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(last updated: June 22, 2018)

Task	MATLAB/Octave	Python NumPy	R	Julia	Task
CREATING MATRICES					
Creating Matrices (here: 3x3 matrix)	<pre>M> A = [1 2 3; 4 5 6; 7 8 9] A = 1 2 3 4 5 6 7 8 9</pre>	<pre>P> A = np.array([[1,2,3], [4,5,6], [7,8,9]]) P> A array([[1, 2, 3], [4, 5, 6], [7, 8, 9]])</pre>	<pre>R> A = matrix(c(1,2,3,4,5,6,7,8,9),nrow=3,byrow=T) # equivalent to # A = matrix(1:9,nrow=3,byrow=T) R> A [,1] [,2] [,3] [1,] 1 2 3 [2,] 4 5 6 [3,] 7 8 9</pre>	<pre>J> A=[1 2 3; 4 5 6; 7 8 9] 3x3 Array{Int64,2}: 1 2 3 4 5 6 7 8 9</pre>	Creating Matrices (here: 3x3 matrix)
Creating an column vector (nx1 matrix)	<pre>M> a = [1; 2; 3] a = 1 2 3</pre>	<pre>P> a = np.array([1,2,3]).reshape(3,1) P> b.shape (3, 1)</pre>	<pre>R> a = matrix(c(1,2,3), nrow=3, byrow=T) R> a [,1] [1,] 1 [2,] 2 [3,] 3</pre>	<pre>J> a=[1; 2; 3] 3-element Array{Int64,1}: 1 2 3</pre>	Creating a column vector (nx1 matrix)
Creating an row vector (1xn matrix)	<pre>M> b = [1 2 3] b = 1 2 3</pre>	<pre>P> b = np.array([1,2,3]).reshape(1, 3) P> b array([[1, 2, 3]]) # note that in numpy, 1D arrays # can be multiplied # with 2d arrays, too</pre>	<pre>R> b = matrix(c(1,2,3), ncol=3) R> b [,1] [,2] [,3] [1,] 1 2 3</pre>	<pre>J> b=[1 2 3] 1x3 Array{Int64,2}: 1 2 3 # note that this is a 2D array.</pre>	Creating an row vector (1xn matrix)

		<code>P> b.shape</code> (1, 3)			
Creating a random m x n matrix	<code>M> rand(3,2)</code> ans = 0.21977 0.10220 0.38959 0.69911 0.15624 0.65637	<code>P> np.random.rand(3,2)</code> array([[0.29347865, 0.17920462], [0.51615758, 0.64593471], [0.01067605, 0.09692771]])	<code>R> matrix(runif(3*2), ncol=2)</code> [,1] [,2] [1,] 0.5675127 0.7751204 [2,] 0.3439412 0.5261893 [3,] 0.2273177 0.223438	<code>J> rand(3,2)</code> 3x2 Array{Float64,2}: 0.36882 0.267725 0.571856 0.601524 0.848084 0.858935	Creating a random m x n matrix
Creating a zero m x n matrix	<code>M> zeros(3,2)</code> ans = 0 0 0 0 0 0	<code>P> np.zeros((3,2))</code> array([[0., 0.], [0., 0.], [0., 0.]])	<code>R> mat.or.vec(3, 2)</code> [,1] [,2] [1,] 0 0 [2,] 0 0 [3,] 0 0	<code>J> zeros(3,2)</code> 3x2 Array{Float64,2}: 0.0 0.0 0.0 0.0 0.0 0.0	Creating a zero m x n matrix
Creating an m x n matrix of ones	<code>M> ones(3,2)</code> ans = 1 1 1 1 1 1	<code>P> np.ones((3,2))</code> array([[1., 1.], [1., 1.], [1., 1.]])	<code>R> matrix(1L, 3, 2)</code> [,1] [,2] [1,] 1 1 [2,] 1 1 [3,] 1 1	<code>J> ones(3,2)</code> 3x2 Array{Float64,2}: 1.0 1.0 1.0 1.0 1.0 1.0	Creating an m x n matrix of ones
Creating an identity matrix	<code>M> eye(3)</code> ans = Diagonal Matrix 1 0 0 0 1 0 0 0 1	<code>P> np.eye(3)</code> array([[1., 0., 0.], [0., 1., 0.], [0., 0., 1.]])	<code>R> diag(3)</code> [,1] [,2] [,3] [1,] 1 0 0 [2,] 0 1 0 [3,] 0 0 1	<code>J> eye(3)</code> 3x3 Array{Float64,2}: 1.0 0.0 0.0 0.0 1.0 0.0 0.0 0.0 1.0	Creating an identity matrix
Creating a diagonal matrix	<code>M> a = [1 2 3]</code> <code>M> diag(a)</code> ans = Diagonal Matrix 1 0 0	<code>P> a = np.array([1,2,3])</code> <code>P> np.diag(a)</code> array([[1, 0, 0], [0, 2, 0], [0, 0, 3]])	<code>R> diag(1:3)</code> [,1] [,2] [,3] [1,] 1 0 0 [2,] 0 2 0 [3,] 0 0 3	<code>J> a=[1, 2, 3]</code> # added commas because julia # vectors are columnar <code>J> diagm(a)</code>	Creating a diagonal matrix

```
0 2 0
0 0 3
```

```
3x3 Array{Int64,2}:
1 0 0
0 2 0
0 0 3
```

