

Trees, Recursion, and Natural Language

John DeNero

Source code: <http://denero.org/content/misc/parse.zip>

Ambiguity

Syntactic Ambiguity in English

Syntactic Ambiguity in English

Programs must be written for people to read¹

¹Preface of Structure and Interpretation of Computer Programs
by Harold Abelson and Gerald Sussman with Julie Sussman

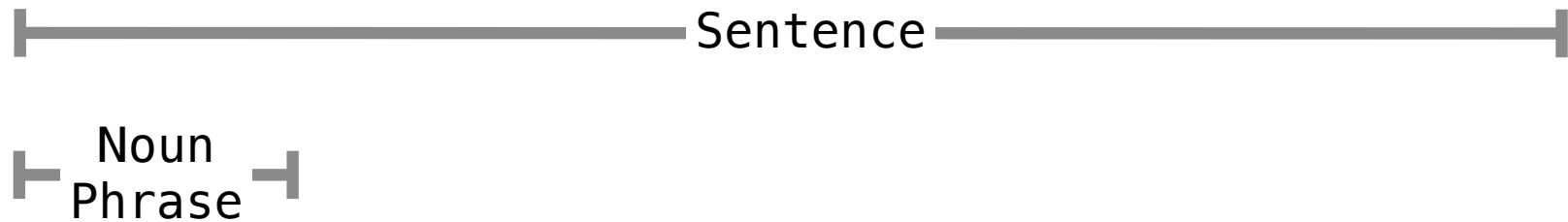
Syntactic Ambiguity in English

|-----Sentence-----|

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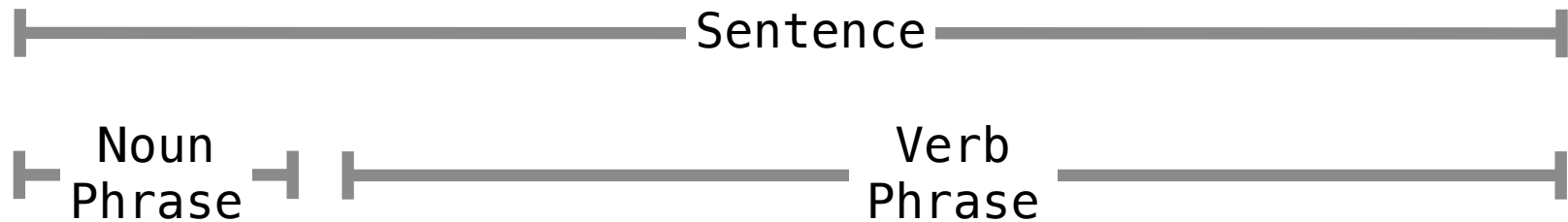
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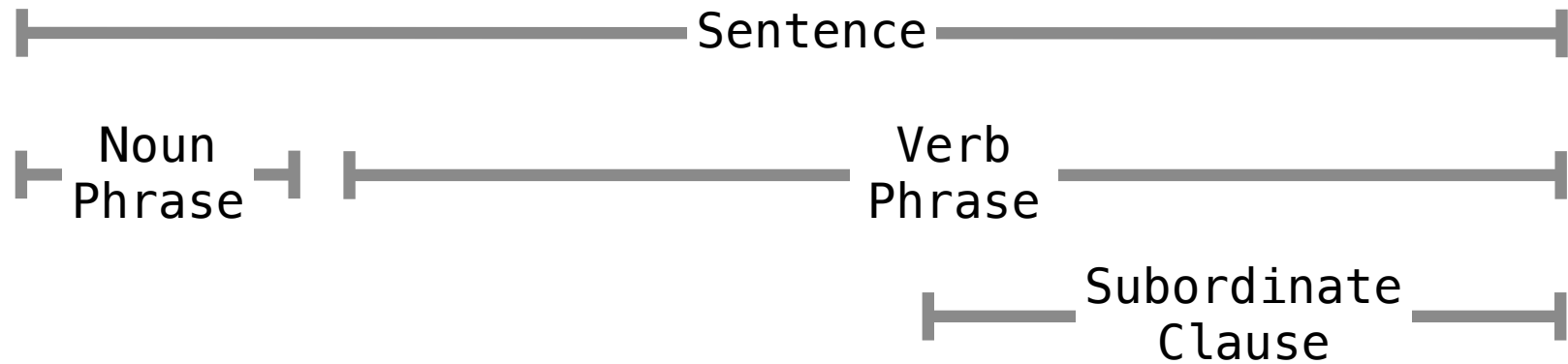
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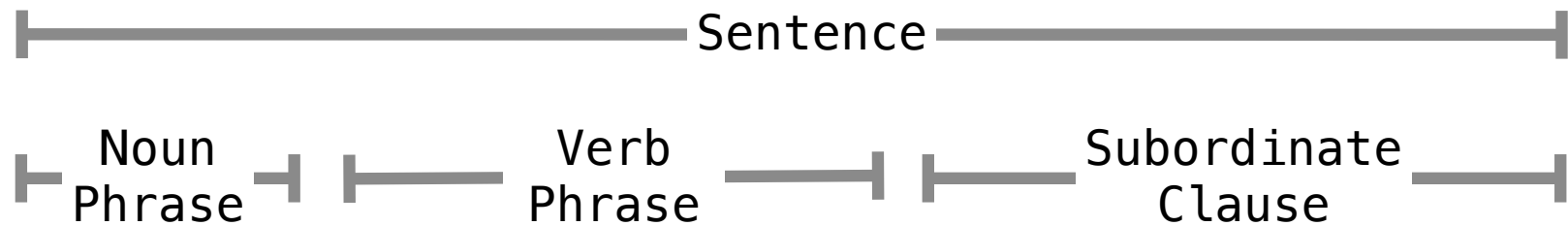
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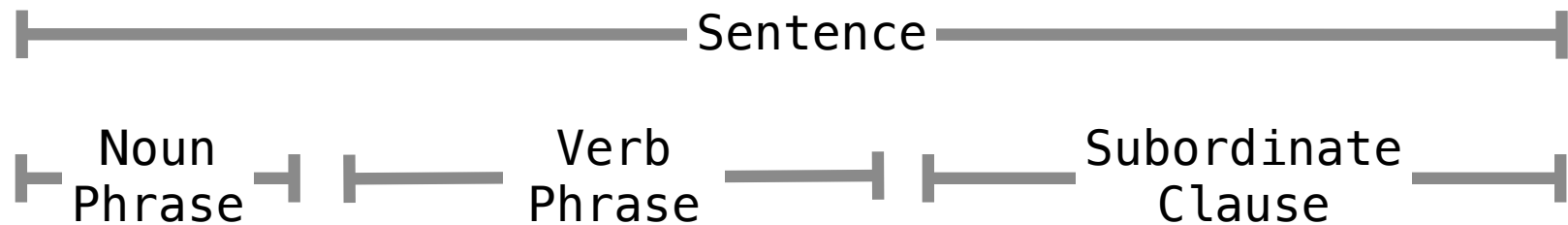
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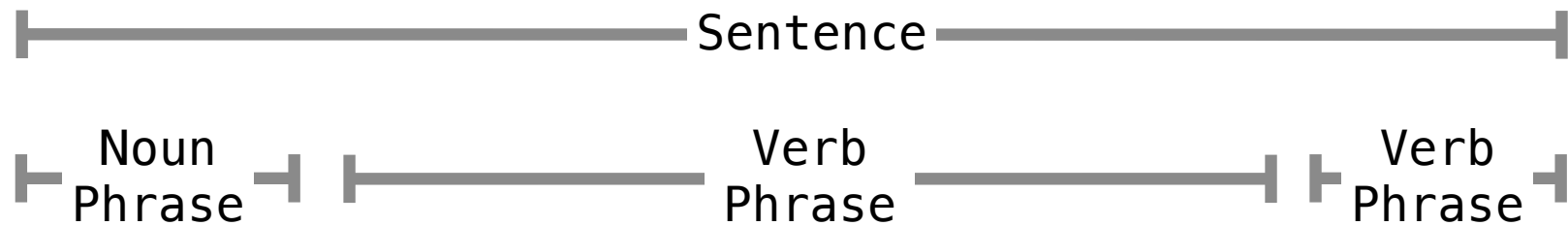


Programs must be written for people to read¹

A program must first be written for it to crash

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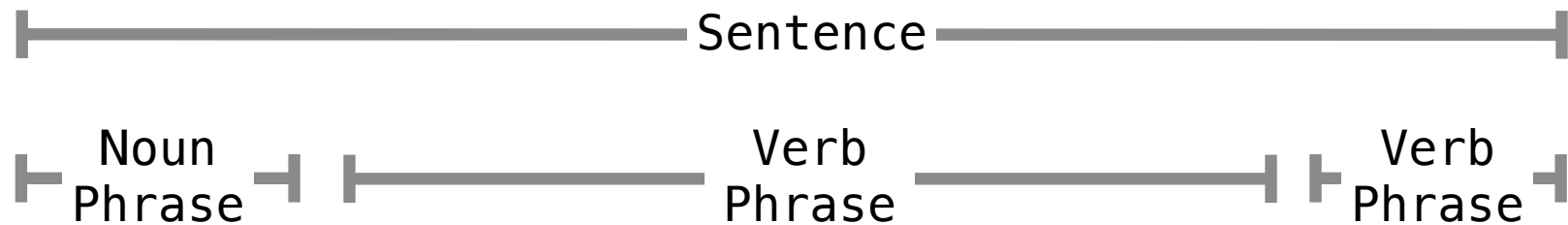
Syntactic Ambiguity in English



Programs must be written for people to read¹

¹Preface of Structure and Interpretation of Computer Programs
by Harold Abelson and Gerald Sussman with Julie Sussman

Syntactic Ambiguity in English



Programs must be written for people to read¹

Programs must be written for people to be useful

¹Preface of Structure and Interpretation of Computer Programs
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Syntactic Ambiguity in English

Programs must be written for people to read

Syntactic Ambiguity in English

pro•gram (*noun*)

a series of coded software instructions.

pro•gram (*verb*)

provide a computer with coded instructions.

Programs must be written for people to read

Syntactic Ambiguity in English

pro•gram (*noun*)

a series of coded software instructions.

pro•gram (*verb*)

provide a computer with coded instructions.

Programs must be written for people to read

must (*verb*)

be obliged to.

must (*noun*)

dampness or mold.

Syntax Trees

Representing Syntactic Structure

Representing Syntactic Structure

Buffalo

Representing Syntactic Structure

Noun

Buffalo

Representing Syntactic Structure



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Noun

Buffalo

Representing Syntactic Structure



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Noun

Buffalo buffalo

Representing Syntactic Structure



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Noun

Buffalo

Verb

buffalo

Representing Syntactic Structure



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Noun

Buffalo

Verb

buffalo

Noun

buffalo

Representing Syntactic Structure



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|—— Sentence ——|

Noun

Buffalo

Verb

buffalo

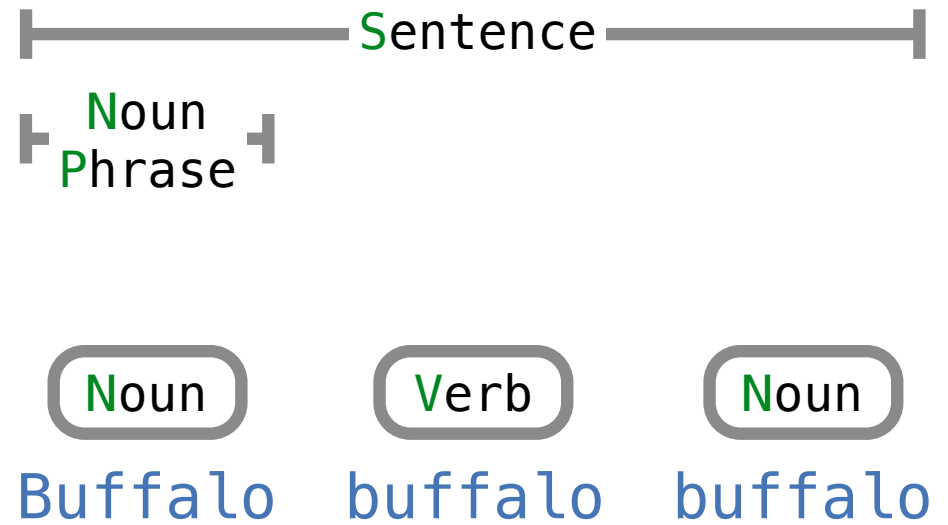
Noun

buffalo

Representing Syntactic Structure



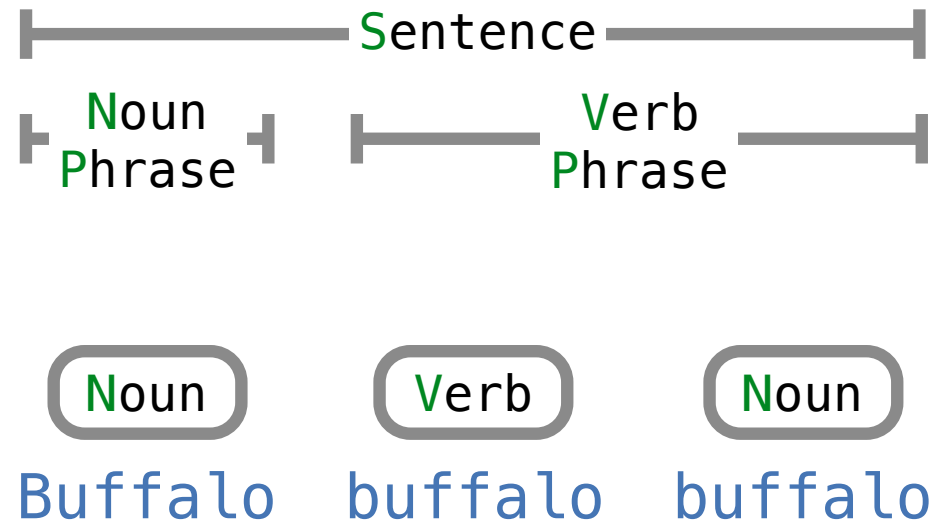
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Representing Syntactic Structure



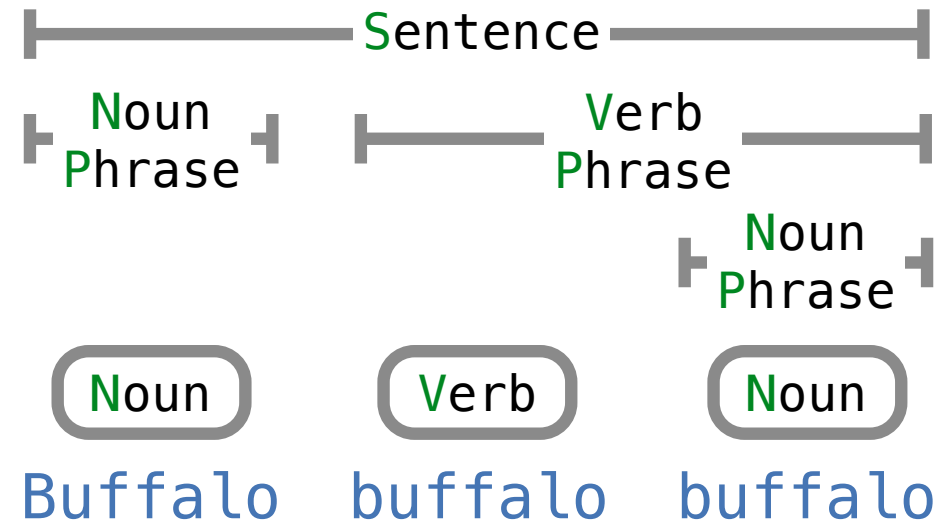
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Representing Syntactic Structure



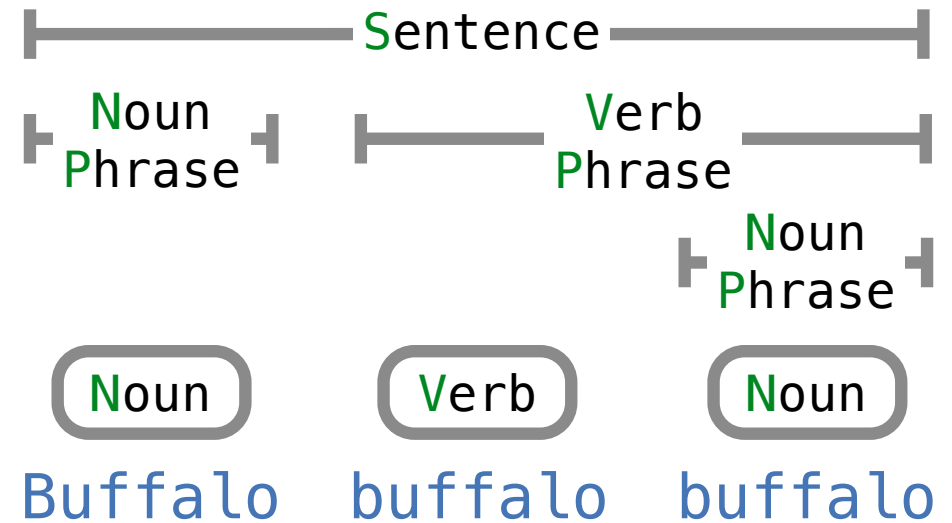
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Representing Syntactic Structure



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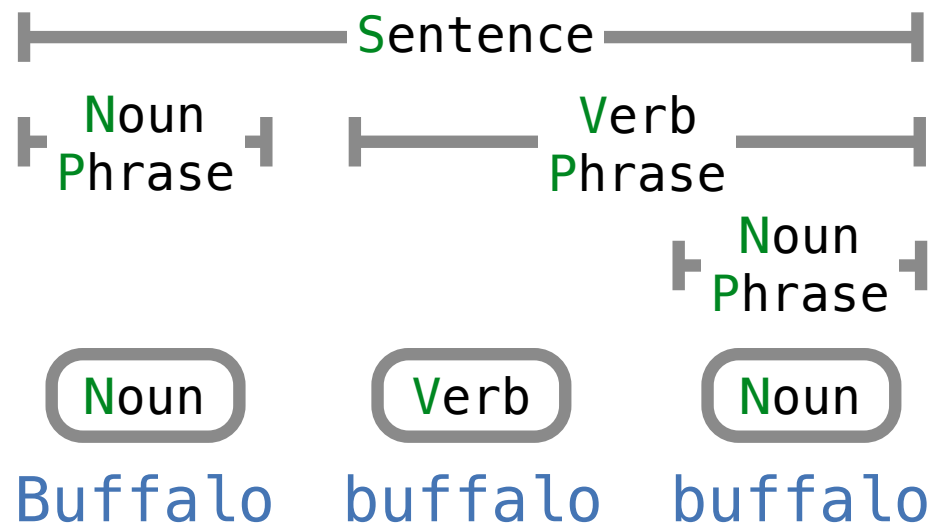


A **Tree** represents a phrase:

