Entropy Maximization in Sparse Matrix by Vector Multiplication ($\max_E SpMV$)

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The peak performance of any SpMV depends primarily on the available memory bandwidth and its effective use. GPUs, ASICs, and new FPGAs have higher and higher bandwidth; however, for large scale and highly sparse matrices, SpMV is still a hard problem because of its random access pattern and workload imbalance. Here, we show how to turn randomness to our advantage. We propose a matrix permutation pre-processing step that aims to maximize the entropy of the distribution of the nonzero elements. We seek any permutation that uniformly distributes the non-zero elements' distribution, thereby generating a SpMV problem that is amenable to work load balancing or to speed up sort algorithms. We conjecture these permutations would be most effective for matrices with no dense rows or columns and, as in preconditioning, when the matrix is reused. We shall show that entropy maximization is an optimization that any architecture may take advantage although in different ways. Most importantly, any developer can consider and deploy. We shall present cases where we can improve performance by 15% on AMD-based (GPU-CPU) systems.

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1 INTRODUCTION

To define the scope of our work, the obvious questions to ask are: first, what randomization or entropy maximization is in the context of sparse matrices; second, why would we use it; third, when it does work. We shall provide formal definitions in the following sections. Here briefly, we will permute randomly the rows and columns of a sparse matrix before multiplying it by a dense vector (SpMV) with the aim of speeding this operation (accordingly the input and output vectors will be permuted).

$$(P_r \mathbf{y}) = (P_r \mathbf{A} P_c) * (P_c^{-1} \mathbf{x})$$

$$\tag{1}$$

Undoubtedly, this scheme requires some restrictions about the matrix structure: for example, it must have no or few dense columns or rows. In this unfortunate case, a sparse/dense partitioning scheme should be used and different algorithms/hardware could be deployed separately instead. Here suffice to say that the partitioning advantages rely on a clear definition of density. For the remainder of this manuscript, we shall assume the former nonzero structure. We use randomization because it is the poor man's way for preconditioning SpMV in our context, and we do not mean it in a pejorative sense.

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Preconditioning speeds up the convergence rate of an iterative linear solver by linearly transforming the associated matrix into a form that affords a faster reduction of the residual error at every iteration. The cost of this transformation is justified by the runtime reduction it affords. Likewise, we foresee randomization playing a similar role for SpMV in the context of iterative linear solvers and other methods (e.g in convolutions) where the matrix is reused.

Sparse linear algebra and GraphBLAS kernels are memory bound and there is a common thread in the scientific computing community to develop acceleration libraries mostly for multi-core systems. These predominantly include multi-core processors and GPUs. The goal is a balanced work distribution and, when applicable, minimal communication [6, 11]. When storage strategy and algorithms must be considered together then GPUs provide the work horse for abundant thrust in research [1]. These works aim at optimal solutions and strive for a clear and complete understanding/exploitation of the software-hardware interface; usually the hardware is composed of symmetric computational units. Interestingly, the SpMV's space and time complexity, which are small, may not warrant more performance because we typically end up utilizing only one-thousandth fraction of the available hardware capacity.

The peak performance of any SpMV accelerator depends primarily on the available memory bandwidth (i.e., DRAM such as DDR or HBM) and the capability of the accelerator to effectively use it. Because SpMV is memory-bound, a more important metric than peak performance alone is the fraction of bandwidth utilized, which captures the overall efficiency of the architecture. GPU platforms exhibit very high bandwidth, see the experimental Section 8: Ellesmere DDR5 224GB/s, Fiji HBM 512GB/s, and Vega 20 HBM 1TB/s. Although utilizing this much bandwidth efficiently is difficult for large scale and highly sparse matrices due to very high random access pattern. Custom architectures based on FPGA or ASIC devices can maximize bandwidth utilization by highly customized data-paths and memory hierarchy designs [3, 4, 13]. Most of the existing accelerators saturate the relatively low memory bandwidth available on FPGA platforms (less than 80 GB/s) [3, 4, 8, 10, 12, 13]. Modern FPGA platforms have multiple HBM stacks to provide large memory bandwidth. However, there is no implementation (currently available) that saturates all of the available DRAM bandwidth for SpMV kernel on HBM-enabled FPGA platforms. Scalability of accelerator design remains a major concern, and it is an active area of research.

FPGA platforms used in early works exhibit low peak performance due to the scarcity of external memory bandwidth [3, 7, 14]. For example, Microsoft's implementation of SpMV uses an FPGA platform which only has 2 DDR2-400 memory banks with a resulting bandwidth of 6.4 GB/s [7]. The accelerator is running at 100 MHz, it reads 64 Bytes of data every cycle, which corresponds to 5 non-zeros at every cycle (a non-zero is about 12 Bytes). At best, the peak performance is 10 double precision operations every cycle at 100 MHz, which is 1 GFLOPS (only). In 2009, Convey systems Inc. released the Convey HC-1 FPGA platform. It has 16 DDR2-677 memories resulting in overall 80 GB/s memory bandwidth [10]. The accelerator logic runs at 150 MHz. It consumes 512 Bytes of data every cycle, which corresponds to around 40 non-zeros every cycle. At best, the peak performance is 80 double precision operations every cycle at 150 MHz, which is 12 GFLOPS.

One of the key building blocks for custom architecture solutions is a multi-ported buffer used to storing vector entries [3]. During execution, multiple column indices are used as addresses to read corresponding vector entries; we shall provide more details about the application in Section 2. Designing a buffer with a very large number of read ports is challenging. One solution is *banking* as a mechanism to store partitioned vector entries. Although banking could allow very high throughput indexing unless the same entry is required multiple times and its reads are purely sequential causing loss of bandwidth. For example, hashing techniques and data duplication are possible solutions for this problem. However, another issue arises: When we distribute SpMV computations across *p*-nodes, some of the nodes, say *k*, finish later than the rest because of unbalanced work loads (i.e.,

number of nonzero element) in row/column major traversal. This is a common phenomena for matrices where few rows or columns are dense. These k nodes are referred to as *laggard nodes*. By applying random permutation of columns/rows, we are attempting to balance the loads across all p workers so that there are no laggards. From this hardware vantage point, randomization or maximizing the entropy of the non-zero element distribution is an optimization transform and provides a clear context for our work.

Clearly, accelerating SpMV is a hard many-parameters optimization problem dependent on the choice of algorithm, data structures, and dedicated hardware (CPU, GPUs, FPGA's, Custom ASIC's). Rather, our goal is to provide a tool, we may say a naive tool, to help understand how the structure of the matrix may affect the HW-SW solution. For the readers in the field of algorithms, SpMV can be mapped into a sorting algorithm. For example, finding elements $x_{i,j}$ and $x_{i,k>j}$ in a sparse matrix requires to find row i and then columns j and k. Sorting is a method to find if an element is in a list with no prior or limited knowledge of its contents. Sorting can be used to prepare the matrix and to find elements in between sparse matrices and sparse vectors. In custom architectures, sorting networks are used to route matrix and vector elements to functional units. In a sense, if one is stuck with a sorting algorithm and a poor distribution, randomization may alter the distribution and throttle performance. Interestingly, the best sorting algorithm is a function of the distribution of the elements [5, 9].

We organize this work as follows: In Section 2, we define the matrix by vector operation; in Section 3, we define what we mean by randomization or entropy maximization. We use randomization to create a uniform distribution in Section 5 and measure uniformity by entropy in Section 4. We present how we drive our experiments to show the effects of randomization in Section 6. In the last sections, we present a summary of the results: we present our work loads for the given benchmarks in Section 7, and the complete set of measures for an AMD CPU and GPUs systems in Section 8.

2 BASIC NOTATIONS

Let us start by describing the basic notations so we can clear the obvious (or not). A Sparse-matrix by vector multiplication SpMV on an (semi) ring based on the operations (+,*) is defined as $\mathbf{y} = \mathbb{M}\mathbf{x}$ so that $y_i = \sum_j M_{i,j} * y_j$ where $M_{i,j} = 0$ are not represented nor stored. Most of the experimental results in Section 8 are based on the classic addition (+) and multiplication (*) in floating point precision using 64 bits (i.e., double floating point precision) albeit are extensible to other semi-rings. For instance, it is well known that SpMV defined on the semi-ring (min,+) is a kernel in computing an all-pairs shortest paths starting with a graph adjacency matrix, and in using a Boolean algebra we can check if two nodes are connected, which is slightly simpler.

We identify a sparse matrix \mathbb{M} of size $M \times N$ as having O(M+N) non-zero elements, number of non zero nnz. Thus the complexity of $\mathbb{M}x$ is $O(M+N) \approx 2nnz$. Also, we must read at least nnz elements and thus the complexity is $\Theta(M+N) \approx nnz$. We can appreciate that reading the data is as complex as the overall operation. Of course, the definition of sparsity may vary. We represent the matrix \mathbb{M} by using the coordinate list COO or and the compressed sparse row CSR^1 formats. The COO represents the non-zero of a matrix by a triplet (i, j, v); very often there are three identical-in-size vectors for the ROW, COLUMN, and VALUE. The COO format takes $3 \times nnz$ space and two consecutive elements in the value array are not bound to be neither in the same row nor column. In fact, we know only that $VALUE[i] = M_{ROW[i],COLUMN[i]}$.

The CSR format stores elements in the same row and with increasing column values consecutively. There are three arrays V, COL, and ROW. The ROW is sorted in increasing order. Its size is M, and ROW[i] is an index in V and COL describing where i-th row starts (i.e., if row i exists). Accordingly,

 $^{^{1}}$ a.k.a. Compressed row storage CRS.

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 $M_{i,*}$ is stored in V[ROW[i] : ROW[i+1]]. The column indices are stored at COL[ROW[i] : ROW[i+1]] and sorted increasingly. The CSR format takes $2 \times nnz + M$ space and a row vector of the matrix can be found in O(1).

The computation $y_i = \sum_j M_{i,j} * x_j$ is a sequence of scalar products and, using the CSR format, is computed as follows:

$$Index = ROW[i] : ROW[i+1]$$
$$y_i = \sum_{\ell \in Index} V[\ell] * x_{COL[\ell]}$$

The matrix row is contiguous (in memory) and rows are stored in increasing order. However, the access of the dense vector x has no particular pattern, well increasing.

The COO format can be endowed with certain properties. For example, we can sort the array by row and add row information to achieve the same properties of CSR. In contrast, transposing a "sorted" COO matrix simply entails swapping of the arrays ROW and COL. Think about matrix multiply (one of us does constantly). Each scalar product achieves peak performance if the reads of the vector x are streamlined as much as possible and so the reads of the vector V. If we have multiple cores, each could compute a subset of the y_i and a clean data load balancing can go a long way. If we have few functional units, we would like to have a constant stream of independent * and * operations but with data already in registers. That is, data pre-fetch will go a long way especially for $x_{COL[i]}$, which may have an irregular pattern.

3 RANDOMIZATION AND ENTROPY MAXIMIZATION

We define Randomization as row or column permutation transform of the matrix \mathbb{M} (thus a permutation of y and x), and we choose these by a pseudo-random process. The obvious question is to as why should we seek randomization transforms? The sparsity of a given matrix \mathbb{M} has a non-zero element distribution induced by the nature of the original problem or by some imposed ordering on the respective nodes of its associated graph. This distribution may be computationally incompatible with the chosen algorithm or architecture. For instance, it can induce some load imbalance in the computation. We could break this load imbalance by seeking to maximize entropy for this distribution. Our conjecture is that would favor the average case performance rather than the worse case when operating on the "max-entropy transformed" matrix.

For linear system solvers, if we know the matrix \mathbb{M} , and we know the architecture, preconditioning (when affordable) is a better solution. If we run experiments long enough, we choose the best permutation(s) for the architecture, permute \mathbb{M} , and go on testing the next. On one end, preconditioning exerts a full understanding of both the matrix (the problem) and how the final solution will be computed (architecture). On the other end, the simplicity of a random permutation requires no information about the matrix, the vector, and the architecture. Such a simplicity can be exploited directly in Hardware. We are after an understanding when randomization is just enough: We seek to let the hardware do its best with the least effort, or at least with the appearance to be effortless.

Interestingly, this work stems from a sincere surprise about randomization efficacy and its application on custom SpMV. Here, we wish to study this problem systematically so that to help future hardware designs. Intuitively, if we can achieve a uniform distribution of the rows of matrix \mathbb{M} we can have provable expectation of its load balancing across multiple cores. If we have a uniform distribution of accesses on x we could exploit column load balancing and exploit better sorting algorithms: In practice, the reading of $x_{COL[i]}$ can be reduced to a sorting, and there we know that different sparsity may require different algorithms. This may be a lot to unpack but it

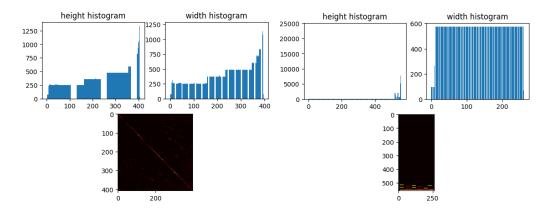


Fig. 1. Left: OPF 3754. Right: LP OSA 07. These are histograms where we represent normalized buckets and counts

translates to a better performance of the sequential algorithm without changing the algorithm or to improved bandwidth utilization.

We will show that (different) randomness affects architectures and algorithms differently, making randomization a suitable optimization transform especially when the application and hardware are at odds: Hardware (unless programmable) is difficult to change and the matrix sparsity is simple to change. We want to show that there is a randomness hierarchy that we can distinguish as global and local. There are simple-to-find cases where the sparsity breaks randomness optimization. For instance, matrices with dense rows or columns are better partitioned into sparse and dense components and operated on separately.

4 ENTROPY

Patterns in sparse matrices are often visually pleasing, see Figure 1 where we present the height histogram, the width histograms, and a two-dimensional histogram as heat map. We will let someone else using AI picture classification. Intuitively, we would like to express a measure of uniform distribution and here we apply the basics: *Entropy*. Given an histogram $i \in [0, M-1]$ $h_i \in \mathbb{N}$, we define $S = \sum_{i=0}^{M-1} h_i$ and thus we have a probability distribution function $p_i = \frac{h_i}{S}$. The *information* of bin i is defined as $I(i) = -\log_2 p_i$. If we say that the stochastic variable X has PDF p_i than the entropy of X is defined as.

$$H(x) = -\sum_{i=0}^{M-1} p_i \log_2 p_i = \sum_{i=0}^{M-1} p_i I(i) = E[I_x]$$
 (2)

The maximum entropy is when $\forall i, p_i = p = \frac{1}{M}$; that is, we are observing a uniform distributed event. Our randomization should aim at higher entropy numbers. The entropy for matrix LP OSA 07 is 8.41 and for OPF 3754 is 8.39. We use the entropy specified in the Scipy stats module. A single number is concise and satisfying. If you are pondering why they are so close contrary to their sparsity we discuss this next.

5 UNIFORM DISTRIBUTION

We know that we should **not** compare the entropy numbers of two matrices because entropy does not use any information about the order of the buckets, it uses only their probabilities. By

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construction, the matrices are quite different in sparsity and in shapes, however their entropy numbers are close. Two matrices with the same number of non-zeros, spaced well enough in the proper number of bin, will have the same entropy. To appreciate their different sparsity, we should compare their entropy distributions by Jensen-Shannon measure [2] or we could use cumulative distribution function (CDF) measures, which imply an order. Here, we use a representation of a hierarchical 2D-entropy, see Figure 2, where the entropy is split into 2x2, 4x4 and 8x8 (or fewer if the distribution is not square). We have hierarchical entropy heat maps.

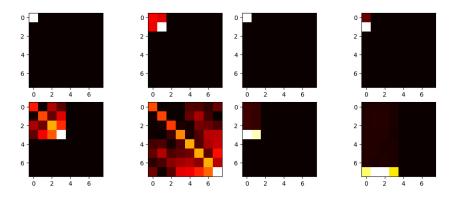


Fig. 2. Hierarchical 2D entropy for OPF 3754 (left) and LP OSA 07 (right).

We can see that even a small 2D-entropy matrix summarizes the nature of the original matrix because it has spatial information. In this work, the entropy matrix is used mostly for visualization purpose more than for comparison purpose. Of course, we can appreciate how the matrix LP OSA 07 has a few very heavy rows and they are clustered. This matrix will help us showing how randomization need some tips. Now we apply row and column random permutation once by row and one by column: Figure 3: OPF has now entropy 11.27 and LP 9.26. The numerical difference is significant. The good news is that for entropy, being an expectation, we can use simple techniques like bootstrap to show that the difference is significant or we have shown that Jensen-Shannon can be used and a significance level is available. What we like to see is the the hierarchical entropy heat map is becoming *more* uniform for at least one of the matrix.

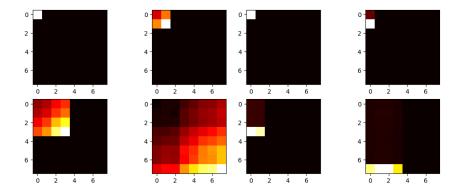


Fig. 3. Hierarchical 2D entropy after row and column random permutation for OPF 3754 (left) and LP OSA 07 (right).

In practice, permutations need some help especially for relatively large matrices. As you can see, the permutation affects locally the matrix. Of course, it depends on the implementation of the random permutation, we use *numpy* for this. It is reasonable that a slightly modified version of the original is still a random selection and unfortunately they seem too likely in practice. We need to compensate or help the randomization. If we are able to identify the row and column that divide high and low density, we could use them as pivot for a shuffle like in a quick-sort algorithm. We could apply a sorting algorithm but its complexity will the same of SpMV. We use a gradients operations to choose the element with maximum steepness, Figure 4 and 5.

LP achieves entropy 8.67 and 9.58 and OPF achieves 10.47 and 11.40.

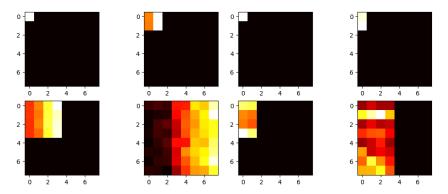


Fig. 4. Hierarchical 2D entropy after height gradient based shuffle and row random permutation for OPF 3754 (left) and LP OSA 07 (right).

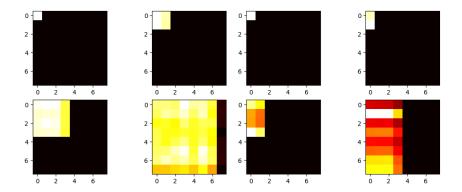


Fig. 5. Hierarchical 2D entropy after height and width gradient shuffle and row and column random permutation for OPF 3754 (left) and LP OSA 07 (right).

If the goal is to achieve a uniformly sparse matrix, it seems that we have the tools to compute and to measure such a sparsity. We admit that we do not try to find the best permutation. But our real goal is to create a work bench where randomization can be tested on different architectures and different algorithms. A randomization with a measurable uniform distribution is preferable than just random. We are interested to find out when random is enough or not enough. Also, consider that to achieve a uniform distribution, we do not need a random transformation and any permutation balancing the number of non-zero is possible, but for now not looked for.

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6 MEASURING THE RANDOMIZATION EFFECTS

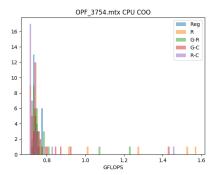
Whether or not this ever applied to the reader, when we have timed algorithms (i.e., measure execution time), we came to expect variation. The introduction of randomization may hide behind the ever present variance, after all these are algorithms on *small* inputs: small error can be comparable to the overall execution time. Here, we must address this concern even before describing the experiments.

First, we execute every algorithm between 1000 and 5000 times. The time of each experiment is in the seconds, providing a granularity for which we are confident the measuring time error is under control. Thus, for each experiment we provide an average execution time: we measure the time and we divide by the number of trials. Cold starts, the first iteration, are still accounted. To make the measure portable across platform we present GFLOPS, that is, Giga (10^{12}) floating operations per second: 2*nnz divided by the average time in seconds.

Then we repeat the same experiment 32 times. Permutations in *numpy* Python uses a seed that is time sensitive: thus every experiment is independent from the previous. The number 32 is an old statistic trick and it is a minimum number of independent trials to approximate a normal distribution. In practice, they are not but the number is sufficient for most of the cases and it is an excellent starting point.

A short hand legend: **Reg** is the regular matrix without any permutation; **R** stands for random *Row* permutation; **G-R** stands for gradient-based row shuffle and random row permutation; **G-C** stands for gradient-based column shuffle and random column permutation; **R-C** stands for random row and column permutation. This legend is used in the pictures to be concise, in the tables in the following sections, we use a verbose description. We shall clarify the gradient based approach in the experimental results section 8. Intuitively, we help the random permutation by a quick targeting of high and low volume of the histogram (and thus the matrix).

In Figure 6, we show two plots respectively of the CPU performance using COO and CSR SpMV algorithms for the matrix OPF 3754. The figure represents histograms: The x is GFLOPS and the y label is the number of counts. Thus we show what is the performance distribution of an algorithm. We can see that the CSR algorithms are consistent and the Regular (i.e., the original) has always the best performance. Also the variance of the computation time is small and the shape is approximately Gaussian. Different story for the COO, the permutations introduce long tails, thus $2\times$ performance advantage.



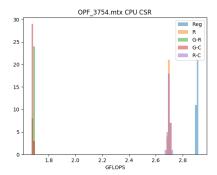


Fig. 6. CPU COO (left) and CPU CSR (left) for OPF 3754

If we take the original matrix and split into parts having the same number of rows, and execute them in parallel using different cores, we can see in Figure 7 that randomization is quite useful.

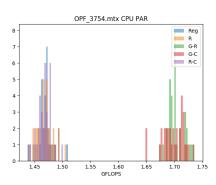


Fig. 7. Parallel CPU CSR for OPF 3754

In Figure 8, 9 and 10, randomization is harmful to the GPU implementation. The OPF 375 matrix is mostly diagonal, thus the vector x is read in close quarters, randomization breaks it. If the load balance is fixed (i.e., by dividing the matrix by row and in equal row), randomization is beneficial.

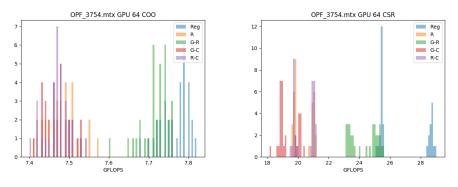


Fig. 8. Vega 20, GPU 64bits COO (left) and GPU CSR (right) for OPF 3754

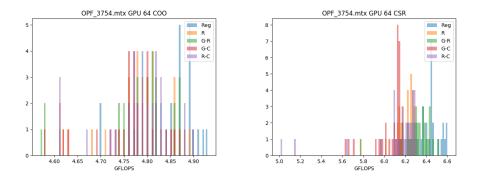
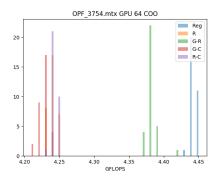


Fig. 9. Ellesmere, GPU 64bits COO (left) and GPU CSR (right) for OPF 3754

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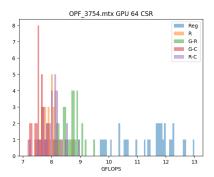


Fig. 10. Fiji, GPU 64bits COO (left) and GPU CSR (right) for OPF 3754

For matrix LP OSA 07, randomization helps clearly only for CPU CSR as we show in Figure 11. In Figure 12, 13, and 14, we can see that randomization is harmful but for one GPU, we can show that a single exception is possible (40% improvement).

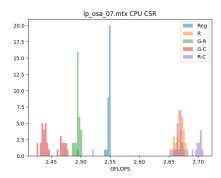
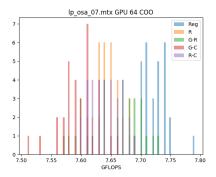


Fig. 11. CPU CSR for LP OSA 07



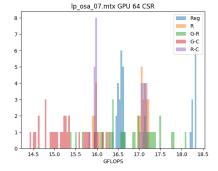


Fig. 12. Vega 20, GPU 64bits COO (left) and GPU CSR (right) for OPF 3754

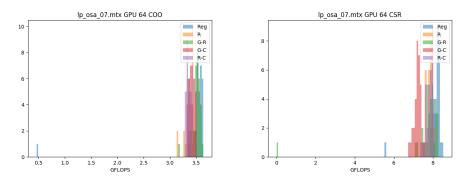


Fig. 13. Ellesmere, GPU 64bits COO (left) and GPU CSR (right) for OPF 3754

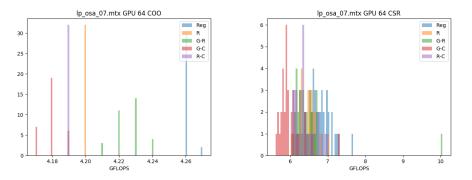


Fig. 14. Fiji, GPU 64bits COO (left) and GPU CSR (right) for OPF 3754

An example, the matrix MULT DCOP 01, is where randomization is useful for the CPU, GPU, and the parallel version Figure 15, 16 - 19 and the gains can be up to 10-15%. Consider, we can achieve these improvements without any insights to the architecture, the algorithms and their relationships.

