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Question 1

a. Keys are:  $AB C D E F$ ,  $AB C D E$ ,  $AB D E F$ ,  $AB C D F$ ,  $AB C D$ ,  
 $AB D E$ ,  $AB D$ ,  $B C D$

candidate keys:  $AB D$ ,  $B C D$

b. using  $AB D$  as candidate key

BCNF needs all  $X$  in  $X \rightarrow Y$  for  $X$  to be a super key

$AB \rightarrow C$

$DC \rightarrow AE$

$E \rightarrow F$

↑

all do not satisfy

BCNF is also not satisfied.

$\therefore DC \rightarrow AE$  and  $C$  is not a prime ~~key~~ attribute

$\therefore$  This relation is only at 2NF

c.  $(A, B, C, D)$ ,  $(B, C, D, E, F)$

$AB \rightarrow C$  is preserved in the first

$DC \rightarrow AE$  is not preserved in either

$\therefore$  The decomposition is not dependency preserving

## Question 2

$SSN \rightarrow ENAME, BDATE, ADDRESS, DNUMBER$

$DNUMBER \rightarrow DNAME, DMGRSSN$

a.  $SSN^+ = \{ENAME, BDATE, ADDRESS, DNUMBER, DNAME, DMGRSSN, SSN\}$

$DNAME^+ = \{DNAME\}$

b. No dependency can be removed

$\therefore$  The set of relations  $\Gamma$  is minimal

Any removal causes loss of data

c. Update anomaly:

If  $DNUMBER$  changes in the Department relation, then the  $SSN \rightarrow DNUMBER$  may not be updated properly

Insertion anomaly:

If an employee is added without  $DNUMBER$  existence

Deletion anomaly:

If an employee's department is deleted, then  $DNUMBER$  does not exist anymore

### Question 3

$$AB \rightarrow C$$

$$C \rightarrow D$$

$$D \rightarrow A$$

a. Non-trivial FD's :

$$AB \rightarrow C, C \rightarrow D, D \rightarrow A$$

$$\therefore AB \rightarrow D, AB \rightarrow A, C \rightarrow A$$

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b. candidate keys:

$$\underline{AB, CB, DB}$$

c. BCNF violations:

$$C \rightarrow D, D \rightarrow A$$

$AB \rightarrow C$  is valid

d. Decomposition:

$$R_1(A, B, C), R_2(C, D), R_3(D, A)$$

#### Question 4

$$A \rightarrow C$$

$$AB \rightarrow C$$

$$C \rightarrow DI$$

$$CD \rightarrow I$$

$$EC \rightarrow AB$$

$$EI \rightarrow C$$

$C \rightarrow DI$ ,  $\therefore CD \rightarrow I$  is redundant

$A \rightarrow C$ ,  $\therefore AB \rightarrow C$  is redundant

$$A \rightarrow C$$

$$C \rightarrow DI$$

$$EC \rightarrow AB$$

$$EI \rightarrow C$$

$A \rightarrow C$ ,  $\therefore C \rightarrow DI$  is redundant

$$A \rightarrow DI$$

$$EC \rightarrow AB$$

$$EI \rightarrow C$$



### Question 5

- i. The relation is not in 1NF due to the last row of the data. The relation itself is in 1NF.
- ii. The relation is ~~not~~ in 2NF as the candidate key is student-ID and no partial dependencies exist.
- iii. The relation is not in 3NF as there exists a transitive relation:

Student-ID  $\rightarrow$  Hostel-Block

Hostel-Block  $\rightarrow$  fees

converting to 3NF:

$R_1(\text{Student-ID}, \text{Hostel-Block}), R_2(\text{Hostel-Block}, \text{fees})$