Representing Syntactic Structure



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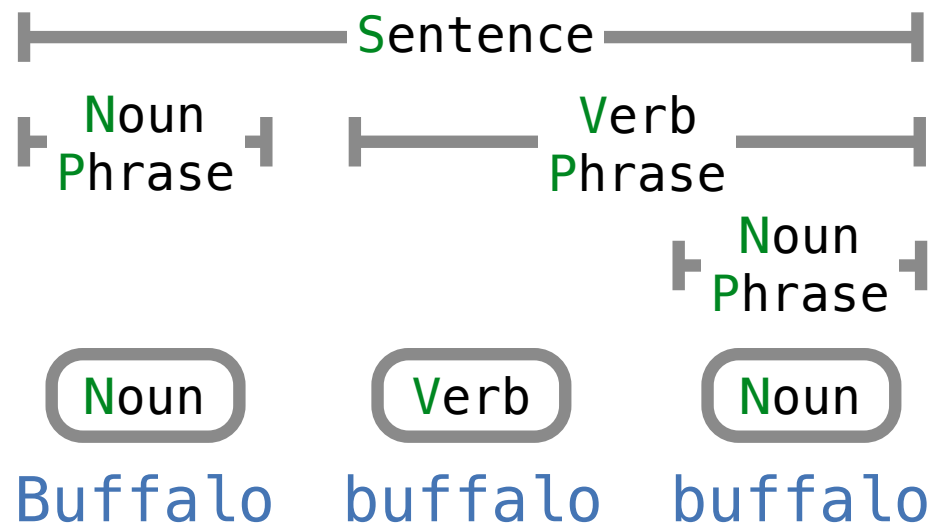
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Representing Syntactic Structure



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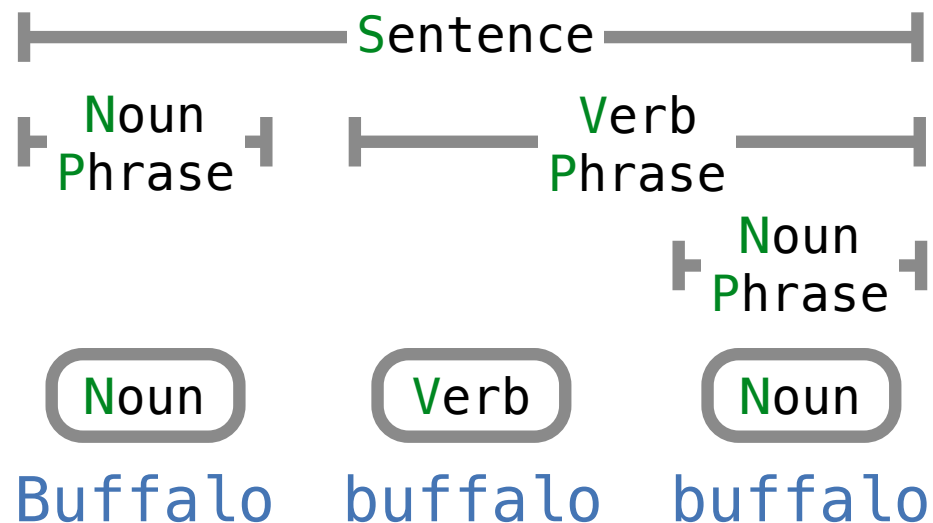
A **Tree** represents a phrase:

- **tag** -- What kind of phrase (e.g., **S**, **NP**, **VP**)
- **branches** -- Sequence of **Tree** or **Leaf** components

Representing Syntactic Structure



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A **Tree** represents a phrase:

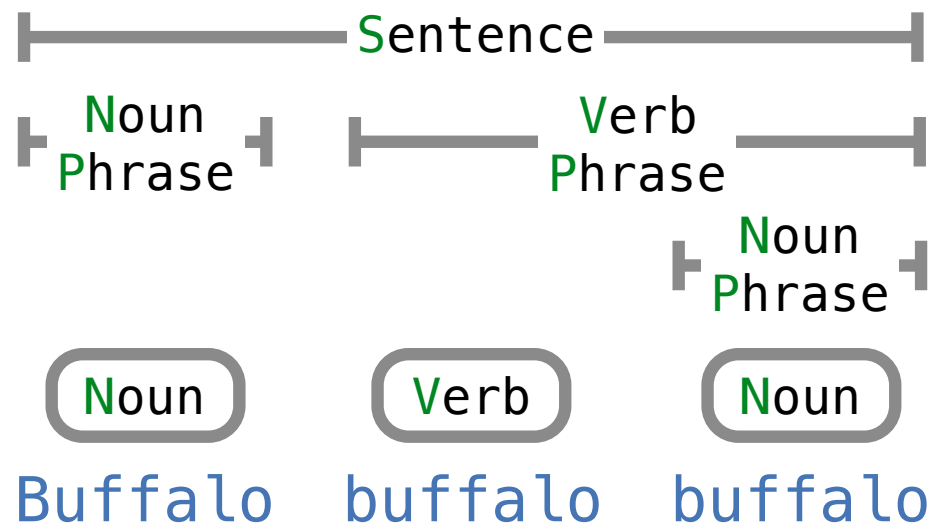
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A **Leaf** represents a single word:

Representing Syntactic Structure



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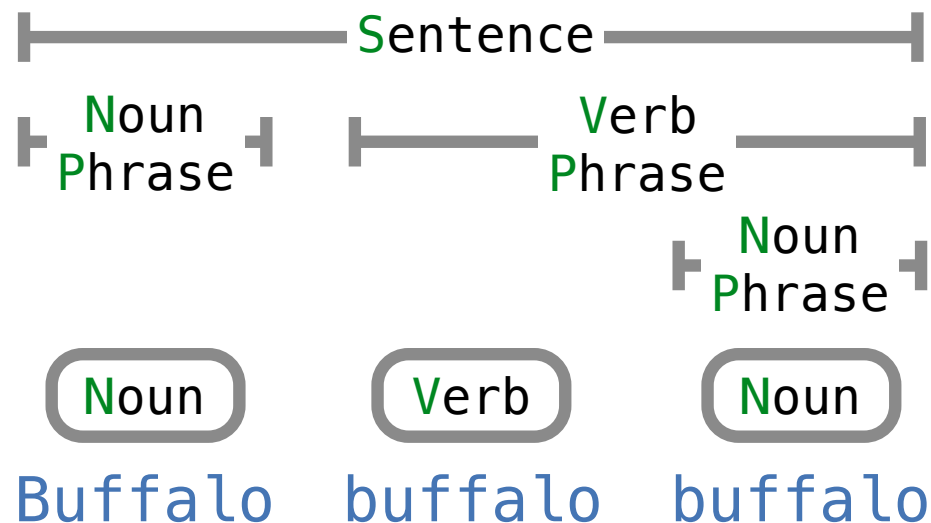
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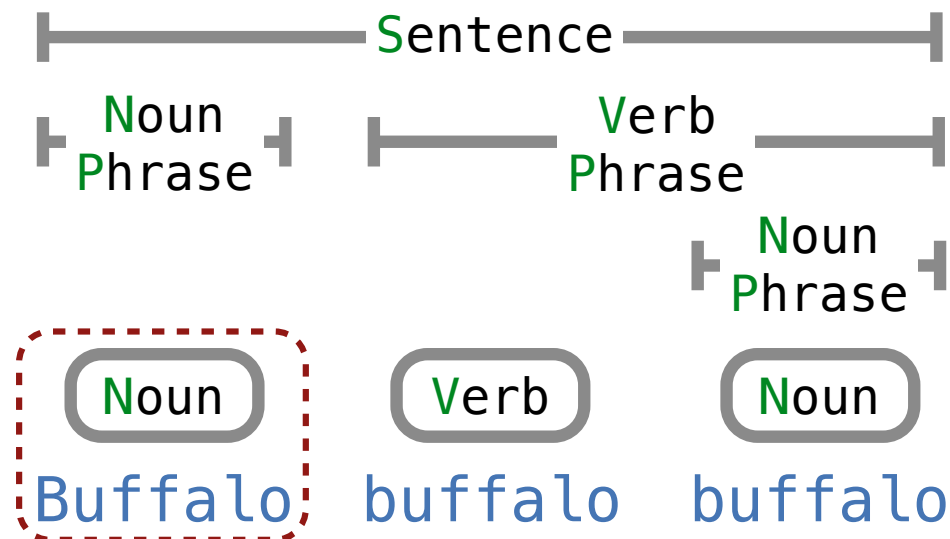
A **Leaf** represents a single word:

- **tag** -- What kind of word (e.g., **N**, **V**)
- **word** -- The word

Representing Syntactic Structure



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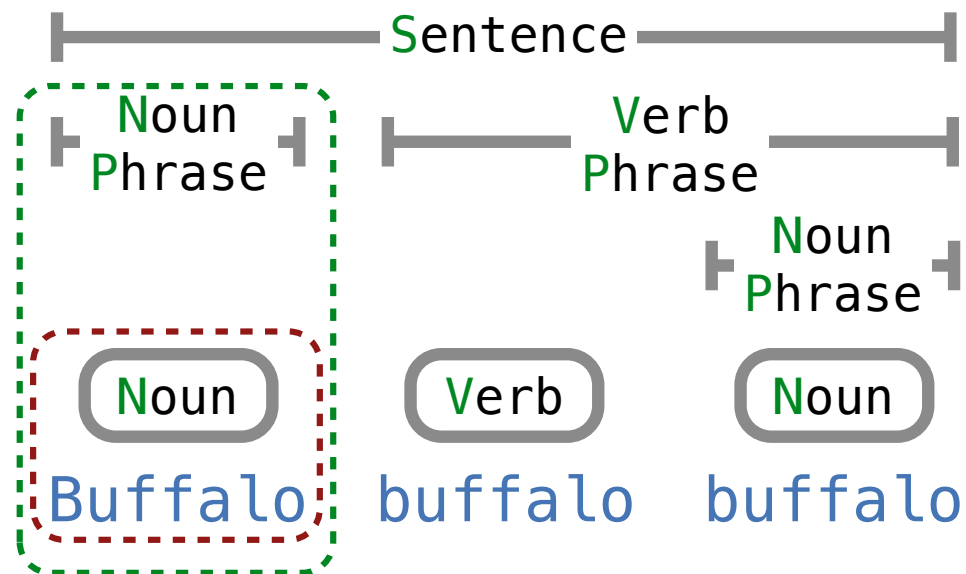
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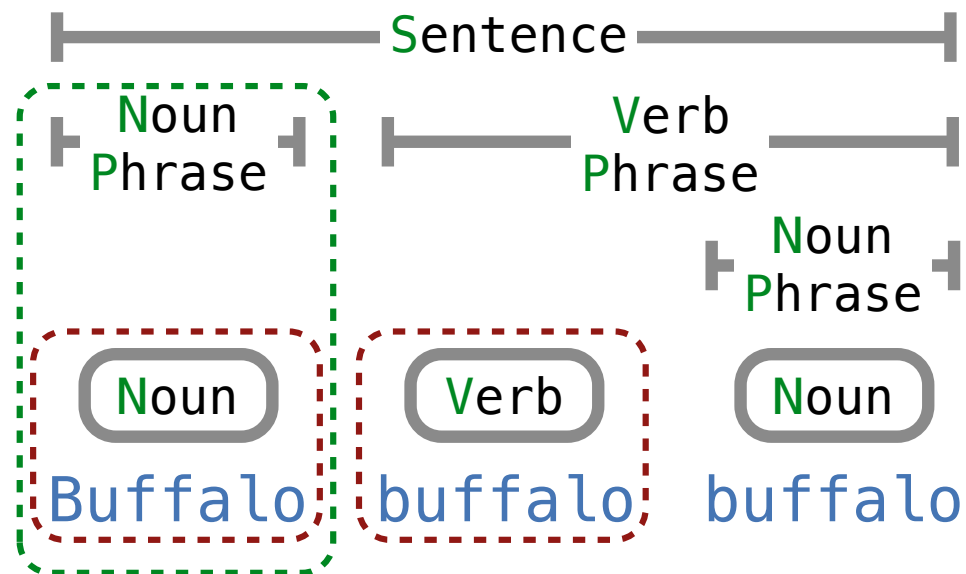
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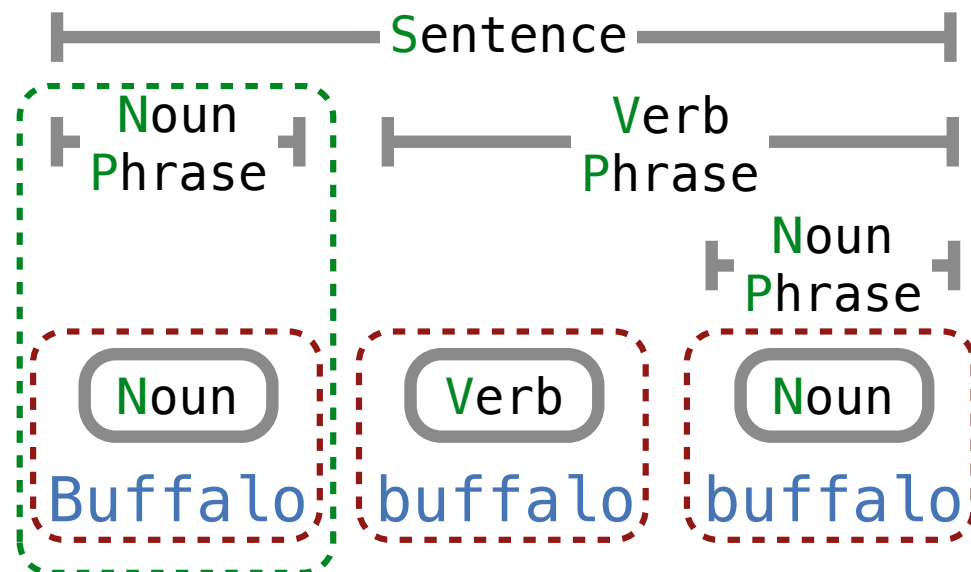
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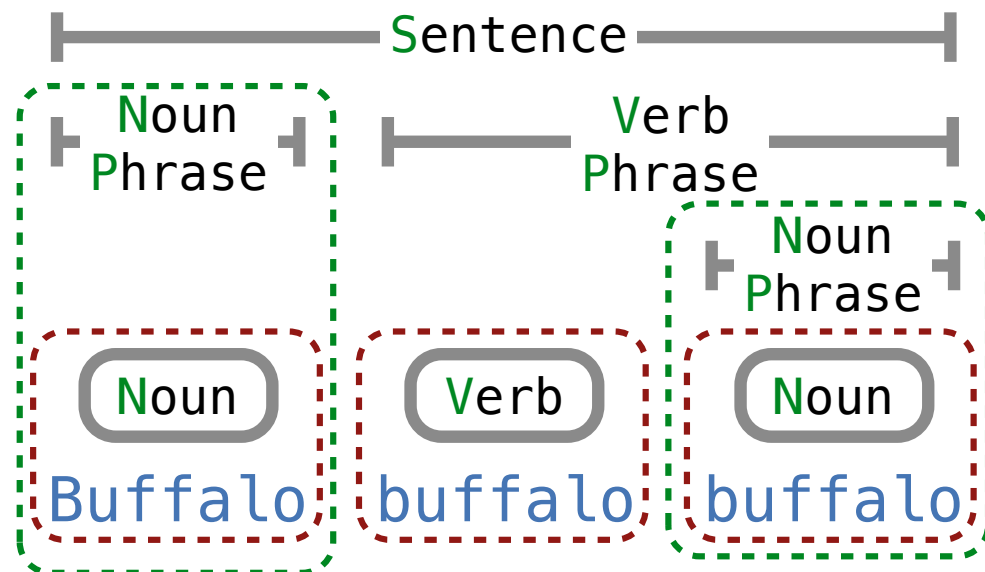
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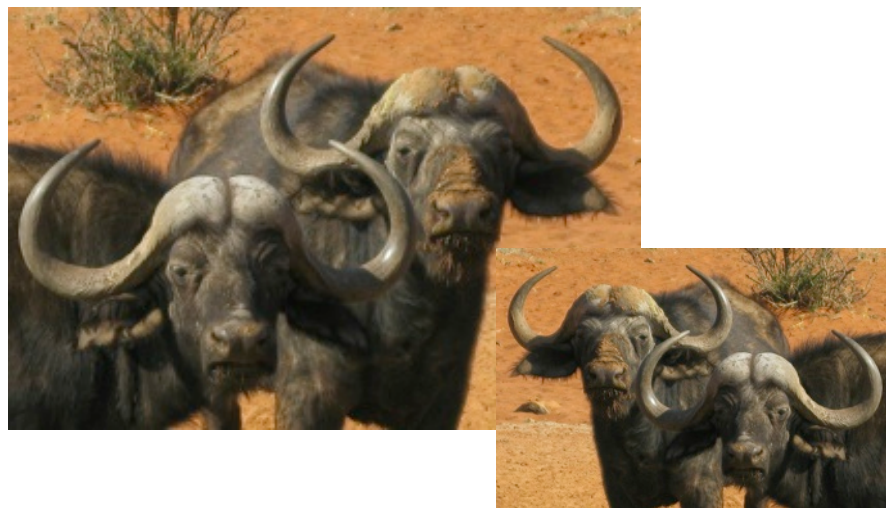
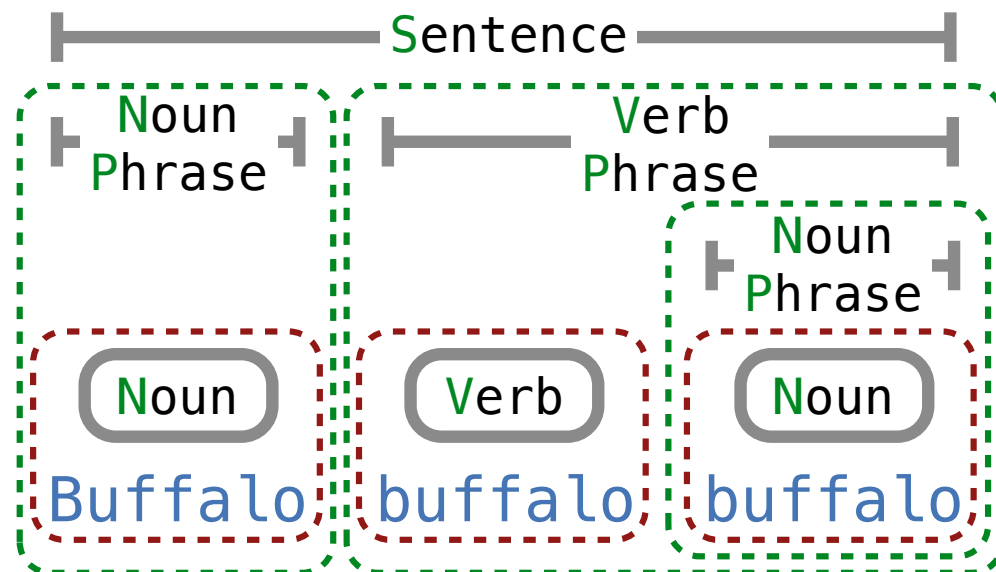


