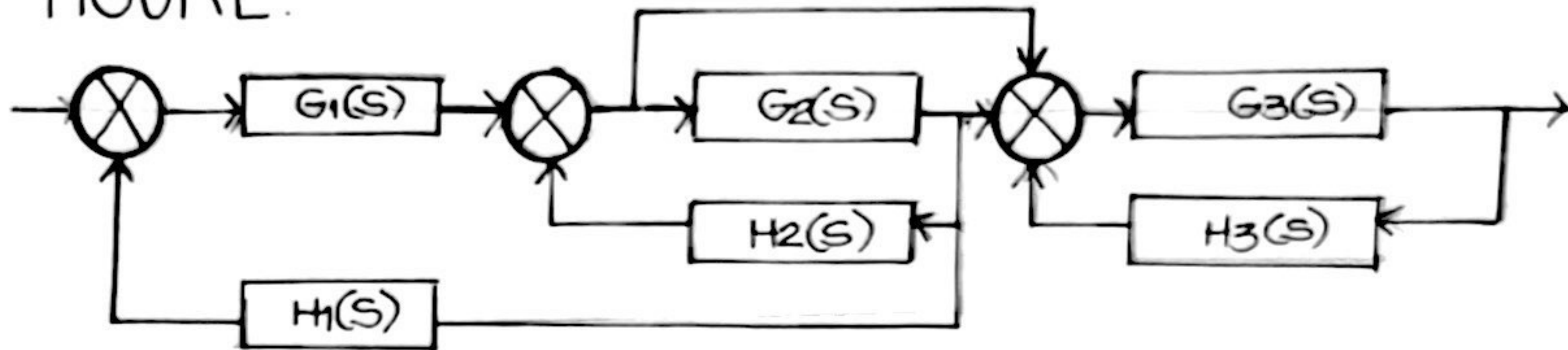


BLOCK DIAGRAM ALGEBRA, LABORATORY 3
ECE 425 | ME 4203

BLOCK DIAGRAM 1

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FIGURE:



GIVEN:

$$G_1(s) = 1/s^2$$

$$G_2(s) = 1/s + 1$$

$$G_3(s) = 1/s$$

$$H_1(s) = 1/s$$

$$H_2(s) = 1/(s-1)$$

$$H_3(s) = s^{-1}$$

SOLVING =

$$\begin{aligned} &= \frac{G_2}{1 + G_2 H_2} \\ &= \frac{[1/(s+1)]}{1 + [(1/s+1)(1/s-1)]} \\ &= \frac{[1/(s+1)]}{1 + [1/(s^2-1)]} \\ &= \frac{[1/(s+1)]}{[s^2-1+1]/[s^2-1]} \\ &= \frac{[1/(s+1)]}{s^2/[s^2-1]} \\ &= \frac{1}{s+1} \cdot \frac{s^2-1}{s^2} \\ &= \frac{s^2-1}{s^3+s^2} \end{aligned}$$

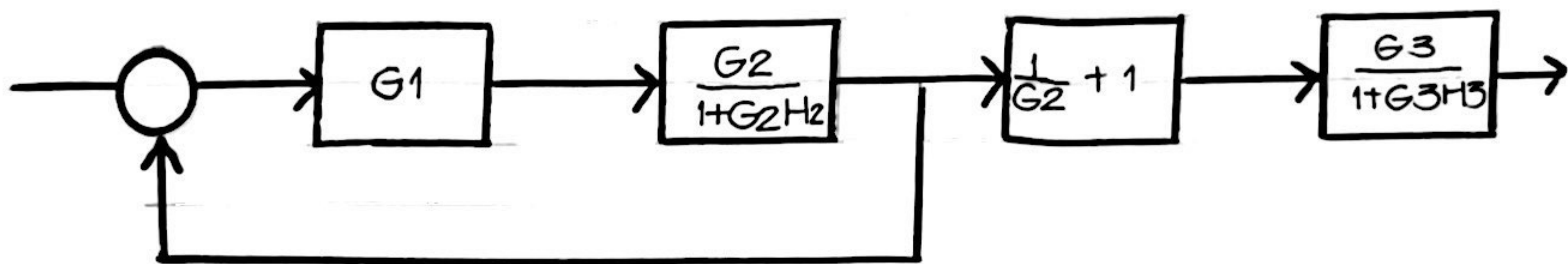
$$\begin{aligned} &= \frac{1}{G_2} + 1 \\ &= 1/[1/s+1] + 1 \\ &= 1 \cdot \frac{s+1}{1} + 1 \\ &= s+2 \end{aligned}$$

LABORATORY 3, BLOCK DIAGRAM NO. 1

FOR G_3 , PARALLEL

$$\begin{aligned}
 &= \frac{G_3}{1+G_3H_3} = \frac{[1/s]}{1+[(1/s)(1/s-2)]} \\
 &= \frac{[1/s]}{1+[1/(s^2-2s)]} \\
 &= \frac{[1/s]}{(s^2-2s+1)/(s^2-2s)} \\
 &= \frac{1}{s} \cdot \frac{s^2-2s}{s^2-2s+1} \\
 &= \frac{s^2-2s}{s^3-2s^2+s}
 \end{aligned}$$

