addr iter i
```

There is an implicit lock (say k_x) that is used for the pong and the system cycles in between locks (k_x and k_0). These three operations will be execute a number of iterations i and using a ping/pong

they will load different slices of data and compute different slices of data.

In our environment padding is common and we can manage by a custom load (from memtile to core) and this requires a custom load that will not be repeated

```
## Head top pad < 50 us First comp block
LOADFM Lock k_0 mem-tile addr_0 core addr iter 1
CONV iteration 1
WRITEFM Lock k_1 mem-tile addr_1 core addr iter 1
## Body iteration > 50 us < 150 us
## k_0 -> k_2 -> k_4 Lock Chain
LOADFM Lock k_2 mem-tile addr_2 core addr iter 9
CONV iteration 7
WRITEFM Lock k_3 mem-tile addr_3 core addr iter 9
## tail bottom pad > 150 us Last computation block
LOADFM Lock k_4 mem-tile addr_4 core addr iter 1
CONV iteration 1
WRITEFM Lock k_5 mem-tile addr_5 core addr iter 1
```

See Figure 3 for how this code will play out in practice. At this stage we have all the information we need. Per layer, the code generation is a two pass process: first, we generate code for the all load/store and then we combine them into chains having dependency so that to be logically correct and as fast as possible. Take the code above and we introduce a chain information.

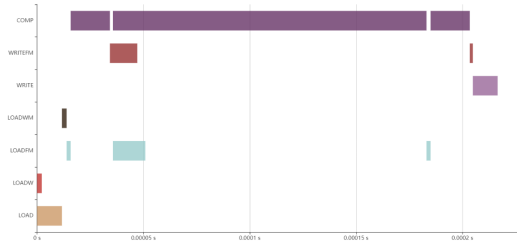


Figure 3: Resnet single convolution with padding for 4x4: legend AIE: LOAD Activation DDR to Mem, LOADW weights DDR to Mem, LOADFM Activation Mem to AIE2 cores, LOADW weights Mem to AIE2, WRITE Mem to DDR, WRITEFM AIE2 to Mem, COMP Computation

4.5 Time Estimation

At this stage, we need to explain how we can capture the execution time and visualize it as in Figure 3.

We start by the Time estimates for DDR to Mem-Tile. We have two communication types: activations and weights. Per mem-tile there are two dedicated channels.

- If we share activations and weights in the same mem-tile, we can use one channel for activations and one for weights. Thus the loads from DDR to MEM-tile (LOAD and LOADW) are parallel with a bandwidth of 4GB/s. Writes from mem-tile to DDR (WRITE) can use both channels (8GB/s).
- If activations and weights go to different mem-tiles (2 and 2), each load is parallel and 8GB/s. Writes are identical.

Although, mem-tile are circular buffers to improve the memory allocation, the streaming is not applicable here.

The Memtile connections with AIE cores can be designed differently. We assume here a few channels with again 4GB/s bandwidth. One memtile can broadcast inputs to a cores column (and to the nearest neighbor). These communications are for activations (LOADFM). One Memtile can broadcast to rows of cores (or the nearest neighbor), these are for weights (LOADWM). We assume that the column and row communications are parallel and each memtile core connection is parallel.

Every communication with iteration 1 is synchronous and sequential: the load, convolution, and store is executed one after the other but every core is independent. For synchronization and for bookkeeping, we assume that AIE2 weights communication (from memtile) to core are synchronous and halting.

Every communication with iteration larger than one, we assume that load, computation (COMP), and store (WRITEFM) are executed in parallel and the overall execution time is the maximum of the estimated time multiplied by the number of iterations.

We estimate the execution time of a subvolume by the number of operations divided by the maximum number of operations per cycle which is in our scenario: $4 \times 8 \times 8 = 256$ operations per cycle and 1GHz frequency. This is obviously a very optimistic validation. The execution time is a feature of the analysis but for us the estimate of the communications is more compelling and we can easily mute the computation contribution. Note however, that sparsity really reduces the computation time.

We do not account the wait and synchronization which are necessary to reprogram the fabric. These are very expensive running on a few milliseconds.

4.6 Convolution example

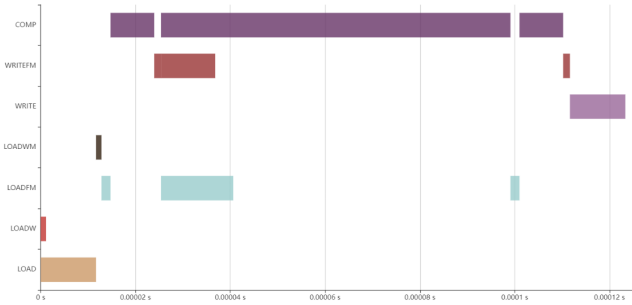


Figure 4: Resnet single convolution with padding and sparsity for 4x4 AIE

Here and in Figure 3 and 4, we give a full convolution example with and without sparsity and with padding. In this way we can explain how the time is really estimated and also how the hardware works in principle.