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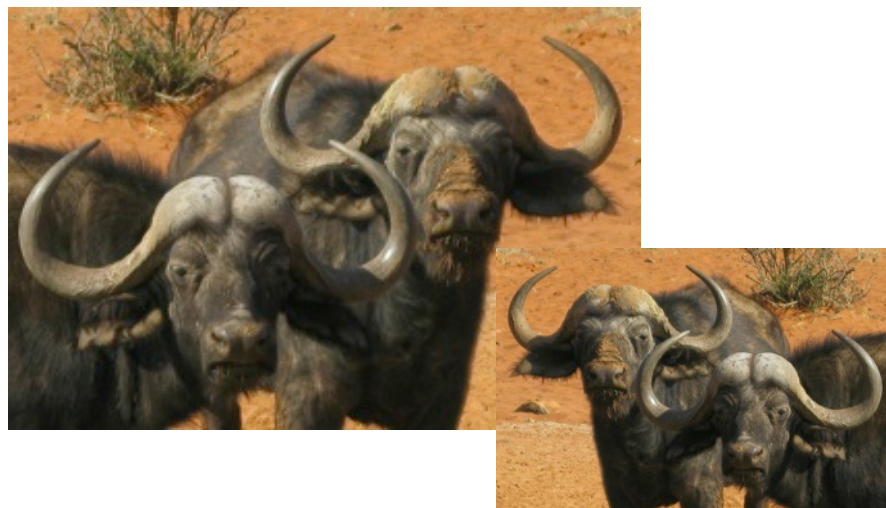
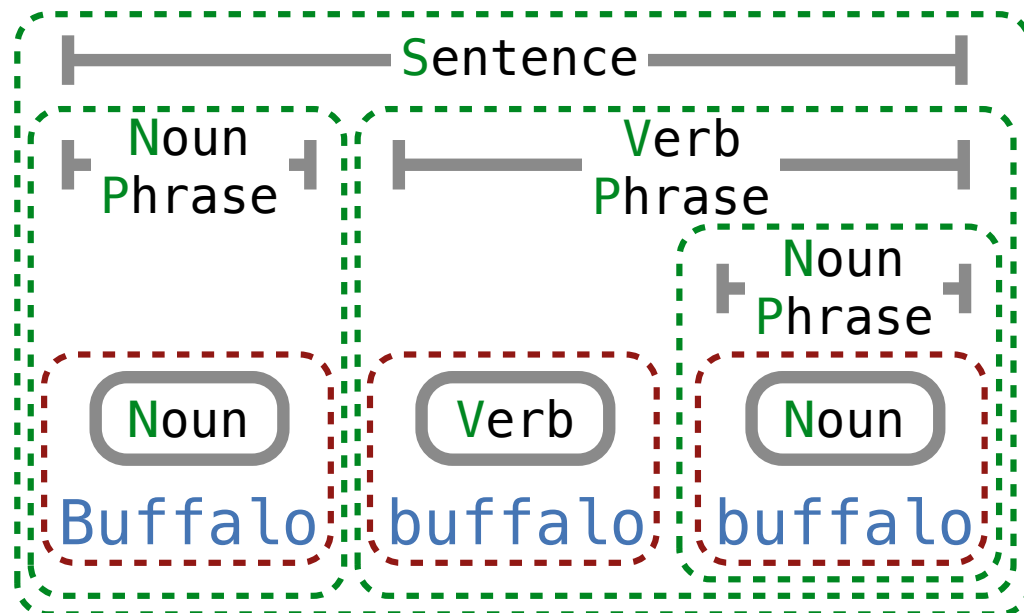


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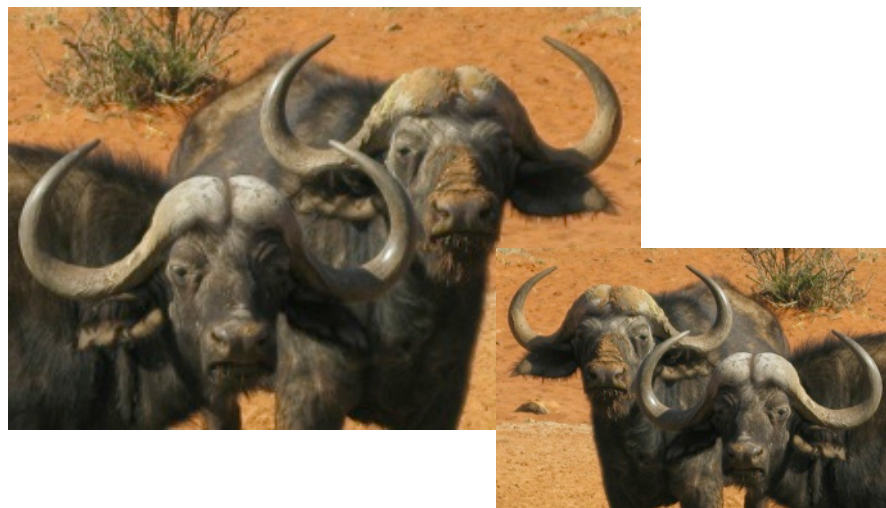
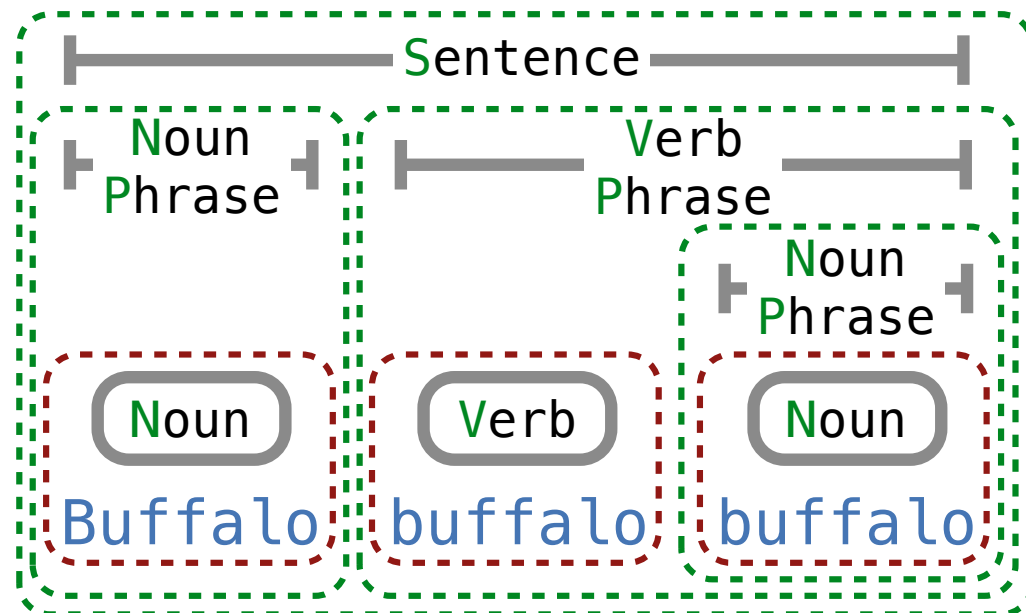


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- **word** — The word

(Demo)

Grammars

Context-Free Grammar Rules

Context-Free Grammar Rules

A grammar rule describes how a tag can be expanded.

Context-Free Grammar Rules

A grammar rule describes how a tag can be expanded.

$$S \rightarrow NP VP$$

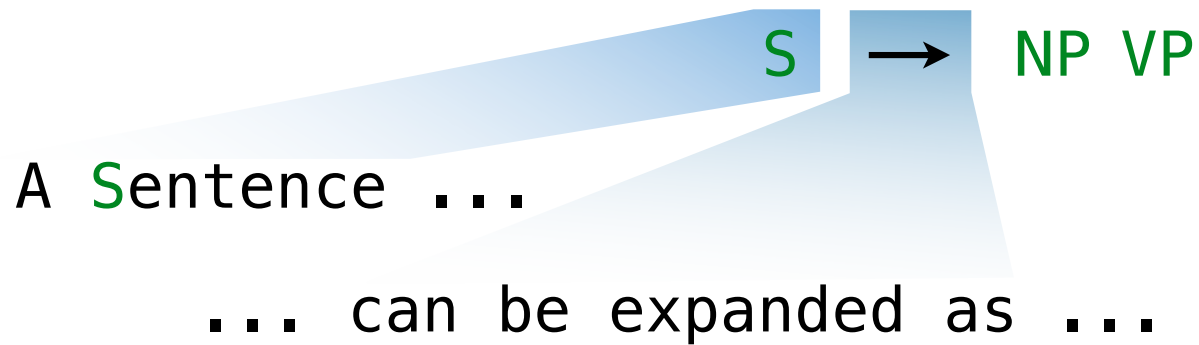
Context-Free Grammar Rules

A grammar rule describes how a tag can be expanded.

A  **S** → **NP VP**
A **S**entence ...

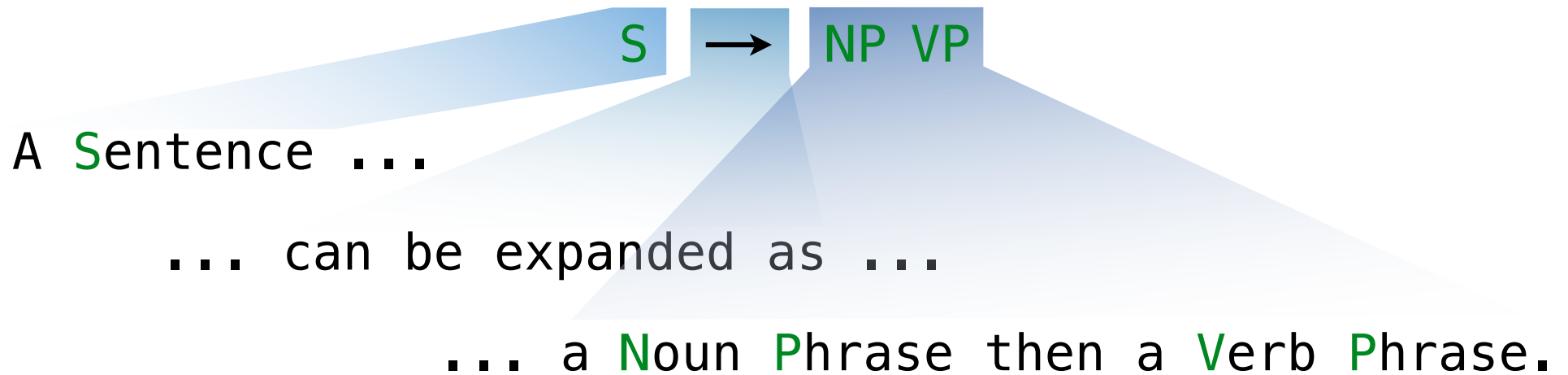
Context-Free Grammar Rules

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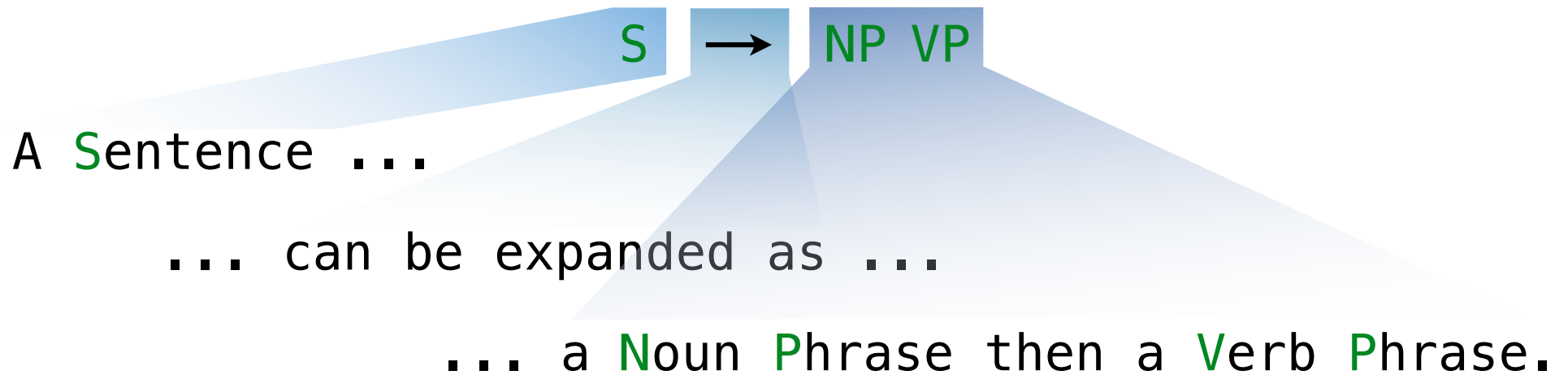
Context-Free Grammar Rules

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Context-Free Grammar Rules

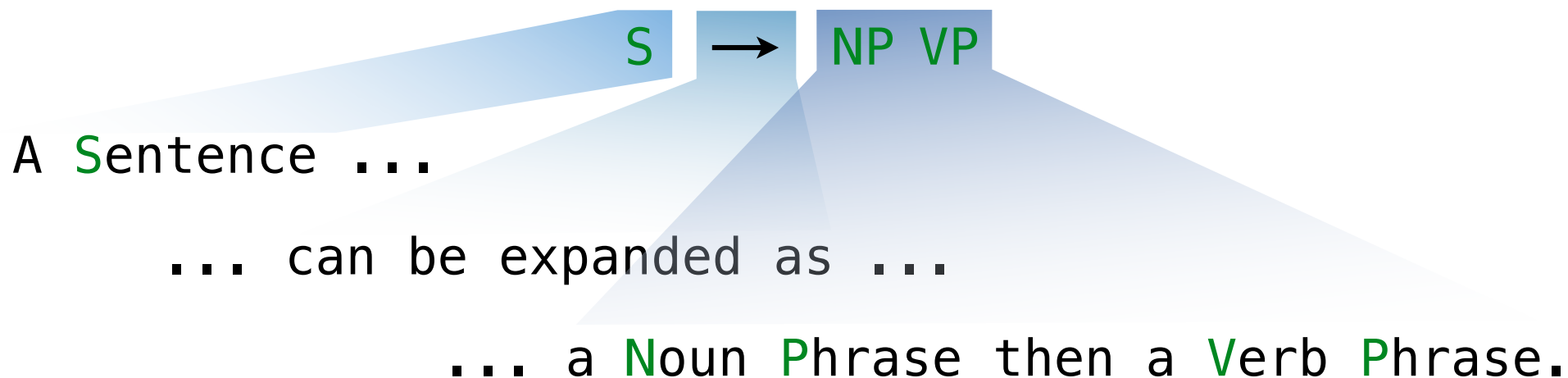
A grammar rule describes how a tag can be expanded.



$S \rightarrow NP VP$

Context-Free Grammar Rules

A grammar rule describes how a tag can be expanded.



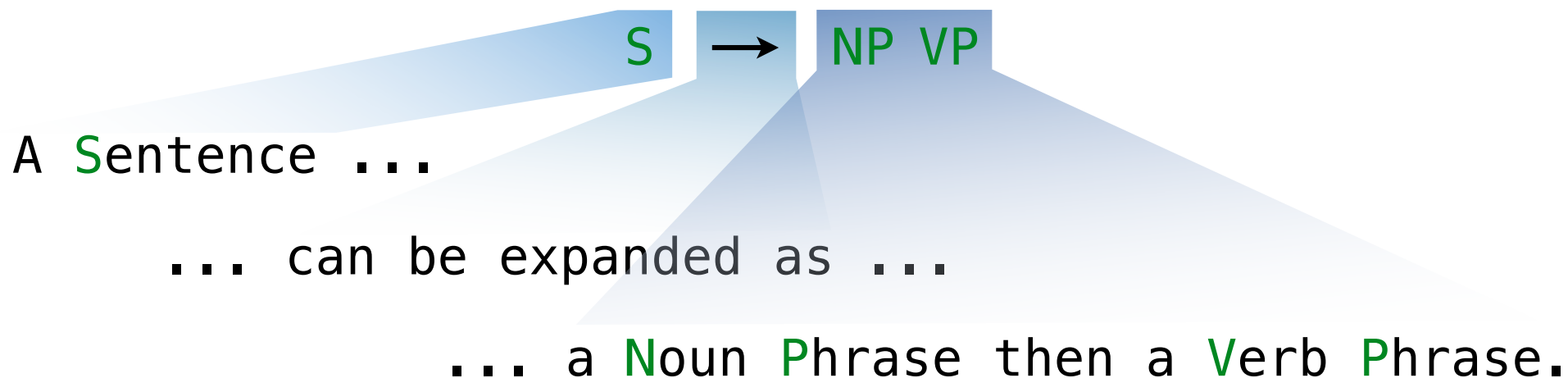
S → **NP VP**



Context-Free Grammar Rules

A grammar rule describes how a tag can be expanded.

A **S**entence ...
... can be expanded as ...
... a **N**oun **P**hrase then a **V**erb **P**hrase.

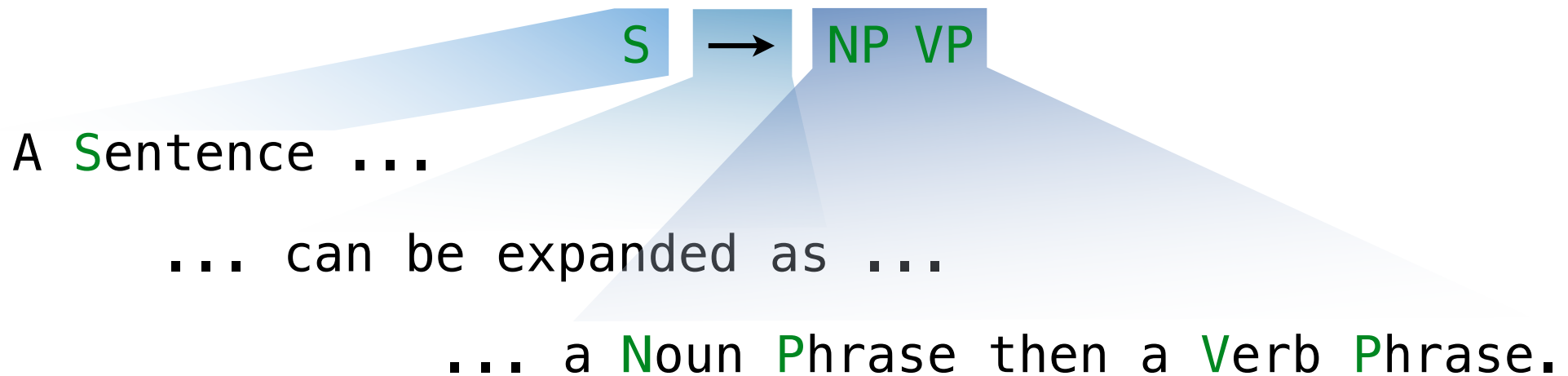
A diagram illustrating the expansion of a grammar rule. At the top, a blue box labeled 'S' is followed by a right-pointing arrow and then a blue box labeled 'NP VP'. Below this, a light blue trapezoidal shape expands from the 'S' box to the 'NP VP' box, representing the expansion process. The text 'A Sentence ...' is aligned with the 'S' box, and '... can be expanded as ...' is centered under the trapezoid. Below that, '... a Noun Phrase then a Verb Phrase.' is aligned with the 'NP VP' box.

S → **NP VP**



Context-Free Grammar Rules

A grammar rule describes how a tag can be expanded.