ACCESSING MATRIX ELEMENTS

Getting the dimension
of a matrix
(here: 2D, rows x cols)

```
M> A = [1 2 3; 4 5 6]
A =
1 2 3
4 5 6

M> size(A)
ans =
2 3
```

```
P> A = np.array([ [1,2,3], [4,5,6] ])

P> A
array([[1, 2, 3],
       [4, 5, 6]])

P> A.shape
(2, 3)
```

```
R> A = matrix(1:6,nrow=2,byrow=T)

R> A
[,1] [,2] [,3]
[1,] 1 2 3
[2,] 4 5 6

R> dim(A)
[1] 2 3
```

```
J> A=[1 2 3; 4 5 6]
2x3 Array{Int64,2}:
1 2 3
4 5 6

J> size(A)
(2,3)
```

Getting the dimension
of a matrix
(here: 2D, rows x cols)

Selecting rows

```
M> A = [1 2 3; 4 5 6; 7 8 9]

% 1st row
M> A(1,:)
ans =
1 2 3

% 1st 2 rows
M> A(1:2,:)
ans =
1 2 3
4 5 6
```

```
P> A = np.array([ [1,2,3], [4,5,6], [7,8,9] ])

# 1st row
P> A[0,:]
array([1, 2, 3])

# 1st 2 rows
P> A[0:2,:]
array([[1, 2, 3], [4, 5, 6]])
```

```
R> A = matrix(1:9,nrow=3,byrow=T)

# 1st row
R> A[1,]
[1] 1 2 3

# 1st 2 rows
R> A[1:2,]
[,1] [,2] [,3]
[1,] 1 2 3
[2,] 4 5 6
```

```
J> A=[1 2 3; 4 5 6; 7 8 9];
#semicolon suppresses output

#1st row
J> A[1,:]
1x3 Array{Int64,2}:
1 2 3

#1st 2 rows
J> A[1:2,:]
2x3 Array{Int64,2}:
1 2 3
4 5 6
```

Selecting rows

Selecting columns

```
M> A = [1 2 3; 4 5 6; 7 8 9]

% 1st column
```

```
P> A = np.array([ [1,2,3], [4,5,6], [7,8,9] ])

# 1st column (as row vector)
```

```
R> A = matrix(1:9,nrow=3,byrow=T)

# 1st column as row vector
```

```
J> A=[1 2 3; 4 5 6; 7 8 9];

#1st column
```

