

# Extendible Hashing

# Terminology

## Words we'll be using

- Depth
  - Number of bits measured in a directory (global) or bucket (local)
  - Example:
    - 4 base 10 = 100 base 2
    - . = 101
    - . = 110
    - 7 base 10 = 111

Classifying with depth of 1, we read 1 bit from the right  
Same as doing  $k \% (2^n)$  for an 'n' depth structure

Classifying  
with Depth 1

4	6
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Right bit 0

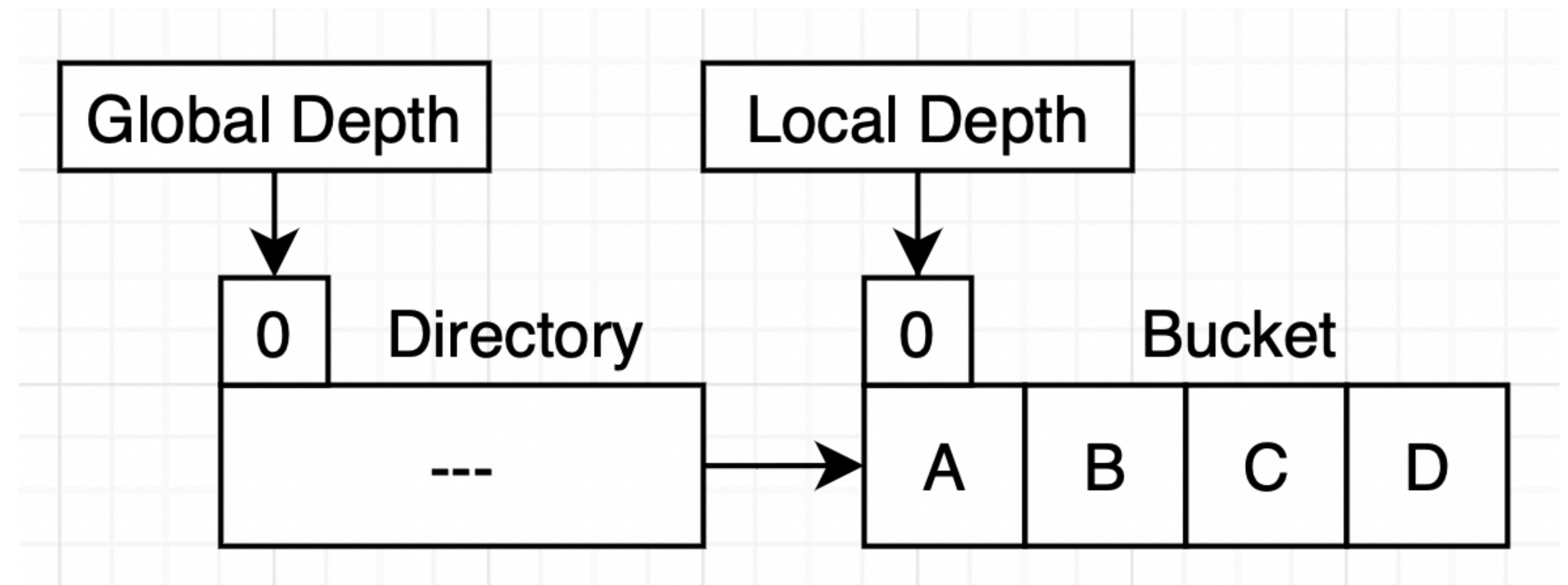
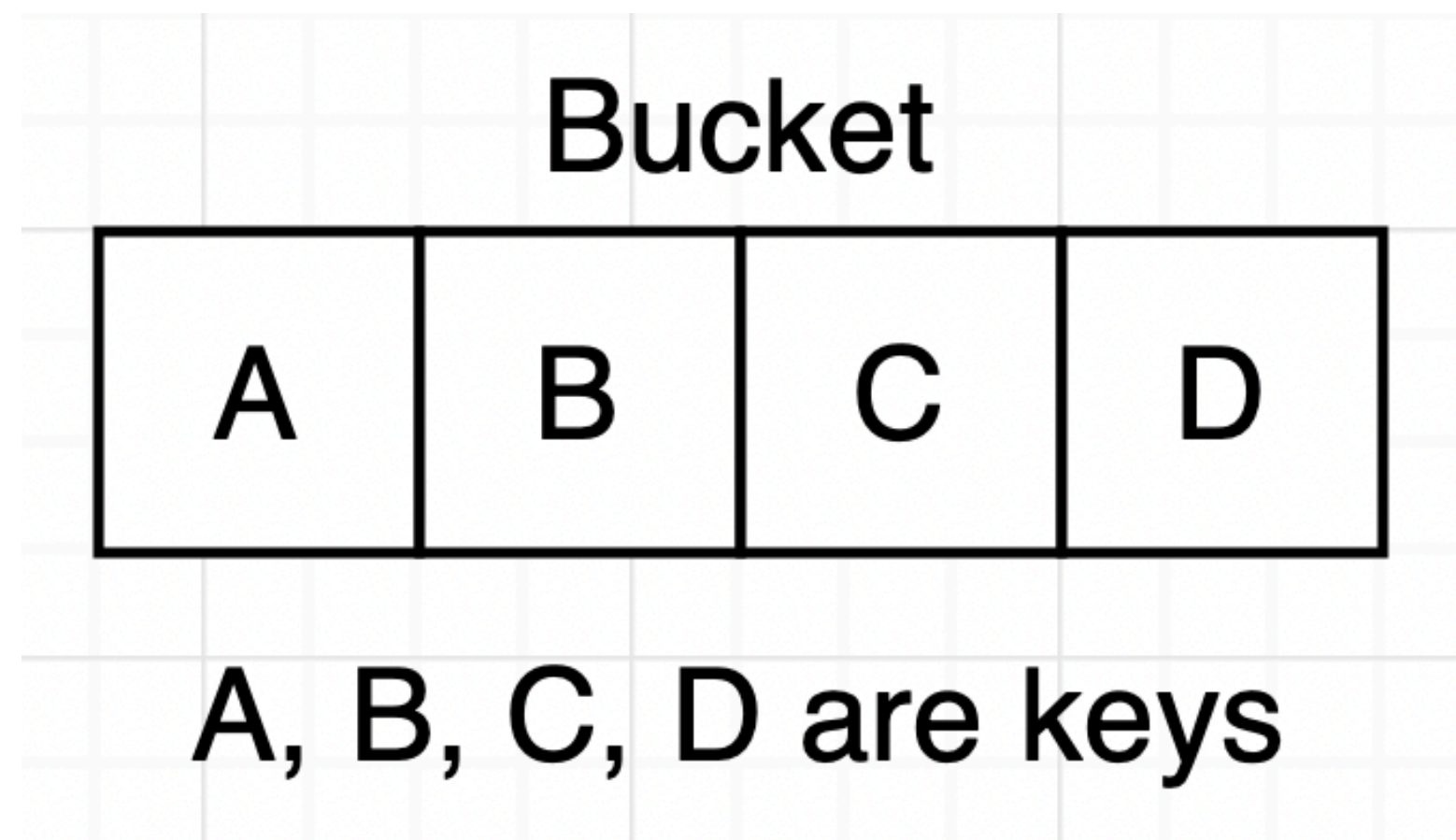
5	7
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Right bit 1