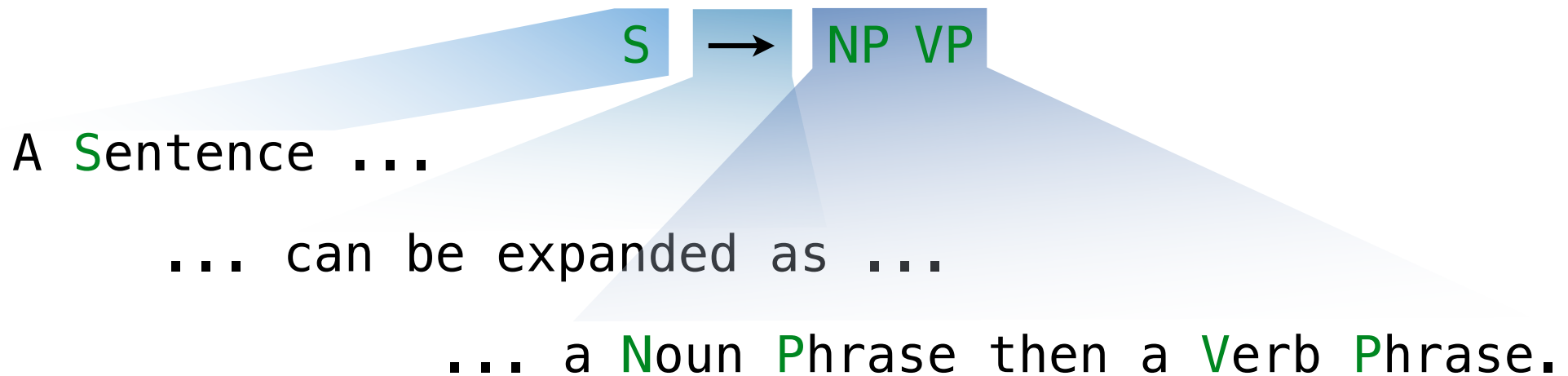


S → **NP VP**
NP → **N**

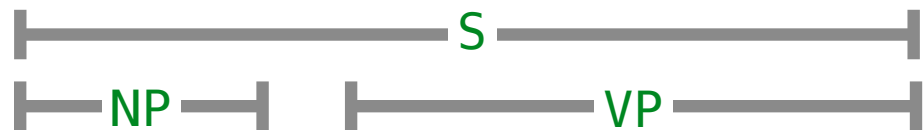


Context-Free Grammar Rules

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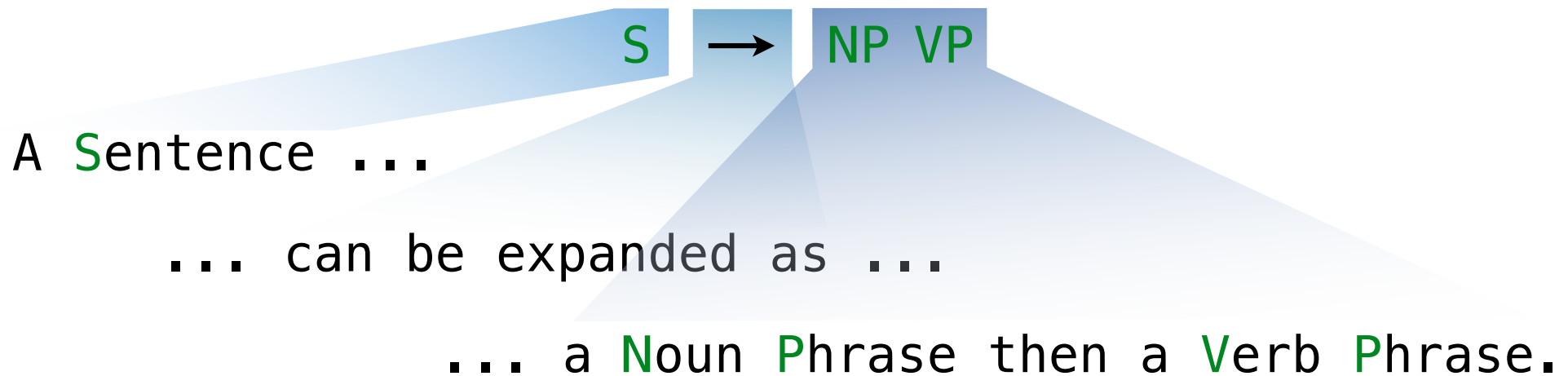
S → **NP VP**
NP → **N**



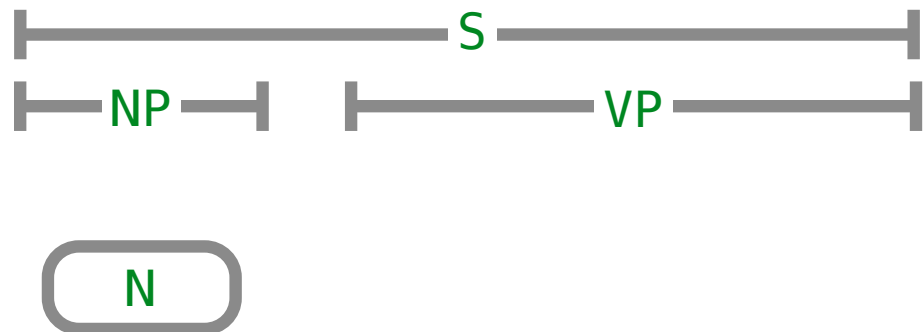
N

Context-Free Grammar Rules

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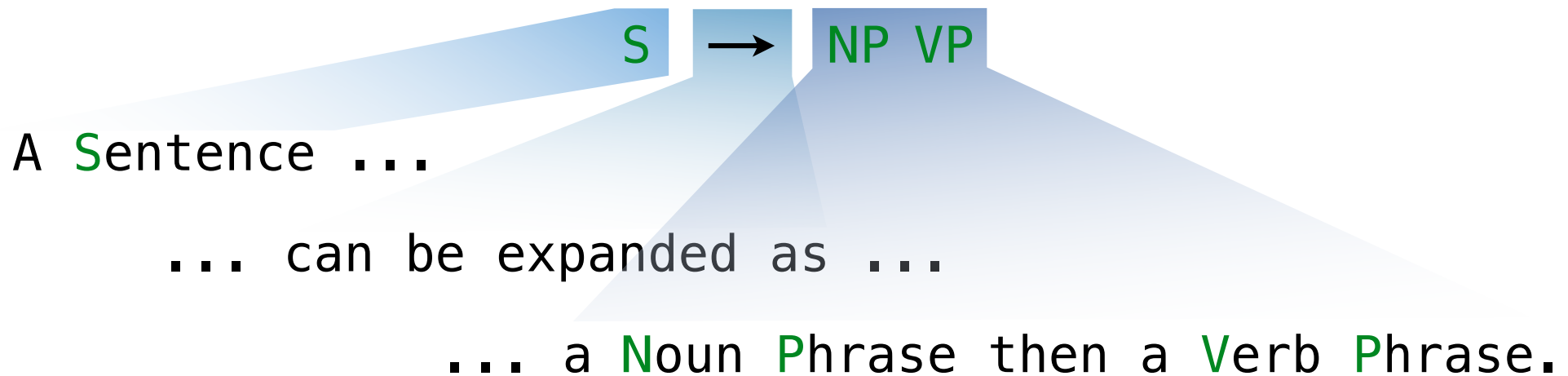


S → **NP VP**
NP → **N**
N → buffalo

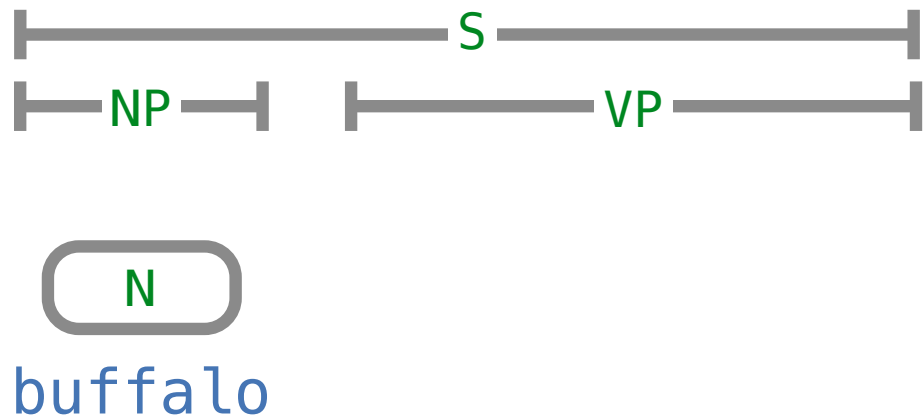


Context-Free Grammar Rules

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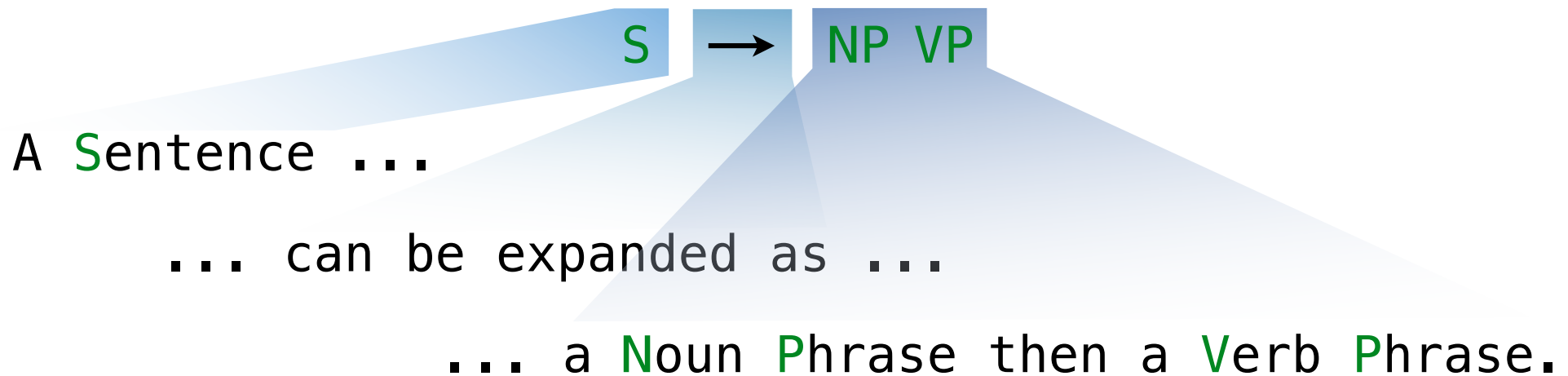


S → **NP** **VP**
NP → **N**
N → buffalo

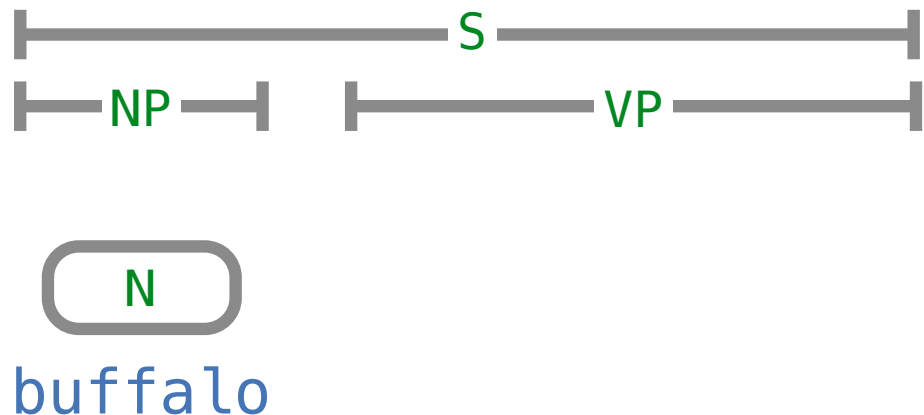


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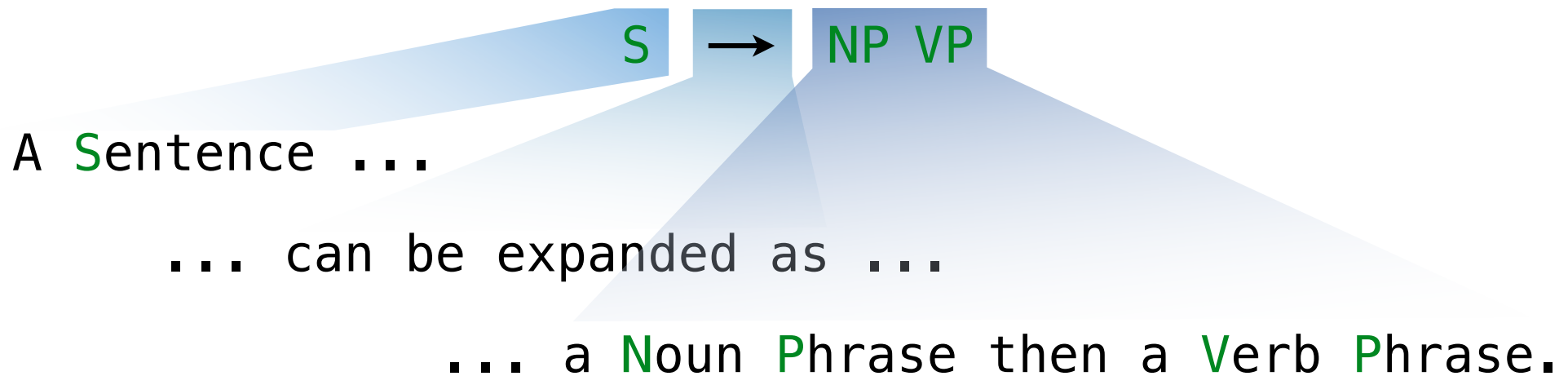


S → **NP VP**
NP → **N**
N → buffalo
VP → **V NP**

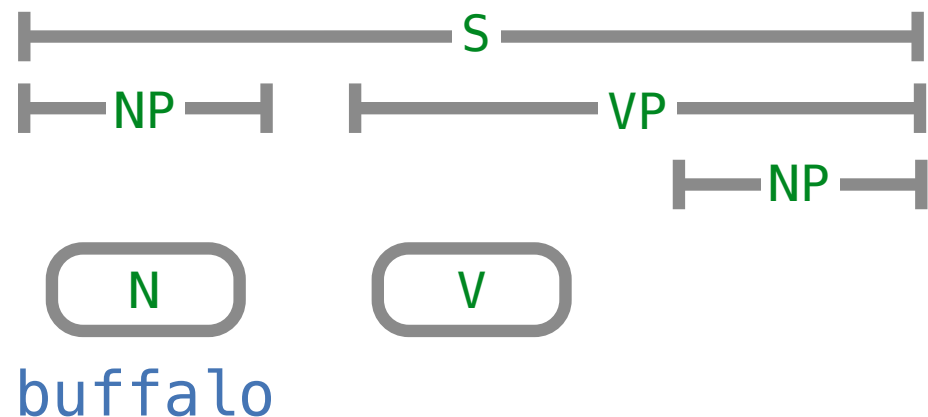


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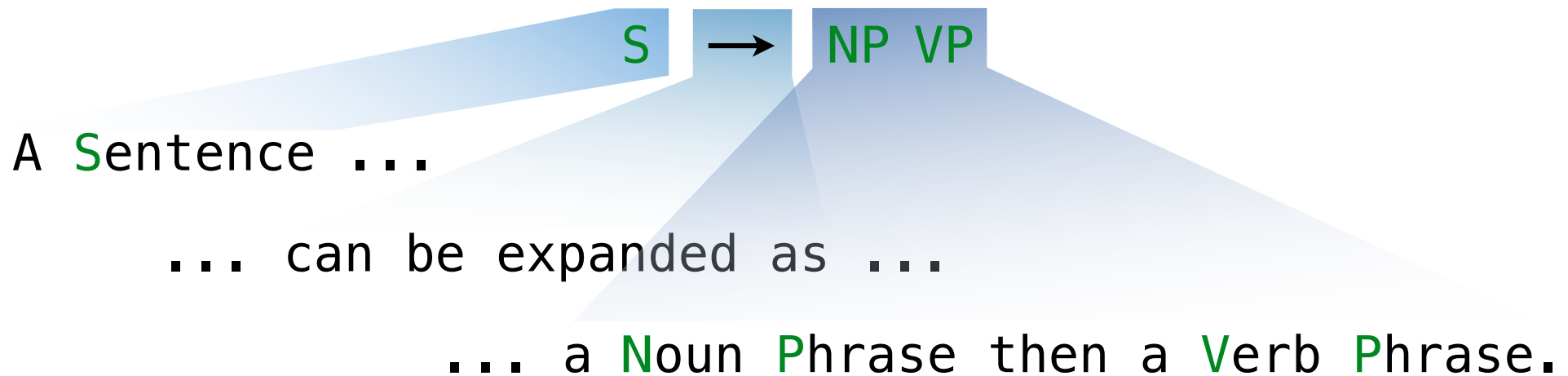


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NP → **N**
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VP → **V NP**

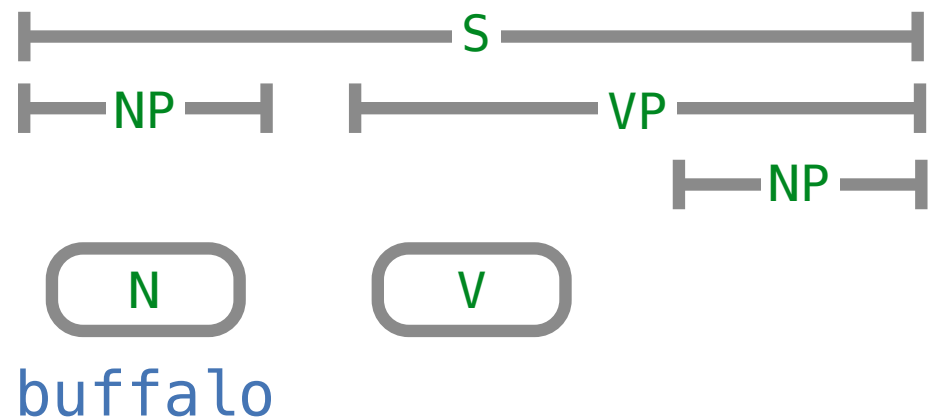


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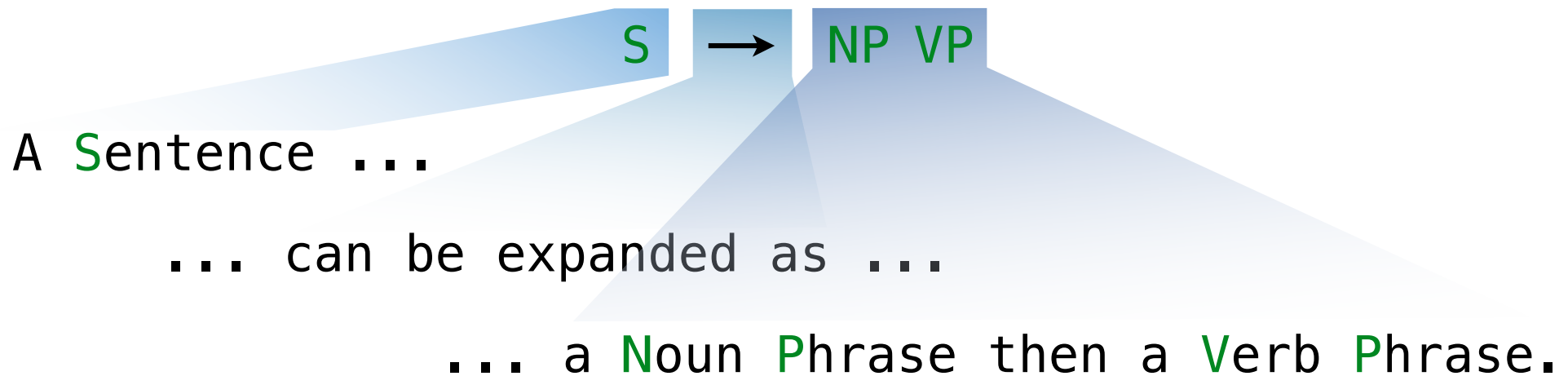


S → **NP VP**
NP → **N**
N → buffalo
VP → **V NP**
V → buffalo

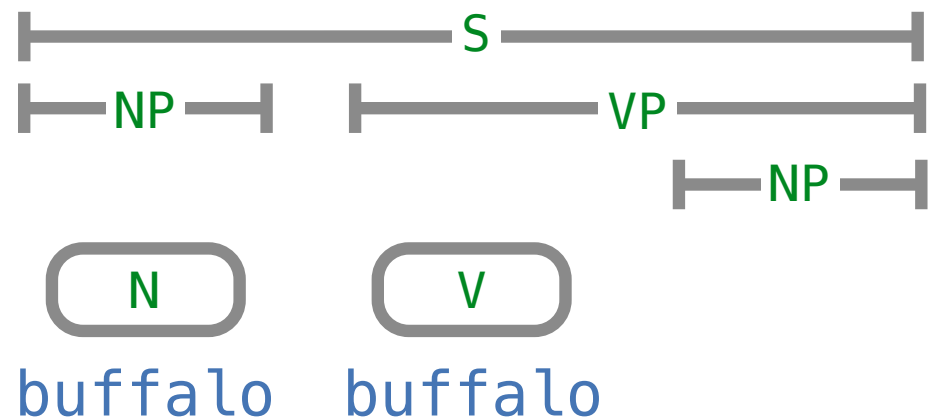


Context-Free Grammar Rules

A grammar rule describes how a tag can be expanded.