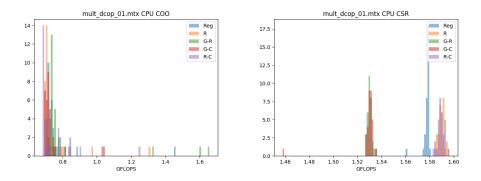
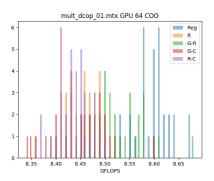


Fig. 15. CPU COO (left) and CPU CSR (right) for MULT DCOP 01

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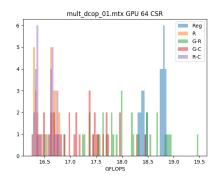
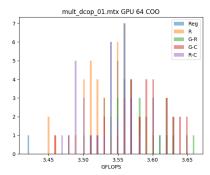


Fig. 16. Vega 20, GPU 64bits COO (left) and GPU CSR (right) for MULT DCOP 01



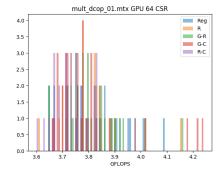
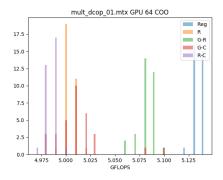


Fig. 17. Ellesmere, GPU 64bits COO (left) and GPU CSR (right) for MULT DCOP 01



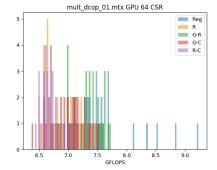


Fig. 18. Fiji, GPU 64bits COO (left) and GPU CSR (right) for MULT DCOP 01

What does it mean when randomization does not work? The matrices we use in this work are not chosen randomly (pun not intended), they are the matrices that are difficult to handle in our custom SpMV engines using a combination of sorting networks and systolic arrays. If randomization does not work in our simplified work bench, will not work in our specialized architecture because the reorganization of the matrix or the input and output vector does not have the necessary parallelism,

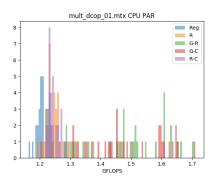


Fig. 19. Parallel CPU CSR for MULT DCOP 01

data locality, and data streaming. We need to do something else. In this case disrupting the memory pattern is not sufficient. Thus, if we cannot beat the pattern, we must exploit it, well not in this work.

7 WORKLOADS

In the previous sections, we defined what we mean for randomization and we present our tools of tricks for the measure of the effects of randomization. Here we describe the work loads, the applications, we use to test the effects of the randomization.

7.1 Python COO and CSR algorithms

The simplicity to compute the SpMV by the code z = A*b in Python is very rewarding. By change of the matrix storage format, A = A.tocsr(); z = A*b, we have a different algorithm. The performance exploitation is moved to the lower level. The CSR implementation is often two times faster but there are edge cases where the COO and COO with randomization can go beyond and be surprisingly better: MUL DCOP 03 is an example where COO can do well.

Intuitively, Randomization can affect the performance because the basic implementation is a sorting algorithm and it is a fixed algorithm. There are many sorting algorithms and each can be optimal for a different initial distribution. If we knew what is the sorting algorithm we could tailor the input distribution. Here we just play with it.

In Section 8, we present all the results for CPU and GPUS. Keep in mind that these problems are hard, in the sense they do not have fancy performance sheets (these architectures can achieve Tera FLOPs sustained performance for dense computations). If we go through diligently, we can see that there is a 15x performance difference between the single thread CPU and Vega 20 GPU (i.e, 3 vs 40 GFLOPS).

7.2 Parallel CSR using up to 16 cores

Python provides the concept of Pool to exploit a naive parallel computation. We notice that work given to a Pool is split accordingly to the number of elements to separate HW cores. We also noticed that the work load move from a core to another, thus not ideal. Also we notice that Pool introduce a noticeable overhead: a Pool of 1, never achieves the performance of the single thread z = A * b. Using Pool allows us to investigate how a naive row partitioning without counting can scale up with number of cores. We tested by splitting the rows to 1–16 cores evenly (one thread per core) and we present the performance for only the best configuration. The randomization goal is to

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distribute the work uniformly: a balanced work distribution avoid the unfortunate case where a single core does all the work. We are pleased by the simplicity of the benchmark and we know we can do better.

7.3 GPU COO and CSR algorithms

In this work, we use AMD GPUs and *rocSPARSE* is their current software. The software has a few glitches but overall can be used for different generation of AMD GPUs. We use the COO and CSR algorithms and we provide performance measure for double precision only. The ideas of using different GPUs: it is important to verify that the randomization can be applied independently of the HW. We are not here to compare performance across GPUs and CPUs. Often the limitation is the software, how the software can exploit the hardware or how the software will make easy to use a specific GPU. For example, the Fiji architecture is clearly superior to the Ellesmere, however the latter have better support and the system overall is more stable and user friendly.

The performance of the CSR algorithm is about two times faster than the COO. Most of the algorithms count the number of sparse elements in a row and thus they can decide the work load partition accordingly. Counting give you an edge but without changing the order of the computation there could be cases where the work load is not balanced and a little randomization could help and it does.

7.4 Randomization sometimes works

For the majority of the cases we investigated and reported in the following sections, Randomization does not work. However, there are cases where randomization does work and does work for different algorithms and architectures. If you are in the business of preconditioning, permutations are pretty cheap. If you can find a good one just consider like a preconditioning matrix, which it is.

This shows also that HW has to be more conscious, well the HW designer should, and accept that there are options at software level, at matrix level and beyond.

8 EXPERIMENTAL RESULTS

The main hardware setup is a AMD Threadripper with 16 cores. We have three Radeon GPUs: Vega 20 7nm, Pro 2xFiji, and Pro 2xEllesmere.

Vega 20 can deliver 3.5TFLOPS in double precision and it has 1TB/s HBM memory. Each Fiji provides 0.5 TFLOPS in double precision and has 512GB/s HBM, the card has two chips. The Ellesmere provides 0.3TFLOPS in double precision and has 224GB/s DDR5, the card has two chips. In the performance plots presented earlier and in the following, you will notice that the performance gap between these GPUs is not so marked. We can safely state that $vega \sim 2 \times Fiji$ and $Fiji \sim 2 \times ellesmere$

There are 4 basic randomization formats:

- Random Row Permutation, we take the original matrix and permute the rows.
- Random Row and Column Permutation, we take the original matrix and permute the rows and the columns.
- **Gradient based row permutation**, we compute the row histogram and we compute the gradient: $h_{i+1} h_i$. We find a single point where the gradient is maximum, this is the pivot for a shuffle like a magician would shuffle a deck of cards. Then we permute the two parts randomly.
- Gradient based row and column permutation, As above but also for the columns.

For large matrices (large number of columns and rows) a permutation tends to be a close variation of the original, still a random permutation. The gradient allows us to describe two areas of the

original matrix where there is a clear and de-marked density variation: for example, there are two uniform distributed sub matrices but one denser than the other. A shuffle redistributes every other sample/card to different parts and these can be permuted locally.

We report in the following the performance results GFLOPS, we introduce a * following the best performance. This is tedious to read and, we assure, to write. The code and the results are available as software repository. Remember each experiment is based on 32 different runs and thus we report maximum, minimum, and mean as a summary. We use the symbol H for entropy.

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9 VEGA VII	AND THREADRIPPER	Row-Premute	
	AND TIME/ADMITTER	Kow-Freiliute	CPU COO min 0.684 max 0.780 mean 0.705
mult_dcop_03.mtx			CPU CSR min 1.558 max* 1.596 mean 1.588
Regular	CPU COO min 0.728 max 0.880 mean 0.757		GPU 64 COO min 8.360 max 8.490 mean 8.433
	CPU CSR min 1.563 max 1.581 mean 1.577		CSR min 16.240 max 16.750 mean 16.552
	GPU 64 COO min 8.540 max* 8.670 mean 8.619		CPU PAR min 1.182 max 1.277 mean 1.242
	CSR min 18.320 max 18.930 mean 18.620	Row-Gradient	H min 10.737 max 10.742 mean 10.740
	CPU PAR min 1.170 max 1.269 mean 1.226	KOW-Gradient	CPU COO min 0.704 max 1.373 mean 0.790
D D	H min 9.689 max 9.689 mean 9.689		CPU CSR min 1.518 max 1.535 mean 1.529
Row-Premute	CPU COO min 0.710 max 0.845 mean 0.724		GPU 64 COO min 8.420 max 8.590 mean 8.517
	CPU CSR min 1.549 max* 1.597 mean 1.589		CSR min 16.680 max*19.550 mean 17.907
	GPU 64 COO min 8.360 max 8.540 mean 8.442		CPU PAR min 1.328 max* 1.713 mean 1.484
	CSR min 16.260 max 16.780 mean 16.551	Column-Gradient	H min 10.572 max 10.585 mean 10.581
	CPU PAR min 1.205 max 1.319 mean 1.263	COTUMNI OF BUTEFIL	CPU COO min 0.697 max 1.460 mean 0.742
Row-Gradient	H min 10.737 max 10.742 mean 10.740		CPU CSR min 1.517 max 1.534 mean 1.527
NOW GLAGIETT	CPU COO min 0.706 max 1.603 mean 0.806		GPU 64 COO min 8.330 max 8.490 mean 8.420
	CPU CSR min 1.493 max 1.534 mean 1.528		CSR min 16.020 max 18.390 mean 17.303
	GPU 64 COO min 8.430 max 8.610 mean 8.527		CPU PAR min 1.321 max 1.709 mean 1.557 H min 10.823 max*10.843 mean 10.835
	CSR min 17.070 max*18.970 mean 18.115	Row-Column-Permute	n IIIII 10.023 IIIdx^10.043 IIIedii 10.033
	CPU PAR min 1.331 max 1.695 mean 1.513	Now Column 1 Clinate	CPU COO min 0.691 max 0.746 mean 0.698
Column-Gradient	H min 10.576 max 10.585 mean 10.580		CPU CSR min 1.568 max 1.595 mean 1.587
COTUMNI-OF AUTERL	CPU COO min 0.694 max* 1.632 mean 0.797		GPU 64 COO min 8.350 max 8.500 mean 8.436
	CPU CSR min 1.491 max 1.534 mean 1.529		CSR min 16.250 max 16.780 mean 16.517
	GPU 64 COO min 8.350 max 8.520 mean 8.429		CPU PAR min 1.187 max 1.280 mean 1.228
	CSR min 15.970 max 18.180 mean 17.124	lp_fit2d.mtx	H min 10.739 max 10.743 mean 10.740
	CPU PAR min 1.321 max* 1.728 mean 1.514	Regular	
Day Caluma Damusta	H min 10.826 max*10.840 mean 10.833	negazar	CPU COO min 0.774 max 0.804 mean 0.793
Row-Column-Permute	CPU COO min 0.688 max 0.757 mean 0.696		CPU CSR min 2.538 max 2.550 mean 2.547
	CPU CSR min 1.490 max 1.595 mean 1.584		GPU 64 COO min 7.060 max 7.170 mean 7.101
	GPU 64 COO min 8.380 max 8.500 mean 8.445		CSR min 15.650 max*18.700 mean 18.031
	CSR min 16.230 max 16.780 mean 16.513		CPU PAR min 1.537 max 1.645 mean 1.590 H min 11.109 max 11.109 mean 11.109
	CPU PAR min 1.192 max 1.274 mean 1.237	Row-Premute	n milli ii.i05 max ii.i05 mean ii.i05
mult door 01 mtu	H min 10.737 max 10.742 mean 10.740		CPU COO min 0.740 max 0.776 mean 0.746
mult_dcop_01.mtx Regular			CPU CSR min 3.302 max* 3.328 mean 3.317
Regutal	CPU COO min 0.710 max 1.453 mean 0.761		GPU 64 COO min 7.040 max* 7.180 mean 7.098
	CPU CSR min 1.561 max 1.581 mean 1.578		CSR min 15.690 max 18.580 mean 16.732
	GPU 64 COO min 8.520 max 8.670 mean 8.597		CPU PAR min 1.327 max 1.482 mean 1.422 H min 11.098 max 11.105 mean 11.101
	CSR min 18.320 max 18.870 mean 18.636	Row-Gradient	III III II. 030 max II. 103 mean II. 101
	CPU PAR min 1.163 max 1.246 mean 1.212 H min 9.689 max 9.689 mean 9.689		CPU COO min 0.739 max* 2.092 mean 1.091
Row-Premute	n IIIII 9.009 IIIAX 9.009 IIIEAII 9.009		CPU CSR min 2.539 max 2.546 mean 2.543
	CPU COO min 0.699 max 1.305 mean 0.745		GPU 64 COO min 7.040 max 7.150 mean 7.100
	CPU CSR min 1.585 max 1.597 mean 1.590		CSR min 15.520 max 18.560 mean 17.547 CPU PAR min 1.401 max 1.661 mean 1.525
	GPU 64 COO min 8.360 max 8.520 mean 8.446		H min 11.109 max 11.109 mean 11.109
	CSR min 16.260 max 16.780 mean 16.528	Column-Gradient	
	CPU PAR min 1.192 max 1.298 mean 1.242 H min 10.738 max 10.742 mean 10.740		CPU COO min 0.726 max 2.065 mean 1.011
Row-Gradient	11 111 10.730 max 10.742 mcan 10.740		CPU CSR min 2.539 max 2.550 mean 2.546
	CPU COO min 0.709 max* 1.656 mean 0.819		GPU 64 COO min 6.800 max 7.140 mean 7.080
	CPU CSR min 1.527 max 1.535 mean 1.530		CSR min 15.480 max 18.560 mean 16.866 CPU PAR min 1.391 max* 1.737 mean 1.563
	GPU 64 COO min 8.450 max* 8.680 mean 8.527		H min 11.329 max 11.333 mean 11.331
	CSR min 16.520 max*19.480 mean 17.984 CPU PAR min 1.280 max 1.704 mean 1.485	Row-Column-Permute	
	H min 10.572 max 10.585 mean 10.581		CPU COO min 0.746 max 0.782 mean 0.754
Column-Gradient			CPU CSR min 3.310 max 3.324 mean 3.318
	CPU COO min 0.698 max 1.042 mean 0.737		GPU 64 COO min 7.030 max 7.160 mean 7.100 CSR min 15.730 max 18.530 mean 17.362
	CPU CSR min 1.458 max 1.536 mean 1.528		CPU PAR min 1.340 max 1.451 mean 1.401
	GPU 64 COO min 8.340 max 8.600 mean 8.443		H min 11.099 max 11.104 mean 11.102
	CSR min 16.360 max 18.450 mean 17.247 CPU PAR min 1.307 max* 1.712 mean 1.494	bloweya.mtx	
	H min 10.823 max*10.841 mean 10.835	Regular	
Row-Column-Permute			CPU COO min 0.727 max* 1.815 mean 0.892
	CPU COO min 0.683 max 1.247 mean 0.749		CPU CSR min 2.867 max* 2.936 mean 2.917 GPU 64 COO min 0.000 max 0.000 mean 0.000
	CPU CSR min 1.583 max* 1.595 mean 1.590		CSR min 0.000 max 0.000 mean 0.000
	GPU 64 COO min 8.370 max 8.500 mean 8.435 CSR min 16.250 max 16.780 mean 16.518		CPU PAR min 1.680 max* 1.751 mean 1.719
	CPU PAR min 1.206 max 1.291 mean 1.243		H min 7.205 max 7.205 mean 7.205
	H min 10.738 max 10.742 mean 10.740	Row-Premute	ODI 000 1 0 070 1 1-1
mult_dcop_02.mtx			CPU COO min 0.678 max 1.483 mean 0.746
Regular			CPU CSR min 2.311 max 2.326 mean 2.320 GPU 64 COO min 6.840 max* 7.270 mean 6.930
	CPU COD min 1.615 max* 1.677 mean 1.652		CSR min 15.650 max 16.800 mean 16.233
	CPU CSR min 1.539 max 1.579 mean 1.575 GPU 64 COO min 8.530 max* 8.700 mean 8.614		CPU PAR min 1.649 max 1.730 mean 1.682
	CSR min 18.290 max 18.890 mean 18.597		H min 11.026 max 11.031 mean 11.029
	CPU PAR min 1.120 max 1.248 mean 1.211	Row-Gradient	CPU COO min 0.708 max 1.209 mean 0.779
	H min 9.689 max 9.689 mean 9.689		CI O COO IIIIII W./WO IIIAX I.ZWY IIIEAII W.//Y

