

GROUP 4
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MANUAL CALCULATION (BLOCK DIAGRAM NO. 2)

$$2. G_1(s) = \frac{1}{s^2}$$

$$G_2(s) = 1/(s+1)$$

$$G_3(s) = 1/s$$

$$G_4(s) = 1/2s$$

$$H_1(s) = 1/s$$

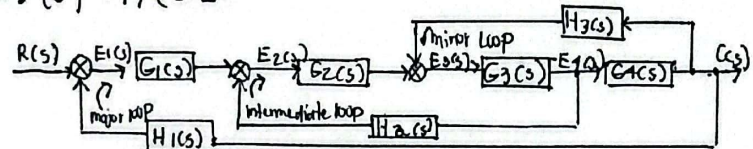
$$H_2(s) = 1/(s-1)$$

$$H_3(s) = 1/(s-2)$$

$$s^2 - 4s + 1$$

PARALLEL

$$\begin{aligned} \frac{G_3}{1 + G_3 G_4 H_3} &= \frac{\frac{1}{s}}{1 + \left(\frac{1}{s}\right)\left(\frac{1}{2s}\right)\left(\frac{1}{s-2}\right)} \\ &= \frac{\frac{1}{s}}{1 + \frac{1}{2s^2} \left(\frac{1}{s-2}\right)} \\ &= \frac{\frac{1}{s}}{1 + \frac{1}{2s^3 - 4s^2}} \\ &= \frac{1}{s} \cdot \frac{2s^3 - 4s^2}{2s^3 - 4s^2 + 1} \\ &= \frac{2s^3 - 4s^2}{2s^4 - 4s^3 + s} \end{aligned}$$



SERIES: $G_2 G_3 H_3 G_2$

$$G_2 = \frac{1}{s+1}$$

$$\begin{aligned} G_2 G_3 H_3 H_4 &= \left[\frac{2s^3 - 4s^2}{2s^4 - 4s^3 + s} \right] \left(\frac{1}{s+1} \right) = \frac{2s^3 - 4s^2}{2s^5 - 4s^4 + s^2 + 2s^4 - 4s^3 + s} \\ &= \frac{2s^3 - 4s^2}{2s^5 - 2s^4 - 4s^3 + s^2 + s} \\ &= \frac{2s^3 - 4s^2}{2s^5 - 2s^4 - 4s^3 + s^2 + s} \\ &= \frac{2s^3 - 4s^2}{2s^5 - 4s^4 - 2s^3 + 7s^2 - 2s^2 - s + (2s^3 - 4s^2)} \\ &= \frac{2s^3 - 4s^2}{2s^5 - 4s^4 - 2s^3 + 2s^2 - s} \end{aligned}$$

PARALLEL $G_2 G_3 H_3 G_2 H_2$

$$\frac{G_2 G_3 H_3 G_2}{1 + G_2 G_3 H_3 G_2 H_2} = \frac{\frac{2s^3 - 4s^2}{2s^5 - 2s^4 - 4s^3 + s^2 + s}}{1 + \frac{2s^3 - 4s^2}{2s^5 - 2s^4 - 4s^3 + s^2 + s} \left(\frac{1}{s-1} \right)}$$

BLOCK DIAGRAM NO. 2

$$\frac{G2G3H3G2}{1+G2G3H3G2H2} = 1 + \frac{\frac{2s^3-4s^2}{2s^5-2s^4-4s^3+s^2+s}}{\frac{2s^3-4s^2}{2s^6-2s^5-2s^5+2s^4-4s^4+4s^3+s^3}}$$

$$= \frac{\frac{2s^3-4s^2}{2s^5-2s^4-4s^3+s^2+s}}{1 + \frac{2s^3-4s^2}{2s^6-4s^5-2s^4+5s^3-s}}$$

$$= \frac{2s^3-4s^2}{2s^5-2s^4-4s^3+s^2+s} \cdot \frac{2s^6-4s^5-2s^4+5s^3-s}{2s^6-4s^5-2s^4+5s^3-s+2s^3-4s^2}$$

$$= \frac{2s^3-4s^2}{2s^5-2s^4-4s^3+s^2+s} \cdot \frac{2s^6-4s^5-2s^4+5s^3-s}{2s^6-4s^5-2s^4+7s^3-4s^2-s}$$

$$= \frac{4s^9-16s^8+12s^7+18s^6-20s^5-2s^4+4s^3}{4s^{11}-12s^{10}-4s^9+36s^8-16s^7-20s^6+23s^5+7s^4-5s^3-s^2}$$