Selecting columns

	<pre> M> A(:,1) ans = 1 4 7 % 1st 2 columns M> A(:,1:2) ans = 1 2 4 5 7 8 </pre>	<pre> P> A[:,0] array([1, 4, 7]) # 1st column (as column vector) P> A[:,[0]] array([[1], [4], [7]]) # 1st 2 columns P> A[:,0:2] array([[1, 2], [4, 5], [7, 8]]) </pre>	<pre> R> t(A[,1]) [,1] [,2] [,3] [1,] 1 4 7 # 1st column as column vector R> A[,1] [1] 1 4 7 # 1st 2 columns R> A[:,1:2] [,1] [,2] [1,] 1 2 [2,] 4 5 [3,] 7 8 </pre>	<pre> J> A[:,1] 3-element Array{Int64,1}: 1 4 7 #1st 2 columns J> A[:,1:2] 3x2 Array{Int64,2}: 1 2 4 5 7 8 </pre>	
Extracting rows and columns by criteria (here: get rows that have value 9 in column 3)	<pre> M> A = [1 2 3; 4 5 9; 7 8 9] A = 1 2 3 4 5 9 7 8 9 M> A(A(:,3) == 9,:) ans = 4 5 9 7 8 9 </pre>	<pre> P> A = np.array([[1,2,3], [4,5,9], [7,8,9]]) P> A array([[1, 2, 3], [4, 5, 9], [7, 8, 9]]) P> A[A[:,2] == 9] array([[4, 5, 9], [7, 8, 9]]) </pre>	<pre> R> A = matrix(1:9,nrow=3,byrow=T) R> A [,1] [,2] [,3] [1,] 1 2 3 [2,] 4 5 9 [3,] 7 8 9 R> A[A[,3]==9,] [1] 7 8 9 </pre>	<pre> J> A=[1 2 3; 4 5 9; 7 8 9] 3x3 Array{Int64,2}: 1 2 3 4 5 9 7 8 9 # use '==' for # element-wise check J> A[A[:,3] .==9, :] 2x3 Array{Int64,2}: 4 5 9 7 8 9 </pre>	Extracting rows and columns by criteria (here: get rows that have value 9 in column 3)
Accessing elements (here: 1st element)	<pre> M> A = [1 2 3; 4 5 6; 7 8 9] M> A(1,1) ans = 1 </pre>	<pre> P> A = np.array([[1,2,3], [4,5,6], [7,8,9]]) P> A[0,0] 1 </pre>	<pre> R> A = matrix(c(1,2,3,4,5,6,7,8,9),nrow=3,byrow=T) R> A[1,1] [1] 1 </pre>	<pre> J> A=[1 2 3; 4 5 6; 7 8 9]; J> A[1,1] 1 </pre>	Accessing elements (here: 1st element)

MANIPULATING SHAPE AND DIMENSIONS

**Converting
a matrix into a row vector (by
column)**

```
M> A = [1 2 3; 4 5 6; 7 8 9]

M> A(:)

ans =
```

```
P> A = np.array([[1,2,3],[4,5,6],[7,8,9]])

P> A.flatten() # returns a copy

array([1, 4, 7, 2, 5, 8, 3, 6, 9])

1# alternatively A.ravel()
4# ravel() returns a view
7
2
5
8
3
6
9
```

```
R> A = matrix(1:9,nrow=3,byrow=T)

R> as.vector(A)

[1] 1 4 7 2 5 8 3 6 9
```

```
J> A=[1 2 3; 4 5 6; 7 8 9]

J> vec(A)

9-element Array{Int64,1}:
```

**Converting
a matrix into a row vector (l**

```
1
4
7
2
5
8
3
6
9
```

**Converting
row to column vectors**

```
M> b = [1 2 3]

M> b = b'

b =

1
2
3
```

```
P> b = np.array([1, 2, 3])

P> b = b[np.newaxis].T

# alternatively
# b = b[:,np.newaxis]

P> b

array([[1],
       [2],
       [3]])
```

```
R> b = matrix(c(1,2,3), ncol=3)

R> t(b)

[1,]
[1,] 1
[2,] 2
[3,] 3
```

```
J> b=vec([1 2 3])

3-element Array{Int64,1}:

1
2
3
```

**Converting
row to column vectors****Reshaping Matrices****(here: 3x3 matrix to row vector)**

```
M> A = [1 2 3; 4 5 6; 7 8 9]

A =

1 2 3
4 5 6
7 8 9

M> total_elements = numel(A)

M> B = reshape(A,1,total_elements)
% or reshape(A,1,9)

B =

1 4 7 2 5 8 3 6 9
```

```
P> A = np.array([[1,2,3],[4,5,6],[7,8,9]])

P> A

array([[1, 2, 3],
       [4, 5, 6],
       [7, 8, 9]])

P> total_elements = np.prod(A.shape)

P> B = A.reshape(1, total_elements)

# alternative shortcut:
```

```
R> A = matrix(1:9,nrow=3,byrow=T)

R> A

[1,] [2] [3]
[1,] 1 2 3
[2,] 4 5 6
[3,] 7 8 9

R> total_elements = dim(A)[1] * dim(A)[2]

R> B = matrix(A, ncol=total_elements)
```

```
J> A=[1 2 3; 4 5 6; 7 8 9]

3x3 Array{Int64,2}:

1 2 3
4 5 6
7 8 9

J> total_elements=length(A)

9

J> B=reshape(A,1,total_elements)

1x9 Array{Int64,2}:

1 4 7 2 5 8 3 6 9
```