It is clear from the Figures above that there are three computations (COMP). We load the weight and activations once in memtiles. There are actually one load per memtile for a total of 4 loads per activations and 4 loads for weights. Because each load is to a different memtile, they are parallel. The activation and weights communications are using two different channels and then are in parallel with 4GB/s bandwidth.

There is a single load of the weights from mem-tiles to each core. This is done once and it is blocking (LOADWM) but it can be as easily made non blocking and parallel to the activations. There is a computation using padding (top-padding) and you can see the sequential execution of load to cores (LOADFM), computation (COMP), and write to memtile (WRITEFM). This computation has iteration 1. There are 9 iterations for three instructions: we can see the load, the computation, and write in parallel. This is obviously a simplification; there will be a little load poking out at the beginning and a writing poking out at the end. Then we conclude with the final computation with padding at the bottom of the computation.

In this particular scenario, the computation dominates the execution time and compression basically cut the execution time by half: from 200 μ s to 130 μ s. There are convolutions in Resnet that realize up to $2\times$ performance but also there are convolutions that are dominated by the read or by the writing, and where sparsity help only in space saving. We shall relax sparsity requirements for those convolutions.

5 RESULTS

Table 2: Execution Time estimates

AIE2	Model	Dense sec	Sparse sec
2x2	Resnet	2.492347e-02	1.582626e-02
3x3		1.269543e-02	8.661490e-03
4x4		1.077318e-02	7.064918e-03
5x5		failed	4.303485e-03
6x6		5.712521e-03	4.490127e-03
7x7		4.205991e-03	3.212234e-03
8x8		6.376768e-03	4.602027e-03
2x2	IncV3	4.283837e-02	2.440544e-02
3x3		2.386600e-02	1.422390e-02
4x4		1.740967e-02	1.012540e-02
5x5		9.690552e-03	failed
6x6		1.063962e-02	6.439692e-03
7x7		8.727651e-03	failed
8x8		9.093276e-03	5.666152e-03
2x2	VGG16	4.476212e-02	2.608593e-02
3x3		failed	1.002015e-02
4x4		1.371000e-02	8.852128e-03
5x5		failed	4.336479e-03
6x6		failed	5.770197e-03
7x7		7.455440e-03	5.288551e-03
8x8		9.203393e-03	6.502333e-03

In Table 2, we present the performance of sparsity applied to all the convolutions (except the first one) for Resnet 50, Inception V3, and VGG16.

When we generate the code for each instruction, we compute the execution time. So if we inspect the assembly code we will find time information in the context whether or not each instruction contribute directly. For data movement to and from DDR and memtile, we reduce the contribution (sum directly). There is no streaming or communication overlapping, thus the sum.

For mem-tile to and from core communications and core computations, we create a time series. We explain in the previous section how we account for the execution time for instruction with and without iterations. All of this will be an attribute of the layer (node in the graph computation). To create a complete time estimate, we just need to take the schedule of the computation and the graph, visit each node accordingly to the schedule, write a *json* file describing the time series, then by *javascript* we can visualize the time series using a browser. The Figures in this paper are generated directly.

For a 4×4 AIE set up, Resnet 50 fits in memtile from the beginning to the last operation (beside the first convolution and this is by construction). The estimates advantage by sparsity is almost completely achieved. We provide with the software also all the experimental results and showing the compiler output in long form.

Corner cases are represented as failure in Table 2. Some cases is because of inability to break the weight tensor evenly, sometime is for incorrect data management especially for prime numbers. These are all issues will be address as the technology matures. Please, note that VGG16 using 8×8 is slower than 7×7 by using sparse. It may happen because a symmetric computation my use too small sub-volume computations and thus more iterations.

6 CONCLUSIONS AND CONTEXT

This is a multifaceted problem and we present a complete solution from training techniques, compilers, code generation, HW definition, and time estimations. It is a vertical software system and more complex than just a prototype.

This could be seen as a quantization and sparsification problem: How to reduce the footprint of a CNN network. There are post training techniques that are targeting quantization and unstructured sparsity [7] and all the references within. We need to be more aggressive and training for it (as starting point [9]), our sparsity is not really a property of the model and software can describe it and the hardware can take advantage (but we do not need to have hardware support at instruction level).

This work stemmed from a collaboration between Xilinx and Numenta and the idea set forward by the authors in [2], where the model are too dense and there is a lot we can do about it.

The difficulty of generate code for complex architectures can be described and solved in different ways. There are recent attempts of introducing SW/HW solution for spatial processors like ours [4, 10, 15]. Usually major attention is given only to matrix multiplication and GPUs [8] [13], we can work on only static sparsity at this time.

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