### Question 6

The combination of SPJ is a candidate key

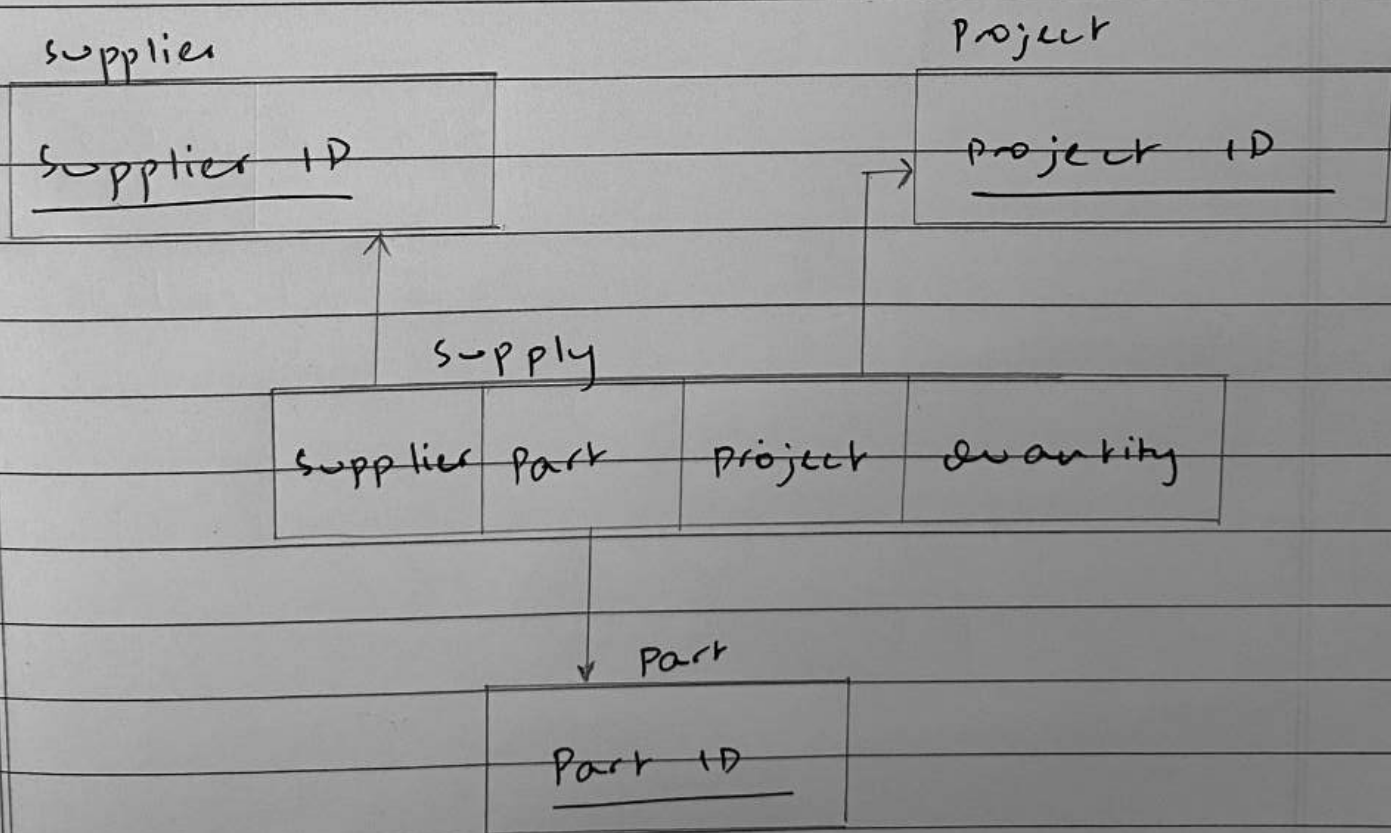
- i. Insertion anomaly: The same SPJ combination can be inserted, which destroys the uniqueness.

Deletion anomaly: If a P or J is deleted, the reference number is now lost.