Reshaping Matrices**(here: 3x3 matrix to row vector)**

		<pre># A.reshape(1,-1) R> B [,1] [,2] [,3] [,4] [,5] [,6] [,7] [,8] [,9] [1,] 1 4 7 2 5 8 3 6 9 P> B array([[1, 2, 3, 4, 5, 6, 7, 8, 9]]) P> A = np.array([[1, 2, 3], [4, 5, 6]]) P> B = np.array([[7, 8, 9],[10,11,12]]) P> C = np.concatenate((A, B), axis=0) P> C array([[1, 2, 3], [4, 5, 6], [7, 8, 9], [10, 11, 12]])</pre>		
Concatenating matrices	<pre>M> A = [1 2 3; 4 5 6] M> B = [7 8 9; 10 11 12] M> C = [A; B] 1 2 3 4 5 6 7 8 9 10 11 12</pre>		<pre>R> A = matrix(1:6,nrow=2,byrow=T) R> B = matrix(7:12,nrow=2,byrow=T) R> C = rbind(A,B) R> C [,1] [,2] [,3] [1,] 1 2 3 [2,] 4 5 6 [3,] 7 8 9 [4,] 10 11 12 J> A=[1 2 3; 4 5 6]; J> B=[7 8 9; 10 11 12]; J> C=[A; B] 4x3 Array{Int64,2}: 1 2 3 4 5 6 7 8 9 10 11 12</pre>	Concatenating matrices
Stacking vectors and matrices	<pre>M> a = [1 2 3] M> b = [4 5 6] M> c = [a' b'] c = 1 4 2 5 3 6 M> c = [a; b] c = 1 2 3 4 5 6</pre>	<pre>P> a = np.array([1,2,3]) P> b = np.array([4,5,6]) P> np.column_stack([a,b]) array([[1, 4], [2, 5], [3, 6]]) P> np.row_stack([a,b]) array([[1, 2, 3], [4, 5, 6]])</pre>	<pre>R> a = matrix(1:3, ncol=3) R> b = matrix(4:6, ncol=3) R> matrix(rbind(A, B), ncol=2) [,1] [,2] [1,] 1 5 [2,] 4 3 R> rbind(A,B) [,1] [,2] [,3] [1,] 1 2 3 [2,] 4 5 6</pre>	Stacking vectors and matrices

BASIC MATRIX OPERATIONS

Matrix-scalar operations	<pre> M> A = [1 2 3; 4 5 6; 7 8 9] M> A * 2 ans = 2 4 6 8 10 12 14 16 18 M> A + 2 M> A - 2 M> A / 2 </pre>	<pre> P> A = np.array([[1,2,3], [4,5,6], [7,8,9]]) P> A * 2 array([[2, 4, 6], [8, 10, 12], [14, 16, 18]]) P> A + 2 P> A - 2 P> A / 2 # Note that NumPy was optimized for # in-place assignments # e.g., A += A instead of # A = A + A </pre>	<pre> R> A = matrix(1:9, nrow=3, byrow=T) R> A * 2 [,1] [,2] [,3] [1,] 2 4 6 [2,] 8 10 12 [3,] 14 16 18 R> A + 2 R> A - 2 R> A / 2 </pre>	<pre> J> A=[1 2 3; 4 5 6; 7 8 9]; # elementwise operator J> A .* 2 3x3 Array{Int64,2}: 2 4 6 8 10 12 14 16 18 J> A .+ 2; J> A .- 2; J> A ./ 2; </pre>	Matrix-scalar operations
Matrix-matrix multiplication	<pre> M> A = [1 2 3; 4 5 6; 7 8 9] M> A * A ans = 30 36 42 66 81 96 102 126 150 </pre>	<pre> P> A = np.array([[1,2,3], [4,5,6], [7,8,9]]) P> np.dot(A,A) # or A.dot(A) array([[30, 36, 42], [66, 81, 96], [102, 126, 150]]) </pre>	<pre> R> A = matrix(1:9, nrow=3, byrow=T) R> A %% A [,1] [,2] [,3] [1,] 30 36 42 [2,] 66 81 96 [3,] 102 126 150 </pre>	<pre> J> A=[1 2 3; 4 5 6; 7 8 9]; J> A * A 3x3 Array{Int64,2}: 30 36 42 66 81 96 102 126 150 </pre>	Matrix-matrix multiplication
Matrix-vector multiplication	<pre> M> A = [1 2 3; 4 5 6; 7 8 9] M> b = [1; 2; 3] M> A * b ans = 14 32 50 </pre>	<pre> P> A = np.array([[1,2,3], [4,5,6], [7,8,9]]) P> b = np.array([[1], [2], [3]]) P> np.dot(A,b) # or A.dot(b) array([[14], [32], [50]]) </pre>	<pre> R> A = matrix(1:9, ncol=3) R> b = matrix(1:3, nrow=3) R> t(b %% A) [,1] [1,] 14 [2,] 32 [3,] 50 </pre>	<pre> J> A=[1 2 3; 4 5 6; 7 8 9]; J> b=[1; 2; 3]; J> A*b 3-element Array{Int64,1}: 14 32 50 </pre>	Matrix-vector multiplication
Element-wise matrix-matrix operations	<pre> M> A = [1 2 3; 4 5 6; 7 8 9] </pre>	<pre> P> A = np.array([[1,2,3], [4,5,6], [7,8,9]]) </pre>	<pre> R> A = matrix(1:9, nrow=3, byrow=T) </pre>	<pre> J> A=[1 2 3; 4 5 6; 7 8 9]; </pre>	Element-wise matrix-matrix operations

