

### Question 1

$$M = 1011, -M = 11110101$$

$$Q = 10010011$$

$$A = 0$$

$$n = 8$$

→ Initialize:

$$M = 00001011, A = 00000000, Q = 10010011$$

→ Shift left:

$$M = 00010110, A = 00000001, Q = 0010011_$$

→  $A = A - M$ :

$$M = 00010110, A = 11110110, Q = 0010011$$

→  $Q(0) = 0$ , restore  $A = A + M$

$$M = 00010110, A = \overset{00}{\cancel{11}}000001, Q = 00100110$$

$$n = 7$$

→ Shift left:

$$M = 000101100, A = 00000010, Q = 0100110_$$

→  $A = A - M$ :

$$M = 000101100, A = 11110111, Q = 0100110_$$

→  $Q(0) = 0$ , restore  $A = A + M$

$$M = 000101100, A = 00000010, Q = 01001100$$

$$n = 6$$

→ Shift left:

$$M = 01011000, A = 00000100, Q = 1001100_$$

→  $A = A - M$

$$M = 01011000, A = 11111001, Q = 1001100_$$

→  $Q(0) = 0$ , restore  $A = A + M$

$$M = 01011000, A = 00000100, Q = 10011000$$

$$u = 5$$

→ Shift left

$$M = 10110000, A = 00001001, Q = 0011000_$$

→  $A = A - M$

$$M = 10110000, A = 11111110, Q = 0011000_$$

→  $Q(0) = 0$ , restore  $A$

$$M = 10110000, A = 00001001, Q = 00110000$$

$$u = 4$$

→ Shift left

$$M = ~~10~~ 01100000, A = 000$$

$$M = 01100000, A = 00010010, Q = 0110000_$$

→  $A = A - M$

$$M = 01100000, A = 00000111, Q = 0110000_$$

→  $Q(0) = 1$

$$M = 01100000, A = 00000111, Q = 01100001$$

$$u = 3$$

→ Shift left

$$M = 11000000, A = 00001110, Q = 1100001_$$

→  $A = A - M$

$$M = 11000000, A = 00000011, Q = 1100001_$$

→  $Q(0) = 1$

$$M = 11000000, A = 00000011, Q = 11000011$$

$$u = 2$$

→ Shift left