REDUCED DIAGRAM SO FAR



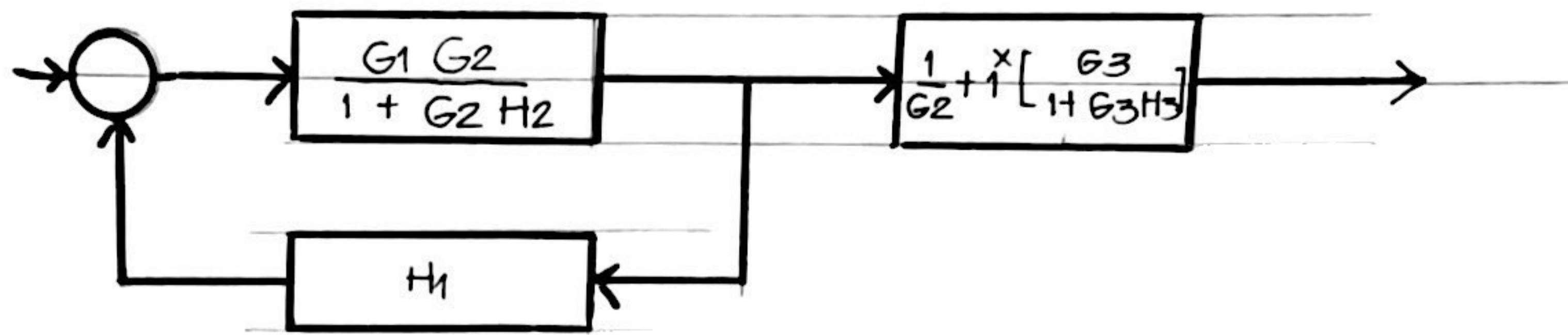
FOR $\cdot [(1/G_2) + 1] \cdot [G_3/(1+G_3H_3)]$

$$\begin{aligned}
 &= \frac{s^2-2s}{s^3-2s^2+s} \times (s+2) \\
 &= \frac{s^3-2s^2+2s^2-4s}{s^3-2s^2+s} \\
 &= \frac{s^3-4s}{s^3-2s^2+s}
 \end{aligned}$$

FOR $G_1 \times [G_2/(1+G_2H_2)]$

$$\begin{aligned}
 &= \frac{1}{s^2} \times \frac{s^2-1}{s^3+s^2} \\
 &= \frac{s^2-1}{s^5+s^4}
 \end{aligned}$$

LABORATORY 3, BLOCK DIAGRAM NO.1

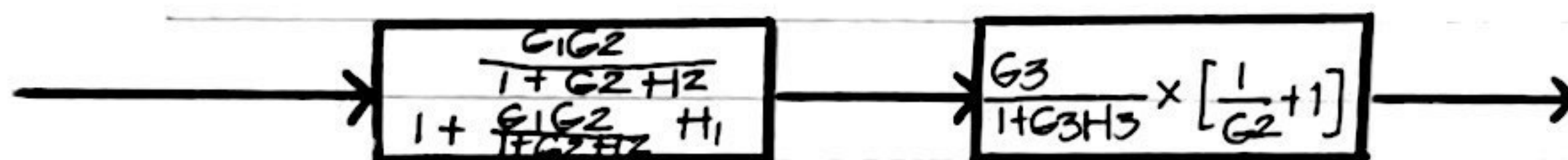


$$\left[\frac{G_1 G_2}{1 + G_2 H_2} \right] / \left[1 + \frac{G_1 G_2}{1 + G_2 H_2} \times H_1 \right] = \frac{s^2 - 1 / s^3 + s^4}{1 + [s^2 - 1 / s^3 + s^4] (1/s)}$$

FINAL ANSWER

$$= \frac{s^8 + s^7 - s^6 - s^5}{s^{11} + s^{10} + s^9 + s^7 + s^6 - s^5 - s^4}$$

$$\begin{aligned} &= \frac{s^2 - 1 / s^3 + s^4}{1 + (s^2 - 1 / s^3 + s^4)} \\ &= \frac{s^2 - 1 / s^3 + s^4}{s^6 + s^3 + s^2 - 1 / s^4 + s^5} \\ &= \frac{s^2 - 1}{s^3 + s^4} \times \frac{s^6 + s^5}{s^6 + s^3 + s^2 - 1} \\ &= \frac{s^8 + s^7 - s^6 - s^5}{s^{11} + s^{10} + s^7 - s^5 + s^{10} + s^9 + s^6 - s^4} \end{aligned}$$



$$\begin{aligned} &= \frac{s^8 + s^7 - s^6 - s^5}{s^{11} + s^{10} + s^9 + s^7 + s^6 - s^5 - s^4} \times \frac{s^3 - 4s}{s^3 - 2s^2 + s} \\ &= \frac{s^{11} + s^{10} - 5s^9 - 5s^8 + 4s^7 + 4s^6}{s^{14} - 2s^{12} + 2s^{10} - s^9 - 2s^8 + 2s^7 + s^6 - s^5} \end{aligned}$$

$$R(s) \rightarrow \frac{s^{11} + s^{10} - 5s^9 - 5s^8 + 4s^7 + 4s^6}{s^{14} - 2s^{12} + 2s^{10} - s^9 - 2s^8 + 2s^7 + s^6 - s^5} \rightarrow c(s)$$