S → **NP VP**
NP → **N**
N → buffalo
VP → **V NP**
V → buffalo

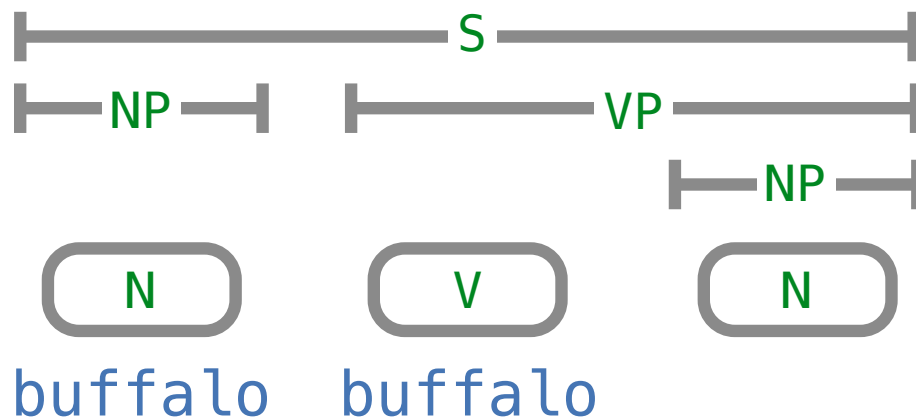


Context-Free Grammar Rules

A grammar rule describes how a tag can be expanded.

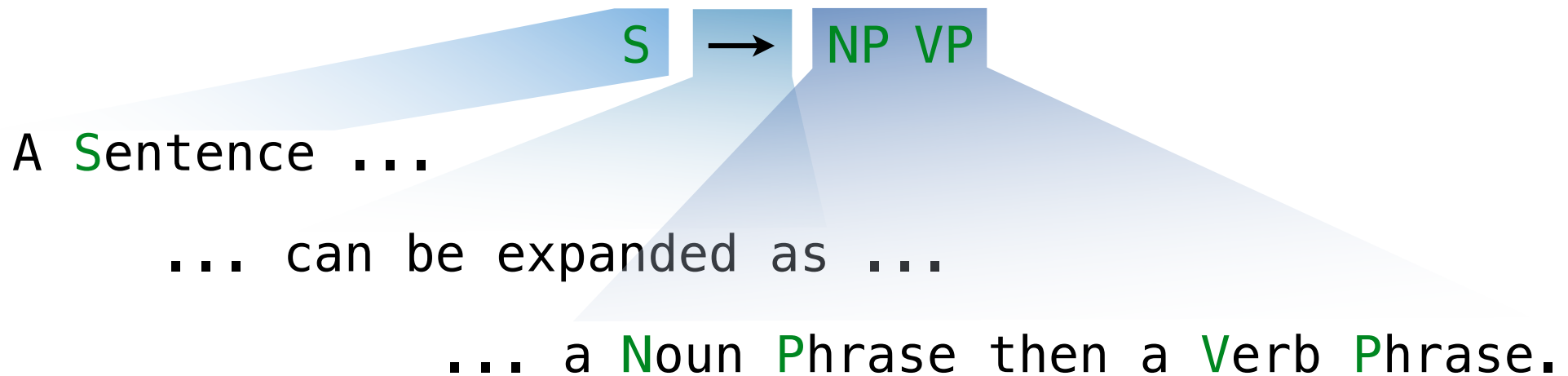
A **S**entence ...
... can be expanded as ...
... a **N**oun **P**hrase then a **V**erb **P**hrase.

S → **NP** **VP**
NP → **N**
N → buffalo
VP → **V** **NP**
V → buffalo

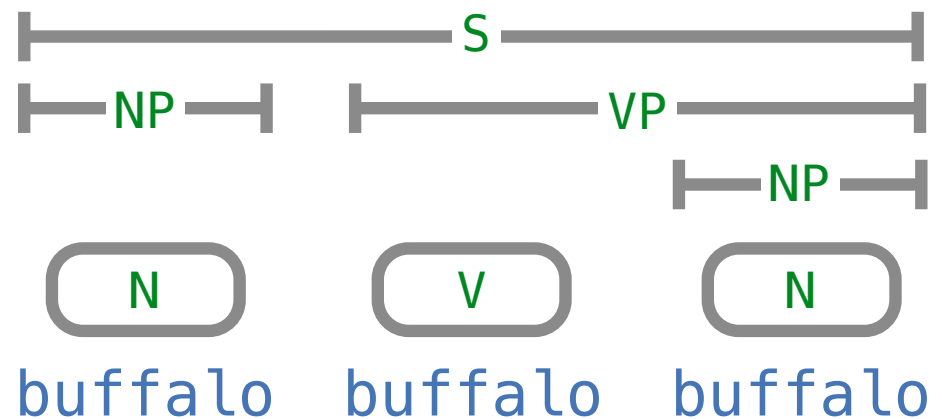


Context-Free Grammar Rules

A grammar rule describes how a tag can be expanded.

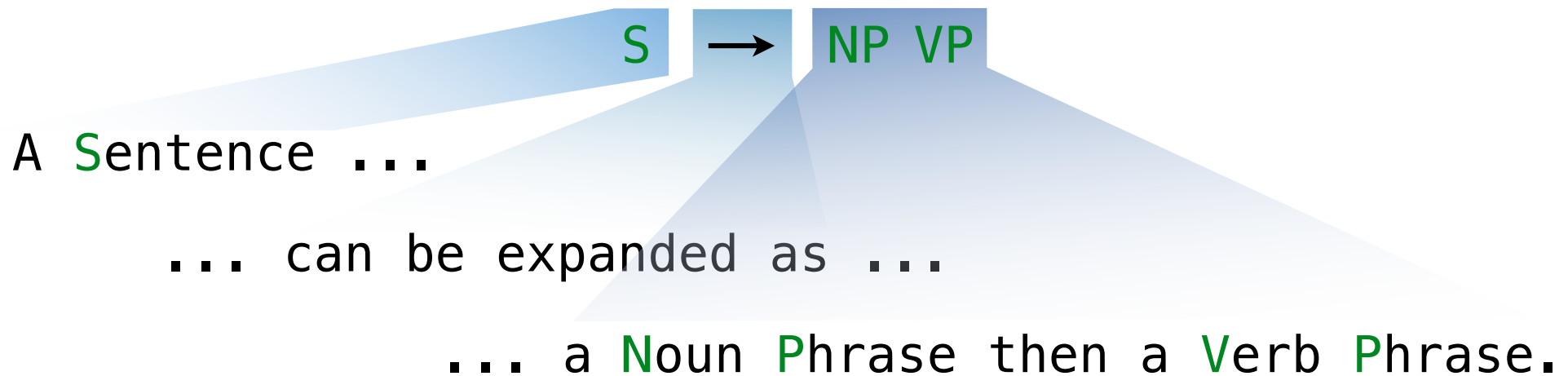


S → **NP VP**
NP → **N**
N → buffalo
VP → **V NP**
V → buffalo

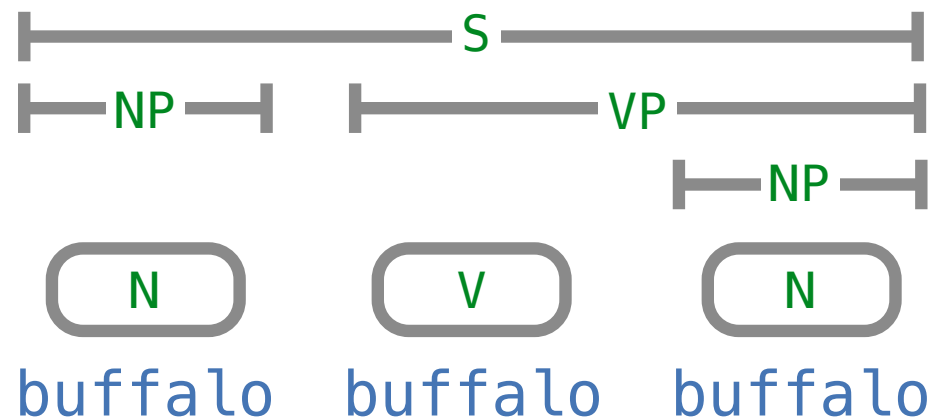


Context-Free Grammar Rules

A grammar rule describes how a tag can be expanded.



S → **NP** **VP**
NP → **N**
N → buffalo
VP → **V** **NP**
V → buffalo



(Demo)

Parsing

Exhaustive Parsing

Recursively expand, but force words to match input.

Exhaustive Parsing

Recursively expand, but force words to match input.

buffalo buffalo buffalo buffalo

Exhaustive Parsing

Recursively expand, but force words to match input.



buffalo buffalo buffalo buffalo

Exhaustive Parsing

Recursively expand, but force words to match input.



buffalo buffalo buffalo buffalo



Exhaustive Parsing

Recursively expand, but force words to match input.

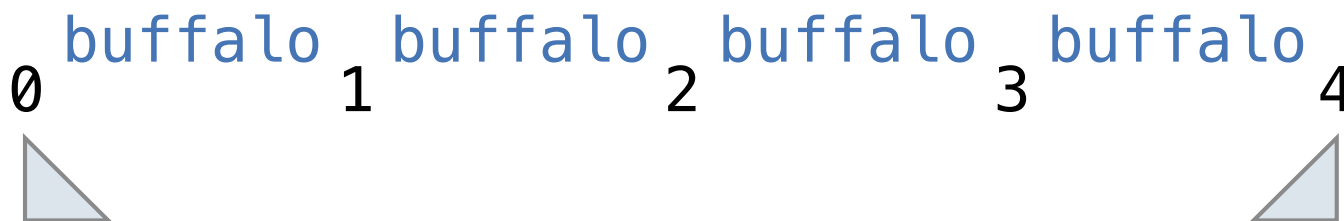


buffalo buffalo buffalo buffalo



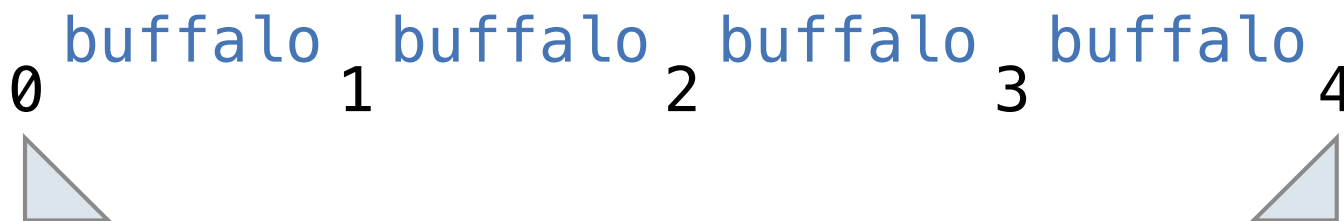
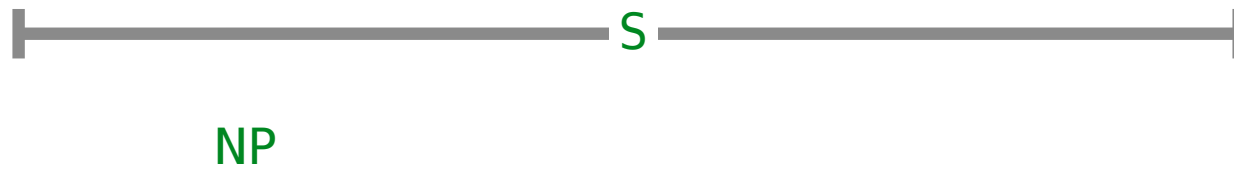
Exhaustive Parsing

Recursively expand, but force words to match input.



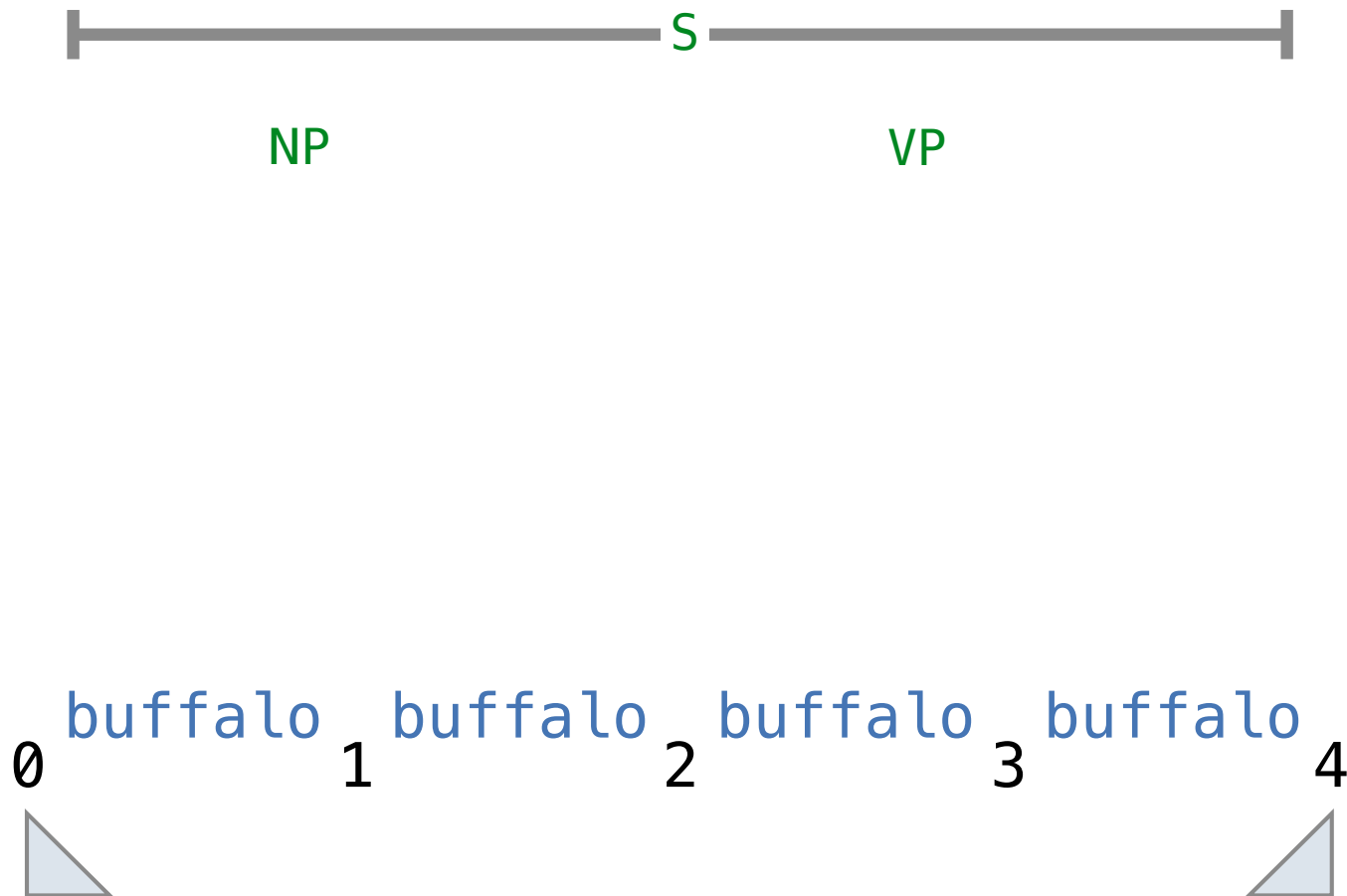
Exhaustive Parsing

Recursively expand, but force words to match input.



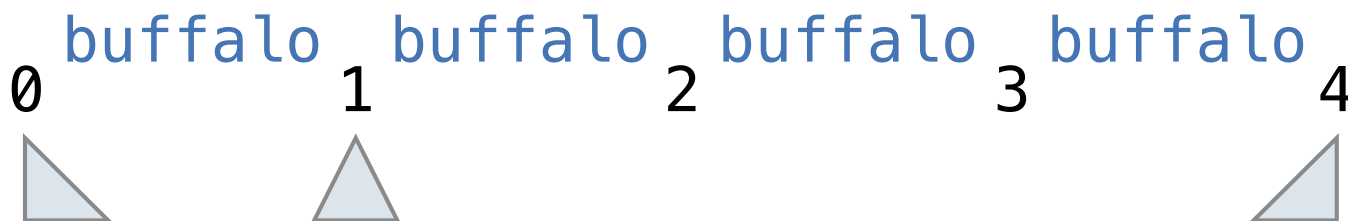
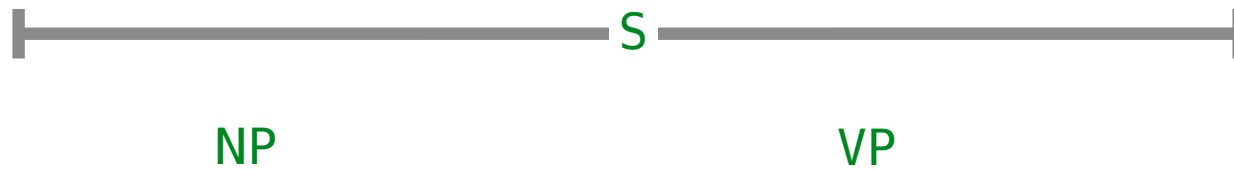
Exhaustive Parsing

Recursively expand, but force words to match input.