$$M = 10000000, A = 00000111, Q = 1000011_$$

→  $A = A - M$

$$M = 10000000, A = 11111100, Q = 1000011_$$

→  $Q(0) = 0$ , restore  $A$

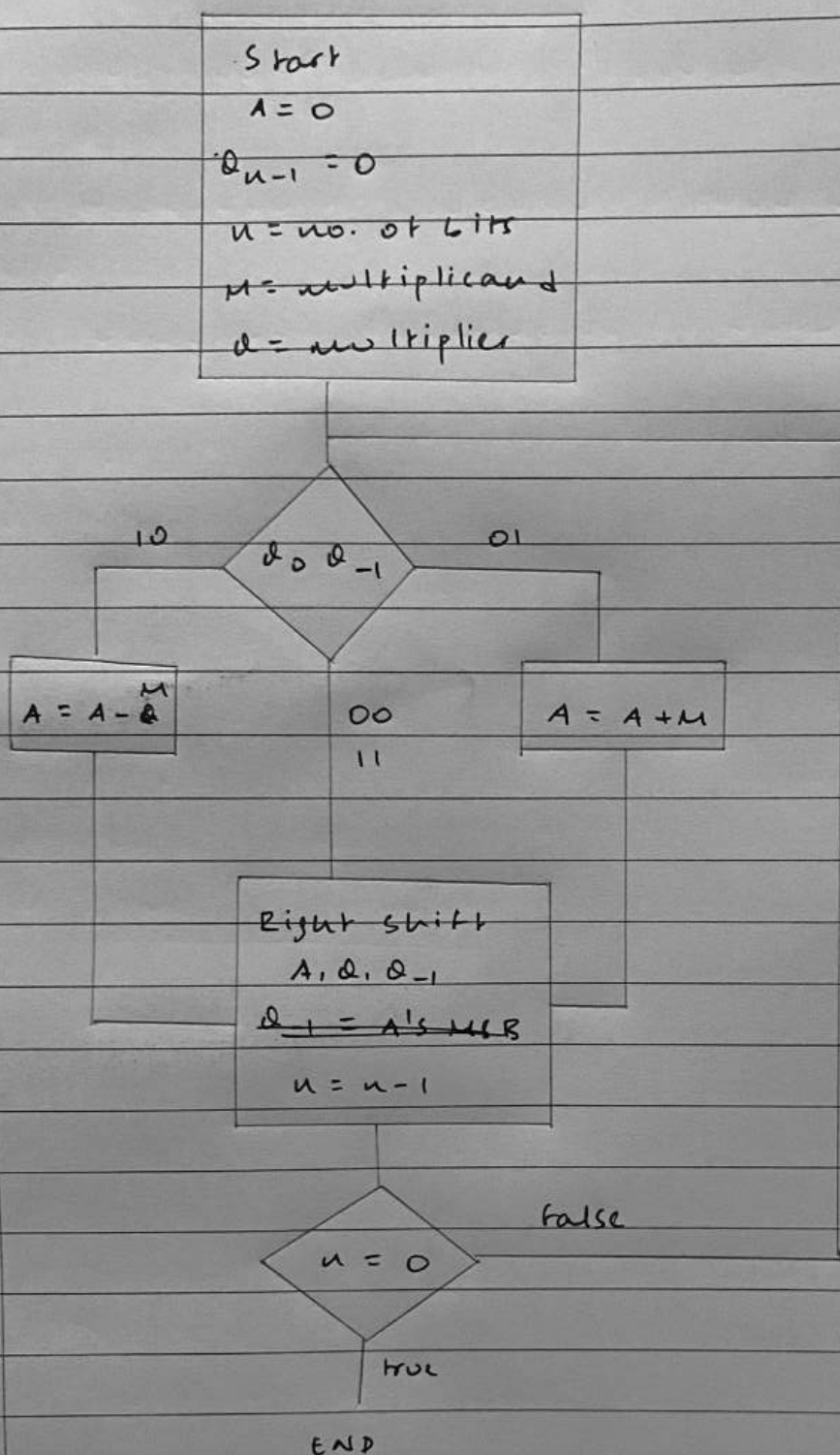
$$M = 10000000, A = 00000111, Q = 10000110$$

→ Shift left

$$\rightarrow A = A - M$$
$$\rightarrow Q(0) = 1$$
$$\mu = 1011 = 11$$
$$\begin{array}{r} 2 = 147 = 13 + 4 \\ \hline 4 \quad \quad 11 \quad \quad 11 \end{array}$$
$$A = 100 = 4 \text{ (remainder)}$$
$$Q = 1101 = 13 \text{ (quotient)}$$



## Question 2



$$M = -9 = 1011, -M = 01001$$

$$Q = -12 = 10100$$

$$Q_{-1} = 0$$

$$n = 5$$

$$\rightarrow Q_0 Q_{-1} = 00, \text{ shift right}$$

$$A = 00000, Q = 01010, Q_{-1} = 0$$

$$u = 4$$

→  $Q_0 Q_{-1} = 00$ , shift right

$$A = 00000, Q = 00101, Q_{-1} = 0$$

$$u = 3$$

→  $Q_0 Q_{-1} = 10$ ,  $A = A - M$

$$A = 01001, Q = 00101, Q_{-1} = 0$$

→ shift right

$$A = 00100, Q = 10010, Q_{-1} = 1$$

$$u = 2$$

→  $Q_0 Q_{-1} = 01$ ,  $A = A + M$

$$A = 11011, Q = 10010, Q_{-1} = 1$$

→ shift right

$$A = 11101, Q = 11001, Q_{-1} = 0$$

$$u = 1$$

→  $Q_0 Q_{-1} = 10$ ,  $A = A - M$

$$A = 00110, Q = 11001, Q_{-1} = 0$$

→ shift right

$$A = 00011, Q = 01100, Q_{-1} = 1$$

$AQ = \text{mult result}$

$$M \times Q = -9 \times -12 = 108 = 0101100$$

$$AQ = 0001101100$$

$$= 01101100$$

$$= 108$$

### Question 3

3-address machine	Fetch	Exec.	Memory Traffic
SUB A, B, C	4	3	7
MPY A, A, D	4	3	7
	8	6	14

2-address machine	Fetch	Exec.	Memory Traffic
MOV T1, B	3	2	5
SUB T1, C	3	3	6
MPY T1, D	3	3	6
MOV A, T1	3	2	5
	12	10	22