	CPU CSR	min 1 648	max 1.735	mean 1 709		CSR min 24.340 max 26.140 mean 25.393
		00 min 6.920				CPU PAR min 2.184 max 2.272 mean 2.223
		R min 16.950				H min 11.873 max 11.882 mean 11.878
	CPU PAR		max 1.743		Row-Column-Permute	11 11.075 max 11.002 mcan 11.070
	H		max 10.304 i		Non column lei mace	CPU COO min 0.707 max 0.748 mean 0.714
Column-Gradient	• •					CPU CSR min 2.458 max 2.511 mean 2.506
	CPU COO	min 0.709	max 1.536	mean 0.817		GPU 64 COO min 10.880 max 11.070 mean 10.957
	CPU CSR		max 1.753			CSR min 24.890 max 26.490 mean 25.642
	GPU 64 CO	00 min 6.800	max 7.120	mean 6.865		CPU PAR min 2.209 max 2.282 mean 2.240
	CSR	R min 15.480	max*17.710	mean 16.470		H min 11.834 max*11.840 mean 11.838
	CPU PAR	min 1.446	max 1.718	mean 1.591	brainpc2.mtx	
	Н	min 10.880	max 10.886 i	mean 10.883	Regular	
Row-Column-Permute						CPU COO min 0.732 max 0.751 mean 0.744
	CPU COO		max 1.024			CPU CSR min 2.885 max* 2.916 mean 2.909
	CPU CSR		max 2.340			GPU 64 COO min 0.000 max 0.000 mean 0.000
		00 min 6.880				CSR min 0.000 max 0.000 mean 0.000
		R min 15.610				CPU PAR min 1.276 max 1.299 mean 1.286
	CPU PAR		max 1.668		Barra Barrana ta	H min 7.478 max 7.478 mean 7.478
1	Н	min 11.025	max*11.032	mean 11.029	Row-Premute	CRU COO 0.727 0.055 0.726
lp_osa_07.mtx Regular						CPU COO min 0.727 max 0.855 mean 0.736 CPU CSR min 2.385 max 2.411 mean 2.397
regutai	CPU COO	min 0 715	max 1.798	mean 0 885		GPU 64 COO min 8.120 max 8.410 mean 8.206
	CPU CSR		max 2.551			CSR min 18.670 max 19.960 mean 19.536
		0 min 7.650				CPU PAR min 1.293 max 1.340 mean 1.314
		R min 16.390				H min 9.809 max 9.813 mean 9.811
	CPU PAR		max 1.012		Row-Gradient	11 1111 3.003 max 3.013 mean 3.011
	Н		max 8.412		Now Gradient	CPU COO min 0.696 max* 1.546 mean 0.785
Row-Premute		0.712	3.712	3.712		CPU CSR min 1.361 max 1.420 mean 1.411
Now 11 cmate	CPU COO	min 0 720	max* 2.078	mean 1 104		GPU 64 COO min 8.190 max* 8.550 mean 8.302
	CPU CSR		max* 2.679			CSR min 18.700 max*21.000 mean 19.890
		00 min 7.610				CPU PAR min 1.435 max 1.666 mean 1.549
		R min 15.910				H min 9.721 max 9.727 mean 9.723
	CPU PAR		max 0.940		Column-Gradient	
	Н	min 9.255	max 9.258	mean 9.256		CPU COO min 0.698 max 1.467 mean 0.746
Row-Gradient						CPU CSR min 1.377 max 1.423 mean 1.414
	CPU COO	min 0.725	max 2.078	mean 1.041		GPU 64 COO min 8.110 max 8.290 mean 8.187
	CPU CSR		max 2.502			CSR min 18.090 max 20.190 mean 19.217
		00 min 7.570				CPU PAR min 1.345 max* 1.681 mean 1.518
		R min 15.370				H min 10.369 max*10.372 mean 10.370
	CPU PAR		max 1.796		Row-Column-Permute	
	Н	min 8.637	max 8.678	mean 8.672		CPU COO min 0.698 max 1.390 mean 0.788
Column-Gradient						CPU CSR min 2.387 max 2.410 mean 2.399
	CPU COO		max 1.990			GPU 64 COO min 8.120 max 8.260 mean 8.191
	CPU CSR		max 2.477			CSR min 18.530 max 19.960 mean 19.307
		00 min 7.510				CPU PAR min 1.295 max 1.347 mean 1.319
		R min 14.410			ala a a a a a a a a a a a a a a a a a a	H min 9.809 max 9.813 mean 9.811
	CPU PAR H		max 1.774 max* 9.603		shermanACb.mtx	
Row-Column-Permute	п	11111 3.447	IIIax^ 3.003	illean 9.570	Regular	0011 000 1 0 740 4 004 0 750
NOW COTUMN TETMALE						
	CPLL COO	min 0 738	may 1 950	mean 1 071		CPU COO min 0.712 max 1.201 mean 0.756
	CPU COO		max 1.950			CPU CSR min 1.558 max 1.601 mean 1.596
	CPU CSR	min 2.522	max 2.709	mean 2.675		CPU CSR min 1.558 max 1.601 mean 1.596 GPU 64 COO min 7.080 max* 7.370 mean 7.184
	CPU CSR GPU 64 CO	min 2.522 00 min 7.600	max 2.709 max 7.690	mean 2.675 mean 7.641		CPU CSR min 1.558 max 1.601 mean 1.596 GPU 64 COO min 7.080 max* 7.370 mean 7.184 CSR min 17.580 max*19.480 mean 18.770
	CPU CSR GPU 64 CO CSF	min 2.522 00 min 7.600 R min 15.820	max 2.709 max 7.690 max 17.190	mean 2.675 mean 7.641 mean 16.572		CPU CSR min 1.558 max 1.601 mean 1.596 GPU 64 COO min 7.080 max* 7.370 mean 7.184 CSR min 17.580 max*19.480 mean 18.770 CPU PAR min 1.286 max 1.511 mean 1.447
	CPU CSR GPU 64 CO	min 2.522 00 min 7.600 R min 15.820 min 0.891	max 2.709 max 7.690	mean 2.675 mean 7.641 mean 16.572 mean 0.924	Row-Premute	CPU CSR min 1.558 max 1.601 mean 1.596 GPU 64 COO min 7.080 max* 7.370 mean 7.184 CSR min 17.580 max*19.480 mean 18.770
ex19.mtx	CPU CSR GPU 64 CO CSF CPU PAR	min 2.522 00 min 7.600 R min 15.820 min 0.891	max 2.709 max 7.690 max 17.190 max 0.944	mean 2.675 mean 7.641 mean 16.572 mean 0.924	Row-Premute	CPU CSR min 1.558 max 1.601 mean 1.596 GPU 64 COO min 7.080 max* 7.370 mean 7.184 CSR min 17.580 max*19.480 mean 18.770 CPU PAR min 1.286 max 1.511 mean 1.447
ex19.mtx Regular	CPU CSR GPU 64 CO CSF CPU PAR	min 2.522 00 min 7.600 R min 15.820 min 0.891	max 2.709 max 7.690 max 17.190 max 0.944	mean 2.675 mean 7.641 mean 16.572 mean 0.924	Row-Premute	CPU CSR min 1.558 max 1.601 mean 1.596 GPU 64 COO min 7.080 max* 7.370 mean 7.184 CSR min 17.580 max 1.611 mean 18.770 CPU PAR min 18.266 max 1.511 mean 1.447 H min 8.600 max 8.600 mean 8.600 CPU COO min 0.689 max 0.890 mean 0.704 CPU CSR min 1.600 max 1.630 mean 1.618
	CPU CSR GPU 64 CO CSR CPU PAR H	min 2.522 00 min 7.600 R min 15.820 min 0.891 min 9.255 min 0.732	max 2.709 max 7.690 max 17.190 max 0.944 max 9.258 max* 1.837	mean 2.675 mean 7.641 mean 16.572 mean 0.924 mean 9.256 mean 1.076	Row-Premute	CPU CSR min 1.558 max 1.601 mean 1.596 GPU 64 COU min 7.080 max* 7.370 mean 7.184 CSR min 17.580 max*19.480 mean 18.770 CPU PAR min 1.286 max 1.511 mean 1.447 H sin 8.600 max 8.600 mean 8.600 CPU COO min 0.689 max 0.890 mean 0.704
	CPU CSR GPU 64 CO CSF CPU PAR H CPU COO CPU CSR	min 2.522 00 min 7.600 R min 15.820 min 0.891 min 9.255 min 0.732 min 2.563	max 2.709 max 7.690 max 17.190 max 0.944 max 9.258 max* 1.837 max* 2.586	mean 2.675 mean 7.641 mean 16.572 mean 0.924 mean 9.256 mean 1.076 mean 2.577	Row-Premute	CPU CSR min 1.558 max 1.601 mean 1.596 GPU 64 COU min 7.080 max* 7.370 mean 7.184 CSR min 17.580 max*19.480 mean 18.770 CPU PAR min 1.286 max 1.511 mean 1.447 H min 8.600 max 8.600 mean 8.600 CPU COO min 0.689 max 0.890 mean 0.704 CPU CSR min 1.600 max 1.630 mean 1.618 GPU 64 COO min 7.000 max 7.180 mean 7.618 CSR min 15.760 max 17.240 mean 16.625
	CPU CSR GPU 64 CO CSR CPU PAR H CPU COO CPU CSR GPU 64 COC	min 2.522 20 min 7.600 R min 15.820 min 0.891 min 9.255 min 0.732 min 2.563 O min 11.340	max 2.709 max 7.690 max 17.190 max 0.944 max 9.258 max* 1.837 max* 2.586 max*11.860	mean 2.675 mean 7.641 mean 16.572 mean 0.924 mean 9.256 mean 1.076 mean 2.577 mean 11.441	Row-Premute	CPU CSR min 1.558 max 1.601 mean 1.596 GPU 64 COU min 7.080 max* 7.370 mean 7.184 CSR min 17.580 max 19.480 mean 18.770 CPU PAR min 1.286 max 1.511 mean 1.447 H min 8.600 max 8.600 mean 8.600 CPU COU min 0.689 max 0.890 mean 0.704 CPU CSR min 1.600 max 1.630 mean 1.618 GPU 64 COU min 7.000 max 7.180 mean 7.061 CSR min 15.760 max 17.240 mean 16.625 CPU PAR min 1.395 max 1.419 mean 1.355
	CPU CSR GPU 64 CO CSR CPU PAR H CPU COO CPU CSR GPU 64 COC CSR	min 2.522 00 min 7.600 R min 15.820 min 0.891 min 9.255 min 0.732 min 2.563 00 min 11.340 R min 36.010	max 2.709 max 7.690 max 17.190 max 0.944 max 9.258 max* 1.837 max* 2.586 max*11.860 max*40.960	mean 2.675 mean 7.641 mean 16.572 mean 9.256 mean 1.076 mean 2.577 mean 11.441 mean 38.048		CPU CSR min 1.558 max 1.601 mean 1.596 GPU 64 COU min 7.080 max* 7.370 mean 7.184 CSR min 17.580 max*19.480 mean 18.770 CPU PAR min 1.286 max 1.511 mean 1.447 H min 8.600 max 8.600 mean 8.600 CPU COO min 0.689 max 0.890 mean 0.704 CPU CSR min 1.600 max 1.630 mean 1.618 GPU 64 COO min 7.000 max 7.180 mean 7.618 CSR min 15.760 max 17.240 mean 16.625
	CPU CSR GPU 64 CO CSF CPU PAR H CPU COO CPU CSR GPU 64 COC CSR CPU PAR	min 2.522 00 min 7.600 R min 15.820 min 0.891 min 9.255 min 0.732 min 2.563 0 min 11.340 R min 36.010 min 2.019	max 2.709 max 7.690 max 17.190 max 0.944 max 9.258 max* 1.837 max* 2.586 max*11.860 max*40.960 max 2.204	mean 2.675 mean 7.641 mean 16.572 mean 0.924 mean 1.076 mean 2.577 mean 11.441 mean 38.048 mean 2.130	Row-Premute Row-Gradient	CPU CSR min 1.558 max 1.601 mean 1.596 GPU 64 COO min 7.080 max* 7.370 mean 7.184 CSR min 17.580 max* 19.480 mean 18.770 CPU PAR min 1.286 max 1.511 mean 1.447 H min 8.600 max 8.600 mean 8.600 CPU COO min 0.689 max 0.890 mean 0.704 CPU CSR min 1.600 max 1.630 mean 1.618 GPU 64 COO min 7.000 max 7.180 mean 7.618 GPU 64 COO min 7.000 max 71.240 mean 16.625 CPU PAR min 15.760 max 17.240 mean 16.365 H min 10.376 max 10.380 mean 10.379
Regular	CPU CSR GPU 64 CO CSR CPU PAR H CPU COO CPU CSR GPU 64 COC CSR	min 2.522 00 min 7.600 R min 15.820 min 0.891 min 9.255 min 0.732 min 2.563 0 min 11.340 R min 36.010 min 2.019	max 2.709 max 7.690 max 17.190 max 0.944 max 9.258 max* 1.837 max* 2.586 max*11.860 max*40.960	mean 2.675 mean 7.641 mean 16.572 mean 0.924 mean 1.076 mean 2.577 mean 11.441 mean 38.048 mean 2.130		CPU CSR min 1.558 max 1.601 mean 1.596 GPU 64 COU min 7.080 max* 7.370 mean 7.184 CSR min 17.580 max 1.511 mean 1.447 H min 8.600 max 8.600 mean 8.600 CPU COU min 0.689 max 0.890 mean 0.704 CPU CSR min 1.600 max 1.630 mean 1.618 GPU 64 COU min 7.000 max 7.180 mean 1.618 GPU 64 COU min 7.000 max 7.180 mean 1.625 CPU PAR min 1.296 max 1.419 mean 1.365 H min 10.376 max 10.380 mean 10.379 CPU COO min 0.704 max 1.615 mean 0.806
	CPU CSR GPU 64 CO CSF CPU PAR H CPU COO CPU CSR GPU 64 COC CSR CPU PAR H	min 2.522 NO min 7.600 R min 15.820 min 0.891 min 9.255 min 0.732 min 2.563 O min 11.340 R min 36.010 min 2.019 min 8.228	max 2.709 max 7.690 max 17.190 max 9.944 max 9.258 max* 1.837 max* 2.586 max*11.860 max*40.960 max 2.204 max 8.228	mean 2.675 mean 7.641 mean 16.572 mean 9.225 mean 1.076 mean 2.577 mean 11.441 mean 38.048 mean 2.130 mean 8.228		CPU CSR min 1.558 max 1.601 mean 1.596 GPU 64 COU min 7.080 max* 7.370 mean 7.184 CSR min 17.580 max 1.613 mean 18.770 CPU PAR min 1.286 max 1.511 mean 1.447 H min 8.600 max 8.600 mean 8.600 CPU COU min 0.689 max 0.890 mean 0.704 CPU CSR min 1.600 max 1.630 mean 1.618 GPU 64 COU min 7.000 max 7.180 mean 7.061 CSR min 15.760 max 17.240 mean 16.625 CPU PAR min 1.296 max 10.380 mean 10.379 CPU COU min 0.704 max 10.380 mean 10.379 CPU COU min 0.704 max 1.615 mean 0.806 CPU CSR min 1.355 max 1.370 mean 1.362
Regular	CPU CSR GPU 64 COC CSS CPU PAR H CPU COO CPU CSR GPU 64 COC CSR CPU PAR H CPU COO	min 2.522 DO min 7.600 min 0.891 min 9.255 min 0.732 min 2.563 D min 11.340 R min 36.010 min 2.019 min 8.228 min 0.718	max 2.709 max 7.690 max 17.190 max 9.258 max* 1.837 max* 2.586 max*11.860 max*40.960 max 2.204 max 8.228 max 0.751	mean 2.675 mean 7.641 mean 16.572 mean 9.256 mean 2.577 mean 1.076 mean 2.577 mean 11.441 mean 38.048 mean 2.130 mean 8.228 mean 0.732		CPU CSR min 1.558 max 1.601 mean 1.596 GPU 64 COO min 7.080 max* 7.370 mean 7.184 CSR min 17.580 max* 19.480 mean* 18.770 CPU PAR min 1.286 max 1.511 mean 1.447 H min 8.600 max 8.600 mean 8.600 CPU COO min 0.689 max 0.890 mean 0.704 CPU CSR min 1.600 max 1.630 mean 1.618 GPU 64 COO min 7.000 max 71.80 mean 7.081 CSR min 15.760 max 17.240 mean 16.625 CPU PAR min 1.296 max 1.419 mean 1.365 H min 10.376 max 10.380 mean 10.379 CPU COO min 0.704 max 1.615 mean 0.806 CPU CSR min 1.555 max 1.370 mean 1.362 GPU 64 COO min 7.020 max 7.160 mean 7.083
Regular	CPU CSR GPU 64 CO CSF CPU PAR H CPU COO CPU CSR GPU 64 COO CSR CPU PAR H CPU COO CPU CSR	min 2.522 DO min 7.600 min 7.600 min 0.891 min 9.255 min 0.732 min 2.563 D min 11.340 R min 36.010 min 2.019 min 8.228 min 0.718 min 0.718	max 2.709 max 7.690 max 17.190 max 0.944 max 9.258 max* 1.837 max* 2.586 max*11.860 max*40.960 max 40.960 max 2.228 max 2.228 max 2.507	mean 2.675 mean 7.641 mean 16.572 mean 0.924 mean 2.556 mean 1.076 mean 2.577 mean 11.441 mean 38.048 mean 2.238 mean 0.732 mean 0.732 mean 2.498		CPU CSR min 1.558 max 1.601 mean 1.596 GPU 64 COU min 7.080 max* 7.370 mean 7.184 CSR min 17.580 max 1.511 mean 1.447 H min 8.600 max 8.600 mean 8.600 CPU COU min 0.689 max 0.890 mean 0.704 CPU CSR min 1.600 max 1.630 mean 1.618 GPU 64 COU min 7.000 max 7.180 mean 1.625 CPU PAR min 15.760 max 17.240 mean 16.625 CPU PAR min 10.376 max 10.380 mean 10.375 H min 10.376 max 10.380 mean 10.375 CPU COO min 0.704 max 1.615 mean 0.806 CPU CSR min 1.355 max 1.370 mean 1.365 GPU 64 COO min 7.000 max 7.160 mean 7.083 CSR min 0.000 max 1.6290 mean 1.5076
Regular	CPU CSR GPU 64 COS CPU PAR H CPU COO CPU CSR GPU 64 COC CSR CPU PAR H CPU COO CPU CSR GPU 64 COC CSR CPU PAR CPU COO CPU CSR GPU 64 COC	min 2.522 DO min 7.600 min 7.600 min 0.891 min 9.255 min 0.732 min 2.563 D min 11.340 R min 36.010 min 2.019 min 8.228 min 0.718 min 0.718 min 0.718	max 2.709 max 7.690 max 17.190 max 0.944 max 9.258 max* 1.837 max* 2.586 max*40.960 max 2.204 max 8.228 max 0.751 max 1.090 max 1.090	mean 2.675 mean 7.641 mean 16.572 mean 9.226 mean 1.076 mean 1.076 mean 2.577 mean 38.048 mean 2.130 mean 0.732 mean 0.732 mean 0.732 mean 10.949		CPU CSR min 1.558 max 1.601 mean 1.596 GPU 64 COU min 7.080 max* 7.370 mean 7.184 CSR min 17.580 max 1.513 mean 18.770 CPU PAR min 1.286 max 1.511 mean 1.447 H min 8.600 max 8.600 mean 8.600 CPU COO min 0.689 max 0.890 mean 0.704 CPU CSR min 1.600 max 1.630 mean 1.618 GPU 64 COU min 7.000 max 7.180 mean 7.061 CSR min 15.760 max 17.240 mean 16.625 CPU PAR min 1.395 max 10.380 mean 10.379 CPU COO min 0.704 max 10.380 mean 10.379 CPU COO min 0.704 max 1.615 mean 0.806 CPU CSR min 1.355 max 1.370 mean 1.362 GPU 64 COU min 7.020 max 7.160 mean 7.083 CSR min 0.000 max 16.290 mean 15.076 CPU PAR min 1.256 max 1.520 mean 1.405
Regular	CPU CSR GPU 64 COS CPU PAR H CPU COO CPU CSR GPU 64 COC CSR CPU PAR H CPU COO CPU CSR GPU CSR CPU PAR GPU COO CPU CSR GPU 64 COC CSR GPU 64 COC CSR GPU 64 COC CSR GPU 64 COC CSR	min 2.522 NO min 7.600 min 0.891 min 9.255 min 0.732 min 2.563 O min 11.340 N min 12.019 min 2.288 min 0.718 min 2.488 O min 10.810 N min 12.488	max 2.709 max 7.690 max 17.190 max 9.944 max 9.258 max* 1.837 max* 2.586 max*14.860 max*40.960 max 2.204 max 0.751 max 2.507 max 11.090 max 26.410	mean 2.675 mean 7.641 mean 16.572 mean 9.256 mean 2.557 mean 1.441 mean 38.048 mean 2.130 mean 0.732 mean 0.732 mean 0.949 mean 10.949 mean 12.557	Row-Gradient	CPU CSR min 1.558 max 1.601 mean 1.596 GPU 64 COU min 7.080 max* 7.370 mean 7.184 CSR min 17.580 max 1.511 mean 1.447 H min 8.600 max 8.600 mean 8.600 CPU COU min 0.689 max 0.890 mean 0.704 CPU CSR min 1.600 max 1.630 mean 1.618 GPU 64 COU min 7.000 max 7.180 mean 1.625 CPU PAR min 15.760 max 17.240 mean 16.625 CPU PAR min 10.376 max 10.380 mean 10.375 H min 10.376 max 10.380 mean 10.375 CPU COO min 0.704 max 1.615 mean 0.806 CPU CSR min 1.355 max 1.370 mean 1.365 GPU 64 COO min 7.000 max 7.160 mean 7.083 CSR min 0.000 max 1.6290 mean 1.5076
Regular	CPU CSR GPU 64 CO CSF CPU PAR H CPU COO CPU CSR GPU 64 COC CSF CPU PAR H CPU COO CPU CSR GPU 64 COC CSC CPU PAR CPU COO CPU CSR GPU 64 COC CSC CPU PAR	min 2.522 DO min 7.600 min 7.600 min 0.891 min 9.255 min 0.732 min 2.563 D min 11.340 R min 36.010 min 2.019 min 8.228 min 0.718 min 2.488 O min 10.810 R min 24.880 O min 10.810 R min 24.880 min 10.810 min 1.978	max 2.709 max 7.690 max 17.190 max 0.944 max 9.258 max* 1.837 max* 2.586 max*11.860 max*40.960 max 40.960 max 2.280 max 2.2507 max 11.090 max 2.2507 max 11.090 max 2.290	mean 2, 675 mean 7, 641 mean 16, 572 mean 0, 924 mean 2, 577 mean 11, 441 mean 38, 048 mean 2, 130 mean 2, 130 mean 2, 498 mean 10, 949 mean 12, 5527 mean 12, 135		CPU CSR min 1.558 max 1.601 mean 1.596 GPU 64 COO min 7.080 max* 7.370 mean 7.184 CSR min 17.580 max* 19.480 mean 18.770 CPU PAR min 1.286 max 1.511 mean 1.447 H min 8.600 max 8.600 mean 8.600 CPU COO min 0.689 max 0.890 mean 0.704 CPU CSR min 1.600 max 1.630 mean 1.618 GPU 64 COO min 7.000 max 7.180 mean 1.6625 CPU PAR min 15.760 max 17.240 mean 16.625 CPU PAR min 10.376 max 10.380 mean 10.379 CPU COO min 0.704 max 1.615 mean 0.806 CPU CSR min 1.355 max 1.370 mean 1.365 GPU 64 COO min 7.020 max 7.160 mean 7.083 CSR min 0.000 max 16.290 mean 15.076 CPU PAR min 1.256 max 1.520 mean 1.405 H min 9.915 max 9.925 mean 9.921
Regular Row-Premute	CPU CSR GPU 64 COS CPU PAR H CPU COO CPU CSR GPU 64 COC CSR CPU PAR H CPU COO CPU CSR GPU CSR CPU PAR GPU COO CPU CSR GPU 64 COC CSR GPU 64 COC CSR GPU 64 COC CSR GPU 64 COC CSR	min 2.522 DO min 7.600 min 7.600 min 0.891 min 9.255 min 0.732 min 2.563 D min 11.340 R min 36.010 min 2.019 min 8.228 min 0.718 min 2.488 O min 10.810 R min 24.880 O min 10.810 R min 24.880 min 10.810 min 1.978	max 2.709 max 7.690 max 17.190 max 9.944 max 9.258 max* 1.837 max* 2.586 max*14.860 max*40.960 max 2.204 max 0.751 max 2.507 max 11.090 max 26.410	mean 2, 675 mean 7, 641 mean 16, 572 mean 0, 924 mean 2, 577 mean 11, 441 mean 38, 048 mean 2, 130 mean 2, 130 mean 2, 498 mean 10, 949 mean 12, 5527 mean 12, 135	Row-Gradient	CPU CSR min 1.558 max 1.601 mean 1.596 GPU 64 COU min 7.080 max* 7.370 mean 7.184 CSR min 17.580 max 1.511 mean 1.447 H min 8.600 max 8.600 mean 8.600 CPU COU min 0.689 max 0.890 mean 0.704 CPU CSR min 1.760 max 1.630 mean 1.618 GPU 64 COU min 7.000 max 7.180 mean 7.061 CSR min 15.760 max 17.240 mean 16.625 CPU PAR min 1.296 max 1.419 mean 1.365 H min 10.376 max 10.380 mean 10.379 CPU COU min 0.704 max 1.615 mean 0.806 CPU CSR min 1.555 max 1.370 mean 1.362 GPU 64 COU min 7.020 max 7.160 mean 1.626 CPU PAR min 1.256 max 1.290 mean 1.5076 CPU PAR min 1.256 max 1.520 mean 1.405 H min 9.915 max 9.925 mean 9.921 CPU COU min 0.702 max* 1.626 mean 0.844
Regular	CPU CSR GPU 64 COC CSF CPU PAR H CPU COO CPU CSR GPU 64 COC CSR CPU PAR H CPU COO CPU CSR GPU 64 COC CPU CSR GPU 64 COC CPU PAR H CPU COO CPU CSR GPU 64 COC CSF CPU PAR H	min 2.522 DO min 7.6820 min 0.891 min 9.255 min 0.732 min 2.563 D min 11.340 R min 36.010 min 2.019 min 8.228 min 0.718 min 0.718 min 1.4860 min 1.978 min 11.836	max 2.709 max 7.690 max 17.190 max 0.944 max 9.258 max* 1.837 max* 2.586 max*40.960 max 2.204 max 8.228 max 0.751 max 2.507 max 11.090 max 26.410 max 2.290 max 11.840	mean 2.675 mean 7.641 mean 16.572 mean 9.226 mean 1.076 mean 2.577 mean 38.048 mean 2.130 mean 8.228 mean 0.732 mean 10.949 mean 25.527 mean 2.135 mean 11.838	Row-Gradient	CPU CSR min 1.558 max 1.601 mean 1.596 GPU 64 COO min 7.080 max* 7.370 mean 7.184 CSR min 17.580 max 15.311 mean 1.447 H min 8.600 max 8.600 mean 8.600 CPU COO min 0.689 max 0.890 mean 0.704 CPU CSR min 1.600 max 1.630 mean 1.616 GPU 64 COO min 7.000 max 7.180 mean 1.625 CPU PAR min 1.296 max 1.7.240 mean 16.625 CPU PAR min 1.296 max 1.419 mean 1.365 H min 10.376 max 10.380 mean 10.379 CPU COO min 0.704 max 1.615 mean 0.806 GPU CSR min 1.555 max 1.370 mean 1.362 GPU 64 COO min 7.020 max 7.160 mean 7.083 CSR min 0.000 max 16.290 mean 15.076 CPU PAR min 1.256 max 15.230 mean 15.076 CPU PAR min 1.256 max 15.230 mean 15.076 CPU COO min 7.020 max 7.160 mean 7.083 CSR min 0.900 max 16.290 mean 15.076 H min 9.915 max 9.925 mean 9.921 CPU COO min 0.702 max* 1.626 mean 0.844 CPU CSR min 1.327 max 1.374 mean 1.364
Regular Row-Premute	CPU CSR GPU 64 CO CSR CPU PAR H CPU COO CPU CSR GPU 64 COC CSR CPU PAR H CPU COO CPU CSR GPU 64 COC CSR GPU 64 COC CPU CSR CPU PAR H CPU COO	min 2.522 DO min 7.600 min 7.600 min 0.891 min 9.255 min 0.732 min 2.563 D min 11.340 R min 36.010 min 2.019 min 8.228 min 0.718 min 2.488 O min 10.810 R min 24.860 min 11.878 min 11.836 min 0.722	max 2.709 max 7.690 max 17.190 max 0.944 max 9.258 max* 1.837 max* 2.586 max*11.860 max*40.960 max 40.960 max 2.280 max 1.090 max 11.090 max 2.290 max 11.840 max 1.794	mean 2, 675 mean 7, 641 mean 16, 572 mean 0, 924 mean 2, 577 mean 11, 441 mean 38, 048 mean 2, 130 mean 2, 130 mean 10, 949 mean 10, 949 mean 12, 5, 527 mean 11, 838 mean 1, 838 mean 2, 135 mean 11, 838 mean 0, 769	Row-Gradient	CPU CSR min 1.558 max 1.601 mean 1.596 GPU 64 COU min 7.080 max* 7.370 mean 7.184 CSR min 17.580 max* 19.480 mean 18.770 CPU PAR min 1.286 max 1.511 mean 1.447 H min 8.600 max 8.600 mean 8.600 CPU COU min 0.689 max 0.890 mean 0.704 CPU CSR min 1.600 max 1.630 mean 1.618 GPU 64 COU min 7.000 max 7.180 mean 1.6625 CPU PAR min 1.296 max 1.419 mean 1.365 H min 10.376 max 10.380 mean 10.379 CPU COO min 0.704 max 1.615 mean 0.806 CPU CSR min 1.355 max 1.370 mean 1.365 GPU 64 COO min 0.7020 max 1.615 mean 0.806 CPU CSR min 0.000 max 16.290 mean 15.076 CPU PAR min 1.256 max 1.370 mean 1.365 H min 0.000 max 16.290 mean 15.076 CPU PAR min 1.256 max 1.520 mean 1.405 H min 0.915 max 9.925 mean 9.921 CPU COO min 0.702 max 1.620 mean 1.405 H min 0.915 max 9.925 mean 0.921 CPU COO min 0.702 max 1.620 mean 1.405 H min 1.256 max 1.520 mean 1.405 H min 0.915 max 9.925 mean 0.921
Regular Row-Premute	CPU CSR GPU 64 CO CSR CPU PAR H CPU COO CPU CSR GPU 64 COC CSR CPU PAR H CPU COO CPU CSR GPU 64 COC CSR GPU 64 COC CSR CPU PAR H CPU COO CSS CPU PAR H CPU COO CSS CPU PAR CSS CPU CSR	min 2.522 DO min 7.600 min 7.600 min 0.891 min 9.255 min 0.732 min 2.563 D min 11.340 R min 36.010 min 2.019 min 8.228 min 0.718 min 2.488 O min 10.810 R min 24.860 min 11.836 min 0.722 min 0.722 min 0.722 min 0.722 min 0.722	max 2.709 max 7.690 max 17.190 max 0.944 max 9.258 max* 1.887 max* 2.586 max*11.860 max 2.204 max 2.204 max 2.207 max 11.090 max 26.410 max 21.794 max 1.794 max 2.421	mean 2.675 mean 7.641 mean 16.572 mean 0.924 mean 9.256 mean 1.076 mean 2.577 mean 11.441 mean 38.048 mean 2.130 mean 2.130 mean 2.289 mean 10.949 mean 25.527 mean 11.838 mean 1.769 mean 2.416	Row-Gradient	CPU CSR min 1.558 max 1.601 mean 1.596 GPU 64 COU min 7.080 max* 7.370 mean 7.184 CSR min 17.580 max 1.511 mean 1.447 H min 8.600 max 8.600 mean 8.600 CPU COU min 0.689 max 0.890 mean 0.704 CPU CSR min 1.600 max 1.630 mean 1.618 GPU 64 COU min 7.000 max 7.180 mean 1.618 GPU 64 COU min 7.000 max 7.180 mean 1.625 CPU PAR min 1.296 max 1.419 mean 1.365 H min 10.376 max 10.380 mean 10.379 CPU COO min 0.704 max 1.615 mean 0.806 CPU CSR min 1.355 max 1.370 mean 1.362 GPU 64 COO min 7.020 max 7.160 mean 7.083 CPU COO min 0.704 max 1.520 mean 1.362 GPU 64 COO min 7.020 max 7.160 mean 7.083 CPU COO min 0.702 max 7.160 mean 1.405 H min 9.915 max 9.925 mean 9.921 CPU COO min 0.702 max 1.626 mean 0.844 CPU CSR min 0.000 max 1.526 mean 0.844 CPU CSR min 0.702 max 1.374 mean 1.364 GPU 64 COO min 6.920 max 1.374 mean 1.364 GPU 64 COO min 6.920 max 1.270 mean 7.030 CSR min 0.000 max 15.260 mean 1.7030 CSR min 0.000 max 15.260 mean 1.364
Regular Row-Premute	CPU CSR GPU 64 COS CPU PAR H CPU COO CPU CSR GPU 64 COC CSR CPU PAR H CPU COO CPU CSR GPU 64 COC	min 2.522 DO min 7.600 min 7.600 min 0.891 min 9.255 min 0.732 min 2.563 D min 11.340 R min 36.010 min 2.019 min 8.228 min 0.718 min 0.718 min 1.848 O min 10.810 R min 24.880 min 1.978 min 11.836 min 0.722 min 0.722 min 0.722 min 0.722 min 1.2407 O min 11.210	max 2.709 max 7.690 max 17.190 max 9.258 max* 1.837 max* 2.586 max*40.960 max 2.204 max 0.751 max 11.800 max 2.507 max 11.800 max 2.200 max 11.840 max 2.200 max 11.840 max 1.794	mean 2.675 mean 7.641 mean 16.572 mean 9.256 mean 1.076 mean 2.577 mean 2.577 mean 2.130 mean 8.228 mean 0.732 mean 10.949 mean 2.135 mean 1.838 mean 1.838 mean 1.838	Row-Gradient	CPU CSR min 1.558 max 1.601 mean 1.596 GPU 64 COO min 7.080 max* 7.370 mean 7.184 CSR min 17.580 max 1.511 mean 1.447 H min 8.600 max 8.600 mean 8.600 CPU COO min 0.689 max 0.890 mean 0.704 CPU CSR min 1.600 max 1.630 mean 1.618 GPU 64 COO min 7.000 max 7.180 mean 7.061 CSR min 15.760 max 17.240 mean 16.625 CPU PAR min 1.296 max 1.419 mean 13.65 H min 10.376 max 10.380 mean 10.379 CPU COO min 7.020 max 7.160 mean 7.083 CSR min 0.704 max 1.615 mean 0.806 GPU GSR min 1.355 max 1.370 mean 1.362 GPU 64 COO min 7.020 max 7.160 mean 7.083 CSR min 0.000 max 16.290 mean 15.076 H min 9.915 max 9.925 mean 9.921 CPU COO min 0.702 max* 1.626 mean 0.844 CPU CSR min 1.327 max 1.374 mean 1.364 GPU GSR min 1.327 max 1.374 mean 7.034 CSR min 0.000 max 15.260 mean 7.036 CSR min 0.702 max* 7.210 mean 7.036 CSR min 0.700 max 7.210 mean 7.036 CSR min 0.700 max 7.210 mean 7.037 CPU COO min 6.920 max 7.210 mean 7.036 CSR min 0.000 max 15.260 mean 1.364
Regular Row-Premute	CPU CSR GPU 64 COS CPU PAR H CPU COO CPU CSR GPU 64 COC CSR CPU PAR H CPU COO CPU CSR GPU 64 COC	min 2.522 DO min 7.600 min 7.600 min 0.891 min 0.732 min 2.563 D min 11.340 R min 36.010 min 2.019 min 2.488 O min 10.810 R min 24.880 min 10.810 min 1.978 min 11.836 min 0.722 min 2.467 O min 11.210 R min 3.920	max 2.709 max 7.690 max 17.190 max 0.944 max 9.258 max*11.860 max*40.960 max 40.960 max 2.280 max 11.090 max 12.290 max 11.840 max 1.794 max 1.794 max 1.480 max 34.690	mean 2.675 mean 7.641 mean 16.572 mean 0.924 mean 2.575 mean 11.441 mean 38.048 mean 2.130 mean 2.498 mean 10.949 mean 2.5527 mean 1.838 mean 1.838 mean 1.838 mean 2.135 mean 1.838	Row-Gradient	CPU CSR min 1.558 max 1.601 mean 1.596 GPU 64 COU min 7.080 max* 7.370 mean 7.184 CSR min 17.580 max 1.511 mean 1.447 H min 8.600 max 8.600 mean 8.600 CPU COU min 0.689 max 0.890 mean 0.704 CPU CSR min 1.600 max 1.630 mean 1.618 GPU 64 COU min 7.000 max 7.180 mean 1.618 GPU 64 COU min 7.000 max 7.180 mean 1.625 CPU PAR min 1.296 max 1.419 mean 1.365 H min 10.376 max 10.380 mean 10.379 CPU COO min 0.704 max 1.615 mean 0.806 CPU CSR min 1.355 max 1.370 mean 1.362 GPU 64 COO min 7.020 max 7.160 mean 7.083 CPU COO min 0.704 max 1.520 mean 1.362 GPU 64 COO min 7.020 max 7.160 mean 7.083 CPU COO min 0.702 max 7.160 mean 1.405 H min 9.915 max 9.925 mean 9.921 CPU COO min 0.702 max 1.626 mean 0.844 CPU CSR min 0.000 max 1.526 mean 0.844 CPU CSR min 0.702 max 1.374 mean 1.364 GPU 64 COO min 6.920 max 1.374 mean 1.364 GPU 64 COO min 6.920 max 1.270 mean 7.030 CSR min 0.000 max 15.260 mean 1.7030 CSR min 0.000 max 15.260 mean 1.364
Regular Row-Premute	CPU CSR GPU 64 COC CSR CPU PAR H CPU COO CPU CSR GPU 64 COC CSR CPU PAR H CPU COO CPU CSR GPU 64 COC CSR CPU PAR CPU COO CPU CSR GPU 64 COC CSG CPU PAR CPU COO CPU CSR GPU 64 COC CSG CPU CSR GPU 64 COC CSG CPU CSR CPU CSC CPU CSC CPU CSC CSC CPU CSC	min 2.522 DO min 7.600 min 7.600 min 0.732 min 0.732 min 0.732 min 2.563 D min 11.340 R min 36.010 min 2.019 min 8.228 min 0.718 min 2.488 O min 10.810 R min 24.860 min 11.836 min 0.722 min 2.407 O min 11.210 min 31.920 min 31.920 min 31.920 min 31.920 min 12.84	max 2.709 max 7.690 max 17.190 max 9.258 max* 1.837 max* 2.586 max*40.960 max 2.204 max 0.751 max 11.800 max 2.507 max 11.800 max 2.200 max 11.840 max 2.200 max 11.840 max 1.794	mean 2.675 mean 7.641 mean 16.572 mean 0.924 mean 2.577 mean 11.441 mean 38.048 mean 2.130 mean 10.949 mean 2.5.527 mean 11.838 mean 11.838 mean 0.769 mean 2.416 mean 11.317 mean 3.246 mean 2.232	Row-Gradient Column-Gradient	CPU CSR min 1.558 max 1.601 mean 1.596 GPU 64 COO min 7.080 max* 7.370 mean 7.184 CSR min 17.580 max 1.511 mean 1.447 H min 8.600 max 8.600 mean 8.600 CPU COO min 0.689 max 0.890 mean 0.704 CPU CSR min 1.600 max 1.630 mean 1.618 GPU 64 COO min 7.000 max 7.180 mean 7.061 CSR min 15.760 max 17.240 mean 16.625 CPU PAR min 1.296 max 1.419 mean 13.65 H min 10.376 max 10.380 mean 10.379 CPU COO min 7.020 max 7.160 mean 7.083 CSR min 0.704 max 1.615 mean 0.806 GPU GSR min 1.355 max 1.370 mean 1.362 GPU 64 COO min 7.020 max 7.160 mean 7.083 CSR min 0.000 max 16.290 mean 15.076 H min 9.915 max 9.925 mean 9.921 CPU COO min 0.702 max* 1.626 mean 0.844 CPU CSR min 1.327 max 1.374 mean 1.364 GPU GSR min 1.327 max 1.374 mean 7.034 CSR min 0.000 max 15.260 mean 7.036 CSR min 0.702 max* 7.210 mean 7.036 CSR min 0.700 max 7.210 mean 7.036 CSR min 0.700 max 7.210 mean 7.037 CPU COO min 6.920 max 7.210 mean 7.036 CSR min 0.000 max 15.260 mean 1.364
Regular Row-Premute	CPU CSR GPU 64 COC CSR CPU PAR H CPU COO CPU CSR GPU 64 COC CSR CPU PAR H CPU COO CPU CSR GPU 64 COC CSR GPU 64 COC CSR GPU 64 COC CSR CPU PAR H CPU COO CSC CPU PAR CPU COO CSC CPU CSR GPU 64 COC CSC CPU PAR CPU COO CSC CSC CPU PAR	min 2.522 DO min 7.600 min 7.600 min 0.732 min 0.732 min 0.732 min 2.563 D min 11.340 R min 36.010 min 2.019 min 8.228 min 0.718 min 2.488 O min 10.810 R min 24.860 min 11.836 min 0.722 min 2.407 O min 11.210 min 31.920 min 31.920 min 31.920 min 31.920 min 12.84	max 2.709 max 7.690 max 17.190 max 0.944 max 9.258 max* 1.837 max* 2.586 max*11.860 max 2.204 max 2.204 max 11.090 max 2.41 max 11.794 max 1.794 max 1.794 max 3.4690 max 3.4690 max 2.302	mean 2.675 mean 7.641 mean 16.572 mean 0.924 mean 2.577 mean 11.441 mean 38.048 mean 2.130 mean 10.949 mean 2.5.527 mean 11.838 mean 11.838 mean 0.769 mean 2.416 mean 11.317 mean 3.246 mean 2.232	Row-Gradient Column-Gradient	CPU CSR min 1.558 max 1.601 mean 1.596 GPU 64 COU min 7.080 max* 7.370 mean 7.184 CSR min 17.580 max 1.511 mean 1.447 H min 8.600 max 8.600 mean 8.600 CPU COU min 0.689 max 0.890 mean 0.704 CPU CSR min 1.600 max 1.630 mean 1.618 GPU 64 COU min 7.000 max 7.180 mean 1.618 GPU 64 COU min 7.000 max 7.180 mean 1.6625 CPU PAR min 1.296 max 10.330 mean 10.375 H min 10.376 max 10.380 mean 10.375 CPU COO min 0.704 max 1.615 mean 10.375 CPU COO min 7.000 max 7.160 mean 15.656 GPU 64 COU min 7.020 max 7.160 mean 1.365 H min 10.376 max 10.380 mean 10.379 CPU COO min 7.020 max 7.160 mean 7.083 CSR min 0.000 max 16.290 mean 15.076 CPU PAR min 1.256 max 1.520 mean 1.405 H min 9.915 max 9.925 mean 9.921 CPU COO min 6.702 max* 1.626 mean 0.844 CPU CSR min 1.327 max 1.374 mean 1.364 GPU 64 COU min 6.702 max* 1.626 mean 0.844 CPU CSR min 0.000 max 15.260 mean 1.405 GPU 64 COU min 6.702 max* 1.525 mean 1.364 GPU 64 COU min 6.702 max* 1.525 mean 1.365 GSR min 0.000 max 15.260 mean 1.4279 CPU PAR min 1.283 max* 1.531 mean 1.385 min 1.283 max* 1.531 mean 1.385 min 1.252 max 10.595 mean 10.590
Regular Row-Premute Row-Gradient	CPU CSR GPU 64 COC CSR CPU PAR H CPU COO CPU CSR GPU 64 COC CSR CPU PAR H CPU COO CPU CSR GPU 64 COC CSR GPU 64 COC CSR GPU 64 COC CSR CPU PAR H CPU COO CSC CPU PAR CPU COO CSC CPU CSR GPU 64 COC CSC CPU PAR CPU COO CSC CSC CPU PAR	min 2.522 DO min 7.600 min 7.600 min 0.891 min 0.732 min 2.563 D min 11.340 R min 36.010 min 2.019 min 8.228 min 0.718 min 2.488 O min 10.810 min 12.863 O min 11.386 min 0.722 min 2.487 O min 11.836 min 0.722 min 2.497 O min 11.920 min 2.184 min 10.742	max 2.709 max 7.690 max 17.190 max 0.944 max 9.258 max* 1.837 max* 2.586 max*11.860 max 2.204 max 2.204 max 11.090 max 2.41 max 11.794 max 1.794 max 1.794 max 3.4690 max 3.4690 max 2.302	mean 2, 675 mean 7, 641 mean 16, 572 mean 0, 924 mean 2, 577 mean 11, 441 mean 38, 048 mean 2, 130 mean 2, 498 mean 10, 949 mean 2, 135 mean 11, 838 mean 1, 838 mean 2, 416 mean 1, 317 m	Row-Gradient Column-Gradient	CPU CSR min 1.558 max 1.601 mean 1.596 GPU 64 COO min 1.7680 max* 7.370 mean 7.184 CSR min 17.580 max* 1.511 mean 1.447 H min 8.600 max 8.600 mean 8.600 CPU COO min 0.689 max 0.890 mean 0.704 CPU CSR min 1.600 max 1.630 mean 1.616 GPU 64 COO min 7.000 max 7.180 mean 7.061 CSR min 15.760 max 17.240 mean 16.625 CPU PAR min 1.296 max 1.419 mean 1.365 H min 10.376 max 10.380 mean 10.379 CPU COO min 7.020 max 7.160 mean 7.083 CSR min 0.704 max 1.615 mean 0.806 GPU GSR min 1.555 max 1.370 mean 1.362 GPU 64 COO min 7.020 max 7.160 mean 7.083 CSR min 0.000 max 16.290 mean 15.076 H min 9.915 max 9.925 mean 9.921 CPU COO min 0.702 max* 1.626 mean 0.844 CPU CSR min 1.327 max 1.374 mean 1.364 GPU GSR min 0.000 max 15.260 mean 1.405 H min 1.283 max* 1.531 mean 1.364 GPU GSR min 0.000 max 15.260 mean 1.4279 CPU PAR min 1.283 max* 1.531 mean 1.385 H min 10.572 max 10.595 mean 10.590 CPU COO min 0.707 max 1.532 mean 0.924
Regular Row-Premute Row-Gradient	CPU CSR GPU 64 COC CSF CPU PAR H CPU COO CPU CSR GPU 64 COC CSR CPU PAR H CPU COO CPU CSR GPU 64 COC CPU CSR GPU 64 COC CPU CSR GPU 64 COC CSF CPU PAR H CPU COO CPU CSR GPU 64 COC CSF CPU PAR H	min 2.522 DO min 7.600 min 7.600 min 0.732 min 0.732 min 0.732 min 2.563 D min 11.340 R min 36.010 min 2.019 min 8.228 min 0.718 min 2.488 O min 10.810 R min 24.860 min 11.836 min 0.722 min 2.407 O min 11.210 min 12.019 min 12.019 min 12.019 min 13.920 min 13.920 min 2.184 min 10.742 min 0.720	max 2.709 max 7.690 max 17.190 max 0.944 max 9.258 max*11.860 max*40.960 max 40.960 max 2.280 max 11.090 max 11.090 max 12.290 max 11.840 max 2.410 max 2.421 max 11.490 max 34.690 max 4.690 max 4.690 max 1.751	mean 2.675 mean 7.641 mean 16.572 mean 0.924 mean 2.556 mean 11.441 mean 38.048 mean 2.130 mean 10.949 mean 12.527 mean 11.838 mean 2.135 mean 11.838 mean 2.416 mean 1.317 mean 3.246 mean 2.232 mean 10.742	Row-Gradient Column-Gradient	CPU CSR min 1.558 max 1.601 mean 1.596 GPU 64 COU min 7.080 max* 7.370 mean 7.184 CSR min 17.580 max 1.511 mean 1.447 H min 8.600 max 8.600 mean 8.600 CPU COO min 0.689 max 8.600 mean 8.600 CPU CSR min 1.500 max 1.630 mean 1.618 GPU 64 COO min 7.000 max 7.180 mean 1.618 GPU 64 COO min 7.000 max 7.180 mean 1.6625 CPU PAR min 1.296 max 1.419 mean 1.365 H min 10.376 max 10.380 mean 10.379 CPU COO min 0.704 max 1.615 mean 0.806 CPU CSR min 1.355 max 1.370 mean 1.365 GPU CSR min 1.355 max 1.370 mean 1.365 GPU GSR min 0.000 max 16.290 mean 15.076 CPU PAR min 1.256 max 1.520 mean 1.407 CPU CSR min 0.000 max 1.520 mean 1.407 CPU CSR min 0.702 max* 1.626 mean 0.844 CPU CSR min 1.237 max 1.374 mean 1.364 GPU 64 COO min 6.920 max 7.210 mean 7.030 CSR min 0.000 max 15.260 mean 14.279 CPU COO min 6.920 max 7.210 mean 7.030 CSR min 0.000 max 15.250 mean 14.259 min 1.283 max* 1.531 mean 1.354 H min 10.572 max 10.595 mean 10.590 CPU COO min 0.707 max 1.532 mean 0.924 CPU COO min 0.606 max* 1.634 mean 1.624
Regular Row-Premute Row-Gradient	CPU CSR GPU 64 COC CSF CPU PAR H CPU COO CPU CSR GPU 64 COC CSF CPU PAR H CPU COO CPU CSR GPU 64 COC CSF CPU PAR H CPU COO CPU CSR GPU 64 COC CSF CPU PAR H CPU COO CPU CSR GPU 64 COC CSF CPU PAR H CPU COO CPU CSR GPU 64 COC CSF CPU PAR CPU COO CSSC CPU PAR CPU COO CPU CSR	min 2.522 DO min 7.600 min 7.600 min 0.732 min 0.732 min 0.732 min 2.563 D min 11.340 R min 36.010 min 2.019 min 8.228 min 0.718 min 2.488 O min 10.810 R min 24.860 min 11.836 min 0.722 min 2.407 O min 11.210 min 12.019 min 12.019 min 12.019 min 13.920 min 13.920 min 2.184 min 10.742 min 0.720	max 2.709 max 7.690 max 17.190 max 0.944 max 9.258 max* 1.837 max* 2.586 max*40.960 max 2.204 max 0.751 max 11.090 max 26.410 max 11.840 max 11.840 max 11.840 max 11.480 max 34.690 max 12.421 max 11.480 max 34.690 max 2.421 max 10.757 max 10.757 max 2.421 max 11.480 max 34.690 max 2.421 max 10.757	mean 2.675 mean 7.641 mean 16.572 mean 9.256 mean 1.076 mean 2.577 mean 2.577 mean 2.136 mean 2.130 mean 2.498 mean 2.5527 mean 10.949 mean 25.527 mean 21.338 mean 0.769 mean 2.135 mean 11.317 mean 33.246 mean 12.312 mean 11.317 mean 33.246 mean 2.436 mean 2.432 mean 10.748	Row-Gradient Column-Gradient	CPU CSR min 1.558 max 1.601 mean 1.596 GPU 64 COU min 7.080 max* 7.370 mean 7.184 CSR min 17.580 max 1.511 mean 1.447 H min 8.600 max 8.600 mean 8.600 CPU COU min 0.689 max 0.890 mean 0.704 CPU CSR min 1.600 max 1.630 mean 1.618 GPU 64 COU min 7.000 max 7.180 mean 1.6625 CPU PAR min 15.760 max 17.240 mean 16.625 CPU PAR min 1.296 max 1.419 mean 1.365 H min 10.376 max 10.380 mean 10.379 CPU COO min 0.704 max 1.615 mean 10.379 CPU COO min 0.704 max 1.615 mean 1.365 GPU 64 COO min 7.000 max 7.180 mean 10.379 CPU COO min 0.704 max 1.615 mean 0.806 CPU CSR min 1.355 max 1.370 mean 1.365 H min 19.376 max 1.370 mean 1.365 GPU 64 COO min 7.020 max 7.60 mean 7.083 CSR min 0.000 max 16.290 mean 15.076 CPU PAR min 1.256 max 1.520 mean 1.405 H min 9.915 max 9.925 mean 0.921 CPU COO min 6.702 max 7.210 mean 7.030 CSR min 0.000 max 15.260 mean 1.364 GPU 64 COO min 6.920 max 7.210 mean 7.030 CSR min 1.283 max* 1.531 mean 1.384 GPU 64 COO min 6.970 max 1.532 mean 0.924 GPU COO min 0.707 max 1.532 mean 0.924 GPU 64 COO min 6.970 max 7.110 mean 7.045