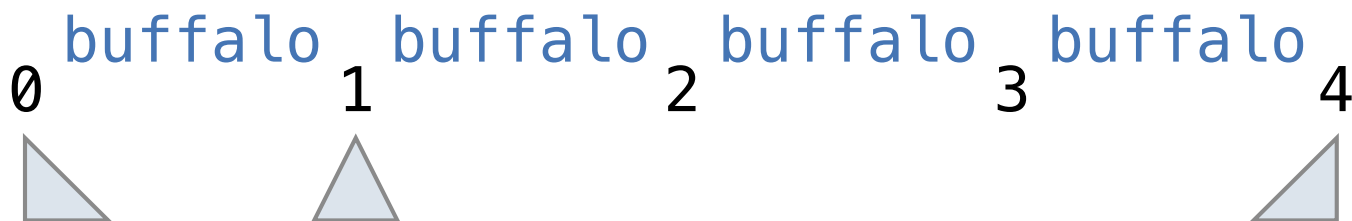
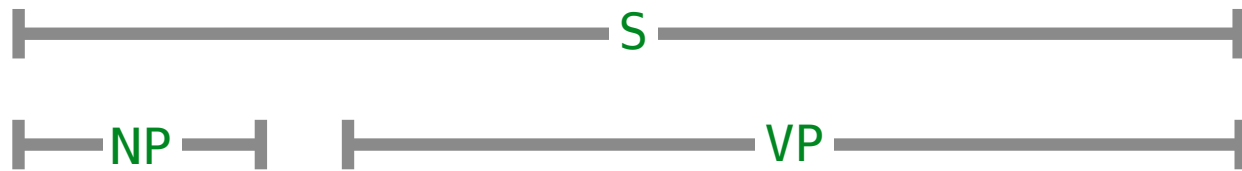
Exhaustive Parsing

Recursively expand, but force words to match input.



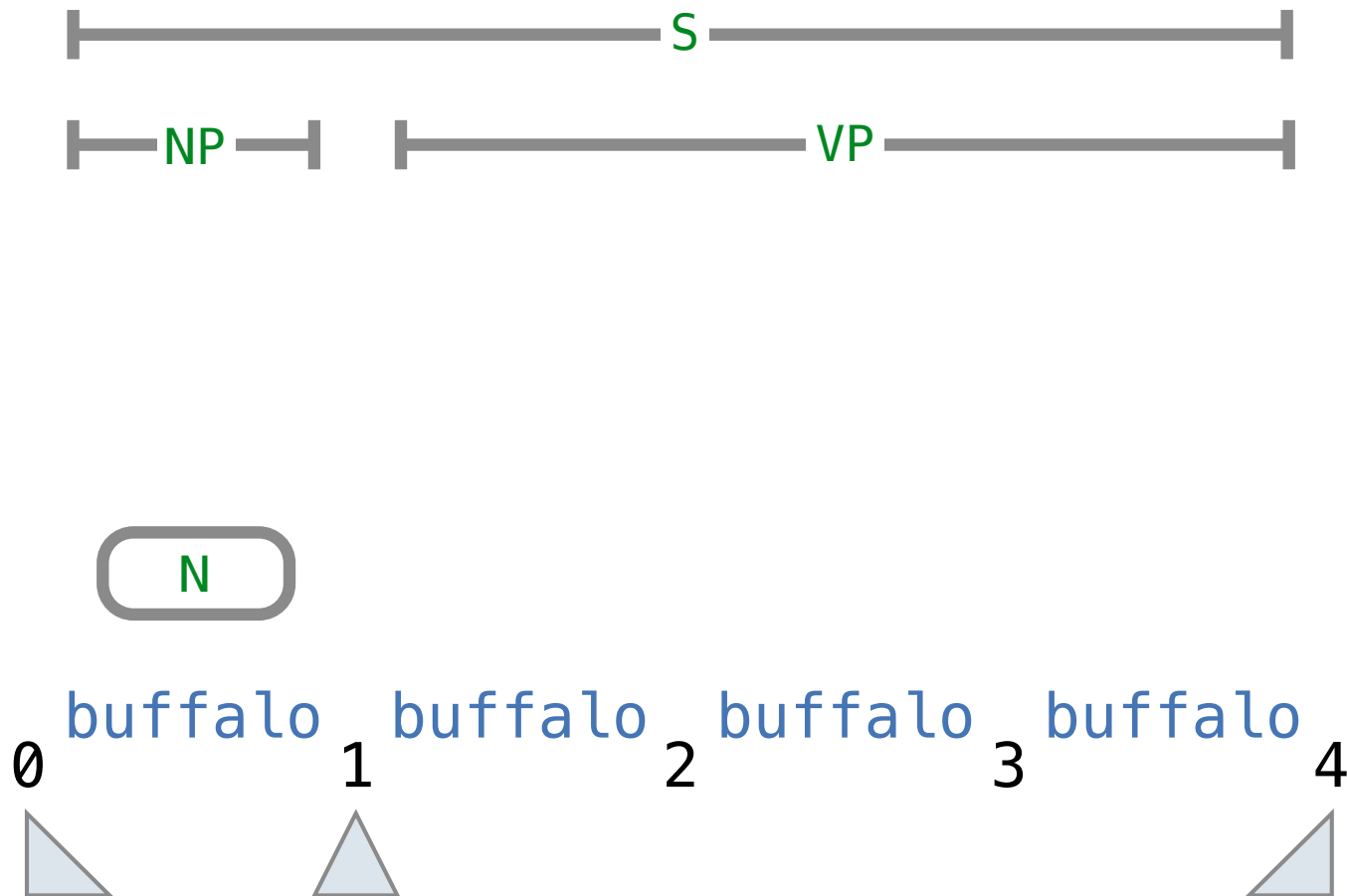
Exhaustive Parsing

Recursively expand, but force words to match input.



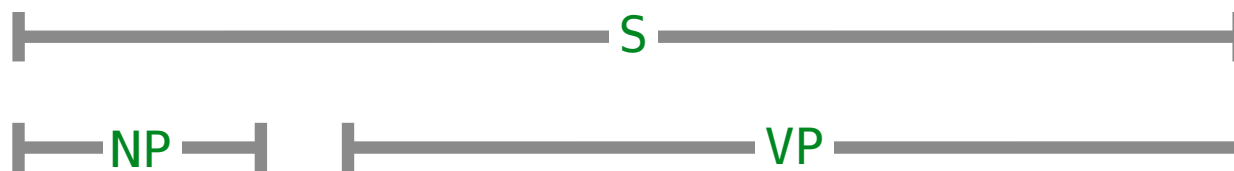
Exhaustive Parsing

Recursively expand, but force words to match input.



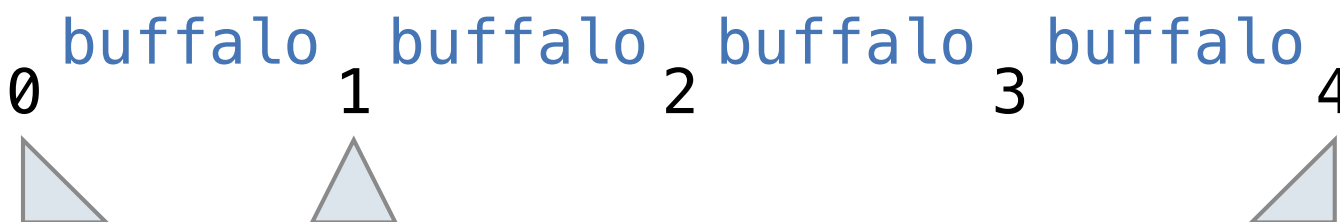
Exhaustive Parsing

Recursively expand, but force words to match input.



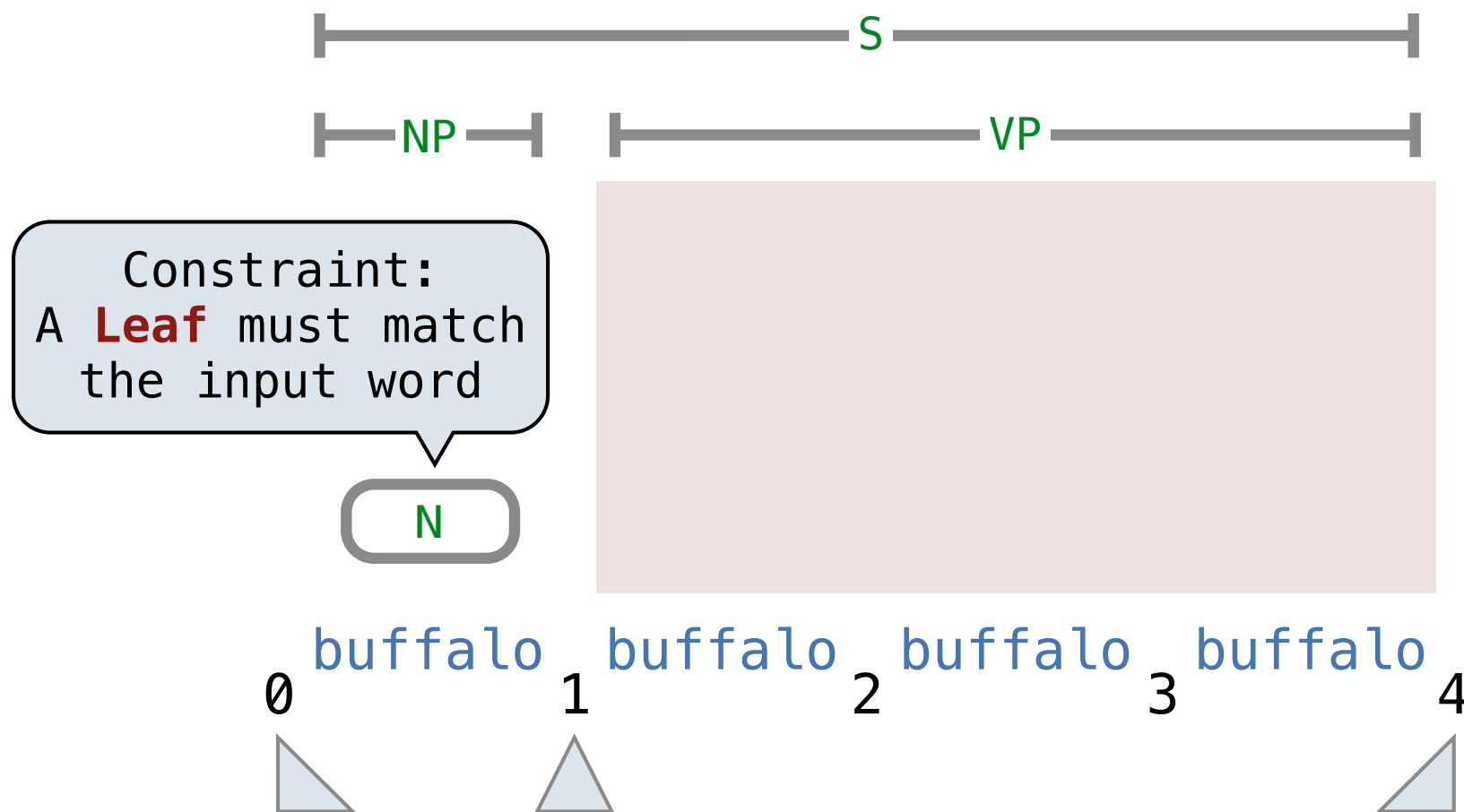
Constraint:
A **Leaf** must match
the input word

N



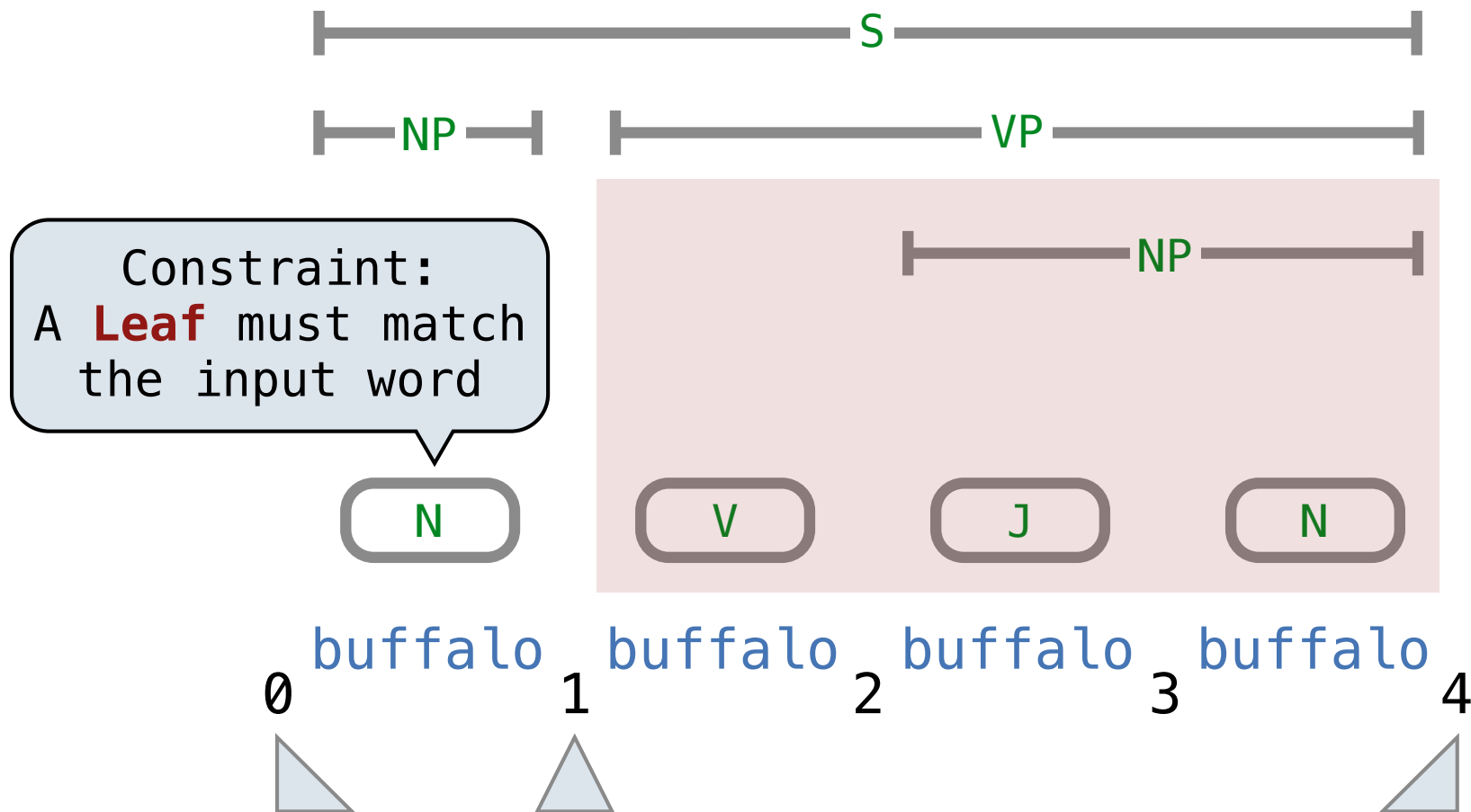
Exhaustive Parsing

Recursively expand, but force words to match input.



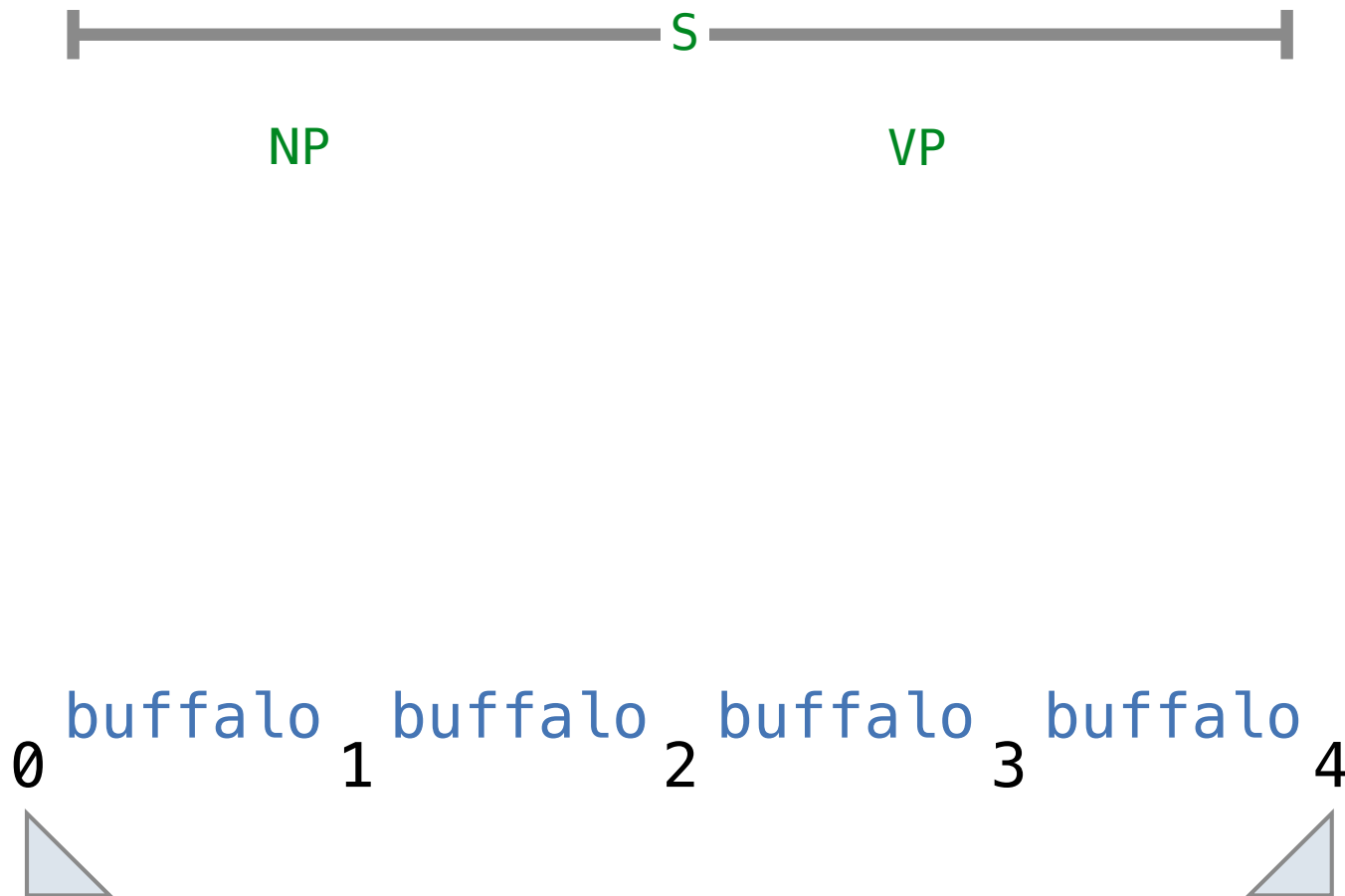
Exhaustive Parsing

Recursively expand, but force words to match input.