# Terminology

## Words we'll be using

- Bucket
  - Has it's own local depth
  - Stores keys in groups of 4
- Directory
  - Stores pointers to contact buckets
  - $2^{\text{global depth}}$  is the number of entries



# Terminology

## Words we'll be using

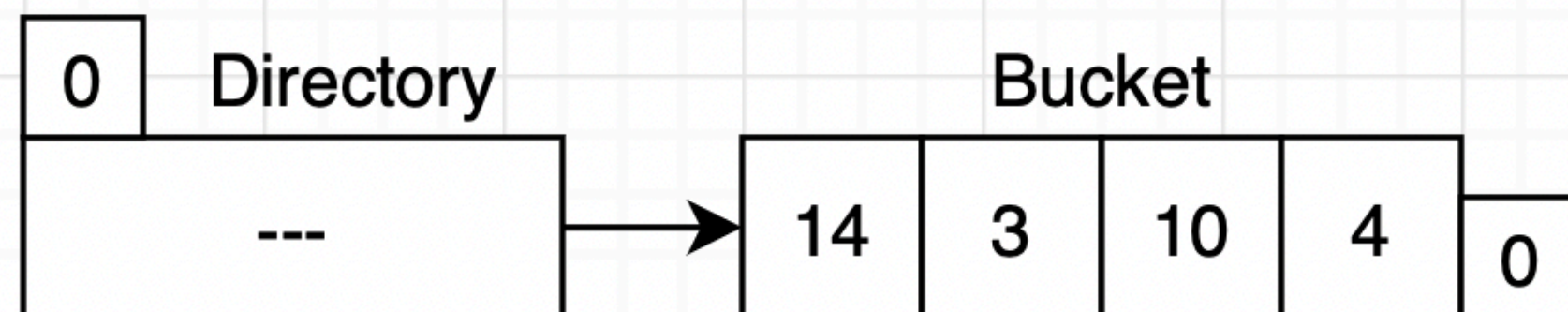
- **Bucket Splitting**
  - When a bucket overflows, we create a new bucket
  - Called bucket splitting because elements in bucket can be split apart
  - Bucket splitting increases the local depth by 1
- **Directory Expansion**
  - When all bucket of a certain directory are filled and no new buckets can be made, the global depth increase by 1 and twice the amount of directories are now available
  - The exact condition is when:  
$$\text{Local Depth (Bucket)} > \text{Global Depth (Directory's)}$$