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	Н	min 10.377	max 10.382 m	ean 10.379	Row-Premute			
cvxqp3.mtx						CPU COO	min 0.733 max	1.640 mean 0.777
Regular						CPU CSR		2.543 mean 2.525
	CPU COO		max 0.720 m					7.320 mean 7.268
	CPU CSR		max* 2.643 m max* 6.220 m			CPU PAR		18.540 mean 18.102 1.595 mean 1.546
			max*22.710 m					10.046 mean 10.044
	CPU PAR		max* 1.860 m		Row-Gradient		11111 10.042 111dx	10.040 mcan 10.044
	Н		max 8.646 m			CPU COO	min 0.712 max	0.926 mean 0.750
Row-Premute						CPU CSR	min 1.819 max	1.846 mean 1.832
	CPU COO		max* 1.577 m					* 7.370 mean 7.298
	CPU CSR		max 2.471 m					*20.740 mean 19.089
			max 6.060 m			CPU PAR		1.554 mean 1.495
			max 19.130 m		Caluma Candinas	Н	min 9.666 max	9.704 mean 9.690
	CPU PAR H		max 1.833 m max 11.033 m		Column-Gradient	CPU COO	min 0 710 may	* 1.690 mean 0.791
Row-Gradient	11	11111 11.020	IIIax 11.033 III	ean ii.ese		CPU CSR		1.836 mean 1.830
non ordatent	CPU COO	min 0.693	max 1.523 m	nean 0.788				7.310 mean 7.211
	CPU CSR		max 1.305 m					18.690 mean 17.617
	GPU 64 CO	0 min 5.920	max 6.000 m	nean 5.962		CPU PAR	min 1.385 max	1.539 mean 1.506
	CSF	R min 16.810	max 18.410 m	ean 17.561		Н	min 10.611 max	*10.659 mean 10.634
	CPU PAR	min 1.378	max 1.485 m	nean 1.429	Row-Column-Permute			
	Н	min 11.061	max 11.069 m	ean 11.064		CPU COO		1.531 mean 0.963
Column-Gradient						CPU CSR		2.648 mean 2.622
	CPU COO		max 1.521 m					7.330 mean 7.244
	CPU CSR		max 1.302 m			CPU PAR		18.520 mean 18.148 1.574 mean 1.528
			max 6.060 m max 18.330 m					10.046 mean 10.044
	CPU PAR		max 1.464 m		OPF_6000.mtx		IIIII 10.041 IIIAX	10.040 illean 10.044
	Н		max*11.135 m		Regular			
Row-Column-Permute						CPU COO	min 0.714 max	0.731 mean 0.720
	CPU COO	min 0.704	max 1.503 m	nean 0.875		CPU CSR	min 2.667 max	* 2.770 mean 2.720
	CPU CSR	min 2.447	max 2.468 m	nean 2.459		GPU 64 COO	min 12.310 max	*12.550 mean 12.425
			max 5.980 m					*43.770 mean 42.075
			max 19.140 m			CPU PAR		1.945 mean 1.845
	CPU PAR		max 1.743 m		D D	Н	min 8.799 max	8.799 mean 8.799
case9.mtx	Н	min 11.028	max 11.035 m	ean II.030	Row-Premute	CPU COO	min 0 600 may	0.710 mean 0.695
Regular						CPU CSR		2.413 mean 2.392
Regular	CPU COO	min 0 721	max* 1.800 m	nean 1 177				11.770 mean 11.549
	CPU CSR		max* 3.046 m					25.580 mean 24.785
	GPU 64 CO	O min 0.000	max 0.000 m	nean 0.000		CPU PAR		1.896 mean 1.829
	CSI	R min 0.000	max 0.000 m	ean 0.000		Н	min 11.872 max	11.877 mean 11.875
	CPU PAR	min 1.508	max 1.605 m	nean 1.573	Row-Gradient			
	Н	min 7.380	max 7.380 m	ean 7.380		CPU COO		0.775 mean 0.739
Row-Premute						CPU CSR		1.689 mean 1.675
	CPU COO		max 1.100 m					12.410 mean 12.205
	CPU CSR		max* 2.626 m					34.910 mean 33.370
			max 7.340 m max 18.500 m			CPU PAR H		* 2.286 mean 2.207 11.116 mean 11.113
	CPU PAR		max * 1.607 m		Column-Gradient		IIIIII III.III IIIAX	11.110 mean 11.113
	Н		max 10.047 m			CPU COO	min 0.715 max	* 1.021 mean 0.743
Row-Gradient						CPU CSR		1.674 mean 1.666
	CPU COO	min 0.716	max 1.701 m	nean 0.804		GPU 64 COO	min 11.340 max	11.560 mean 11.463
	CPU CSR		max 1.840 m					25.470 mean 24.489
			max* 7.510 m			CPU PAR		2.172 mean 2.118
			max*20.710 m			Н	min 12.040 max≯	*12.047 mean 12.043
	CPU PAR H		max 1.593 m max 9.706 m		Row-Column-Permute	CPU COO	min 0 677	0.785 mean 0.687
Column-Gradient	п	11111 9.001	IIIax 9.700 II	lean 9.094		CPU CSR		2.434 mean 2.369
COTUMNI GLAGIENT	CPU COO	min 0 711	max 1.029 m	nean 0 746				11.650 mean 11.538
	CPU CSR		max 1.834 m					25.560 mean 25.008
			max 7.270 m			CPU PAR		1.776 mean 1.709
			max 18.590 m			Н		11.877 mean 11.875
	CPU PAR	min 1.390	max 1.574 m	nean 1.511	OPF_3754.mtx			
	Н	min 10.612	max*10.659 m	ean 10.634	Regular			
Row-Column-Permute						CPU COO		0.774 mean 0.747
	CPU COO		max 1.391 m			CPU CSR		* 2.919 mean 2.908
	CPU CSR		max 2.625 m max 7.320 m					* 7.820 mean 7.766 *29.030 mean 26.756
			max 7.320 m max 18.640 m			CPU PAR		*29.030 mean 26.756 1.508 mean 1.471
	CPU PAR		max 10.040 m			H H		8.393 mean 8.393
	H		max 10.046 m		Row-Premute		0.333 iildX	5.555 mcail 6.535
TSOPF_FS_b9_c6.mtx						CPU COO	min 0.714 max	* 1.574 mean 0.817
Regular						CPU CSR		2.711 mean 2.699
	CPU COO		max 0.734 m				min 7.410 max	7.570 mean 7.484
	CPU CSR		max* 3.052 m					21.190 mean 20.307
			max 0.000 m			CPU PAR		1.505 mean 1.469
			max 0.000 m		Dow-Cradian+	Н	min II.267 max	11.272 mean 11.269
	CPU PAR H		max * 1.602 m max 7.380 m		Row-Gradient	CPU COO	min 0 723 may	1.232 mean 0.775
		/	ax 7.300 II	7.300		0.000	0.723 IIIdX	mcan 0.773