	<pre> M> A .* A ans = 1 4 9 16 25 36 49 64 81 M> A .+ A M> A .- A M> A ./ A </pre>	<pre> P> A * A array([[1, 4, 9], [16, 25, 36], [49, 64, 81]]) P> A + A P> A - A P> A / A # Note that NumPy was optimized for # in-place assignments # e.g., A += A instead of # A = A + A P> A = np.array([[1,2,3], [4,5,6], [7,8,9]]) P> np.power(A,2) array([[1, 4, 9], [16, 25, 36], [49, 64, 81]]) </pre>	<pre> R> A * A [,1] [,2] [,3] [1,] 1 4 9 [2,] 16 25 36 [3,] 49 64 81 R> A + A R> A - A R> A / A </pre>	<pre> J> A .* A 3x3 Array{Int64,2}: 1 4 9 16 25 36 49 64 81 J> A .+ A; J> A .- A; J> A ./ A; </pre>	
Matrix elements to power n (here: individual elements squared)	<pre> M> A = [1 2 3; 4 5 6; 7 8 9] M> A.^2 ans = 1 4 9 16 25 36 49 64 81 </pre>	<pre> P> A = np.array([[1,2,3], [4,5,6], [7,8,9]]) P> np.power(A,2) array([[1, 4, 9], [16, 25, 36], [49, 64, 81]]) </pre>	<pre> R> A = matrix(1:9, nrow=3, byrow=T) R> A ^ 2 [,1] [,2] [,3] [1,] 1 4 9 [2,] 16 25 36 [3,] 49 64 81 </pre>	<pre> J> A=[1 2 3; 4 5 6; 7 8 9]; J> A .^ 2 3x3 Array{Int64,2}: 1 4 9 16 25 36 49 64 81 </pre>	Matrix elements to power n (here: individual elements squared)
Matrix to power n (here: matrix-matrix multiplication with itself)	<pre> M> A = [1 2 3; 4 5 6; 7 8 9] M> A ^ 2 ans = 30 36 42 66 81 96 102 126 150 </pre>	<pre> P> A = np.array([[1,2,3], [4,5,6], [7,8,9]]) P> np.linalg.matrix_power(A,2) array([[30, 36, 42], [66, 81, 96], [102, 126, 150]]) </pre>	<pre> R> A = matrix(1:9, ncol=3) # requires the 'expm' package R> install.packages('expm') R> library(expm) R> A %^% 2 [,1] [,2] [,3] [1,] 30 66 102 [2,] 36 81 126 [3,] 42 96 150 </pre>	<pre> J> A=[1 2 3; 4 5 6; 7 8 9]; J> A ^ 2 3x3 Array{Int64,2}: 30 36 42 66 81 96 102 126 150 </pre>	Matrix to power n (here: matrix-matrix multiplication with itself)
Matrix transpose	<pre> M> A = [1 2 3; 4 5 6; 7 8 9] M> A' </pre>	<pre> P> A = np.array([[1,2,3], [4,5,6], [7,8,9]]) P> A.T </pre>	<pre> R> A = matrix(1:9, nrow=3, byrow=T) R> t(A) </pre>	<pre> J> A=[1 2 3; 4 5 6; 7 8 9] 3x3 Array{Int64,2}: 1 2 3 </pre>	Matrix transpose