FOR G1

$$= \frac{4s^9-16s^8+12s^7+18s^6-20s^5-2s^4+4s^3}{4s^{11}-12s^{10}-4s^9+36s^8-16s^7-20s^6+23s^5+7s^4-5s^3-s^2} \left(\frac{1}{s^2} \right)$$

$$= \frac{4s^9-16s^8+12s^7+18s^6-20s^5-2s^4+4s^3}{4s^{13}-12s^{12}-4s^{11}+36s^{10}-16s^9-20s^8+23s^7+7s^6-5s^5-s^4}$$

FOR G4

$$= \frac{4s^9-16s^8+12s^7+18s^6-20s^5-2s^4+4s^3}{8s^{14}-24s^{13}-8s^{12}+72s^{11}-32s^{10}-56s^9+46s^8+14s^7-10s^6-2s^5}$$

FOR G2G3H3G2H2G1G4H1

$$= \frac{G2G3H3G2H2G1G4H1}{1+G2G3H3G2H2G1G4H1}$$

$$= \frac{4s^9-16s^8+12s^7+18s^6-20s^5-2s^4+4s^3}{8s^{14}-24s^{13}-8s^{12}+72s^{11}-32s^{10}-56s^9+46s^8+14s^7-10s^6-2s^5}$$

$$1 + \frac{4s^9-16s^8+12s^7+18s^6-20s^5-2s^4+4s^3}{8s^{14}-24s^{13}-8s^{12}+72s^{11}-32s^{10}-56s^9+46s^8+14s^7-10s^6-2s^5} \left(\frac{1}{s} \right)$$

BLOCK DIAGRAM NO.2

$$= \frac{4s^9 - 10s^8 + 12s^7 + 10s^6 - 20s^5 - 2s^4 + 4s^3}{8s^{14} - 24s^{13} - 8s^{12} + 72s^{11} - 36s^{10} - 56s^9 + 46s^8 + 14s^7 + 14s^6 - 10s^5 - 2s^4} \cdot \left[\frac{(8s^{14} - 24s^{13} - 8s^{12} + 72s^{11} - 32s^{10} - 56s^9 + 46s^8 + 14s^7 - 10s^{11} \cdot 2s^5)(s)}{(8s^{15} - 24s^{14} - 8s^{13} + 72s^{12} - 32s^{11} - 56s^{10} + 46s^9 + 14s^8 - 10s^7 - 2s^6 + 4s^5} - 16s^9 + 12s^7 + 10s^6 - 20s^5 - 2s^4 + 4s^3} \right]$$

SIMPLIFYING THIS

$$= \frac{4s^{10} - 16s^8 + 12s^7 + 10s^6 - 2s^5 + 4s^4}{8s^{15} - 24s^{14} - 8s^{13} + 72s^{12} - 32s^{11} - 56s^{10} + 4s^9 + 14s^8 - 10s^7 - 2s^6 + 4s^5 - 16s^9 + 12s^7 + 10s^6 - 20s^5 - 2s^4 + 4s^3}$$

$$= \frac{\frac{2s^4(s+1)}{2s^7 - 6s^6 + 4s^5 + 3s^4 - 7s^3 + 6s^2 - 5s + 2}}{2s^5(s-1)(s-2)}$$

$$= \frac{2s^5(s-1)(s-2)}{2s^4(s+1)(2s^7 - 6s^6 + 4s^5 + 3s^4 - 7s^3 + 6s^2 - 5s + 2)}$$

$$= \frac{s(s-1)(s-2)}{(s+1)(2s^7 - 6s^6 + 4s^5 + 3s^4 - 7s^3 + 6s^2 - 5s + 2)}$$

$$= \frac{s^2 - 3s + 2}{2s^8 - 4s^7 - 2s^6 + 7s^5 - 4s^4 - s^3 + s^2 - 3s + 2}$$