	CPU CSR min 1.672 max 1.691 mean 1.685	CSR min 15.680 max 17.870 mean 16.540
	GPU 64 COO min 7.600 max 7.760 mean 7.716	CPU PAR min 1.429 max 1.488 mean 1.468
	CSR min 23.160 max 25.590 mean 24.304	H min 10.931 max 10.945 mean 10.938
	CPU PAR min 1.675 max* 1.736 mean 1.703	Row-Column-Permute
0.1 0.11	H min 10.463 max 10.472 mean 10.468	CPU COO min 0.728 max 1.646 mean 1.037
Column-Gradient	CDU COO min 0 726 may 1 421 man 0 779	CPU CSR min 2.472 max 2.488 mean 2.480
	CPU COO min 0.726 max 1.431 mean 0.778 CPU CSR min 1.671 max 1.685 mean 1.679	GPU 64 COO min 5.410 max 5.480 mean 5.449
	GPU 64 COO min 7.410 max 7.530 mean 7.467	CSR min 15.760 max 17.560 mean 16.654 CPU PAR min 1.428 max 1.513 mean 1.474
	CSR min 18.140 max 20.350 mean 19.315	H min 10.959 max*10.967 mean 10.963
	CPU PAR min 1.650 max 1.736 mean 1.699	gen4.mtx
	H min 11.393 max*11.401 mean 11.397	Regular
Row-Column-Permute		CPU COO min 0.737 max 1.977 mean 1.431
	CPU COO min 0.711 max 1.458 mean 0.751	CPU CSR min 2.674 max 2.688 mean 2.681
	CPU CSR min 2.678 max 2.717 mean 2.700	GPU 64 COO min 5.900 max 6.000 mean 5.954
	GPU 64 COO min 7.400 max 7.540 mean 7.471	CSR min 13.650 max 15.410 mean 14.657
	CSR min 19.560 max 21.150 mean 20.453	CPU PAR min 1.468 max 1.521 mean 1.491
	CPU PAR min 1.440 max 1.499 mean 1.467	H min 9.234 max 9.234 mean 9.234
	H min 11.266 max 11.272 mean 11.269	Row-Premute
c-47.mtx		CPU COO min 0.740 max* 2.048 mean 1.121
Regular	071 000 1 0 754 1 000 1 004	CPU CSR min 2.777 max 2.798 mean 2.790
	CPU COO min 0.754 max* 1.829 mean 1.204	GPU 64 COO min 5.910 max 5.970 mean 5.944
	CPU CSR min 2.610 max* 2.624 mean 2.618	CSR min 13.700 max 15.370 mean 14.541
	GPU 64 COO min 9.530 max* 9.870 mean 9.640 CSR min 23.990 max*25.910 mean 24.992	CPU PAR min 1.468 max 1.546 mean 1.502 H min 10.250 max 10.255 mean 10.252
	CPU PAR min 1.311 max 1.380 mean 1.357	H min 10.250 max 10.255 mean 10.252 Row-Gradient
	H min 8.364 max 8.364 mean 8.364	CPU COO min 0.740 max 1.790 mean 0.994
Row-Premute	11 III11 0.304 IIIAX 0.304 IIIEA11 0.304	CPU CSR min 2.663 max 2.682 mean 2.674
Now 11 clilate	CPU COO min 0.740 max 0.885 mean 0.755	GPU 64 COO min 5.890 max* 6.160 mean 5.946
	CPU CSR min 2.574 max 2.611 mean 2.597	CSR min 13.780 max*17.520 mean 15.601
	GPU 64 COO min 9.320 max 9.510 mean 9.397	CPU PAR min 1.479 max* 1.619 mean 1.569
	CSR min 19.960 max 21.190 mean 20.696	H min 9.939 max 9.955 mean 9.948
	CPU PAR min 1.303 max 1.371 mean 1.345	Column-Gradient
	H min 10.059 max 10.062 mean 10.061	CPU COO min 0.743 max 1.991 mean 0.981
Row-Gradient		CPU CSR min 2.620 max 2.654 mean 2.646
	CPU COO min 0.723 max 0.984 mean 0.753	GPU 64 COO min 5.840 max 5.910 mean 5.885
	CPU CSR min 1.781 max 1.809 mean 1.803	CSR min 13.130 max 17.040 mean 15.008
	GPU 64 COO min 9.380 max 9.660 mean 9.464	CPU PAR min 1.477 max 1.607 mean 1.559
	CSR min 15.770 max 19.090 mean 18.037	H min 10.858 max*10.876 mean 10.864
	CPU PAR min 1.775 max* 1.924 mean 1.868	Row-Column-Permute
Column-Gradient	H min 10.205 max 10.233 mean 10.219	CPU COO min 0.742 max 2.010 mean 1.124 CPU CSR min 2.789 max* 2.800 mean 2.795
corumn-Gradient	CPU COO min 0.715 max 0.926 mean 0.757	GPU 64 COO min 5.900 max 5.980 mean 5.941
	CPU CSR min 1.729 max 1.802 mean 1.791	CSR min 13.640 max 15.410 mean 14.556
	GPU 64 COO min 9.080 max 9.270 mean 9.158	CPU PAR min 1.462 max 1.540 mean 1.504
	CSR min 13.980 max 15.780 mean 14.938	H min 10.250 max 10.253 mean 10.252
	CPU PAR min 1.751 max 1.906 mean 1.846	Maragal_6.mtx
	H min 11.213 max*11.232 mean 11.222	Regular
Row-Column-Permute		CPU COO min 0.725 max 0.741 mean 0.729
	CPU COO min 0.732 max 1.598 mean 0.785	CPU CSR min 2.345 max 2.409 mean 2.372
	CPU CSR min 2.594 max 2.602 mean 2.599	GPU 64 COO min 18.200 max 18.770 mean 18.357
	GPU 64 COO min 9.340 max 9.460 mean 9.394	CSR min 38.310 max*40.240 mean 39.477
	CSR min 19.950 max 21.500 mean 20.544	CPU PAR min 0.789 max 0.813 mean 0.797
	CPU PAR min 1.326 max 1.374 mean 1.354	H min 9.930 max 9.930 mean 9.930
	H min 10.059 max 10.062 mean 10.061	Row-Premute
mhd4800a.mtx		CPU COO min 0.709 max 0.779 mean 0.715
Regular	CDU COO 0 750 - 0 755	CPU CSR min 2.675 max 2.715 mean 2.696
	CPU COO min 0.759 max 0.795 mean 0.780	GPU 64 COO min 17.810 max 18.030 mean 17.935
	CPU CSR min 2.479 max* 2.565 mean 2.557	CSR min 29.650 max 30.580 mean 30.109 CPU PAR min 0.857 max 0.940 mean 0.904
	GPU 64 COO min 5.490 max* 5.650 mean 5.552	
	CSR min 16.700 max 19.460 mean 18.004 CPU PAR min 1.456 max * 1.523 mean 1.492	H min 10.777 max 10.779 mean 10.778 Row-Gradient
	H min 7.132 max 7.132 mean 7.132	CPU COO min 0.710 max* 1.566 mean 0.755
Row-Premute	n IIIII 7.132 IIIdX 7.132 IIIedii 7.132	CPU CSR min 2.042 max 2.159 mean 2.120
Now I remute	CPU COO min 0.695 max 0.943 mean 0.726	GPU 64 COO min 18.460 max*18.960 mean 18.665
	CPU CSR min 2.480 max 2.488 mean 2.485	CSR min 25.650 max 27.330 mean 26.549
	GPU 64 COO min 5.410 max 5.490 mean 5.453	CPU PAR min 2.257 max 2.612 mean 2.416
	CSR min 15.700 max 17.520 mean 16.678	H min 11.251 max 11.301 mean 11.285
	CPU PAR min 1.422 max 1.514 mean 1.474	Column-Gradient
	H min 10.959 max 10.966 mean 10.963	CPU COO min 0.711 max 0.743 mean 0.725
Row-Gradient		CPU CSR min 2.036 max 2.161 mean 2.110
	CPU COO min 0.723 max* 2.029 mean 0.990	GPU 64 COO min 17.840 max 18.860 mean 18.149
	CPU CSR min 2.411 max 2.427 mean 2.421	CSR min 19.410 max 20.690 mean 20.066
	GPU 64 COO min 5.490 max 5.560 mean 5.534	CPU PAR min 2.174 max* 2.546 mean 2.349
	CSR min 16.350 max*19.560 mean 17.784	H min 12.011 max*12.072 mean 12.052
	CPU PAR min 1.441 max 1.509 mean 1.477	Row-Column-Permute
Calumn Cu-di	H min 9.512 max 9.526 mean 9.520	CPU COO min 0.712 max 0.971 mean 0.737
Column-Gradient	CBII COO min A 721 may 1 982 man 2 971	CPU CSR min 2.732 max* 2.751 mean 2.743
	CPU COO min 0.721 max 1.802 mean 0.871 CPU CSR min 2.393 max 2.408 mean 2.404	GPU 64 COO min 17.720 max 18.070 mean 17.911
		CSR min 29.600 max 30.500 mean 29.961
	GPU 64 COO min 5.410 max 5.480 mean 5.453	CPU PAR min 0.827 max 0.954 mean 0.913

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	Н	min 10.776 max	10.778 mean	10.777	Row-Premute	
aft01.mtx						GPU 64 COO min 3.860 max 4.090 mean 4.001
Regular						CSR min 9.520 max 10.340 mean 9.936
	CPU COO	min 0.735 max				H min 11.161 max 11.167 mean 11.165
	CPU CSR	min 3.132 max			Row-Gradient	CDU 64 600 4 010 4 240 4 125
		0 min 6.390 max min 19.990 max				GPU 64 COO min 4.010 max 4.240 mean 4.135 CSR min 5.890 max 11.350 mean 6.882
	CPU PAR	min 1.746 max				H min 10.246 max 10.262 mean 10.256
	Н	min 7.811 max			Column-Gradient	11 IIII 10.240 IIIAX 10.202 IIICAN 10.230
Row-Premute						GPU 64 COO min 3.850 max 4.100 mean 4.012
	CPU COO	min 0.714 max				CSR min 5.460 max 8.790 mean 6.005
	CPU CSR	min 2.864 max				H min 11.112 max 11.122 mean 11.117
		0 min 6.280 max			Row-Column-Permute	
		min 17.980 max				GPU 64 COO min 3.850 max 4.080 mean 3.990
	CPU PAR H	min 1.729 max min 11.162 max				CSR min 5.420 max 6.760 mean 5.977 H min 11.162 max*11.169 mean 11.165
Row-Gradient	11	IIIII II. IUZ IIIdx	11.100 illean	1 11.103	bloweya.mtx	II IIII II.102 IIIAXXII.103 IIIEAN III.103
non ordatent	CPU COO	min 0.735 max	1.806 mear	0.878	Regular	
	CPU CSR	min 2.706 max				GPU 64 COO min 0.000 max 0.000 mean 0.000
	GPU 64 CO	O min 6.390 max	6.500 mear	6.433		CSR min 0.000 max 0.000 mean 0.000
	CSF	min 19.780 max	22.870 mean	20.936		H min 7.205 max 7.205 mean 7.205
	CPU PAR	min 1.710 max			Row-Premute	
	Н	min 10.251 max	10.267 mean	10.257		GPU 64 COO min 3.800 max 3.940 mean 3.875
Column-Gradient	0011 000		4 700			CSR min 3.710 max 4.570 mean 4.399
	CPU COO	min 0.728 max			Daw Candinat	H min 11.025 max 11.031 mean 11.028
	CPU CSR	min 2.521 max O min 6.280 max			Row-Gradient	GPU 64 COO min 3.800 max* 4.120 mean 3.962
		min 18.000 max				CSR min 4.340 max* 4.670 mean 4.546
	CPU PAR	min 1.649 max				H min 10.296 max 10.307 mean 10.300
	Н	min 11.113 max			Column-Gradient	
Row-Column-Permute						GPU 64 COO min 3.880 max 4.100 mean 3.978
	CPU COO	min 0.714 max	1.525 mear	n 0.957		CSR min 4.240 max 4.570 mean 4.412
	CPU CSR	min 2.876 max				H min 10.881 max 10.886 mean 10.883
		O min 6.280 max			Row-Column-Permute	
		min 17.960 max				GPU 64 COO min 3.800 max 3.980 mean 3.885
	CPU PAR	min 1.667 max				CSR min 4.130 max 4.540 mean 4.399 H min 11.025 max*11.033 mean 11.029
TSOPF_RS_b39_c7.mtx	Н	min 11.162 max	*11.100 Illean	1 11.105	brainpc2.mtx	H min 11.025 max*11.033 mean 11.029
Regular					Regular	
Regular	CPU COO	min 0.771 max	0.793 mear	0.780	перата	GPU 64 COO min 0.000 max 0.000 mean 0.000
	CPU CSR	min 3.219 max				CSR min 0.000 max 0.000 mean 0.000
	GPU 64 COC	min 11.070 max				H min 7.478 max 7.478 mean 7.478
	CSR	min 37.050 max	*42.100 mean	39.040	Row-Premute	
	CPU PAR	min 1.910 max				GPU 64 COO min 3.840 max* 6.750 mean 4.110
	Н	min 7.304 max	7.304 mear	n 7.304		CSR min 4.260 max* 4.500 mean 4.437
Row-Premute	0011 000		. 700		B 0 1: 4	H min 9.809 max 9.813 mean 9.811
	CPU COO CPU CSR	min 0.701 max min 2.931 max			Row-Gradient	CDII 64 COO min
		min 10.860 max				GPU 64 COO min 0.640 max 4.030 mean 3.864 CSR min 4.270 max 4.470 mean 4.383
		min 28.730 max				H min 9.722 max 9.727 mean 9.724
	CPU PAR	min 1.760 max			Column-Gradient	11
	Н	min 10.537 max				GPU 64 COO min 0.640 max 4.070 mean 3.898
Row-Gradient						CSR min 4.230 max 4.500 mean 4.386
	CPU COO	min 0.747 max				H min 10.368 max*10.372 mean 10.370
	CPU CSR	min 2.606 max			Row-Column-Permute	
) min 10.850 max				GPU 64 COO min 3.980 max 4.110 mean 4.027
	CSF CPU PAR	min 33.910 max min 2.154 max				CSR min 4.320 max 4.490 mean 4.437 H min 9.809 max 9.813 mean 9.811
	H	min 9.636 max			c-47.mtx	11 IIII1 3.003 IIIAX 3.013 IIIEAN 3.011
Column-Gradient		5.050 11107	. 5.070 mcai	. 5.072	Regular	
	CPU COO	min 0.718 max	* 1.693 mear	0.802		GPU 64 COO min 3.980 max* 4.080 mean 4.026
	CPU CSR	min 2.502 max	2.585 mear	2.547		CSR min 4.760 max 4.850 mean 4.812
	GPU 64 CO) min 10.700 max	10.990 mear	10.804		H min 8.364 max 8.364 mean 8.364
		min 27.230 max			Row-Premute	
	CPU PAR	min 2.128 max				GPU 64 COO min 3.880 max 4.010 mean 3.942
D C.1 D	Н	min 11.131 max	*11.222 mean	111.208		CSR min 4.040 max 4.900 mean 4.807
Row-Column-Permute	CPU COO	min 0.709 max	, A 726 moor	0 716	Row-Gradient	H min 10.059 max 10.063 mean 10.061
	CPU CSR	min 2.917 max			Now drautent	GPU 64 COO min 3.900 max 4.050 mean 3.976
		min 10.840 max				CSR min 4.380 max 4.740 mean 4.630
		min 28.780 max				H min 10.201 max 10.228 mean 10.214
	CPU PAR	min 1.757 max			Column-Gradient	
	Н	min 10.537 max				GPU 64 COO min 3.860 max 3.990 mean 3.936
						CSR min 4.350 max 4.610 mean 4.525
10 ELLECA	DE					H min 11.204 max*11.241 mean 11.222
10 ELLESMI	CKE				Row-Column-Permute	CDII 64 COO min 2 900 4 020 2 050
aft01.mtx						GPU 64 COO min 3.890 max 4.020 mean 3.953 CSR min 4.490 max* 4.920 mean 4.840
Regular						H min 10.058 max 10.063 mean 10.061
		0 min 4.080 max			case9.mtx	101001
		min 9.660 max			Regular	
	Н	min 7.811 max	. /.oii iilear	. /.011		