	<pre>ans = 1 4 7 2 5 8 3 6 9</pre>	<pre>array([[1, 4, 7], [2, 5, 8], [3, 6, 9]])</pre>	<pre>[,1] [,2] [,3] [1,] 1 4 7 [2,] 2 5 8 [3,] 3 6 9</pre>	<pre>4 5 6 7 8 9 J> A' 3x3 Array{Int64,2}: 1 4 7 2 5 8 3 6 9</pre>	
Determinant of a matrix: A -> A 	<pre>M> A = [6 1 1; 4 -2 5; 2 8 7] A = 6 1 1 4 -2 5 2 8 7 M> det(A) ans = -306</pre>	<pre>P> A = np.array([[6,1,1],[4,-2,5], [2,8,7]]) P> A array([[6, 1, 1], [4, -2, 5], [2, 8, 7]]) P> np.linalg.det(A) -306</pre>	<pre>R> A = matrix(c(6,1,1,4,-2,5,2,8,7), nrow=3, byrow=T) R> A [,1] [,2] [,3] [1,] 6 1 1 [2,] 4 -2 5 [3,] 2 8 7 R> det(A) [1] -306</pre>	<pre>J> A=[6 1 1; 4 -2 5; 2 8 7] 3x3 Array{Int64,2}: 6 1 1 4 -2 5 2 8 7 J> det(A) -306</pre>	Determinant of a matrix: A -> A
Inverse of a matrix	<pre>M> A = [4 7; 2 6] A = 4 7 2 6 M> A_inv = inv(A) A_inv = 0.60000 -0.70000 -0.20000 0.40000</pre>	<pre>P> A = np.array([[4, 7], [2, 6]]) P> A array([[4, 7], [2, 6]]) P> A_inverse = np.linalg.inv(A) P> A_inverse array([[0.6, -0.7], [-0.2, 0.4]])</pre>	<pre>R> A = matrix(c(4,7,2,6), nrow=2, byrow=T) R> A [,1] [,2] [1,] 4 7 [2,] 2 6 R> solve(A) [,1] [,2] [1,] 0.6 -0.7 [2,] -0.2 0.4</pre>	<pre>J> A=[4 7; 2 6] 2x2 Array{Int64,2}: 4 7 2 6 J> A_inv=inv(A) 2x2 Array{Float64,2}: 0.6 -0.7 -0.2 0.4</pre>	Inverse of a matrix