1-address machine	Fetch	Exec.	Memory Traffic
LOAD B	2	1	3
SUB C	2	1	3
MPY D	2	1	3
STORE A	2	1	3
	8	4	12

0-address machine	Fetch	Exec.	Memory Traffic
PUSH B	1	0	1
PUSH C	1	0	1
SUB	0	0	0
PUSH D	1	0	1
MPY	0	0	0
POP A	1	0	1
	4	0	4



### Question 4

4, 2, 0, 1, 2, 6, 1, 4, 0, 1, 0, 2, 3, 5, 7

i. FIFO

Access	Cache	
4	4	Miss
2	4, 2	Miss
0	4, 2, 0	Miss
1	4, 2, 0, 1	Miss
2	4, 2, 0, 1	Hit
6	4, 2, 0, 1, 6	Miss
1	2, 0, 1, 6	Hit
4	0, 1, 6, 4	Miss
0	0, 1, 6, 4	Hit
1	0, 1, 6, 4	Hit
0	0, 1, 6, 4	Hit
2	1, 6, 4, 2	Miss
3	6, 4, 2, 3	Miss
5	4, 2, 3, 5	Miss
7	2, 3, 5, 7	Miss

ii. Optimal / LFU

Access	Cache	
4	4	Miss
2	4, 2	Miss
0	4, 2, 0	Miss
1	4, 2, 0, 1	Miss
2	4, 0, 1, 2	Hit
6	0, 1, 2, 6	Miss

Access	Cache	
1	0, 6, 1, 2	Hit
4	6, 4, 1, 2	Miss
0	4, 0, 1, 2	Miss
1	4, 0, 2, 1	Hit
0	4, 0, 2, 1	Hit
2	4, 0, 2, 1	Hit
3	3, 0, 2, 1	Miss
5	5, 0, 2, 1	Miss
7	7, 0, 2, 1	Miss

iii. LRU

Access	Cache	
4	4	Miss
2	4, 2	Miss
0	4, 2, 0	Miss
1	4, 2, 0, 1	Miss
2	4, 0, 1, 2	Hit
6	0, 1, 2, 6	Miss
1	0, 2, 6, 1	Hit
4	2, 6, 1, 4	Miss
0	6, 1, 4, 0	Miss
1	6, 4, 0, 1	Hit
0	6, 4, 1, 0	Hit
2	4, 1, 0, 2	Miss
3	1, 0, 2, 3	Miss
5	0, 2, 3, 5	Miss
7	2, 3, 5, 7	Miss



Question 45

$$T_c = 100 \text{ ns}$$

$$T_m = 1000 \text{ ns}$$

90% read, 10% write

Hit ratio for read = 0.9 =  $h$

write through

$$T_A = h T_c + (1-h)(T_m + T_c)$$

$$\begin{aligned} \Rightarrow T_A &= 0.9 \times 100 + 0.1 \times (1000 + 100) \\ &= 90 + 110 \\ &= \underline{200 \text{ ns for reads}} \end{aligned}$$

$$\begin{aligned} \text{Total access time} &= \frac{80}{100} \times 200 + \frac{20}{100} \times 1000 \\ &= 160 + 200 \\ &= \underline{360 \text{ ns for read + write}} \end{aligned}$$

$$\begin{aligned} \text{Hit ratio including writes} &= 0.8 \times 0.9 \\ &= \underline{0.72} \end{aligned}$$

Question 6

$$\begin{aligned}\text{Address space} &= 24 \text{ bits} \\ &= 3 \text{ bytes}\end{aligned}$$

$$\begin{aligned}\text{Memory space} &= 16 \text{ bits} \\ &= 2 \text{ bytes}\end{aligned}$$

$$\begin{aligned}\text{No. of words} &= \frac{2^n}{\text{Size of word}}\end{aligned}$$

$n = 16$ , because memory is what decides how many words are addressable

$$\begin{aligned}\text{No. of words} &= \frac{2^{16}}{16} \\ &= \underline{4096 \text{ words}}\end{aligned}$$

$$\begin{aligned}\text{No. of pages} &= \frac{2^{24}}{2k} = \frac{2^{24}}{2^{11}} = 2^{13} \\ &= \underline{8k}\end{aligned}$$

$$\begin{aligned}\text{No. of blocks} &= \frac{2^{16}}{2k} = \frac{2^{16}}{2^{11}} = 2^5 \\ &= \underline{32}\end{aligned}$$