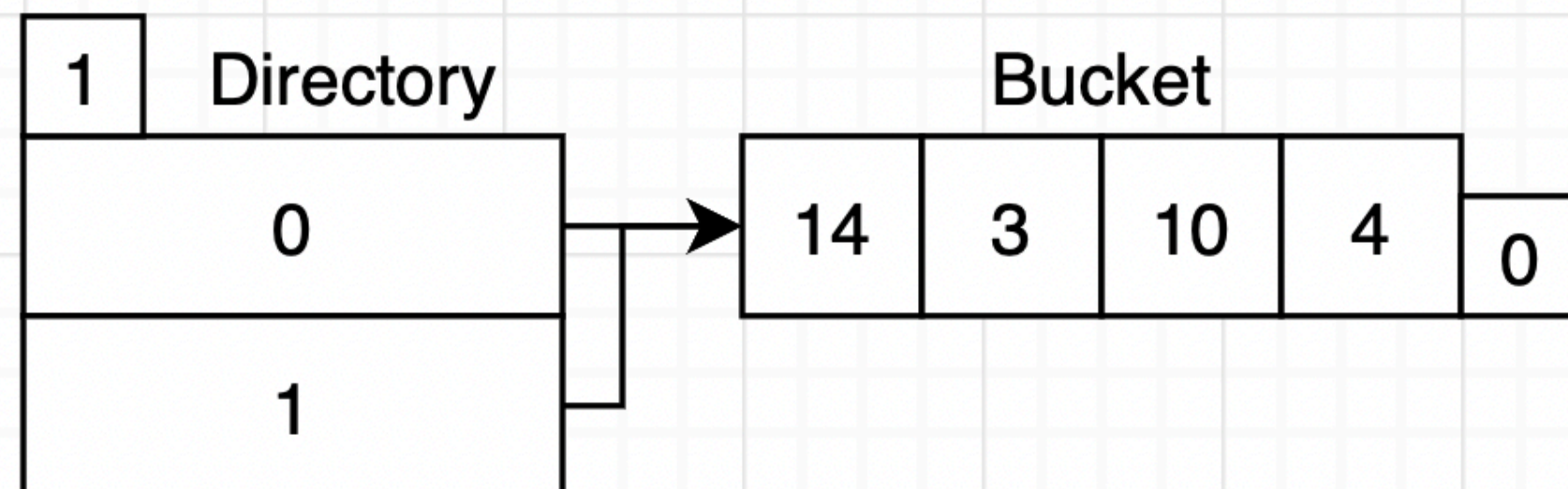
# Example

- Let our keys be 14, 3, 10, 4, 5, 11, 17, 12, 7, 2

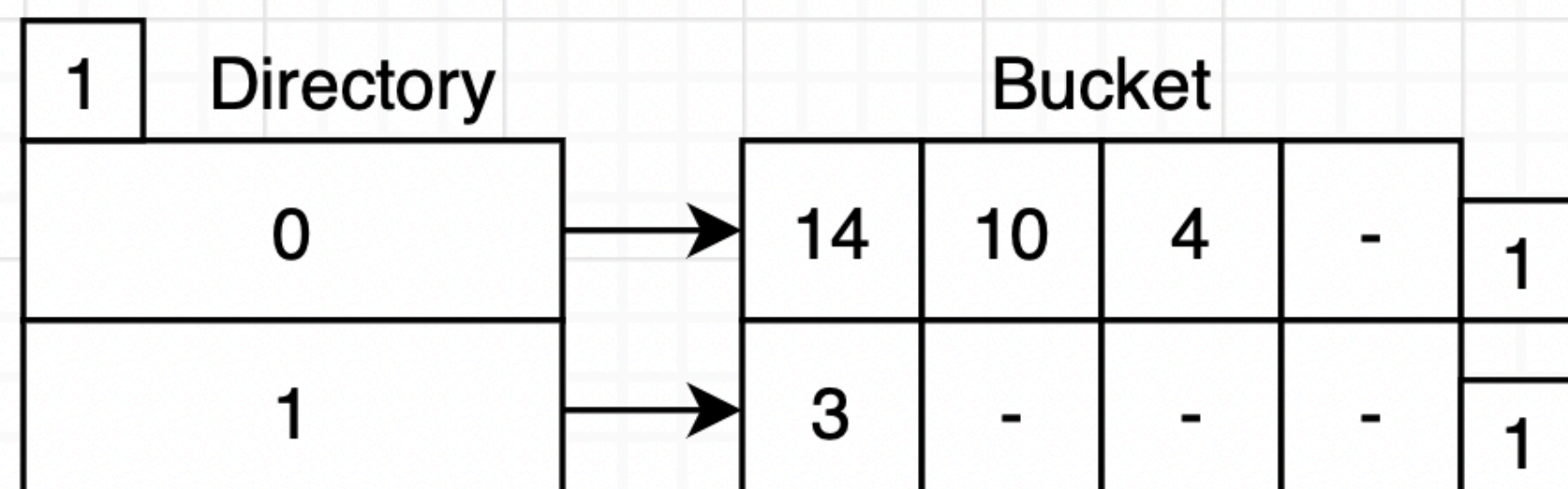