	GPU 64 COO min 0.000 max 0.000 mean 0.000	Н	min 10.250 max 10.255 mean 10.252
	CSR min 0.000 max 0.000 mean 0.000	lp_fit2d.mtx	
	H min 7.380 max 7.380 mean 7.380	Regular	
Row-Premute			COO min 4.360 max* 4.640 mean 4.515
	GPU 64 COO min 4.820 max 4.940 mean 4.859		CSR min 10.080 max 10.900 mean 10.491
	CSR min 5.080 max 6.520 mean 6.342 H min 10.042 max 10.047 mean 10.044	H Row-Premute	min 11.109 max 11.109 mean 11.109
Row-Gradient	n IIIIn 10.042 IIIax 10.047 IIIean 10.044		COO min 4.170 max 4.630 mean 4.476
NOW GLAUTELL	GPU 64 COO min 4.810 max* 4.940 mean 4.876	GI 0 04	CSR min 0.910 max 10.910 mean 10.257
	CSR min 6.100 max* 6.560 mean 6.307	н	min 11.098 max 11.104 mean 11.101
	H min 9.681 max 9.704 mean 9.694	Row-Gradient	
Column-Gradient		GPU 64	COO min 4.370 max 4.630 mean 4.529
	GPU 64 COO min 4.810 max 4.930 mean 4.869		CSR min 10.030 max 10.970 mean 10.624
	CSR min 4.820 max 6.460 mean 6.208	Н	min 11.109 max 11.109 mean 11.109
	H min 10.554 max*10.661 mean 10.638	Column-Gradient	
Row-Column-Permute	CDU 54 500 4 010 4 040 4 054		COO min 4.250 max 4.640 mean 4.499
	GPU 64 COO min 4.810 max 4.940 mean 4.864 CSR min 5.930 max 6.520 mean 6.379	Н	CSR min 8.510 max*11.010 mean 10.505 min 11.328 max*11.333 mean 11.331
	H min 10.041 max 10.047 mean 10.044	Row-Column-Permute	111 11.326 ax* 11.333 eal 11.331
cvxqp3.mtx	11 10.041 max 10.047 mean 10.044		COO min 4.350 max 4.640 mean 4.511
Regular			CSR min 10.040 max 10.790 mean 10.468
	GPU 64 COO min 3.350 max* 3.590 mean 3.483	Н	min 11.097 max 11.106 mean 11.101
	CSR min 5.430 max* 9.260 mean 8.333	lp_osa_07.mtx	
	H min 8.646 max 8.646 mean 8.646	Regular	
Row-Premute		GPU 64	COO min 0.460 max* 3.640 mean 3.456
	GPU 64 COO min 3.230 max 3.480 mean 3.371		CSR min 5.570 max* 8.530 mean 8.106
	CSR min 7.560 max 8.220 mean 7.900	Н	min 8.412 max 8.412 mean 8.412
	H min 11.027 max 11.033 mean 11.030	Row-Premute	
Row-Gradient	ORU 64 000 ' 0 040 0 540 0 000	GPU 64	COO min 3.140 max 3.450 mean 3.367
	GPU 64 COO min 3.240 max 3.510 mean 3.396 CSR min 6.990 max 7.890 mean 7.574	Н	CSR min 7.600 max 8.070 mean 7.853 min 9.255 max 9.258 mean 9.256
	H min 11.060 max 11.069 mean 11.064	Row-Gradient	9.233 3.236 ear 9.236
Column-Gradient	n min 11.000 max 11.005 mean 11.004		COO min 3.190 max 3.610 mean 3.509
COTUMN OF BUTCHE	GPU 64 COO min 3.240 max 3.480 mean 3.374	0.004	CSR min 0.000 max 8.260 mean 7.597
	CSR min 6.980 max 7.900 mean 7.557	н	min 8.583 max 8.678 mean 8.670
	H min 11.126 max*11.134 mean 11.130	Column-Gradient	
Row-Column-Permute		GPU 64	COO min 3.330 max 3.500 mean 3.416
	GPU 64 COO min 3.110 max 3.470 mean 3.365		CSR min 6.730 max 7.540 mean 7.199
	CSR min 4.810 max 8.210 mean 7.742	Н	min 9.542 max* 9.604 mean 9.581
40. 4	H min 11.026 max 11.032 mean 11.030	Row-Column-Permute	
ex19.mtx		GPU 64	COO min 3.290 max 3.430 mean 3.365
Regular	GPU 64 COO min 2.450 max* 2.610 mean 2.564	Н	CSR min 7.390 max 8.060 mean 7.832 min 9.255 max 9.258 mean 9.256
	CSR min 4.490 max 4.760 mean 4.714	Maragal_6.mtx	11111 9.233 1110X 9.230 111eati 9.230
	H min 8.228 max 8.228 mean 8.228	Regular	
Row-Premute	The state and state and state		COO min 4.160 max 4.310 mean 4.217
	GPU 64 COO min 2.000 max 2.040 mean 2.021		CSR min 4.940 max 4.960 mean 4.956
	GPU 64 COO min 2.000 max 2.040 mean 2.021 CSR min 4.640 max 4.780 mean 4.733	н	CSR min 4.940 max 4.960 mean 4.956 min 9.930 max 9.930 mean 9.930
		H Row-Premute	min 9.930 max 9.930 mean 9.930
Row-Gradient	CSR min 4.640 max 4.780 mean 4.733 H min 11.835 max 11.840 mean 11.838	H Row-Premute GPU 64	min 9.930 max 9.930 mean 9.930 COO min 4.220 max 4.240 mean 4.225
Row-Gradient	CSR min 4.640 max 4.780 mean 4.733 H min 11.835 max 11.840 mean 11.838 GPU 64 COO min 2.240 max 2.390 mean 2.329	H Row-Premute GPU 64	min 9.930 max 9.930 mean 9.930 COO min 4.220 max 4.240 mean 4.225 CSR min 4.750 max*13.040 mean 5.133
Row-Gradient	CSR min 4.640 max 4.780 mean 4.733 H min 11.835 max 11.840 mean 11.838 GPU 64 COO min 2.240 max 2.390 mean 2.329 CSR min 4.570 max* 4.850 mean 4.807	H Row-Premute GPU 64 H	min 9.930 max 9.930 mean 9.930 COO min 4.220 max 4.240 mean 4.225
	CSR min 4.640 max 4.780 mean 4.733 H min 11.835 max 11.840 mean 11.838 GPU 64 COO min 2.240 max 2.390 mean 2.329	Row-Premute GPU 64 Row-Gradient	min 9.930 max 9.930 mean 9.930 COO min 4.220 max 4.240 mean 4.225 CSR min 4.750 max*13.040 mean 5.133 min 10.776 max 10.778 mean 10.777
Row-Gradient Column-Gradient	CSR min 4.640 max 4.780 mean 4.733 H min 11.835 max 11.840 mean 11.838 GPU 64 COO min 2.240 max 2.390 mean 2.329 CSR min 4.570 max* 4.850 mean 4.807 H min 10.742 max 10.752 mean 10.747	Row-Premute GPU 64 Row-Gradient	min 9.930 max 9.930 mean 9.930 COO min 4.220 max 4.240 mean 4.225 CSR min 4.750 max*13.040 mean 5.133 min 10.776 max 10.778 mean 10.777 COO min 4.180 max* 4.450 mean 4.245
	CSR min 4.640 max 4.780 mean 4.733 H min 11.835 max 11.840 mean 11.838 GPU 64 COO min 2.240 max 2.390 mean 2.329 CSR min 4.570 max* 4.850 mean 4.807 H min 10.742 max 10.752 mean 10.747 GPU 64 COO min 2.010 max 2.050 mean 2.034	Row-Premute GPU 64 Row-Gradient	min 9.930 max 9.930 mean 9.930 COO min 4.220 max 4.240 mean 4.225 CSR min 4.750 max*13.040 mean 5.133 min 10.776 max 10.778 mean 10.777 COO min 4.180 max* 4.450 mean 4.245 CSR min 4.880 max 4.940 mean 4.915
	CSR min 4.640 max 4.780 mean 4.733 H min 11.835 max 11.840 mean 11.838 GPU 64 COO min 2.240 max 2.390 mean 2.329 CSR min 4.570 max* 4.850 mean 4.807 H min 10.742 max 10.752 mean 10.747	Row-Premute GPU 64 Row-Gradient GPU 64	min 9.930 max 9.930 mean 9.930 COO min 4.220 max 4.240 mean 4.225 CSR min 4.750 max*13.040 mean 5.133 min 10.776 max 10.778 mean 10.777 COO min 4.180 max* 4.450 mean 4.245
	CSR min 4.640 max 4.780 mean 4.733 H min 11.835 max 11.840 mean 11.838 GPU 64 COO min 2.240 max 2.390 mean 2.329 CSR min 4.570 max* 4.850 mean 4.807 H min 10.742 max 10.752 mean 10.747 GPU 64 COO min 2.010 max 2.050 mean 2.034 CSR min 4.570 max 4.760 mean 4.701	Row-Premute GPU 64 H Row-Gradient GPU 64 H Column-Gradient	min 9.930 max 9.930 mean 9.930 COO min 4.220 max 4.240 mean 4.225 CSR min 4.750 max*13.040 mean 5.133 min 10.776 max 10.778 mean 10.777 COO min 4.180 max* 4.450 mean 4.245 CSR min 4.880 max 4.940 mean 4.915
Column-Gradient	CSR min 4.640 max 4.780 mean 4.733 H min 11.835 max 11.840 mean 11.838 GPU 64 COO min 2.240 max 2.390 mean 2.329 CSR min 4.570 max* 4.850 mean 4.807 H min 10.742 max 10.752 mean 10.747 GPU 64 COO min 2.010 max 2.050 mean 2.034 CSR min 4.570 max 4.760 mean 4.701	Row-Premute GPU 64 H Row-Gradient GPU 64 H Column-Gradient	min 9.930 max 9.930 mean 9.930 COO min 4.220 max 4.240 mean 4.225 CSR min 4.750 max*13.040 mean 5.133 min 10.776 max 10.778 mean 10.777 COO min 4.180 max* 4.450 mean 4.245 CSR min 4.880 max 4.940 mean 4.915 min 11.259 max*11.302 mean 11.281
Column-Gradient	CSR min 4.640 max 4.780 mean 4.733 H min 11.835 max 11.840 mean 11.838 GPU 64 COO min 2.240 max 2.390 mean 2.329 CSR min 4.570 max* 4.850 mean 4.867 H min 10.742 max 10.752 mean 10.747 GPU 64 COO min 2.010 max 2.050 mean 2.034 CSR min 4.570 max 4.760 mean 4.701 H min 11.872 max*11.881 mean 11.878 GPU 64 COO min 2.000 max 2.040 mean 2.023 CSR min 0.770 max 4.780 mean 4.594	Row-Premute GPU 64 Row-Gradient GPU 64 Column-Gradient GPU 64 H H	min 9.930 max 9.930 mean 9.930 COO min 4.220 max 4.240 mean 4.225 CSR min 4.750 max*13.040 mean 5.133 min 10.776 max 10.778 mean 10.777 COO min 4.180 max* 4.450 mean 4.245 CSR min 4.880 max 4.940 mean 4.915 min 11.259 max*11.302 mean 11.281 COO min 4.200 max 4.250 mean 4.236
Column-Gradient Row-Column-Permute	CSR min 4.640 max 4.780 mean 4.733 H min 11.835 max 11.840 mean 11.838 GPU 64 COO min 2.240 max 2.390 mean 2.329 CSR min 4.570 max* 4.850 mean 4.807 H min 10.742 max 10.752 mean 10.747 GPU 64 COO min 2.010 max 2.050 mean 2.034 CSR min 4.570 max 4.760 mean 4.701 H min 11.872 max*11.881 mean 11.878 GPU 64 COO min 2.000 max 2.040 mean 2.023	Row-Premute GPU 64 H Row-Gradient GPU 64 H Column-Gradient GPU 64 H Row-Column-Permute	min 9.930 max 9.930 mean 9.930 COO min 4.220 max 4.240 mean 4.225 CSR min 4.750 max*13.040 mean 5.133 min 10.776 max 10.778 mean 10.777 COO min 4.180 max* 4.450 mean 4.245 CSR min 4.880 max 4.940 mean 4.915 min 11.259 max*11.302 mean 11.281 COO min 4.200 max 4.250 mean 4.236 CSR min 4.800 max 4.890 mean 4.859 min 12.022 max 12.073 mean 12.051
Column-Gradient Row-Column-Permute gen4.mtx	CSR min 4.640 max 4.780 mean 4.733 H min 11.835 max 11.840 mean 11.838 GPU 64 COO min 2.240 max 2.390 mean 2.329 CSR min 4.570 max* 4.850 mean 4.867 H min 10.742 max 10.752 mean 10.747 GPU 64 COO min 2.010 max 2.050 mean 2.034 CSR min 4.570 max 4.760 mean 4.701 H min 11.872 max*11.881 mean 11.878 GPU 64 COO min 2.000 max 2.040 mean 2.023 CSR min 0.770 max 4.780 mean 4.594	Row-Premute GPU 64 H Row-Gradient GPU 64 H Column-Gradient GPU 64 H Row-Column-Permute	min 9.930 max 9.930 mean 9.930 COO min 4.220 max 4.240 mean 4.225 CSR min 4.750 max*13.040 mean 5.133 min 10.776 max 10.778 mean 10.777 COO min 4.180 max* 4.450 mean 4.245 CSR min 4.880 max 4.940 mean 4.915 min 11.259 max*11.302 mean 11.281 COO min 4.200 max 4.250 mean 4.236 CSR min 4.800 max 4.890 mean 4.859 min 12.022 max 12.073 mean 12.051 COO min 4.210 max 4.230 mean 4.222
Column-Gradient Row-Column-Permute	CSR min 4.640 max 4.780 mean 4.733 H min 11.835 max 11.840 mean 11.838 GPU 64 COO min 2.240 max 2.390 mean 2.329 CSR min 4.570 max* 4.850 mean 4.807 H min 10.742 max 10.752 mean 10.747 GPU 64 COO min 2.010 max 2.050 mean 2.034 CSR min 4.570 max 4.760 mean 4.701 H min 11.872 max*11.881 mean 11.878 GPU 64 COO min 2.000 max 2.040 mean 2.023 CSR min 0.770 max 4.780 mean 4.594 H min 11.835 max 11.840 mean 11.838	Row-Premute GPU 64 Row-Gradient GPU 64 Column-Gradient GPU 64 Row-Column-Permute GPU 64	min 9.930 max 9.930 mean 9.930 COO min 4.220 max 4.240 mean 4.225 CSR min 4.750 max*13.040 mean 5.133 min 10.776 max 10.778 mean 10.777 COO min 4.180 max* 4.450 mean 4.245 CSR min 4.880 max 4.940 mean 4.915 min 11.259 max*11.302 mean 11.281 COO min 4.200 max 4.250 mean 4.236 CSR min 4.800 max 4.250 mean 4.255 min 12.022 max 12.073 mean 12.051 COO min 4.210 max 4.230 mean 4.222 CSR min 4.860 max 4.230 mean 4.222 CSR min 4.860 max 4.230 mean 4.222
Column-Gradient Row-Column-Permute gen4.mtx	CSR min 4.640 max 4.780 mean 4.733 H min 11.835 max 11.840 mean 11.838 GPU 64 COO min 2.240 max 2.390 mean 2.329 CSR min 4.570 max* 4.850 mean 4.807 H min 10.742 max 10.752 mean 10.747 GPU 64 COO min 2.010 max 2.050 mean 2.034 CSR min 4.570 max 4.760 mean 4.701 H min 11.872 max*11.881 mean 11.878 GPU 64 COO min 2.000 max 2.040 mean 2.023 CSR min 0.770 max 4.780 mean 4.594 H min 11.835 max 11.840 mean 11.838	Row-Premute GPU 64 Row-Gradient GPU 64 Column-Gradient GPU 64 Row-Column-Permute GPU 64 H Row-Column-Permute GPU 64	min 9.930 max 9.930 mean 9.930 COO min 4.220 max 4.240 mean 4.225 CSR min 4.750 max*13.040 mean 5.133 min 10.776 max 10.778 mean 10.777 COO min 4.180 max* 4.450 mean 4.245 CSR min 4.880 max 4.940 mean 4.915 min 11.259 max*11.302 mean 11.281 COO min 4.200 max 4.250 mean 4.236 CSR min 4.800 max 4.890 mean 4.859 min 12.022 max 12.073 mean 12.051 COO min 4.210 max 4.230 mean 4.222
Column-Gradient Row-Column-Permute gen4.mtx	CSR min 4.640 max 4.780 mean 4.733 H min 11.835 max 11.840 mean 11.838 GPU 64 COO min 2.240 max 2.390 mean 2.329 CSR min 4.570 max* 4.850 mean 4.807 H min 10.742 max 10.752 mean 10.747 GPU 64 COO min 2.010 max 2.050 mean 2.034 CSR min 4.570 max 4.760 mean 4.761 H min 11.872 max*11.881 mean 11.878 GPU 64 COO min 2.000 max 2.040 mean 2.023 CSR min 0.770 max 4.780 mean 4.594 H min 11.835 max 11.840 mean 11.838 GPU 64 COO min 4.880 max 4.980 mean 4.900 CSR min 10.020 max*11.300 mean 10.716	Row-Premute	min 9.930 max 9.930 mean 9.930 COO min 4.220 max 4.240 mean 4.225 CSR min 4.750 max*13.040 mean 5.133 min 10.776 max 10.778 mean 10.777 COO min 4.180 max* 4.450 mean 4.245 CSR min 4.880 max 4.940 mean 4.915 min 11.259 max*11.302 mean 11.281 COO min 4.200 max 4.250 mean 4.236 CSR min 4.800 max 4.250 mean 4.255 min 12.022 max 12.073 mean 12.051 COO min 4.210 max 4.230 mean 4.222 CSR min 4.860 max 4.230 mean 4.222 CSR min 4.860 max 4.230 mean 4.222
Column-Gradient Row-Column-Permute gen4.mtx Regular	CSR min 4.640 max 4.780 mean 4.733 H min 11.835 max 11.840 mean 11.838 GPU 64 COO min 2.240 max 2.390 mean 2.329 CSR min 4.570 max* 4.850 mean 4.807 H min 10.742 max 10.752 mean 10.747 GPU 64 COO min 2.010 max 2.050 mean 2.034 CSR min 4.570 max 4.760 mean 4.701 H min 11.872 max*11.881 mean 11.878 GPU 64 COO min 2.000 max 2.040 mean 2.023 CSR min 0.770 max 4.780 mean 4.594 H min 11.835 max 11.840 mean 11.838	Row-Premute GPU 64 Row-Gradient GPU 64 H Column-Gradient GPU 64 H Row-Column-Permute GPU 64 H mhd4800a.mtx Regular	min 9.930 max 9.930 mean 9.930 COO min 4.220 max 4.240 mean 4.225 CSR min 4.750 max*13.040 mean 5.133 min 10.776 max 10.778 mean 10.777 COO min 4.180 max* 4.450 mean 4.245 CSR min 4.880 max 4.940 mean 4.915 min 11.259 max*11.302 mean 11.281 COO min 4.200 max 4.250 mean 4.250 CSR min 4.800 max 4.890 mean 4.859 min 12.022 max 12.073 mean 12.051 COO min 4.210 max 4.230 mean 4.222 CSR min 4.860 max 4.890 mean 4.278
Column-Gradient Row-Column-Permute gen4.mtx	CSR min 4.640 max 4.780 mean 4.733 H min 11.835 max 11.840 mean 11.838 GPU 64 COO min 2.240 max 2.390 mean 2.329 CSR min 4.570 max* 4.850 mean 4.807 H min 10.742 max 10.752 mean 10.747 GPU 64 COO min 2.010 max 2.050 mean 2.034 CSR min 4.570 max 4.760 mean 4.701 H min 11.872 max*11.881 mean 11.878 GPU 64 COO min 2.000 max 2.040 mean 2.023 CSR min 0.770 max 4.780 mean 4.594 H min 11.835 max 11.840 mean 11.838 GPU 64 COO min 4.880 max 4.980 mean 4.900 CSR min 10.020 max*11.300 mean 10.716 H min 9.234 max 9.234 mean 9.234	Row-Premute GPU 64 Row-Gradient GPU 64 Column-Gradient GPU 64 Row-Column-Permute GPU 64 H mhd4800a.mtx Regular GPU 64	min 9.930 max 9.930 mean 9.930 COO min 4.220 max 4.240 mean 4.225 CSR min 4.750 max*13.040 mean 5.133 min 10.776 max 10.778 mean 10.777 COO min 4.180 max* 4.450 mean 4.245 CSR min 4.880 max 4.940 mean 4.915 min 11.259 max*11.302 mean 11.281 COO min 4.200 max 4.250 mean 4.236 CSR min 4.800 max 4.250 mean 4.255 min 12.022 max 12.073 mean 12.051 COO min 4.210 max 4.230 mean 4.222 CSR min 4.860 max 4.230 mean 4.222 CSR min 4.860 max 4.230 mean 4.222
Column-Gradient Row-Column-Permute gen4.mtx Regular	CSR min 4.640 max 4.780 mean 4.733 H min 11.835 max 11.840 mean 11.838 GPU 64 COO min 2.240 max 2.390 mean 2.329 CSR min 4.570 max* 4.850 mean 4.807 H min 10.742 max 10.752 mean 10.747 GPU 64 COO min 2.010 max 2.050 mean 2.034 CSR min 4.570 max 4.760 mean 4.761 H min 11.872 max*11.881 mean 11.878 GPU 64 COO min 2.000 max 2.040 mean 2.023 CSR min 0.770 max 4.780 mean 4.594 H min 11.835 max 11.840 mean 11.838 GPU 64 COO min 4.880 max 4.980 mean 4.900 CSR min 10.020 max*11.300 mean 10.716	Row-Premute GPU 64 Row-Gradient GPU 64 Column-Gradient GPU 64 Row-Column-Permute GPU 64 H mhd4800a.mtx Regular GPU 64	min 9.930 max 9.930 mean 9.930 COO min 4.220 max 4.240 mean 4.225 CSR min 4.750 max*13.040 mean 5.133 min 10.776 max 10.778 mean 10.777 COO min 4.180 max* 4.450 mean 4.245 CSR min 4.880 max 4.940 mean 4.915 min 11.259 max*11.302 mean 11.281 COO min 4.200 max 4.250 mean 4.236 CSR min 4.800 max 4.890 mean 4.859 min 12.022 max 12.073 mean 12.051 COO min 4.210 max 4.230 mean 4.857 min 10.776 max 10.778 mean 10.778 COO min 4.570 max* 4.710 mean 4.608
Column-Gradient Row-Column-Permute gen4.mtx Regular	CSR min 4.640 max 4.780 mean 4.733 H min 11.835 max 11.840 mean 11.838 GPU 64 COO min 2.240 max 2.390 mean 2.329 CSR min 4.570 max* 4.850 mean 4.807 H min 10.742 max 10.752 mean 10.747 GPU 64 COO min 2.010 max 2.050 mean 2.034 CSR min 4.570 max 4.760 mean 4.761 H min 11.872 max*11.881 mean 11.878 GPU 64 COO min 2.000 max 2.040 mean 2.023 CSR min 0.770 max 4.780 mean 4.594 H min 11.835 max 11.840 mean 11.838 GPU 64 COO min 4.880 max 4.980 mean 4.900 CSR min 10.020 max*11.300 mean 10.716 H min 9.234 max 9.234 mean 9.234 GPU 64 COO min 4.860 max 4.930 mean 4.890	Row-Premute	min 9.930 max 9.930 mean 9.930 COO min 4.220 max 4.240 mean 4.225 CSR min 4.750 max*13.040 mean 5.133 min 10.776 max 10.778 mean 10.777 COO min 4.180 max* 4.450 mean 4.245 CSR min 4.880 max 4.940 mean 4.915 min 11.259 max*11.302 mean 11.281 COO min 4.200 max 4.250 mean 4.236 CSR min 4.800 max 4.890 mean 4.859 min 12.022 max 12.073 mean 12.051 COO min 4.210 max 4.230 mean 4.222 CSR min 4.860 max 4.230 mean 4.222 CSR min 10.776 max 10.778 mean 10.778
Column-Gradient Row-Column-Permute gen4.mtx Regular	CSR min 4.640 max 4.780 mean 4.733 H min 11.835 max 11.840 mean 11.838 GPU 64 COO min 2.240 max 2.390 mean 2.329 CSR min 4.570 max* 4.850 mean 4.807 H min 10.742 max 10.752 mean 10.747 GPU 64 COO min 2.010 max 2.050 mean 2.034 CSR min 4.570 max 4.760 mean 4.701 H min 11.872 max*11.881 mean 11.878 GPU 64 COO min 2.000 max 2.040 mean 2.023 CSR min 0.770 max 4.780 mean 4.594 H min 11.835 max 11.840 mean 11.838 GPU 64 COO min 4.880 max 4.980 mean 4.990 CSR min 10.020 max*11.300 mean 10.716 H min 9.234 max 9.234 mean 9.234 GPU 64 COO min 4.860 max 4.930 mean 4.890 CSR min 0.330 max 11.200 mean 10.038 H min 10.249 max 10.254 mean 10.252	Row-Premute	min 9.930 max 9.930 mean 9.930 COO min 4.220 max 4.240 mean 4.225 CSR min 4.750 max*13.040 mean 5.133 min 10.776 max 10.778 mean 10.777 COO min 4.180 max* 4.450 mean 4.245 CSR min 4.880 max 4.940 mean 4.915 min 11.259 max*11.302 mean 11.281 COO min 4.200 max 4.250 mean 4.236 CSR min 4.800 max 4.890 mean 4.859 min 12.022 max 12.073 mean 12.051 COO min 4.210 max 4.230 mean 4.222 CSR min 4.860 max 4.890 mean 4.222 CSR min 10.776 max 10.778 mean 10.778 COO min 4.570 max* 4.710 mean 4.608 CSR min 12.690 max*13.940 mean 13.369 min 7.132 max 7.132 mean 7.132
Column-Gradient Row-Column-Permute gen4.mtx Regular Row-Premute	CSR min 4.640 max 4.780 mean 4.733 H min 11.835 max 11.840 mean 11.838 GPU 64 COO min 2.240 max 2.390 mean 2.329 CSR min 4.570 max* 4.850 mean 4.807 H min 10.742 max 10.752 mean 10.747 GPU 64 COO min 2.010 max 2.050 mean 2.034 CSR min 4.570 max 4.760 mean 4.701 H min 11.872 max*11.881 mean 11.878 GPU 64 COO min 2.000 max 2.040 mean 2.023 CSR min 0.770 max 4.780 mean 4.594 H min 11.835 max 11.840 mean 11.838 GPU 64 COO min 4.880 max 4.980 mean 4.900 CSR min 0.020 max*11.300 mean 10.716 H min 9.234 max 9.234 mean 9.234 GPU 64 COO min 4.860 max 4.930 mean 4.890 CSR min 0.330 max 11.200 mean 10.038 H min 10.249 max 10.254 mean 10.252 GPU 64 COO min 4.860 max* 4.990 mean 4.998	Row-Premute	min 9.930 max 9.930 mean 9.930 COO min 4.220 max 4.240 mean 4.225 CSR min 4.750 max*13.040 mean 5.133 min 10.776 max 10.778 mean 10.777 COO min 4.180 max* 4.450 mean 4.245 CSR min 4.880 max 4.940 mean 4.915 min 11.259 max*11.302 mean 11.281 COO min 4.200 max 4.250 mean 4.256 CSR min 4.800 max 4.890 mean 4.250 min 12.022 max 12.073 mean 12.051 COO min 4.210 max 4.230 mean 4.222 CSR min 4.860 max 4.890 mean 4.222 CSR min 4.860 max 4.890 mean 4.278 COO min 4.210 max 4.230 mean 4.222 CSR min 10.776 max 10.778 mean 10.778 COO min 4.570 max* 4.710 mean 4.608 COO min 7.132 max 7.132 mean 7.132 COO min 4.420 max 4.520 mean 4.445 CSR min 10.520 max 10.880 mean 4.445
Column-Gradient Row-Column-Permute gen4.mtx Regular Row-Premute	CSR min 4.640 max 4.780 mean 4.733 H min 11.835 max 11.840 mean 11.838 GPU 64 COO min 2.240 max 2.390 mean 2.329 CSR min 4.570 max* 4.850 mean 4.807 H min 10.742 max 10.752 mean 10.747 GPU 64 COO min 2.010 max 2.050 mean 2.034 CSR min 4.570 max 4.760 mean 4.701 H min 11.872 max*11.881 mean 11.878 GPU 64 COO min 2.000 max 2.040 mean 2.023 CSR min 0.770 max 4.780 mean 4.594 H min 11.835 max 11.840 mean 11.838 GPU 64 COO min 4.880 max 4.980 mean 4.900 CSR min 10.020 max*11.300 mean 10.716 H min 9.234 max 9.234 mean 9.234 GPU 64 COO min 4.860 max 4.930 mean 14.890 CSR min 0.330 max 11.200 mean 10.338 H min 10.249 max 10.254 mean 10.252 GPU 64 COO min 4.860 max* 4.990 mean 4.908 CSR min 9.160 max* 1.240 mean 10.235	Row-Premute	min 9.930 max 9.930 mean 9.930 COO min 4.220 max 4.240 mean 4.225 CSR min 4.750 max*13.040 mean 5.133 min 10.776 max 10.778 mean 10.777 COO min 4.180 max* 4.450 mean 4.245 CSR min 4.880 max 4.940 mean 4.915 min 11.259 max*11.302 mean 11.281 COO min 4.200 max 4.250 mean 4.236 CSR min 4.800 max 4.890 mean 4.859 min 12.022 max 12.073 mean 12.051 COO min 4.210 max 4.230 mean 4.222 CSR min 4.860 max 4.890 mean 4.222 CSR min 10.776 max 10.778 mean 10.778 COO min 4.570 max* 4.710 mean 4.608 CSR min 12.690 max*13.940 mean 13.369 min 7.132 max 7.132 mean 7.132
Column-Gradient Row-Column-Permute gen4.mtx Regular Row-Premute Row-Gradient	CSR min 4.640 max 4.780 mean 4.733 H min 11.835 max 11.840 mean 11.838 GPU 64 COO min 2.240 max 2.390 mean 2.329 CSR min 4.570 max* 4.850 mean 4.807 H min 10.742 max 10.752 mean 10.747 GPU 64 COO min 2.010 max 2.050 mean 2.034 CSR min 4.570 max 4.760 mean 4.701 H min 11.872 max*11.881 mean 11.878 GPU 64 COO min 2.000 max 2.040 mean 2.023 CSR min 0.770 max 4.780 mean 4.594 H min 11.835 max 11.840 mean 11.838 GPU 64 COO min 4.880 max 4.980 mean 4.900 CSR min 0.020 max*11.300 mean 10.716 H min 9.234 max 9.234 mean 9.234 GPU 64 COO min 4.860 max 4.930 mean 4.890 CSR min 0.330 max 11.200 mean 10.038 H min 10.249 max 10.254 mean 10.252 GPU 64 COO min 4.860 max* 4.990 mean 4.998	Row-Premute	min 9.930 max 9.930 mean 9.930 COO min 4.220 max 4.240 mean 4.225 CSR min 4.750 max*13.040 mean 5.133 min 10.776 max 10.778 mean 10.777 COO min 4.180 max* 4.450 mean 4.245 CSR min 4.880 max 4.940 mean 4.915 min 11.259 max*11.302 mean 11.281 COO min 4.200 max 4.250 mean 4.236 CSR min 4.800 max 4.890 mean 4.859 min 12.022 max 12.073 mean 12.051 COO min 4.210 max 4.230 mean 12.051 COO min 4.210 max 4.230 mean 4.222 CSR min 4.860 max 4.890 mean 4.222 CSR min 10.776 max 10.778 mean 10.778 COO min 4.570 max* 4.710 mean 4.608 CSR min 12.690 max*13.940 mean 13.369 min 7.132 max 7.132 mean 7.132 COO min 4.420 max 4.520 mean 4.445 CSR min 10.520 max 10.880 mean 10.696 min 10.960 max*10.968 mean 10.963
Column-Gradient Row-Column-Permute gen4.mtx Regular Row-Premute	CSR min 4.640 max 4.780 mean 4.733 H min 11.835 max 11.840 mean 11.838 GPU 64 COO min 2.240 max 2.390 mean 2.329 CSR min 4.570 max* 4.850 mean 4.807 H min 10.742 max 10.752 mean 10.747 GPU 64 COO min 2.010 max 2.050 mean 2.034 CSR min 4.570 max 4.760 mean 4.701 H min 11.872 max*11.881 mean 11.878 GPU 64 COO min 2.000 max 2.040 mean 2.023 CSR min 0.770 max 4.780 mean 4.594 H min 11.835 max 11.840 mean 11.838 GPU 64 COO min 4.880 max 4.980 mean 4.990 CSR min 0.020 max*11.300 mean 10.716 H min 9.234 max 9.234 mean 9.234 GPU 64 COO min 4.860 max 4.930 mean 4.890 CSR min 0.330 max 11.200 mean 10.038 H min 10.249 max 10.254 mean 10.252 GPU 64 COO min 4.860 max* 4.990 mean 4.990 CSR min 9.300 max 11.240 mean 10.435 H min 9.939 max 9.961 mean 9.947	Row-Premute	min 9.930 max 9.930 mean 9.930 COO min 4.220 max 4.240 mean 4.225 CSR min 4.750 max*13.040 mean 5.133 min 10.776 max 10.778 mean 10.777 COO min 4.180 max* 4.450 mean 4.945 cSR min 4.880 max 4.940 mean 4.915 min 11.259 max*11.302 mean 11.281 COO min 4.200 max 4.250 mean 4.256 CSR min 4.800 max 4.950 mean 4.859 min 12.022 max 12.073 mean 12.051 COO min 4.210 max 4.230 mean 4.887 min 10.776 max 10.778 mean 10.778 COO min 4.570 max*4.710 mean 4.608 COO min 4.420 max 4.520 mean 4.369 min 7.132 max 7.132 mean 7.132 COO min 4.420 max 4.520 mean 4.445 CSR min 10.520 max 10.880 mean 10.696 min 10.520 max 10.880 mean 10.696 min 10.960 max*10.968 mean 10.963 COO min 4.570 max 4.690 mean 4.605
Column-Gradient Row-Column-Permute gen4.mtx Regular Row-Premute Row-Gradient	CSR min 4.640 max 4.780 mean 4.733 H min 11.835 max 11.840 mean 11.838 GPU 64 COO min 2.240 max 2.390 mean 2.329 CSR min 4.570 max* 4.850 mean 4.807 H min 10.742 max 10.752 mean 10.747 GPU 64 COO min 2.010 max 2.050 mean 2.034 CSR min 4.570 max 4.760 mean 4.701 H min 11.872 max*11.881 mean 11.878 GPU 64 COO min 2.000 max 2.040 mean 2.023 CSR min 0.770 max 4.780 mean 4.594 H min 11.835 max 11.840 mean 11.838 GPU 64 COO min 4.880 max 4.980 mean 4.900 CSR min 10.020 max*11.300 mean 10.716 H min 9.234 max 9.234 mean 9.234 GPU 64 COO min 4.860 max 4.930 mean 10.038 H min 10.249 max 10.254 mean 10.252 GPU 64 COO min 4.860 max* 4.990 mean 4.908 CSR min 9.300 mean 11.240 mean 10.252 GPU 64 COO min 4.860 max* 4.990 mean 4.908 CSR min 9.160 max 11.240 mean 10.435 H min 9.939 max 9.961 mean 9.947 GPU 64 COO min 4.780 max 4.880 mean 4.816	Row-Premute GPU 64 Row-Column-Permute GPU 64 H Row-Column-Permute GPU 64 H Row-Premute GPU 64 H Row-Premute GPU 64 H Row-Premute GPU 64 GPU 64 H Row-Premute GPU 64	min 9.930 max 9.930 mean 9.930 COO min 4.220 max 4.240 mean 4.225 CSR min 4.750 max*13.040 mean 5.133 min 10.776 max 10.778 mean 10.777 COO min 4.180 max* 4.450 mean 4.245 CSR min 4.880 max 4.940 mean 4.915 min 11.259 max*11.302 mean 11.281 COO min 4.200 max 4.250 mean 4.236 CSR min 4.800 max 4.890 mean 4.859 min 12.022 max 12.073 mean 12.051 COO min 4.210 max 4.230 mean 4.222 CSR min 4.860 max 4.990 mean 4.887 min 10.776 max 10.778 mean 10.778 COO min 4.570 max*4.710 mean 4.608 CSR min 7.132 max 7.132 mean 7.132 COO min 4.420 max 4.520 mean 4.450 CSR min 10.520 max 10.880 mean 10.963 COO min 4.570 max 4.500 mean 4.696 min 10.960 max*10.968 mean 10.963 COO min 4.570 max 4.690 mean 4.450 COO min 4.570 max 4.690 mean 4.696 min 10.960 max*10.968 mean 10.963
Column-Gradient Row-Column-Permute gen4.mtx Regular Row-Premute Row-Gradient	CSR min 4.640 max 4.780 mean 4.733 H min 11.835 max 11.840 mean 11.838 GPU 64 COO min 2.240 max 2.390 mean 2.329 CSR min 4.570 max* 4.850 mean 4.807 H min 10.742 max 10.752 mean 10.747 GPU 64 COO min 2.010 max 2.050 mean 2.034 CSR min 4.570 max 4.760 mean 4.701 H min 11.872 max*11.881 mean 11.878 GPU 64 COO min 2.000 max 2.040 mean 2.023 CSR min 0.770 max 4.780 mean 4.594 H min 11.835 max 11.840 mean 11.838 GPU 64 COO min 4.880 max 4.980 mean 4.990 CSR min 0.020 max*11.300 mean 10.716 H min 9.234 max 9.234 mean 9.234 GPU 64 COO min 4.860 max 4.930 mean 4.890 CSR min 0.330 max 11.200 mean 10.038 H min 10.249 max 10.254 mean 10.252 GPU 64 COO min 4.860 max* 4.990 mean 4.990 CSR min 9.300 max 11.240 mean 10.435 H min 9.939 max 9.961 mean 9.947	Row-Premute	min 9.930 max 9.930 mean 9.930 COO min 4.220 max 4.240 mean 4.225 CSR min 4.750 max*13.040 mean 5.133 min 10.776 max 10.778 mean 10.777 COO min 4.180 max* 4.450 mean 4.945 cSR min 4.880 max 4.940 mean 4.915 min 11.259 max*11.302 mean 11.281 COO min 4.200 max 4.250 mean 4.256 CSR min 4.800 max 4.950 mean 4.859 min 12.022 max 12.073 mean 12.051 COO min 4.210 max 4.230 mean 4.887 min 10.776 max 10.778 mean 10.778 COO min 4.570 max*4.710 mean 4.608 COO min 4.420 max 4.520 mean 4.369 min 7.132 max 7.132 mean 7.132 COO min 4.420 max 4.520 mean 4.445 CSR min 10.520 max 10.880 mean 10.696 min 10.520 max 10.880 mean 10.696 min 10.960 max*10.968 mean 10.963 COO min 4.570 max 4.690 mean 4.605
Column-Gradient Row-Column-Permute gen4.mtx Regular Row-Premute Row-Gradient	CSR min 4.640 max 4.780 mean 4.733 H min 11.835 max 11.840 mean 11.838 GPU 64 COO min 2.240 max 2.390 mean 2.329	Row-Premute	min 9.930 max 9.930 mean 9.930 COO min 4.220 max 4.240 mean 4.225 CSR min 4.750 max*13.040 mean 5.133 min 10.776 max 10.778 mean 10.777 COO min 4.180 max* 4.450 mean 4.245 CSR min 4.880 max 4.940 mean 4.915 min 11.259 max*11.302 mean 11.281 COO min 4.200 max 4.250 mean 4.236 CSR min 4.800 max 4.890 mean 4.859 min 12.022 max 12.073 mean 12.051 COO min 4.210 max 4.230 mean 4.222 CSR min 4.860 max 4.990 mean 4.887 min 10.776 max 10.778 mean 10.778 COO min 4.570 max*4.710 mean 4.608 CSR min 7.132 max 7.132 mean 7.132 COO min 4.420 max 4.520 mean 4.450 CSR min 10.520 max 10.880 mean 10.963 COO min 4.570 max 4.500 mean 4.696 min 10.960 max*10.968 mean 10.963 COO min 4.570 max 4.690 mean 4.450 COO min 4.570 max 4.690 mean 4.696 min 10.960 max*10.968 mean 10.963
Column-Gradient Row-Column-Permute gen4.mtx Regular Row-Premute Row-Gradient Column-Gradient	CSR min 4.640 max 4.780 mean 4.733 H min 11.835 max 11.840 mean 11.838 GPU 64 COO min 2.240 max 2.390 mean 2.329	Row-Premute	min 9.930 max 9.930 mean 9.930 COO min 4.220 max 4.240 mean 4.225 CSR min 4.750 max*13.040 mean 5.133 min 10.776 max 10.778 mean 10.777 COO min 4.180 max* 4.450 mean 4.945 cSR min 4.880 max 4.940 mean 11.281 COO min 4.200 max 4.250 mean 4.265 CSR min 4.800 max 4.950 mean 4.859 min 12.022 max 12.073 mean 12.051 COO min 4.210 max 4.230 mean 4.887 min 10.776 max 10.778 mean 10.778 COO min 4.570 max* 4.710 mean 4.608 COO min 4.570 max* 4.710 mean 13.369 min 7.132 max 7.132 mean 7.132 COO min 4.420 max 4.520 mean 4.608 COO min 4.570 max* 4.710 mean 10.778 COO min 4.570 max* 10.778 mean 10.778 COO min 4.570 max* 10.788 mean 10.963 COO min 4.420 max 4.520 mean 4.445 CSR min 10.520 max 10.880 mean 10.963 COO min 4.570 max 4.690 mean 4.695 COO min 4.570 max 4.690 mean 4.605 COO min 4.570 max 4.690 mean 4.605 COR min 4.570 max 9.527 mean 9.520
Column-Gradient Row-Column-Permute gen4.mtx Regular Row-Premute Row-Gradient Column-Gradient	CSR min 4.640 max 4.780 mean 4.733 H min 11.835 max 11.840 mean 11.838 GPU 64 COO min 2.240 max 2.390 mean 2.329 CSR min 4.570 max* 4.850 mean 4.867 H min 10.742 max 10.752 mean 10.747 GPU 64 COO min 2.010 max 2.050 mean 2.034 CSR min 4.570 max 4.760 mean 4.701 H min 11.872 max*11.881 mean 11.878 GPU 64 COO min 2.000 max 2.040 mean 2.023 CSR min 0.770 max 4.780 mean 4.594 H min 11.835 max 11.840 mean 11.838 GPU 64 COO min 4.880 max 4.980 mean 4.900 CSR min 0.020 max*11.300 mean 10.716 H min 9.234 max 9.234 mean 9.234 GPU 64 COO min 4.860 max 4.930 mean 10.252 GPU 64 COO min 4.860 max 4.930 mean 10.252 GPU 64 COO min 4.860 max 4.930 mean 10.252 GPU 64 COO min 4.860 max 4.930 mean 10.252 GPU 64 COO min 4.860 max 4.930 mean 10.252 GPU 64 COO min 4.860 max 4.930 mean 10.252 GPU 64 COO min 4.860 max 4.930 mean 10.252 GPU 64 COO min 4.860 max 4.930 mean 10.435 H min 10.249 max 10.254 mean 10.435 H min 5.939 max 9.961 mean 9.947 GPU 64 COO min 4.780 max 4.880 mean 4.816 CSR min 7.770 max 10.570 mean 9.407 H min 10.851 max*10.876 mean 10.864	Row-Premute	min 9.930 max 9.930 mean 9.930 COO min 4.220 max 4.240 mean 4.225 CSR min 4.750 max*13.040 mean 5.133 min 10.776 max 10.778 mean 10.777 COO min 4.180 max* 4.450 mean 4.245 CSR min 4.880 max 4.940 mean 4.915 min 11.259 max*11.302 mean 11.281 COO min 4.200 max 4.250 mean 4.236 CSR min 4.800 max 4.250 mean 12.051 COO min 4.210 max 4.230 mean 12.051 COO min 4.210 max 4.230 mean 12.073 min 10.776 max 10.778 mean 10.778 COO min 4.570 max*4.710 mean 4.608 CSR min 12.692 max 7.132 mean 7.132 COO min 4.420 max 4.520 mean 4.445 CSR min 10.520 max 10.880 mean 10.696 min 7.132 max 7.132 mean 7.132 COO min 4.420 max 4.520 mean 4.445 COO min 4.570 max 4.580 mean 4.450 COO min 4.570 max 4.590 mean 4.450 COO min 4.570 max 4.590 mean 4.450 COO min 4.570 max 4.590 mean 4.450 COO min 4.570 max 4.690 mean 4.450 CSR min 4.570 max 4.690 mean 4.450 CSR min 4.570 max 4.590 mean 4.450 CSR min 4.570 max 4.590 mean 4.450 CSR min 4.570 max 4.590 mean 4.450 CSR min 4.570 max 9.527 mean 9.520 COO min 4.430 max 9.527 mean 9.520