ADVANCED MATRIX OPERATIONS

Calculating the covariance matrix of 3 random variables (here: covariances of the means of x1, x2, and x3)	<pre>M> x1 = [4.0000 4.2000 3.9000 4.3000 4.1000]'; M> x2 = [2.0000 2.1000 2.0000 2.1000 2.2000]'; M> x3 = [0.60000 0.59000 0.58000 0.62000 0.63000]'; M> cov([x1,x2,x3]) ans = 2.5000e-02 7.5000e-03 1.7500e-03 7.5000e-03 7.0000e-03 1.3500e-03 1.7500e-03 1.3500e-03 4.3000e-04</pre>	<pre>P> x1 = np.array([4, 4.2, 3.9, 4.3, 4.1]) P> x2 = np.array([2, 2.1, 2, 2.1, 2.2]) P> x3 = np.array([0.6, 0.59, 0.58, 0.62, 0.63]) P> np.cov([x1, x2, x3]) Array([[0.025 , 0.0075 , 0.00175], [0.0075 , 0.007 , 0.00135], [0.00175, 0.00135, 0.00043]])</pre>	<pre>R> x1 = matrix(c(4, 4.2, 3.9, 4.3, 4.1), ncol=5) R> x2 = matrix(c(2, 2.1, 2, 2.1, 2.2), ncol=5) R> x3 = matrix(c(0.6, 0.59, 0.58, 0.62, 0.63), ncol=5) R> cov(matrix(c(x1, x2, x3), ncol=3)) [,1] [,2] [,3] [1,] 0.02500 0.00750 0.00175 [2,] 0.00750 0.00700 0.00135 [3,] 0.00175 0.00135 0.00043</pre>	<pre>J> x1=[4.0 4.2 3.9 4.3 4.1]'; J> x2=[2. 2.1 2. 2.1 2.2]'; J> x3=[0.6 .59 .58 .62 .63]'; J> cov([x1 x2 x3]) 3x3 Array{Float64,2}: 0.025 0.0075 0.00175 0.0075 0.007 0.00135 0.00175 0.00135 0.00043</pre>	Calculating the covariance of 3 random variables (here: covariances of the m of x1, x2, and x3)
Calculating eigenvectors and eigenvalues	<pre>M> A = [3 1; 1 3] A = 3 1 1 3 M> [eig_vec,eig_val] = eig(A) eig_vec = -0.70711 0.70711 0.70711 0.70711 eig_val = 2 0 0 4 Diagonal Matrix</pre>	<pre>P> A = np.array([[3, 1], [1, 3]]) P> A array([[3, 1], [1, 3]]) P> eig_val, eig_vec = np.linalg.eig(A) P> eig_val array([4., 2.]) P> eig_vec array([[0.70710678, -0.70710678], [0.70710678, 0.70710678]])</pre>	<pre>R> A = matrix(c(3,1,1,3), ncol=2) R> A [,1] [,2] [1,] 3 1 [2,] 1 3 R> eigen(A) \$values [1] 4 2 \$vectors [,1] [,2] [1,] 0.7071068 -0.7071068 [2,] 0.7071068 0.7071068</pre>	<pre>J> A=[3 1; 1 3] 2x2 Array{Int64,2}: 3 1 1 3 J> (eig_vec,eig_val)=eig(a) ([2.0,4.0], 2x2 Array{Float64,2}: -0.707107 0.707107 0.707107 0.707107)</pre>	Calculating eigenvectors and eigenval
Generating a Gaussian dataset:	<pre>% requires statistics toolbox package % how to install and load it in Octave:</pre>	<pre>P> mean = np.array([0,0])</pre>	<pre># requires the 'mass' package</pre>	<pre># requires the Distributions package from https://github.com/JuliaStats/Distributions.jl</pre>	Generating a Gaussian dati

creating random vectors from the multivariate normal distribution given mean and covariance matrix

(here: 5 random vectors with

mean 0, covariance = 0, variance = 2)

```
% download the package from:
% http://octave.sourceforge.net/packages.php
% pkg install
% ~/Desktop/io-2.0.2.tar.gz
% pkg install
% ~/Desktop/statistics-1.2.3.tar.gz

M> pkg load statistics

M> mean = [0 0]

M> cov = [2 0; 0 2]

cov =

    2    0
    0    2

M> mvnrnd(mean,cov,5)

    2.480150   -0.559906
   -2.933047    0.560212
    0.098206    3.055316
   -0.985215   -0.990936
    1.122528    0.686977
```

```
P> cov = np.array([[2,0],[0,2]])

P> np.random.multivariate_normal(mean, cov, 5)

Array([[ 1.55432624, -1.17972629],
       [-2.01185294,  1.96081908],
       [-2.11810813,  1.45784216],
       [-2.93207591, -0.07369322],
       [-1.37031244, -1.18408792]])
```

```
R> install.packages('MASS')

R> library(MASS)

R> mvrnorm(n=10, mean, cov)

[1,] [,2]
[1,] -0.8407830 -0.1882706
[2,] 0.8496822 -0.7889329
[3,] -0.1564171 0.8422177
[4,] -0.6288779 1.0618688
[5,] -0.5103879 0.1303697
[6,] 0.8413189 -0.1623758
[7,] -1.0495466 -0.4161082
[8,] -1.3236339 0.7755572
[9,] 0.2771013 1.4900494
[10,] -1.3536268 0.2338913
```

```
J> using Distributions

J> mean=[0., 0.]

2-element Array{Float64,1}:
 0
 0

J> cov=[2. 0.; 0. 2.]

2x2 Array{Float64,2}:
 2.0 0.0
 0.0 2.0

J> rand( MvNormal(mean, cov), 5)

2x5 Array{Float64,2}:
 -0.527634 0.370725 -0.761928
 -3.91747 1.47516
 -0.448821 2.21904 2.24561
 0.692063 0.390495
```

creating random vectors from multivariate normal distribution given mean and covariance matrix

(here: 5 random vectors with

mean 0, covariance = 0, var