Inserting first 4 elements



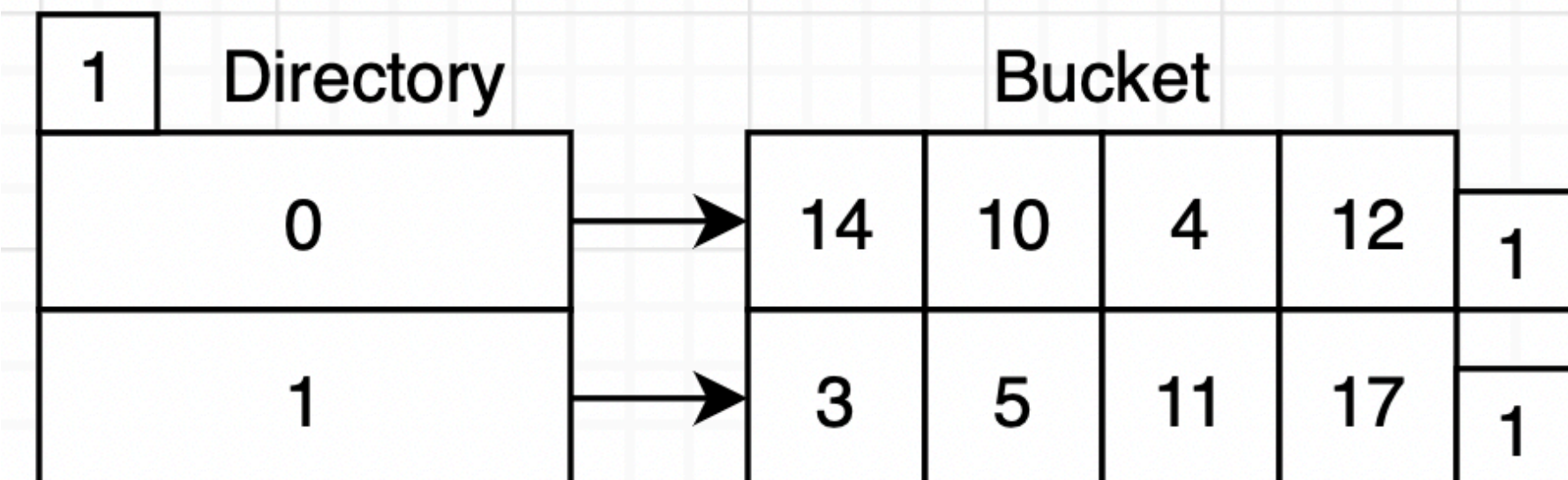
Bucket split cannot happen, so directory expansion does