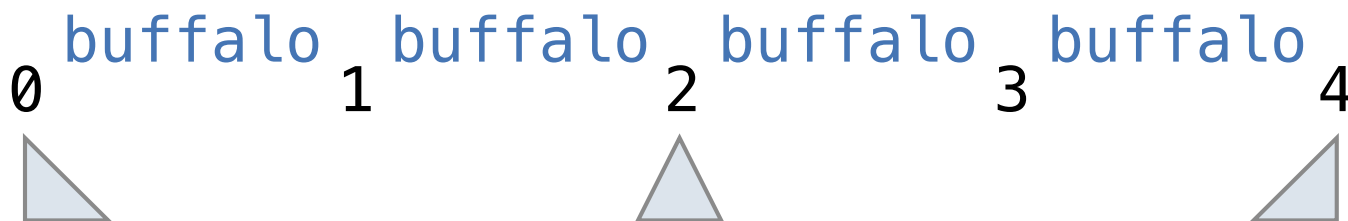
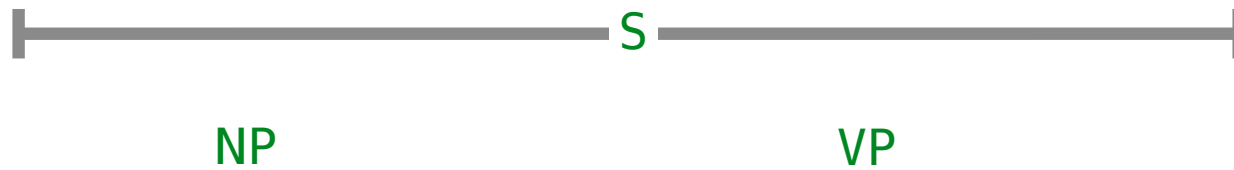
Exhaustive Parsing

Recursively expand, but force words to match input.



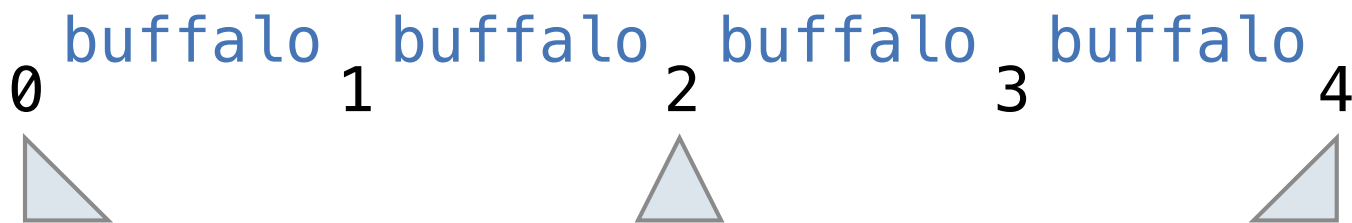
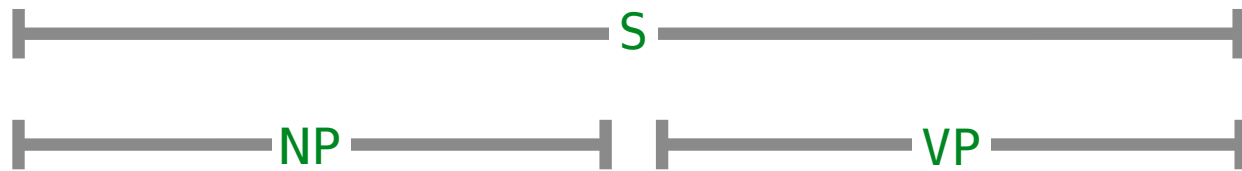
Exhaustive Parsing

Recursively expand, but force words to match input.



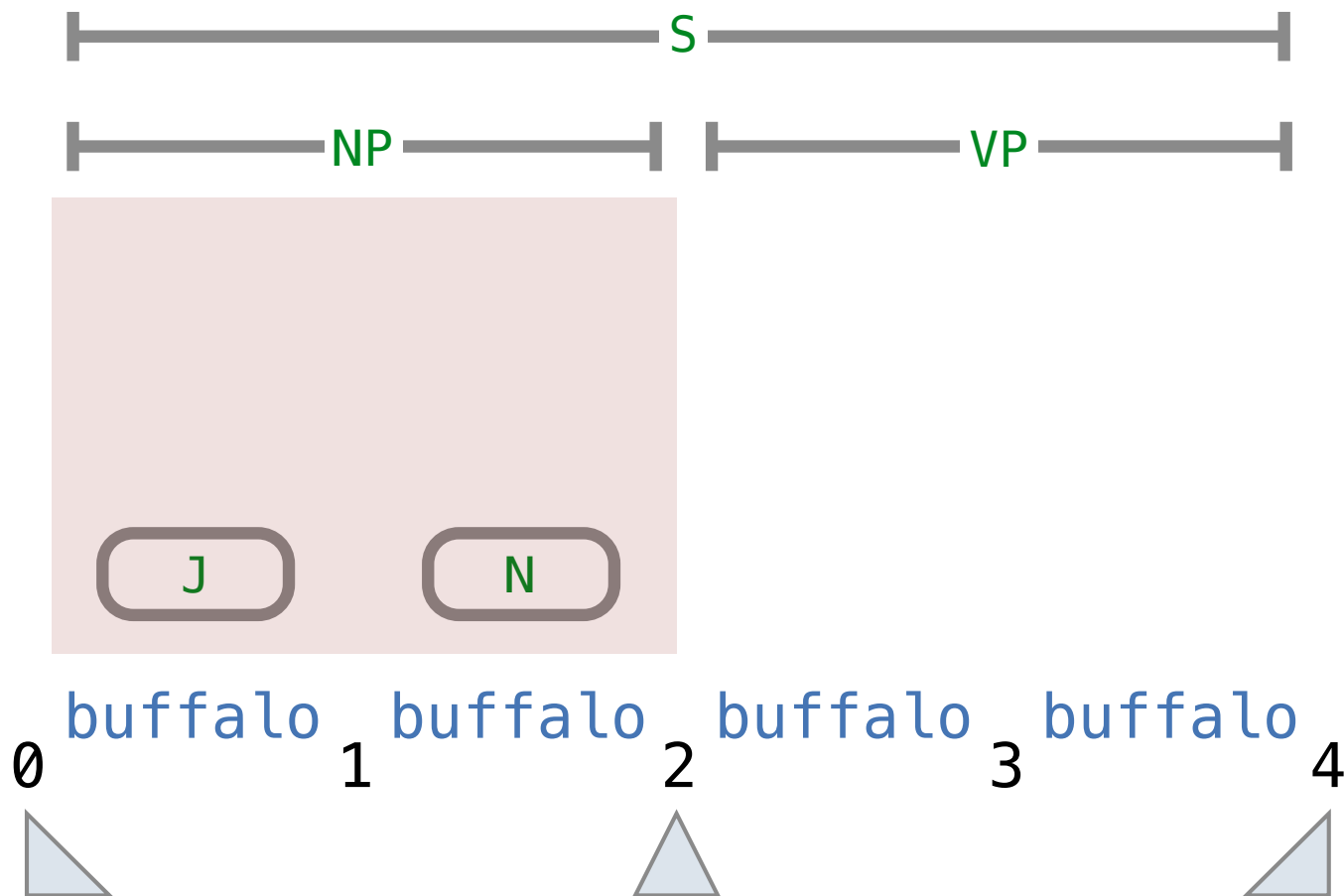
Exhaustive Parsing

Recursively expand, but force words to match input.



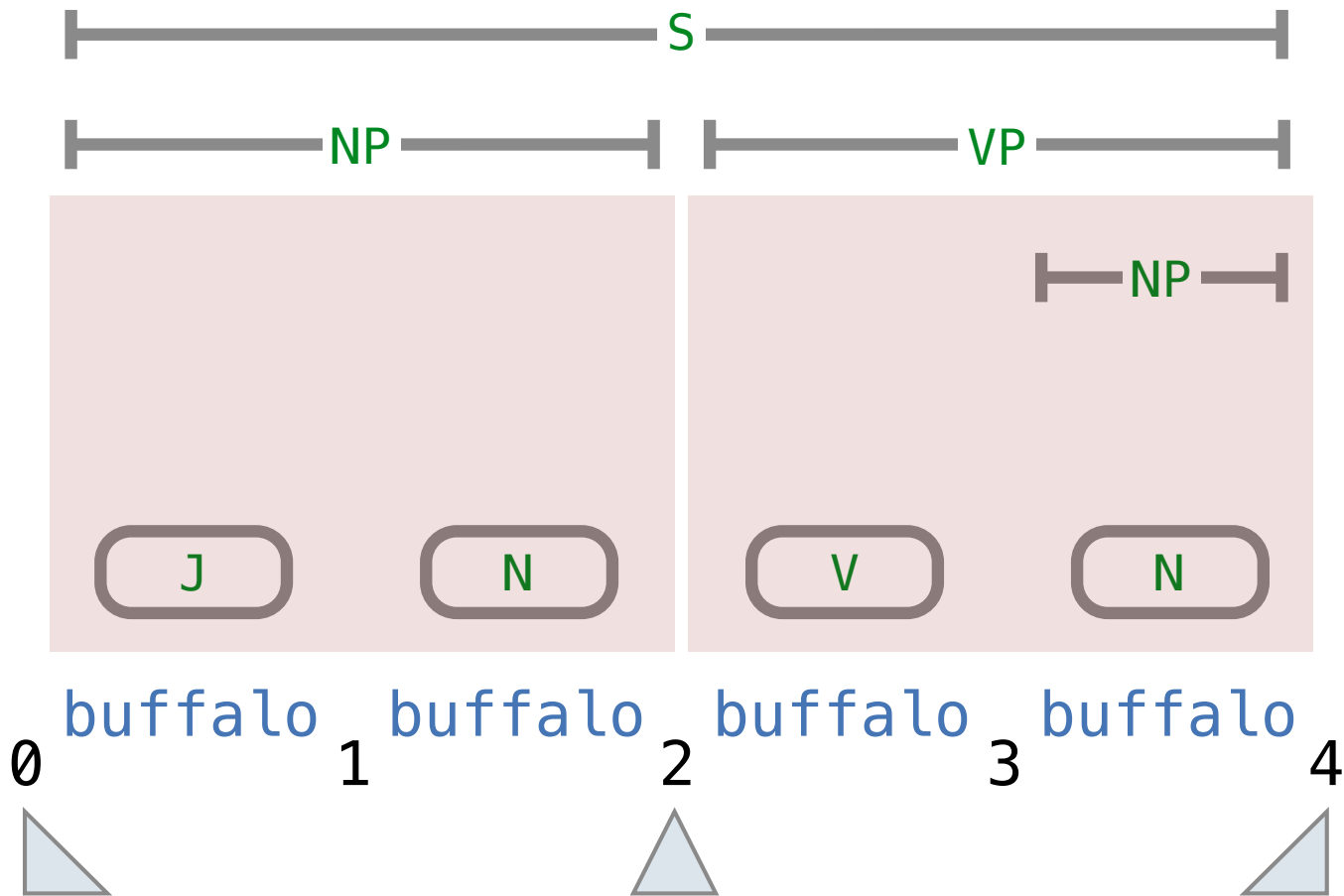
Exhaustive Parsing

Recursively expand, but force words to match input.



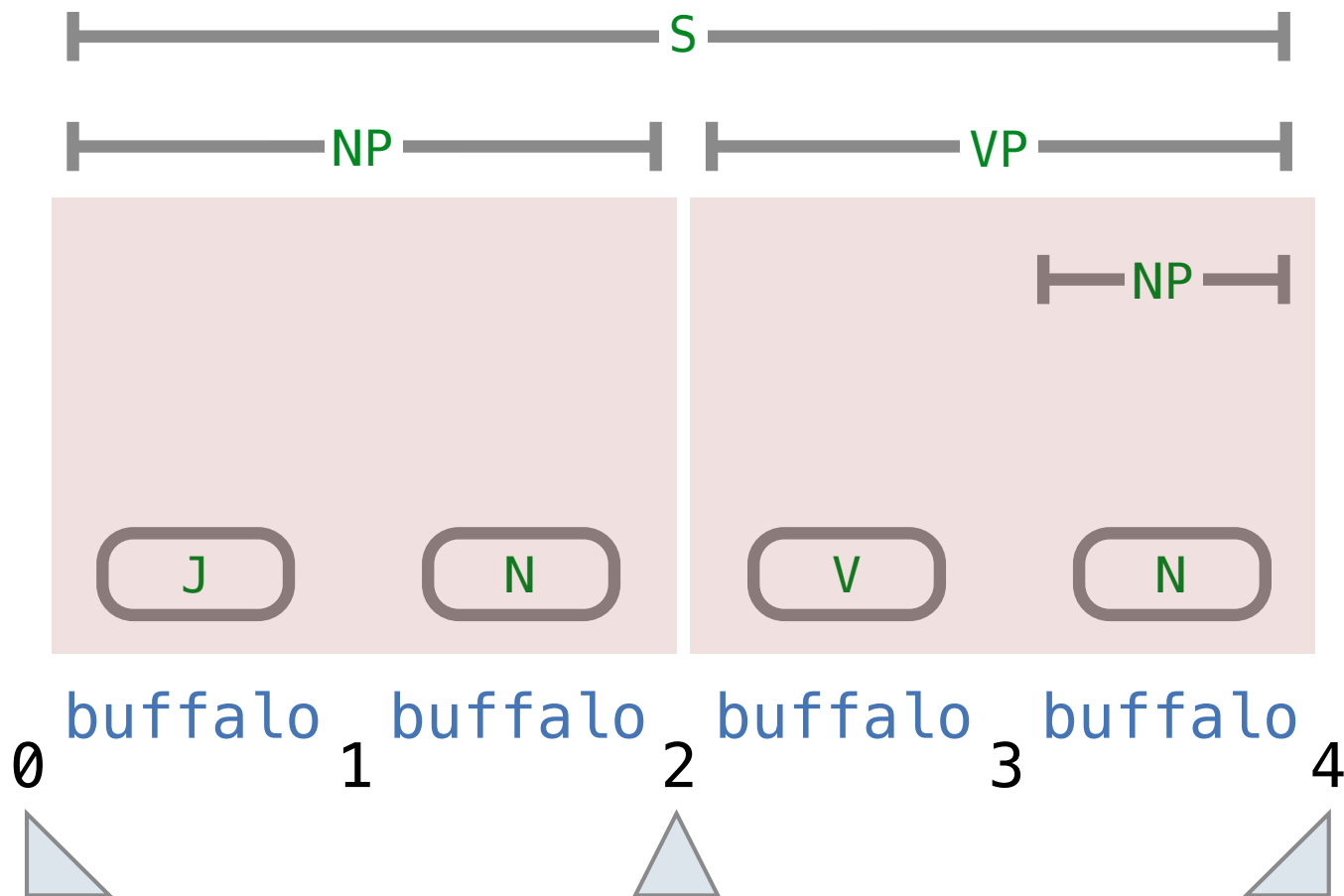
Exhaustive Parsing

Recursively expand, but force words to match input.



Exhaustive Parsing

Recursively expand, but force words to match input.



(Demo)

Learning

(Demo)

Scoring a Tree Using Relative Frequencies

Not all syntactic structures are equally common.

Scoring a Tree Using Relative Frequencies

Not all syntactic structures are equally common.

teacher strikes idle kids

Scoring a Tree Using Relative Frequencies

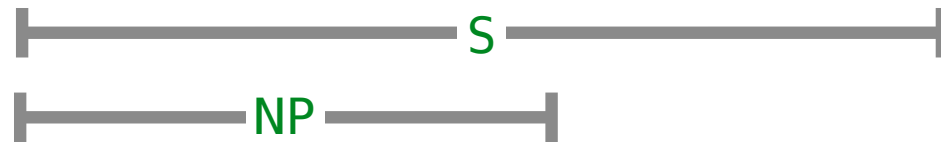
Not all syntactic structures are equally common.



teacher strikes idle kids

Scoring a Tree Using Relative Frequencies

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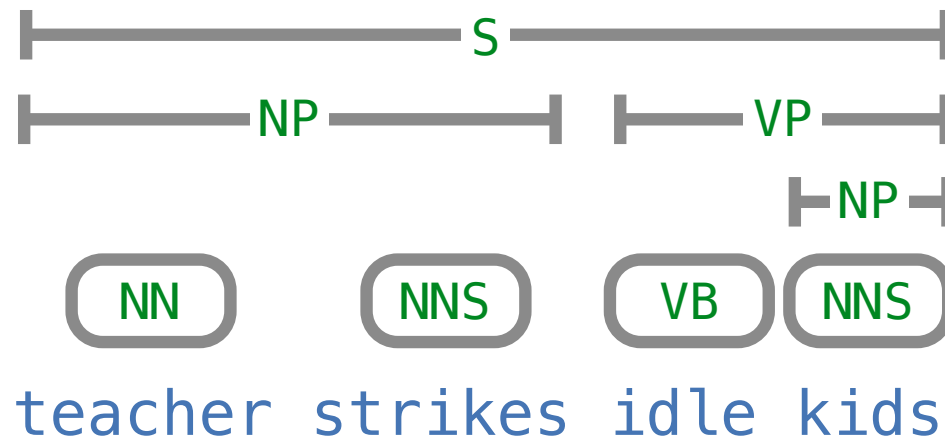
NN

NNS

teacher strikes idle kids

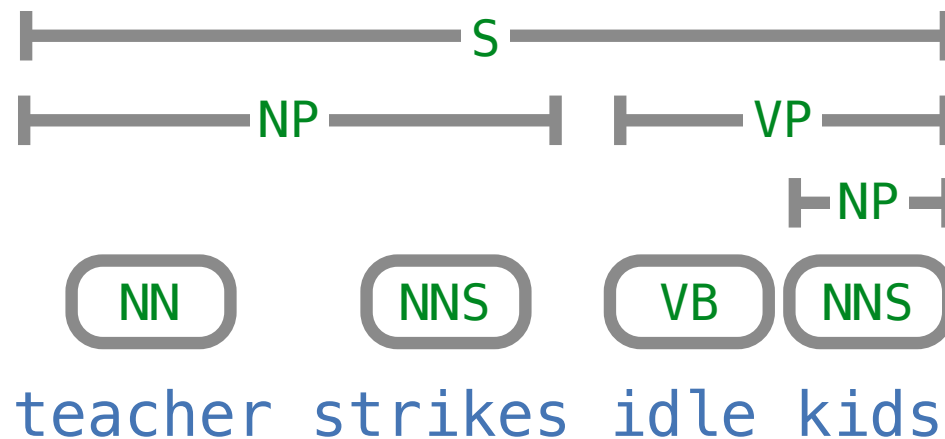
Scoring a Tree Using Relative Frequencies

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Scoring a Tree Using Relative Frequencies

Not all syntactic structures are equally common.