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Row-Column-Permute			GPU 64 COO min 4.580 max 4.870 mean 4.756
	GPU 64 COO min 4.420 max 4.520 mean 4.450		CSR min 5.630 max 6.180 mean 6.055
	CSR min 7.380 max 10.900 mean 10.598		H min 11.394 max*11.401 mean 11.397
	H min 10.959 max 10.967 mean 10.963	Row-Column-Permute	
mult_dcop_01.mtx			GPU 64 COO min 4.610 max 4.900 mean 4.780
Regular	GPU 64 COO min 3.420 max 3.630 mean 3.555		CSR min 5.010 max 6.300 mean 6.113 H min 11.268 max 11.272 mean 11.270
	CSR min 3.650 max 4.090 mean 3.814	OPF_6000.mtx	n miin 11.208 max 11.272 mean 11.270
	H min 9.689 max 9.689 mean 9.689	Regular	
Row-Premute	II MIN 5.005 Max 5.005 Mean 5.005	negazar	GPU 64 COO min 3.780 max* 3.920 mean 3.864
	GPU 64 COO min 3.450 max 3.580 mean 3.521		CSR min 4.270 max 4.360 mean 4.332
	CSR min 3.610 max 4.150 mean 3.785		H min 8.799 max 8.799 mean 8.799
	H min 10.738 max 10.742 mean 10.740	Row-Premute	
Row-Gradient			GPU 64 COO min 3.770 max 3.870 mean 3.821
	GPU 64 COO min 3.510 max* 3.660 mean 3.579		CSR min 3.970 max*11.050 mean 4.439
	CSR min 3.650 max 4.160 mean 3.806		H min 11.872 max 11.877 mean 11.875
Column-Gradient	H min 10.576 max 10.585 mean 10.580	Row-Gradient	GPU 64 COO min 3.700 max 3.870 mean 3.795
COTUMNI-OF AUTERL	GPU 64 COO min 3.460 max 3.650 mean 3.584		CSR min 4.330 max 4.440 mean 4.403
	CSR min 3.660 max* 4.240 mean 3.799		H min 11.109 max 11.116 mean 11.113
	H min 10.826 max*10.842 mean 10.836	Column-Gradient	
Row-Column-Permute			GPU 64 COO min 3.690 max 3.870 mean 3.804
	GPU 64 COO min 3.470 max 3.580 mean 3.532		CSR min 4.260 max 4.340 mean 4.308
	CSR min 3.600 max 3.980 mean 3.743		H min 12.041 max*12.045 mean 12.043
	H min 10.738 max 10.742 mean 10.740	Row-Column-Permute	
mult_dcop_02.mtx			GPU 64 COO min 3.780 max 3.860 mean 3.819
Regular	CDU 64 000 min 2 200 m 2 252		CSR min 4.090 max 4.290 mean 4.259
	GPU 64 COO min 3.390 max 3.660 mean 3.585	ahanman ACh	H min 11.873 max 11.877 mean 11.876
	CSR min 0.960 max 4.330 mean 4.162 H min 9.689 max 9.689 mean 9.689	shermanACb.mtx	
Row-Premute	H min 9.689 max 9.689 mean 9.689	Regular	GPU 64 COO min 2.920 max* 3.140 mean 3.048
Now I remute	GPU 64 COO min 3.310 max 3.600 mean 3.488		CSR min 5.550 max 5.980 mean 5.803
	CSR min 0.620 max 4.290 mean 4.132		H min 8.600 max 8.600 mean 8.600
	H min 10.738 max 10.743 mean 10.740	Row-Premute	
Row-Gradient			GPU 64 COO min 2.760 max 3.020 mean 2.898
	GPU 64 COO min 3.310 max* 3.670 mean 3.593		CSR min 2.660 max 5.830 mean 5.632
	CSR min 4.130 max* 4.430 mean 4.331		H min 10.377 max 10.381 mean 10.379
	H min 10.576 max 10.584 mean 10.580	Row-Gradient	
Column-Gradient	CDU 64 600 min 0 550 min 2 660 min 2 406		GPU 64 COO min 2.800 max 3.040 mean 2.944
	GPU 64 COO min 0.550 max 3.660 mean 3.486 CSR min 3.890 max 4.410 mean 4.275		CSR min 5.330 max* 6.020 mean 5.742 H min 9.919 max 9.925 mean 9.922
	H min 10.831 max *10.843 mean 10.836	Column-Gradient	n IIIII 9.919 IIIAX 9.923 IIIEAII 9.922
Row-Column-Permute	11 111 10.031 max. 10.043 medil 10.030	column oradicite	GPU 64 COO min 2.720 max 3.010 mean 2.926
	GPU 64 COO min 3.470 max 3.590 mean 3.542		CSR min 0.000 max 5.840 mean 5.513
	CSR min 4.190 max 4.290 mean 4.242		H min 10.587 max*10.596 mean 10.591
	H min 10.738 max 10.742 mean 10.740	Row-Column-Permute	
mult_dcop_03.mtx			GPU 64 COO min 2.780 max 3.030 mean 2.939
Regular			CSR min 4.860 max 5.810 mean 5.667
	GPU 64 COO min 3.360 max* 3.660 mean 3.550	T0005 50 10 0 1	H min 10.376 max 10.382 mean 10.379
		TSOPF_FS_b9_c6.mtx	
Row-Premute	H min 9.689 max 9.689 mean 9.689	Regular	GPU 64 COO min 0.000 max 0.000 mean 0.000
Now I remute	GPU 64 COO min 3.450 max 3.580 mean 3.521		CSR min 0.000 max 0.000 mean 0.000
	CSR min 3.610 max 4.160 mean 3.784		H min 7.380 max 7.380 mean 7.380
	H min 10.738 max 10.743 mean 10.740	Row-Premute	
Row-Gradient			GPU 64 COO min 4.540 max 4.940 mean 4.874
	GPU 64 COO min 3.470 max 3.660 mean 3.572		CSR min 6.280 max 6.520 mean 6.403
	CSR min 3.640 max 4.190 mean 3.809	Davida d	H min 10.042 max 10.047 mean 10.044
Column Cood:+	H min 10.572 max 10.584 mean 10.580	Row-Gradient	GPU 64 COO min 4.830 max 4.930 mean 4.875
Column-Gradient	GPU 64 COO min 3.430 max 3.650 mean 3.562		CSR min 5.790 max 4.930 mean 4.875
	CSR min 3.670 max* 4.290 mean 3.793		H min 9.675 max 9.706 mean 9.692
	H min 10.828 max*10.840 mean 10.834	Column-Gradient	3.073 max 3.700 mean 3.032
Row-Column-Permute			GPU 64 COO min 4.790 max* 4.960 mean 4.880
	GPU 64 COO min 3.370 max 3.610 mean 3.502		CSR min 5.760 max 6.450 mean 6.204
	CSR min 3.610 max 3.970 mean 3.744		H min 10.601 max*10.661 mean 10.626
	H min 10.738 max 10.741 mean 10.740	Row-Column-Permute	
OPF_3754.mtx			GPU 64 COO min 4.330 max 4.950 mean 4.845
Regular	CDII 64 COO min		CSR min 5.740 max 6.500 mean 6.375
	GPU 64 COO min 4.700 max* 4.930 mean 4.842 CSR min 6.230 max* 6.600 mean 6.411	TSOPF_RS_b39_c7.mtx	H min 10.041 max 10.046 mean 10.044
	H min 8.393 max 8.393 mean 8.393	Regular	
Row-Premute	mili 0.353 max 0.353 mean 0.353	gutui	GPU 64 COO min 4.300 max* 4.430 mean 4.364
	GPU 64 COO min 4.620 max 4.890 mean 4.787		CSR min 4.480 max 4.750 mean 4.716
	CSR min 5.780 max 6.310 mean 6.192		H min 7.304 max 7.304 mean 7.304
	H min 11.265 max 11.272 mean 11.269	Row-Premute	
Row-Gradient			GPU 64 COO min 4.260 max 4.400 mean 4.353
	GPU 64 COO min 4.570 max 4.870 mean 4.776		CSR min 4.490 max 4.770 mean 4.734
	CSR min 5.770 max 6.510 mean 6.302	Davida d	H min 10.536 max 10.541 mean 10.539
Column-Gradient	H min 10.464 max 10.473 mean 10.468	Row-Gradient	GPU 64 COO min 3.970 max 4.420 mean 4.338
			5. 5 5 . 600 min 5.570 max 4.420 mcan 4.550