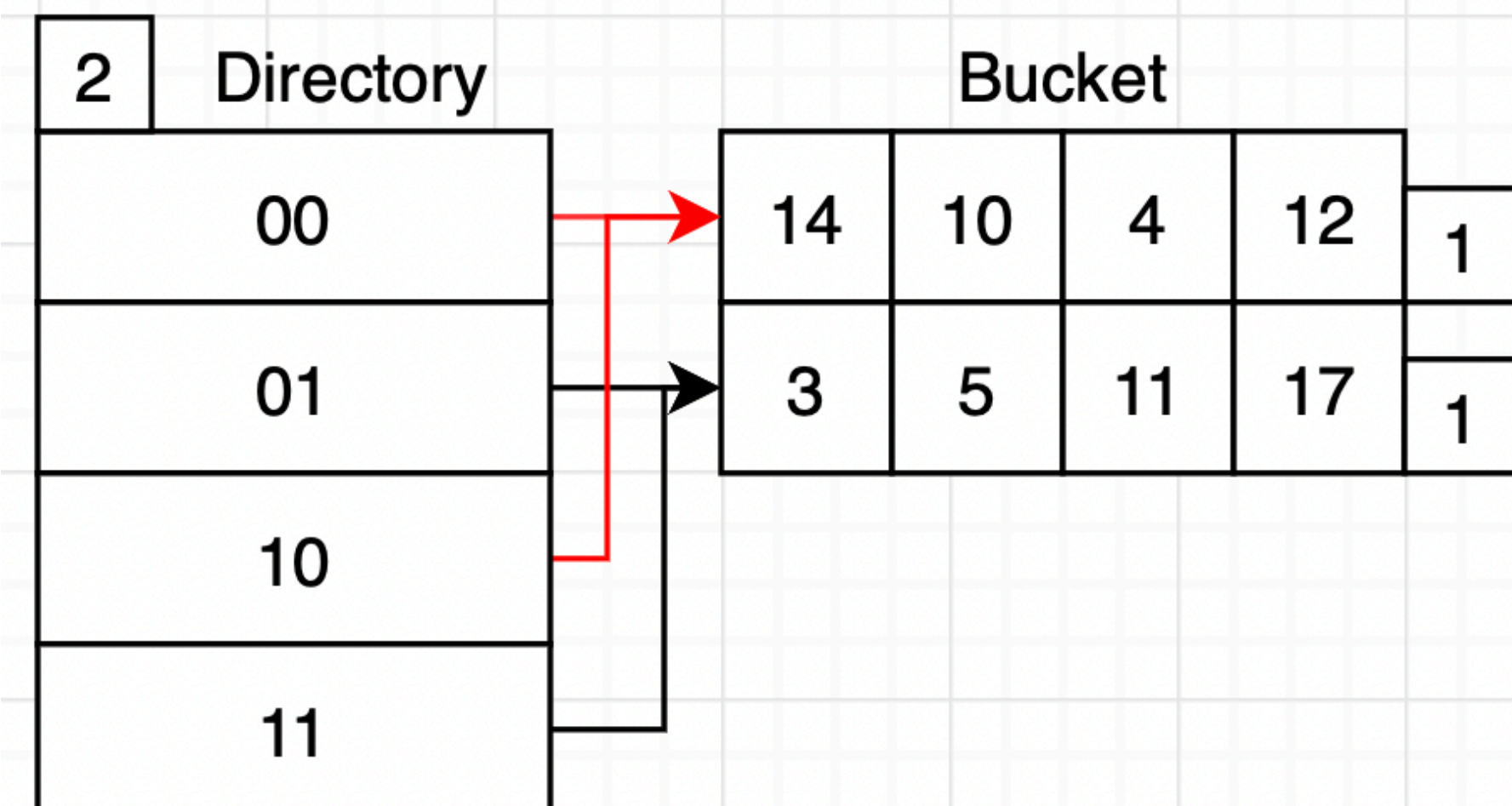
Now bucket split can happen



Next 4 elements are inserted



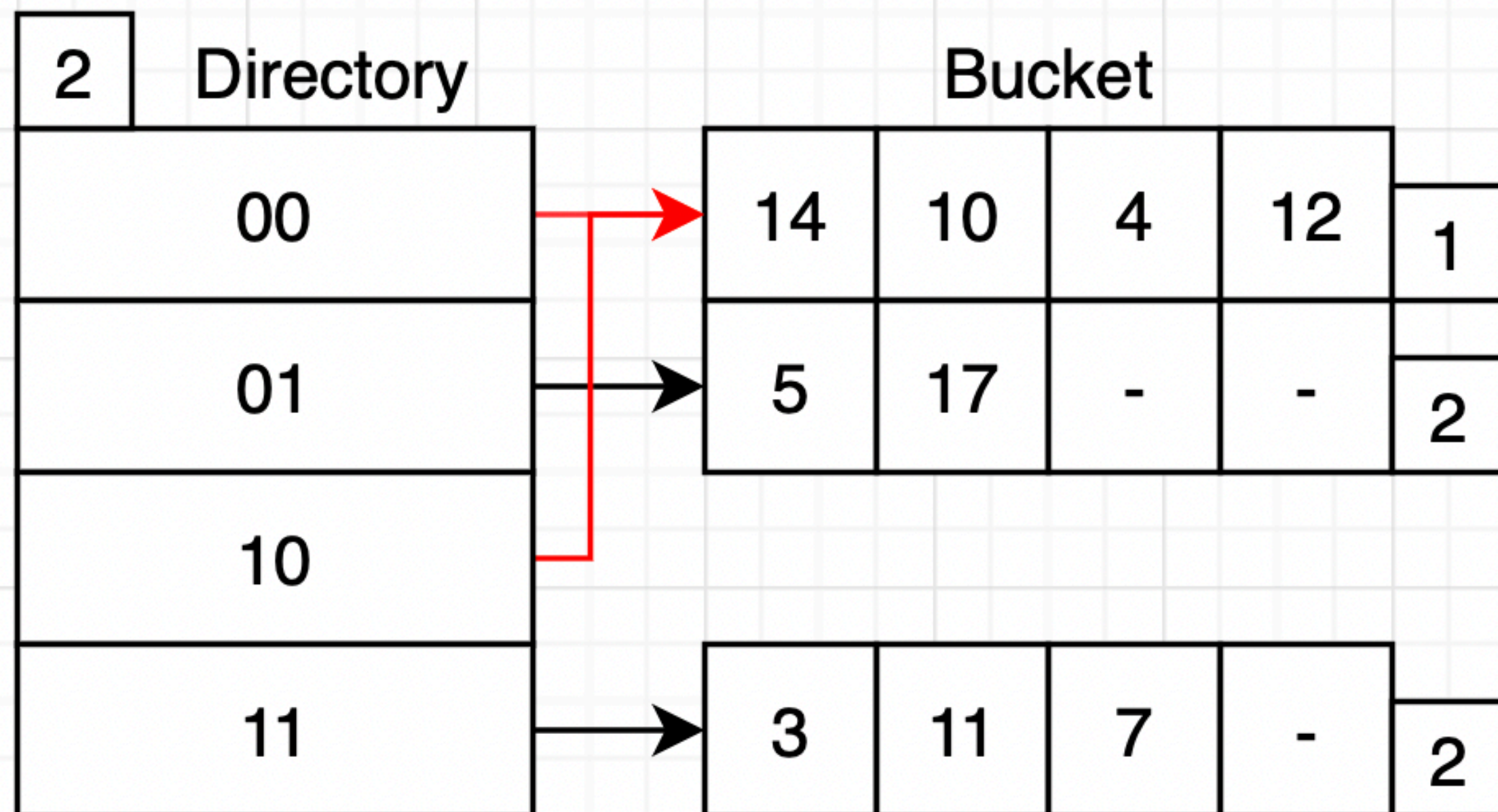
Directory expansion happens





# Example • 14, 3, 10, 4, 5, 11, 17, 12, 7, 2

Now bucket splitting can happen (Inserting 7)



Bucket splitting (Inserting 2)