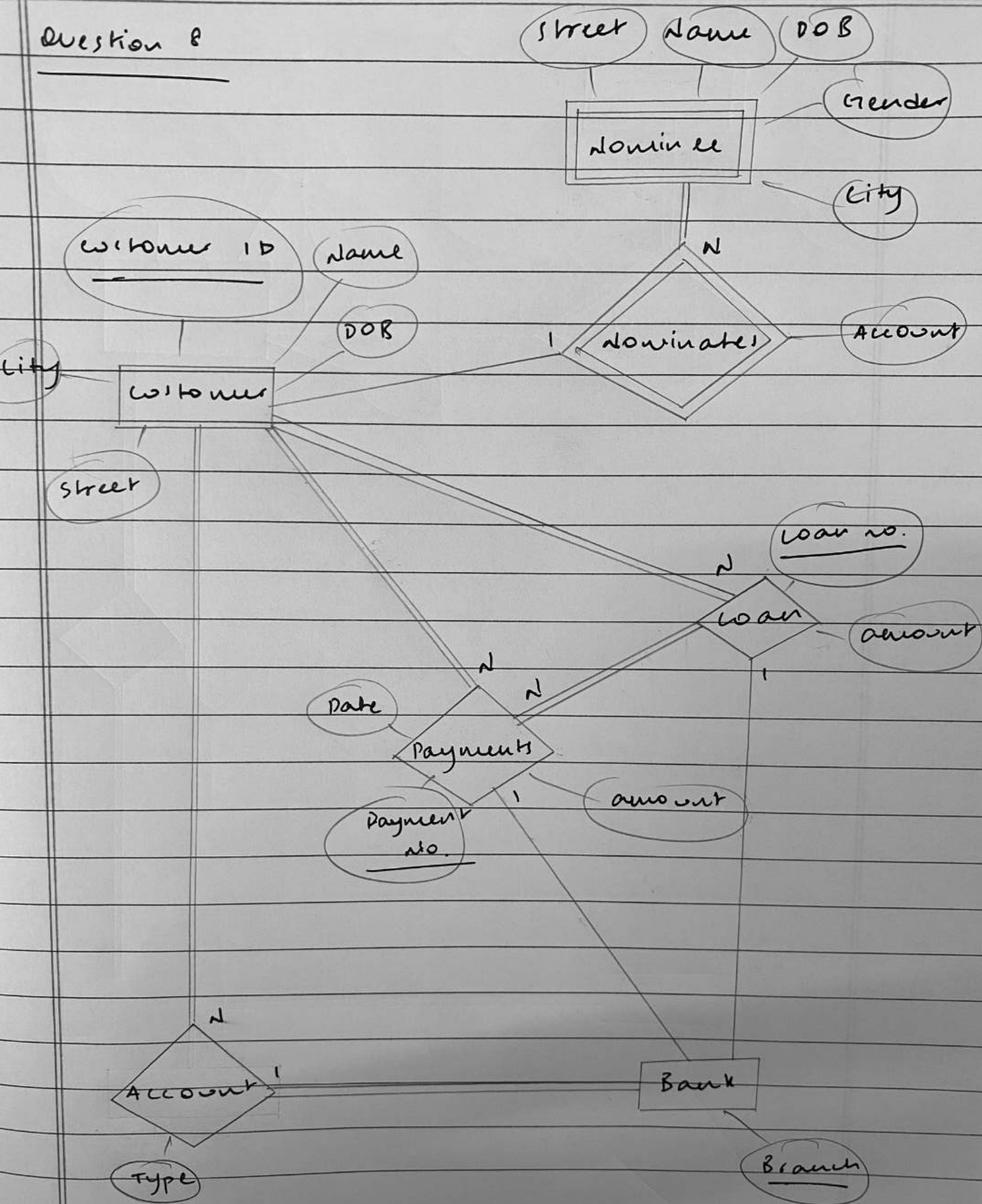
ii.	SP			PJ		
	S#	P#		P#	J#	
	S1	P1		P1	J1	
	S1	P2		P2	J1	
	S2	P1	SJ			
				S#	J#	
				S1	J1	
				S2	J1	

iii. The three tables SP, PJ, SJ are lossless

### Question 7



## Question 8



## Question 9

non additive join property:

if  $R_1$  and  $R_2$  exist

if  $x \in R_1$  and  $x \in R_2$

then  $R_1 \subseteq R_2$  or  $R_2 \subseteq R_1$

comparing relation pairs:

1.  $R_1(AD), R_2(AB) - R_1(AD), R_2(ABCD) - R_1 \subseteq R_2$

2.  $R_1(AD), R_3(BE) - \text{trivial}$

3.  $R_1(AD), R_4(CDE) - (C \rightarrow A) - R_1 \subseteq R_4$

4.  $R_1(AD), R_5(AE) - \text{not satisfied}$

$\therefore$  we can decide that ~~that~~ the relations do not satisfy the non-additive join decomposition losslessly.