	CCD 4 C20 4 020 4 700	D D	
	CSR min 4.620 max* 4.820 mean 4.789 H min 9.638 max 9.644 mean 9.641	Row-Premute	GPU 64 COO min 4.990 max 5.020 mean 5.004
Column-Gradient	11 1111 9.030 max 9.044 mean 9.041		CSR min 6.370 max 7.220 mean 6.771
	GPU 64 COO min 4.240 max 4.430 mean 4.368		H min 10.738 max 10.743 mean 10.740
	CSR min 4.710 max 4.770 mean 4.736	Row-Gradient	
	H min 11.129 max*11.222 mean 11.205		GPU 64 COO min 5.060 max 5.100 mean 5.082
Row-Column-Permute	GPU 64 COO min 4.260 max 4.410 mean 4.359		CSR min 6.730 max 7.720 mean 7.317 H min 10.574 max 10.585 mean 10.580
	CSR min 4.660 max 4.760 mean 4.738	Column-Gradient	n IIIII 10.5/4 IIIax 10.565 IIIeaii 10.560
	H min 10.537 max 10.541 mean 10.539		GPU 64 COO min 4.980 max 5.100 mean 5.012
			CSR min 6.580 max 7.510 mean 7.054
11 FIII			H min 10.828 max*10.842 mean 10.835
11 FIJI		Row-Column-Permute	GPU 64 COO min 4.970 max 5.000 mean 4.986
mult_dcop_03.mtx			CSR min 6.390 max 7.050 mean 6.677
Regular	GPU 64 COO min 5.140 max* 5.140 mean 5.140		H min 10.738 max 10.742 mean 10.740
	CSR min 10.340 max*10.390 mean 10.365	mult_dcop_02.mtx	
	H min 9.689 max 9.689 mean 9.689	Regular	CDU 64 COO min E 120 may E 140 man E 122
Row-Premute			GPU 64 COO min 5.120 max 5.140 mean 5.133 CSR min 6.950 max 7.590 mean 7.336
	GPU 64 COO min 4.970 max 4.990 mean 4.980		H min 9.689 max 9.689 mean 9.689
	CSR min 9.420 max 9.430 mean 9.425	Row-Premute	
Row-Gradient	H min 10.739 max 10.739 mean 10.739		GPU 64 COO min 4.970 max 4.990 mean 4.984
	GPU 64 COO min 5.080 max 5.090 mean 5.085		CSR min 6.440 max 7.110 mean 6.719
	CSR min 9.720 max 10.300 mean 10.010	Row-Gradient	H min 10.738 max 10.742 mean 10.740
	H min 10.579 max 10.582 mean 10.580	Now Gradient	GPU 64 COO min 5.070 max* 5.150 mean 5.086
Column-Gradient	GPU 64 COO min 5.030 max 5.120 mean 5.075		CSR min 6.650 max* 7.930 mean 7.304
	CSR min 9.330 max 9.770 mean 9.550		H min 10.574 max 10.587 mean 10.580
	H min 10.835 max*10.838 mean 10.836	Column-Gradient	CDU 64 COO min 4 000 may 5 040 man 5 012
Row-Column-Permute			GPU 64 COO min 4.980 max 5.040 mean 5.012 CSR min 6.520 max 7.650 mean 7.139
	GPU 64 COO min 5.000 max 5.010 mean 5.005		H min 10.829 max*10.846 mean 10.836
	CSR min 7.580 max 9.460 mean 8.520 H min 10.739 max 10.741 mean 10.740	Row-Column-Permute	
mult_dcop_03.mtx	11 IIII 10.733 IIIAX 10.741 IIIEAN 10.740		GPU 64 COO min 4.970 max 5.050 mean 4.983
Regular			CSR min 6.440 max 7.380 mean 6.779 H min 10.738 max 10.743 mean 10.740
	GPU 64 COO min 5.140 max* 5.140 mean 5.140	lp_fit2d.mtx	n IIII 10.736 IIIax 10.743 IIIean 10.740
	CSR min 10.340 max*10.390 mean 10.365	Regular	
Row-Premute	H min 9.689 max 9.689 mean 9.689		GPU 64 COO min 3.960 max 3.960 mean 3.960
Non 11 cmacc	GPU 64 COO min 4.970 max 4.990 mean 4.980		CSR min 6.360 max 7.450 mean 6.711
	CSR min 9.420 max 9.430 mean 9.425	Row-Premute	H min 11.109 max 11.109 mean 11.109
	H min 10.739 max 10.739 mean 10.739	Now 11 clided	GPU 64 COO min 3.950 max* 3.980 mean 3.953
Row-Gradient	GPU 64 COO min 5.080 max 5.090 mean 5.085		CSR min 6.330 max 7.400 mean 6.661
	CSR min 9.720 max 10.300 mean 10.010	D 0 11 1	H min 11.098 max 11.104 mean 11.101
	H min 10.579 max 10.582 mean 10.580	Row-Gradient	GPU 64 COO min 3.960 max 3.980 mean 3.961
Column-Gradient	ORU 54 000 : 5 000		CSR min 6.270 max*10.770 mean 7.017
	GPU 64 COO min 5.030 max 5.120 mean 5.075 CSR min 9.330 max 9.770 mean 9.550		H min 11.109 max 11.109 mean 11.109
	H min 10.835 max*10.838 mean 10.836	Column-Gradient	
Row-Column-Permute			GPU 64 COO min 3.940 max 3.960 mean 3.950 CSR min 6.270 max 7.370 mean 6.696
	GPU 64 COO min 5.000 max 5.010 mean 5.005		H min 11.329 max*11.334 mean 11.331
	CSR min 7.580 max 9.460 mean 8.520 H min 10.739 max 10.741 mean 10.740	Row-Column-Permute	
mult_dcop_03.mtx	H min 10.739 max 10.741 mean 10.740		GPU 64 COO min 3.950 max 3.960 mean 3.952
Regular			CSR min 6.180 max 7.420 mean 6.641
=	GPU 64 COO min 5.130 max* 5.220 mean 5.142	bloweya.mtx	H min 11.098 max 11.105 mean 11.101
	CSR min 7.250 max* 9.320 mean 7.722	Regular	
Row-Premute	H min 9.689 max 9.689 mean 9.689	-	GPU 64 COO min 0.000 max 0.000 mean 0.000
ow i remute	GPU 64 COO min 4.980 max 5.030 mean 4.999		CSR min 0.000 max 0.000 mean 0.000
	CSR min 6.460 max 8.470 mean 6.950	Row-Premute	H min 7.205 max 7.205 mean 7.205
	H min 10.738 max 10.742 mean 10.740	KOW-F1 elliute	GPU 64 COO min 4.020 max 4.030 mean 4.023
Row-Gradient	GPU 64 COO min 5.070 max 5.140 mean 5.088		CSR min 6.070 max 6.750 mean 6.340
	CSR min 6.780 max 8.700 mean 7.268		H min 11.025 max 11.031 mean 11.028
	H min 10.572 max 10.584 mean 10.580	Row-Gradient	000 54 000 1 4 000 1 4 450
Column-Gradient			GPU 64 COO min 4.090 max* 4.160 mean 4.111 CSR min 5.980 max* 7.370 mean 6.678
	GPU 64 COO min 4.980 max 5.030 mean 5.010		H min 10.295 max 10.304 mean 10.300
	CSR min 6.390 max 7.640 mean 6.982 H min 10.825 max*10.845 mean 10.836	Column-Gradient	
Row-Column-Permute	IIIII 10.023 IIIdX*10.043 IIIedII 10.836		GPU 64 COO min 3.980 max 4.010 mean 3.995
	GPU 64 COO min 4.990 max 5.010 mean 4.997		CSR min 5.880 max 6.780 mean 6.295
	CSR min 6.300 max 7.160 mean 6.636	Row-Column-Permute	H min 10.881 max*10.887 mean 10.883
mult dans 01t	H min 10.738 max 10.743 mean 10.740	SSZG I CI IIIGCE	GPU 64 COO min 4.020 max 4.030 mean 4.023
mult_dcop_01.mtx Regular			CSR min 5.970 max 6.420 mean 6.183
negutai	GPU 64 COO min 5.120 max* 5.140 mean 5.134	1 07	H min 11.025 max 11.033 mean 11.028
	CSR min 6.990 max* 9.230 mean 7.546	lp_osa_07.mtx	
	H min 9.689 max 9.689 mean 9.689	Regular	

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	GPU 64 COO min 4.260 max* 4.270 mean 4.261	H min 10.377 max 10.381 mean 10.379
	CSR min 6.440 max 7.640 mean 6.863	cvxqp3.mtx
	H min 8.412 max 8.412 mean 8.412	Regular
Row-Premute		GPU 64 COO min 3.500 max* 3.540 mean 3.501
	GPU 64 COO min 4.200 max 4.200 mean 4.200	CSR min 11.860 max*13.100 mean 12.694
	CSR min 6.020 max 7.030 mean 6.418	H min 8.646 max 8.646 mean 8.646
	H min 9.255 max 9.257 mean 9.256	Row-Premute
Row-Gradient	GPU 64 COO min 4.210 max 4.240 mean 4.226	GPU 64 COO min 3.360 max 3.370 mean 3.365
	CSR min 6.070 max *10.050 mean 6.498	CSR min 6.210 max 7.610 mean 6.631 H min 11.027 max 11.032 mean 11.030
	H min 8.607 max 8.678 mean 8.671	H min 11.027 max 11.032 mean 11.030 Row-Gradient
Column-Gradient	II IIIII 0.007 IIIAX 0.070 IIIEAII 0.071	GPU 64 COO min 3.370 max 3.380 mean 3.376
COTUMNI OF AUTERIC	GPU 64 COO min 4.170 max 4.190 mean 4.180	CSR min 6.170 max 7.070 mean 6.499
	CSR min 5.610 max 7.300 mean 5.988	H min 11.059 max 11.068 mean 11.064
	H min 9.534 max* 9.601 mean 9.585	Column-Gradient
Row-Column-Permute	ii	GPU 64 COO min 3.350 max 3.390 mean 3.371
	GPU 64 COO min 4.190 max 4.190 mean 4.190	CSR min 6.150 max 7.180 mean 6.531
	CSR min 6.070 max 7.000 mean 6.386	H min 11.125 max*11.133 mean 11.130
	H min 9.255 max 9.257 mean 9.256	Row-Column-Permute
ex19.mtx		GPU 64 COO min 3.350 max 3.380 mean 3.364
Regular		CSR min 6.040 max 7.440 mean 6.603
	GPU 64 COO min 6.140 max* 6.180 mean 6.159	H min 11.028 max 11.033 mean 11.030
	CSR min 12.780 max*14.400 mean 13.328	case9.mtx
	H min 8.228 max 8.228 mean 8.228	Regular
Row-Premute		GPU 64 COO min 0.000 max 0.000 mean 0.000
	GPU 64 COO min 5.820 max 5.850 mean 5.833	CSR min 0.000 max 0.000 mean 0.000
	CSR min 9.870 max 11.070 mean 10.372	H min 7.380 max 7.380 mean 7.380
	H min 11.836 max 11.840 mean 11.838	Row-Premute
Row-Gradient		GPU 64 COO min 4.130 max 4.170 mean 4.134
	GPU 64 COO min 6.070 max 6.120 mean 6.104	CSR min 6.180 max* 9.200 mean 6.796
	CSR min 11.290 max 12.760 mean 12.088	H min 10.041 max 10.046 mean 10.044
	H min 10.743 max 10.752 mean 10.748	Row-Gradient
Column-Gradient		GPU 64 COO min 4.150 max* 4.220 mean 4.163
	GPU 64 COO min 5.760 max 5.840 mean 5.813	CSR min 6.410 max 7.500 mean 6.816
	CSR min 9.710 max 14.220 mean 10.376	H min 9.682 max 9.706 mean 9.693
	H min 11.873 max*11.882 mean 11.878	Column-Gradient
Row-Column-Permute		GPU 64 COO min 4.080 max 4.110 mean 4.096
	GPU 64 COO min 5.810 max 5.860 mean 5.838	CSR min 6.020 max 7.220 mean 6.309
	CSR min 9.920 max 10.820 mean 10.240	H min 10.597 max*10.658 mean 10.631
	H min 11.836 max 11.841 mean 11.838	Row-Column-Permute
brainpc2.mtx		GPU 64 COO min 4.120 max 4.140 mean 4.130
Regular		CSR min 6.210 max 7.200 mean 6.609
Regulai	GPU 64 COO min 0.000 max 0.000 mean 0.000	H min 10.041 max 10.046 mean 10.044
Regutal	CSR min 0.000 max 0.000 mean 0.000	$${\rm H}$$ $${\rm min}$ 10.041 max 10.046 mean 10.044 TSOPF_FS_b9_c6.mtx
		$$\rm H$$ $$\rm min~10.041~max~10.046~mean~10.044$ TSOPF_FS_b9_c6.mtx Regular
Row-Premute	CSR min 0.000 max 0.000 mean 0.000 H min 7.478 max 7.478 mean 7.478	TSOPF_FS_b9_c6.mtx Regular GPU 64 COO min 0.000 max 0.000 mean 0.000
	CSR min 0.000 max 0.000 mean 0.000 min 7.478 max 7.478 mean 7.478 mean 4.773	TSOPF_FS_b9_c6.mtx Regular GPU 64 COO min 0.000 max 0.000 mean 0.000 CSR min 0.000 max 0.000 mean 0.000
	CSR min	TSOPF_FS_b9_c6.mtx Regular GVSR min
Row-Premute	CSR min 0.000 max 0.000 mean 0.000 min 7.478 max 7.478 mean 7.478 mean 4.773	H min 10.041 max 10.046 mean 10.044 Regular GPU 64 COO min 0.000 max 0.000 mean 0.000 CSR min 0.000 max 0.000 mean 0.000 H min 7.380 max 7.380 mean 7.380
	CSR min 0.000 max 0.000 mean 0.000 mean 7.478 max 7.478 mean 7.478 mean 7.478 mean 6.930 max 7.780 mean 4.773 CSR min 6.930 max 7.780 mean 7.310 mean 9.811 mean 9.811 mean 9.811	H min 10.041 max 10.046 mean 10.044 TSOPF_FS_b9_c6.mtx Regular GPU 64 COO min 0.000 max 0.000 mean 0.000 CSR min 0.000 max 0.000 mean 0.000 max 0.000
Row-Premute	CSR min	H min 10.041 max 10.046 mean 10.044
Row-Premute	CSR min	H min 10.041 max 10.046 mean 10.044 Regular GPU 64 COO min 0.000 max 0.000 mean 0.000 max 0.000 mean 0.000 max 0.000 mean 0.00
Row-Premute Row-Gradient	CSR min	H min 10.041 max 10.046 mean 10.044 TSOPF_FS_b9_c6.mtx Regular GPU 64 COO min 0.000 max 0.000 mean 0.000 mean 0.000 max 0.000 mean 0.000 max 0.000 mean 0.000 mean
Row-Premute	CSR min 0.000 max 0.000 mean 0.000 mean 7.478 max 7.478 mean 7.478 mean 7.478 mean 7.478 mean 6.930 max 7.780 mean 7.310 min 9.810 max 9.813 mean 9.811 mean 6.820 max 4.840 mean 4.831 min 7.220 max 8.290 mean 7.583 min 9.721 max 9.725 mean 9.723	M
Row-Premute Row-Gradient	CSR min	H min 10.041 max 10.046 mean 10.044 Regular GPU 64 COO min 0.000 max 0.000 mean 0.000 max 0.000 mean 0.0
Row-Premute Row-Gradient	CSR min	M
Row-Premute Row-Gradient	CSR min	H min 10.041 max 10.046 mean 10.044 Regular GPU 64 COO min 0.000 max 0.000 mean 0.000 max 0.000 mean 0.000 max 0.000 mean 0.00
Row-Premute Row-Gradient Column-Gradient	CSR min	H min 10.041 max 10.046 mean 10.044 Regular
Row-Premute Row-Gradient Column-Gradient	CSR min	H min 10.041 max 10.046 mean 10.044 TSOPF_FS_b9_c6.mtx Regular GPU 64 COO min 0.000 max 0.000 mean 0.000 mean 0.000 mean 0.000 max 0.000 mean 0.000
Row-Premute Row-Gradient Column-Gradient	CSR min	H min 10.041 max 10.046 mean 10.044 Regular
Row-Premute Row-Gradient Column-Gradient	CSR min	H min 10.041 max 10.046 mean 10.044 TSOPF_FS_b9_c6.mtx Regular GPU 64 COO min 0.000 max 0.000 mean 0.000 max 0.000 max 0.000 mean 0.000 max 0.000
Row-Gradient Column-Gradient Row-Column-Permute	CSR min	Regular GPU 64 COO min 4.120 max 10.045 mean 10.045 10.046 mean 10.046
Row-Premute Row-Gradient Column-Gradient Row-Column-Permute	CSR min	H
Row-Premute Row-Gradient Column-Gradient Row-Column-Permute	CSR min	Regular
Row-Premute Row-Gradient Column-Gradient Row-Column-Permute shermanACb.mtx Regular	CSR min	TSOPF_FS_b9_c6.mtx Regular GPU 64 COO min 4.120 max 4.140 mean 4.120 max 6.200 mean 6.640 mea
Row-Premute Row-Gradient Column-Gradient Row-Column-Permute	CSR min	Regular
Row-Premute Row-Gradient Column-Gradient Row-Column-Permute shermanACb.mtx Regular	CSR min	Row-Premute
Row-Premute Row-Gradient Column-Gradient Row-Column-Permute shermanACb.mtx Regular	CSR min	Regular
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Row-Premute Row-Gradient Column-Gradient Row-Column-Permute shermanACb.mtx Regular	CSR min	Regular
Row-Premute Row-Gradient Column-Gradient Row-Column-Permute shermanACb.mtx Regular Row-Premute	CSR min	Row-Premute GPU 64 COO min 0.000 max 0.000 man 0.000 max 0.000 max
Row-Premute Row-Gradient Column-Gradient Row-Column-Permute shermanACb.mtx Regular Row-Premute	CSR min	Regular GPU 64 COO min 0.000 max 0.000 mean 0.0
Row-Premute Row-Gradient Column-Gradient Row-Column-Permute shermanACb.mtx Regular Row-Premute Row-Gradient	CSR min	Regular
Row-Premute Row-Gradient Column-Gradient Row-Column-Permute shermanACb.mtx Regular Row-Premute	CSR min	Row-Premute GPU 64 COO min 0.000 max 0.000 man 0.000 max 0.000 max
Row-Premute Row-Gradient Column-Gradient Row-Column-Permute shermanACb.mtx Regular Row-Premute Row-Gradient	CSR min	Regular GPU 64 COO min 0.000 max 0.000 mean 0.0
Row-Premute Row-Gradient Column-Gradient Row-Column-Permute shermanACb.mtx Regular Row-Premute Row-Gradient	CSR min	Regular GPU 64 COO min 0.000 max 0.000 mean 0.0
Row-Premute Row-Gradient Column-Gradient Row-Column-Permute shermanACb.mtx Regular Row-Premute Row-Gradient Column-Gradient	CSR min	H
Row-Premute Row-Gradient Column-Gradient Row-Column-Permute shermanACb.mtx Regular Row-Premute Row-Gradient	CSR min	H
Row-Premute Row-Gradient Column-Gradient Row-Column-Permute shermanACb.mtx Regular Row-Premute Row-Gradient Column-Gradient	CSR min	H

Row-Column-Permute			GPU 64 COO min 3.240 max 3.260 mean 3.249
	GPU 64 COO min 6.640 max 6.710 mean 6.679		CSR min 5.090 max* 8.660 mean 5.546
	CSR min 9.690 max 10.740 mean 10.050		H min 10.853 max*10.873 mean 10.864
	H min 11.874 max 11.877 mean 11.875	Row-Column-Permute	
OPF_3754.mtx			GPU 64 COO min 3.290 max 3.320 mean 3.296
Regular	GPU 64 COO min 4.430 max* 4.450 mean 4.443		CSR min 5.190 max 7.550 mean 5.659 H min 10.249 max 10.255 mean 10.252
		Maragal 6 mtv	H min 10.249 max 10.255 mean 10.252
	H min 8.393 max 8.393 mean 8.393	Maragal_6.mtx Regular	
Row-Premute	11 IIII 0.333 IIIAX 0.333 IIICAN 0.333	ператаг	GPU 64 COO min 10.580 max 10.620 mean 10.599
NOW I Tellidee	GPU 64 COO min 4.230 max 4.250 mean 4.240		CSR min 15.620 max*16.470 mean 15.832
	CSR min 7.430 max 8.750 mean 7.986		H min 9.930 max 9.930 mean 9.930
	H min 11.266 max 11.272 mean 11.269	Row-Premute	
Row-Gradient			GPU 64 COO min 10.340 max 10.430 mean 10.362
	GPU 64 COO min 4.370 max 4.420 mean 4.382		CSR min 12.880 max 13.340 mean 13.057
	CSR min 8.160 max 9.470 mean 8.682		H min 10.777 max 10.778 mean 10.777
	H min 10.462 max 10.473 mean 10.468	Row-Gradient	
Column-Gradient			GPU 64 COO min 10.650 max*10.740 mean 10.688
	GPU 64 COO min 4.210 max 4.240 mean 4.227		CSR min 12.310 max 13.670 mean 12.562
	CSR min 7.160 max 8.080 mean 7.595		H min 11.247 max 11.300 mean 11.281
	H min 11.394 max*11.401 mean 11.398	Column-Gradient	ODU 64 000 : 40 040
Row-Column-Permute	CDU 64 600 min 4 220 mm 4 250 mm 4 242		GPU 64 COO min 10.340 max 10.440 mean 10.398
	GPU 64 COO min 4.230 max 4.250 mean 4.243 CSR min 7.230 max 8.940 mean 8.056		CSR min 9.480 max 10.110 mean 9.782 H min 12.023 max*12.069 mean 12.047
	H min 11.264 max 11.271 mean 11.269	Row-Column-Permute	n IIIII 12.023 IIIaX*12.009 IIIeaN 12.04/
c-47.mtx	n IIIII 11.204 IIIdX 11.271 IIIedii 11.203	KOW-COTUMIN-Fermine	GPU 64 COO min 10.330 max 10.380 mean 10.356
Regular			CSR min 12.840 max 13.530 mean 13.119
Negutai	GPU 64 COO min 5.320 max* 5.340 mean 5.329		H min 10.776 max 10.778 mean 10.777
	CSR min 8.890 max* 9.590 mean 9.249	aft01.mtx	11 III211 10.776 IIIdx 10.776 IIIcdi1 10.777
	H min 8.364 max 8.364 mean 8.364	Regular	
Row-Premute			GPU 64 COO min 3.680 max* 3.690 mean 3.688
	GPU 64 COO min 5.240 max 5.250 mean 5.241		CSR min 13.860 max*14.830 mean 14.560
	CSR min 7.790 max 8.890 mean 8.214		H min 7.811 max 7.811 mean 7.811
	H min 10.059 max 10.063 mean 10.061	Row-Premute	
Row-Gradient			GPU 64 COO min 3.510 max 3.530 mean 3.513
	GPU 64 COO min 5.230 max 5.260 mean 5.242		CSR min 6.420 max 10.520 mean 7.265
	CSR min 7.080 max 8.050 mean 7.673		H min 11.161 max*11.170 mean 11.165
	H min 10.206 max 10.226 mean 10.218	Row-Gradient	
Column-Gradient			GPU 64 COO min 3.630 max 3.670 mean 3.643
	GPU 64 COO min 5.080 max 5.120 mean 5.105		CSR min 10.760 max 13.510 mean 12.199
	CSR min 5.780 max 6.970 mean 6.359	Caluma Caadiant	H min 10.248 max 10.265 mean 10.258
Row-Column-Permute	H min 11.205 max*11.233 mean 11.222	Column-Gradient	GPU 64 COO min 3.510 max 3.520 mean 3.519
Kow-corullin-refillate	GPU 64 COO min 5.220 max 5.250 mean 5.227		CSR min 6.490 max 11.230 mean 7.645
	CSR min 7.860 max 8.710 mean 8.247		H min 11.112 max 11.121 mean 11.117
	H min 10.059 max 10.064 mean 10.061	Row-Column-Permute	II IIIII II.IIZ IIIAX II.IZI IIIEAII III.II7
mhd4800a.mtx	III TOTOGO IIIAK TOTOGO IIICAN TOTOGO	Non Column Fermace	GPU 64 COO min 3.510 max 3.540 mean 3.515
Regular			CSR min 6.510 max 11.650 mean 7.311
•	GPU 64 COO min 3.090 max* 3.100 mean 3.098		H min 11.161 max 11.168 mean 11.165
	CSR min 11.570 max*12.290 mean 12.092	TSOPF_RS_b39_c7.mtx	
	H min 7.132 max 7.132 mean 7.132	Regular	
Row-Premute			GPU 64 COO min 5.970 max* 6.010 mean 5.988
	GPU 64 COO min 3.020 max 3.020 mean 3.020		CSR min 12.470 max*21.120 mean 13.816
	CSR min 5.560 max 7.270 mean 6.007		H min 7.304 max 7.304 mean 7.304
	H min 10.959 max*10.968 mean 10.963	Row-Premute	
Row-Gradient	ODU 64 000 1 0		GPU 64 COO min 5.840 max 5.870 mean 5.856
	GPU 64 COO min 3.080 max 3.100 mean 3.088		CSR min 10.780 max 15.810 mean 11.425
	CSR min 10.250 max 12.150 mean 11.340	Daw Coodi	H min 10.537 max 10.540 mean 10.539
Column-Gradient	H min 9.509 max 9.528 mean 9.520	Row-Gradient	CDII 64 COO min E 050 5 000 5 075
Column-Gradient	CDU 64 COO min 2 020 may 2 050 man 2 026		GPU 64 COO min 5.950 max 6.000 mean 5.975
	GPU 64 COO min 3.020 max 3.050 mean 3.026 CSR min 5.530 max 10.580 mean 6.432		CSR min 11.520 max 17.250 mean 12.799 H min 9.638 max 9.646 mean 9.641
	H min 10.933 max 10.946 mean 10.939	Column-Gradient	n min 9.036 max 9.046 mean 9.041
Row-Column-Permute	11 III11 10.333 IIIAX 10.340 IIIEAN 10.333	COTUMNI GLAGIETIC	GPU 64 COO min 5.790 max 5.860 mean 5.827
Row-Column-Permute	GPU 64 COO min 3.020 max 3.020 mean 3.020		CSR min 10.500 max 14.080 mean 11.237
	CSR min 5.510 max 6.830 mean 6.136		H min 11.128 max*11.223 mean 11.209
	H min 10.959 max 10.967 mean 10.963	Row-Column-Permute	
gen4.mtx			GPU 64 COO min 5.850 max 5.870 mean 5.855
Regular			CSR min 10.790 max 15.250 mean 11.718
-	GPU 64 COO min 3.300 max* 3.320 mean 3.308		H min 10.537 max 10.541 mean 10.539
		mult_dcop_03.mtx	
	H min 9.234 max 9.234 mean 9.234	Regular	
Row-Premute			GPU 64 COO min 5.130 max* 5.220 mean 5.142
	GPU 64 COO min 3.290 max 3.310 mean 3.299		CSR min 7.250 max* 9.320 mean 7.722
	CSR min 5.190 max 7.420 mean 5.683		H min 9.689 max 9.689 mean 9.689
D 0 11 1	H min 10.249 max 10.254 mean 10.252	Row-Premute	ORU 54 000 1 4 000
Row-Gradient	CDU 64 600 2 200 2 212		GPU 64 COO min 4.980 max 5.030 mean 4.999
	GPU 64 COO min 3.300 max 3.310 mean 3.301		CSR min 6.460 max 8.470 mean 6.950
	CSR min 5.370 max 6.310 mean 5.659	Daw Coodi	H min 10.738 max 10.742 mean 10.740
Column-Gradient	H min 9.934 max 9.958 mean 9.948	Row-Gradient	GPU 64 COO min 5.070 max 5.140 mean 5.088
COTUMNI OF BUTCHE			5.00. COO MITH 5.070 MAX 5.140 Mean 5.000

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CSR min 6.780 max 8.700 mean 7.268 min 10.572 max 10.584 mean 10.580 Column-Gradient

GPU 64 COO min 4.980 max 7.640 mean 6.982 min 10.825 max*10.845 mean 10.836 min 10.738 max 10.743 mean 10.740 mean 6.636 min 10.738 max 10.743 mean 10.740 mean 10.740
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