$S \rightarrow NP VP$

$NP \rightarrow NN NNS$

$VP \rightarrow VB NP$

$NP \rightarrow NNS$

$NN \rightarrow \text{teacher}$

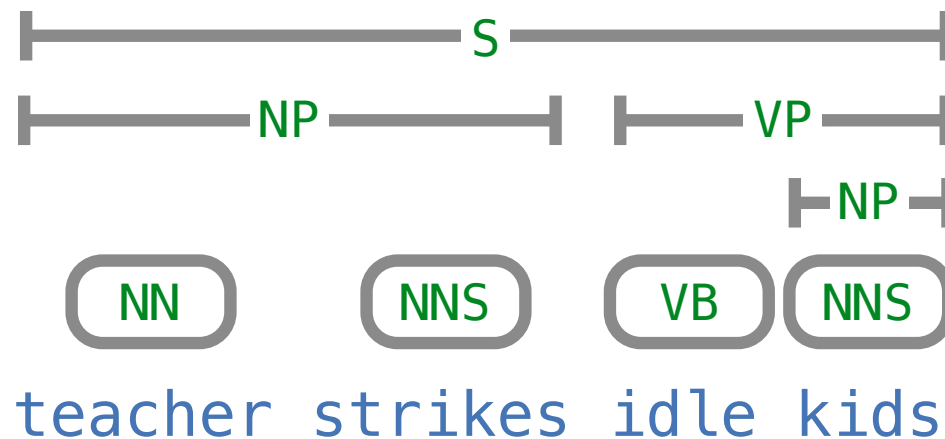
$NNS \rightarrow \text{strikes}$

$VB \rightarrow \text{idle}$

$NNS \rightarrow \text{kids}$

Scoring a Tree Using Relative Frequencies

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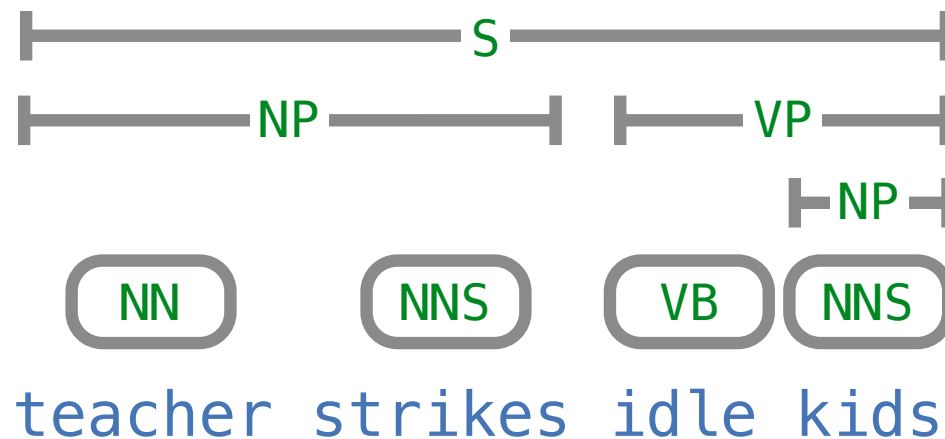


Rule frequency per 100,000 tags

S → NP VP	NN → teacher
NP → NN NNS	NNS → strikes
VP → VB NP	VB → idle
NP → NNS	NNS → kids

Scoring a Tree Using Relative Frequencies

Not all syntactic structures are equally common.

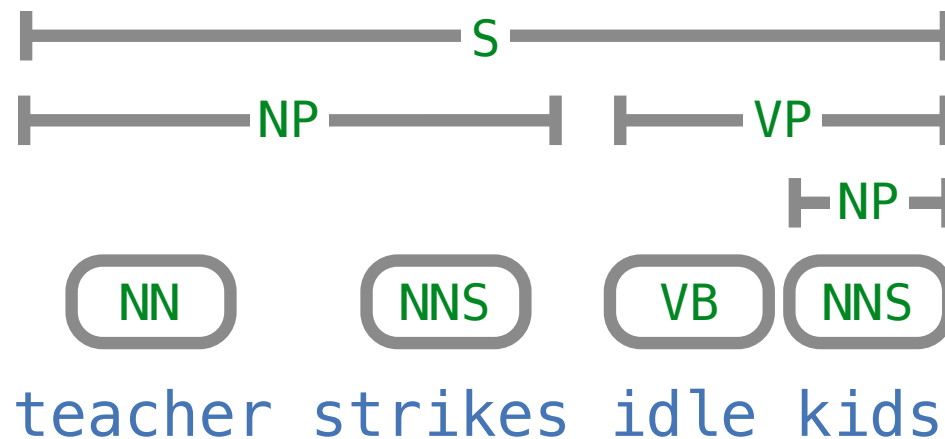


Rule frequency per 100,000 tags

S → NP VP	25372	NN → teacher
NP → NN NNS		NNS → strikes
VP → VB NP		VB → idle
NP → NNS		NNS → kids

Scoring a Tree Using Relative Frequencies

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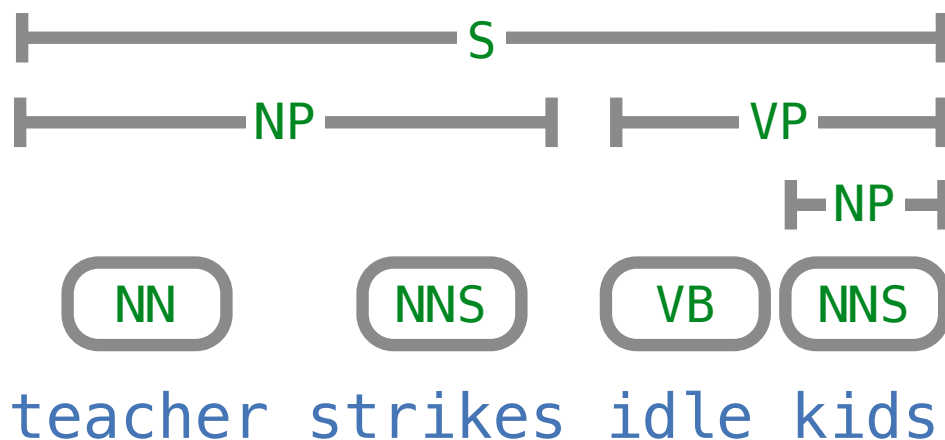


Rule frequency per 100,000 tags

$S \rightarrow NP VP$	25372	$NN \rightarrow$ teacher
$NP \rightarrow NN NNS$	1335	$NNS \rightarrow$ strikes
$VP \rightarrow VB NP$		$VB \rightarrow$ idle
$NP \rightarrow NNS$		$NNS \rightarrow$ kids

Scoring a Tree Using Relative Frequencies

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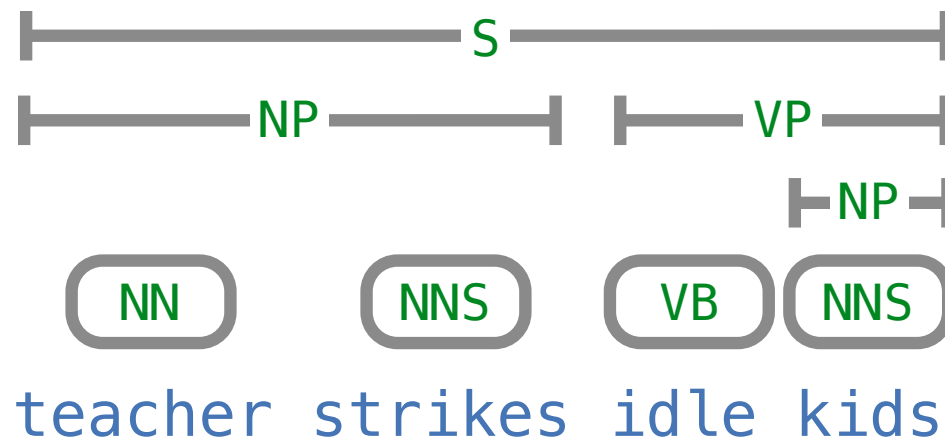


Rule frequency per 100,000 tags

$S \rightarrow NP VP$	25372	$NN \rightarrow$ teacher
$NP \rightarrow NN NNS$	1335	$NNS \rightarrow$ strikes
$VP \rightarrow VB NP$	6679	$VB \rightarrow$ idle
$NP \rightarrow NNS$		$NNS \rightarrow$ kids

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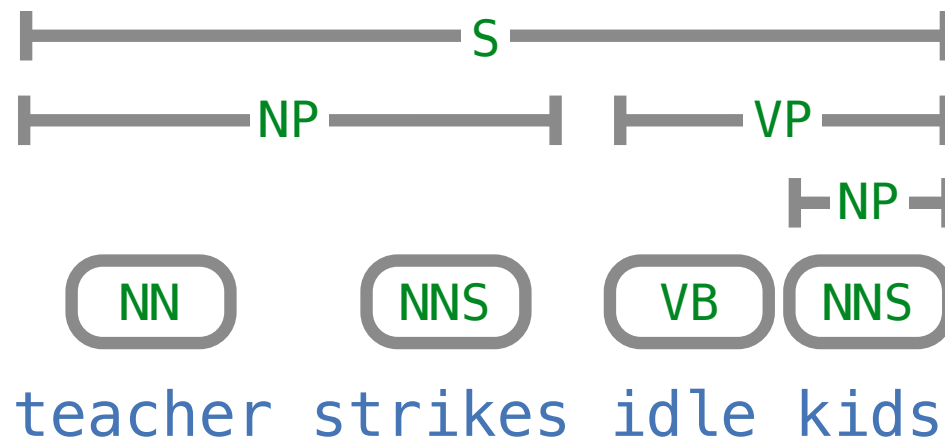


Rule frequency per 100,000 tags

S	→	NP VP	25372	NN	→	teacher
NP	→	NN NNS	1335	NNS	→	strikes
VP	→	VB NP	6679	VB	→	idle
NP	→	NNS	4282	NNS	→	kids

Scoring a Tree Using Relative Frequencies

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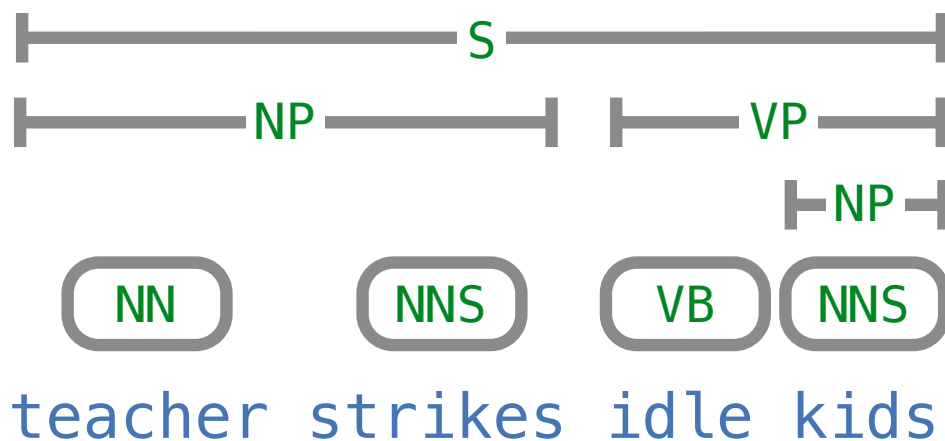


Rule frequency per 100,000 tags

$S \rightarrow NP VP$	25372	$NN \rightarrow teacher$	5
$NP \rightarrow NN NNS$	1335	$NNS \rightarrow strikes$	
$VP \rightarrow VB NP$	6679	$VB \rightarrow idle$	
$NP \rightarrow NNS$	4282	$NNS \rightarrow kids$	

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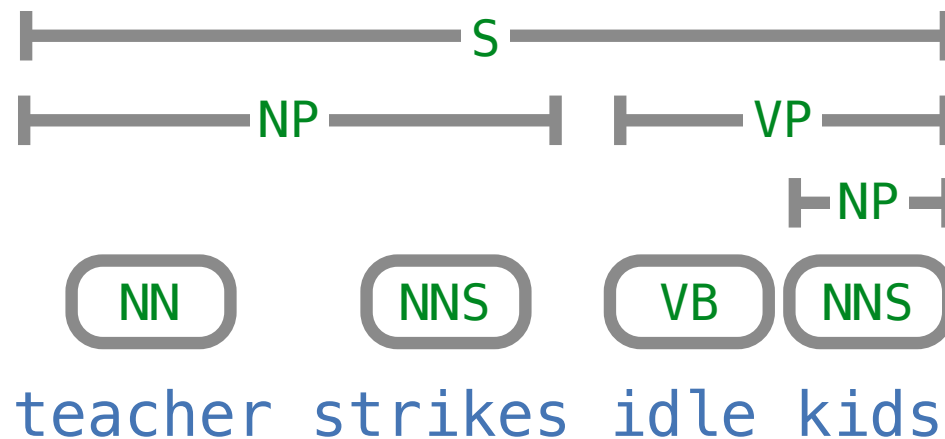


Rule frequency per 100,000 tags

S	→	NP VP	25372	NN	→	teacher	5
NP	→	NN NNS	1335	NNS	→	strikes	25
VP	→	VB NP	6679	VB	→	idle	
NP	→	NNS	4282	NNS	→	kids	

Scoring a Tree Using Relative Frequencies

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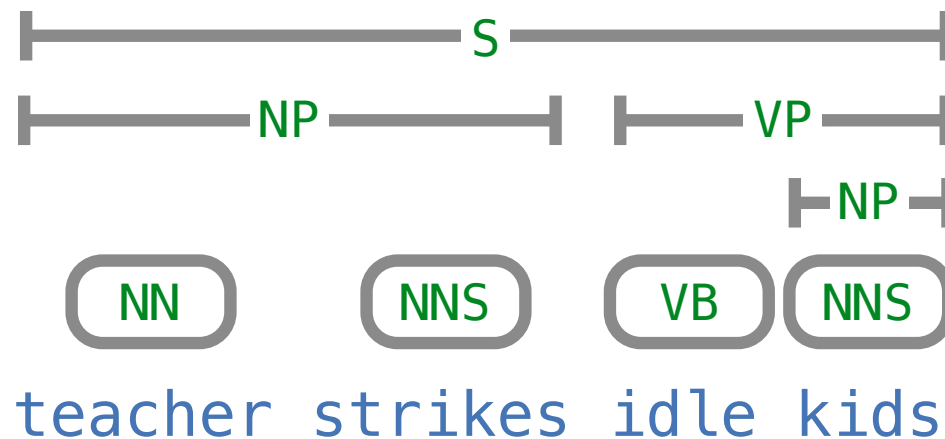


Rule frequency per 100,000 tags

$S \rightarrow NP\ VP$	25372	$NN \rightarrow teacher$	5
$NP \rightarrow NN\ NNS$	1335	$NNS \rightarrow strikes$	25
$VP \rightarrow VB\ NP$	6679	$VB \rightarrow idle$	26
$NP \rightarrow NNS$	4282	$NNS \rightarrow kids$	

Scoring a Tree Using Relative Frequencies

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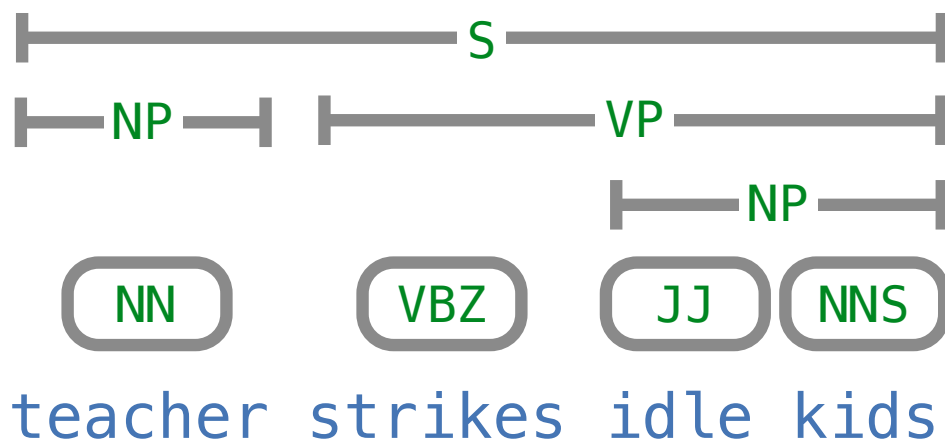


Rule frequency per 100,000 tags

$S \rightarrow NP VP$	25372	$NN \rightarrow teacher$	5
$NP \rightarrow NN NNS$	1335	$NNS \rightarrow strikes$	25
$VP \rightarrow VB NP$	6679	$VB \rightarrow idle$	26
$NP \rightarrow NNS$	4282	$NNS \rightarrow kids$	32

Scoring a Tree Using Relative Frequencies

Not all syntactic structures are equally common.

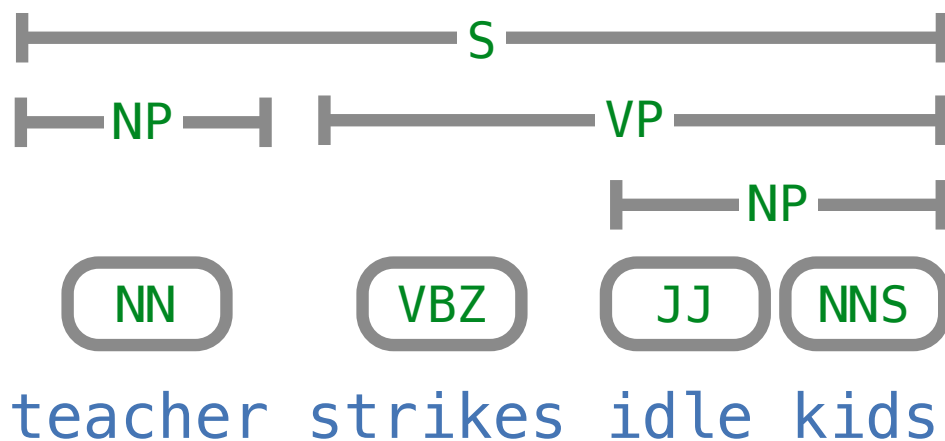


Rule frequency per 100,000 tags

S → NP VP	25372	NN → teacher	5
NP → NN	1335 4358	VBZ → strikes	25 19
VP → VBZ NP	6679 3160	JJ → idle	26 18
NP → JJ NNS	4282 2526	NNS → kids	32

Scoring a Tree Using Relative Frequencies

Not all syntactic structures are equally common.



Rule frequency per 100,000 tags

$S \rightarrow NP\ VP$	25372	$NN \rightarrow teacher$	5
$NP \rightarrow NN$	1335 4358	$VBZ \rightarrow strikes$	25 19
$VP \rightarrow VBZ\ NP$	6679 3160	$JJ \rightarrow idle$	26 18
$NP \rightarrow JJ\ NNS$	4282 2526	$NNS \rightarrow kids$	32

(Demo)