

Can seasonal influenza be eradicated under voluntary vaccination?

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April 6, 2018

Kevin O'Keefe



Steven Strogatz



VACCINES YOU NEED

Influenza Vaccine
What You Need to Know

Why get vaccinated?

Flu ("flu") is a contagious disease that spreads easily between people in the United States every winter, usually between October and May.

Flu is spread mainly by influenza viruses, and is spread mainly by sneezing, and close contact.

Flu, but the risk of getting flu is highest when symptoms come on suddenly and they can include:

(Flu Vacci
Inactiv
Recor
2014

VACCINE INFORMATION ST

METRO

Don't panic!

IT'S THAT TIME AGAIN...

The Grand National: Page 61

www.metro.co.uk

Friday April 17, 2009

BY SUZY AUSTIN

BRITAIN'S worst fears of bird flu again became reality yesterday as a dead swan tested positive for the deadly H5N1 strain of the virus. The male swan, found washed up on the River Colne in Essex, had been tested for the virus by the Government's Avian Influenza Reference Laboratory at Pirbright. It is one of a herd of 1,500 swans which have been tested since last year.



Vaccine coverage

Proportion of the population that is vaccinated



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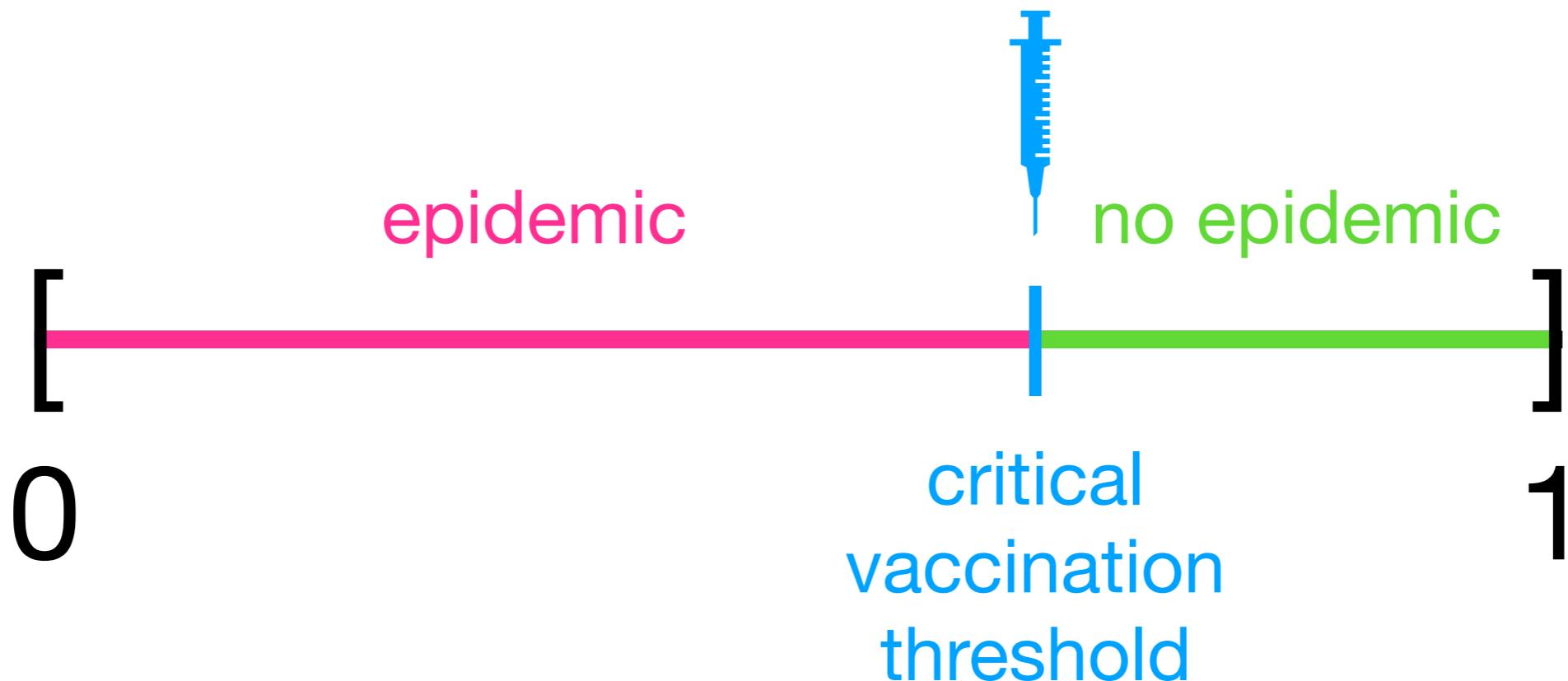
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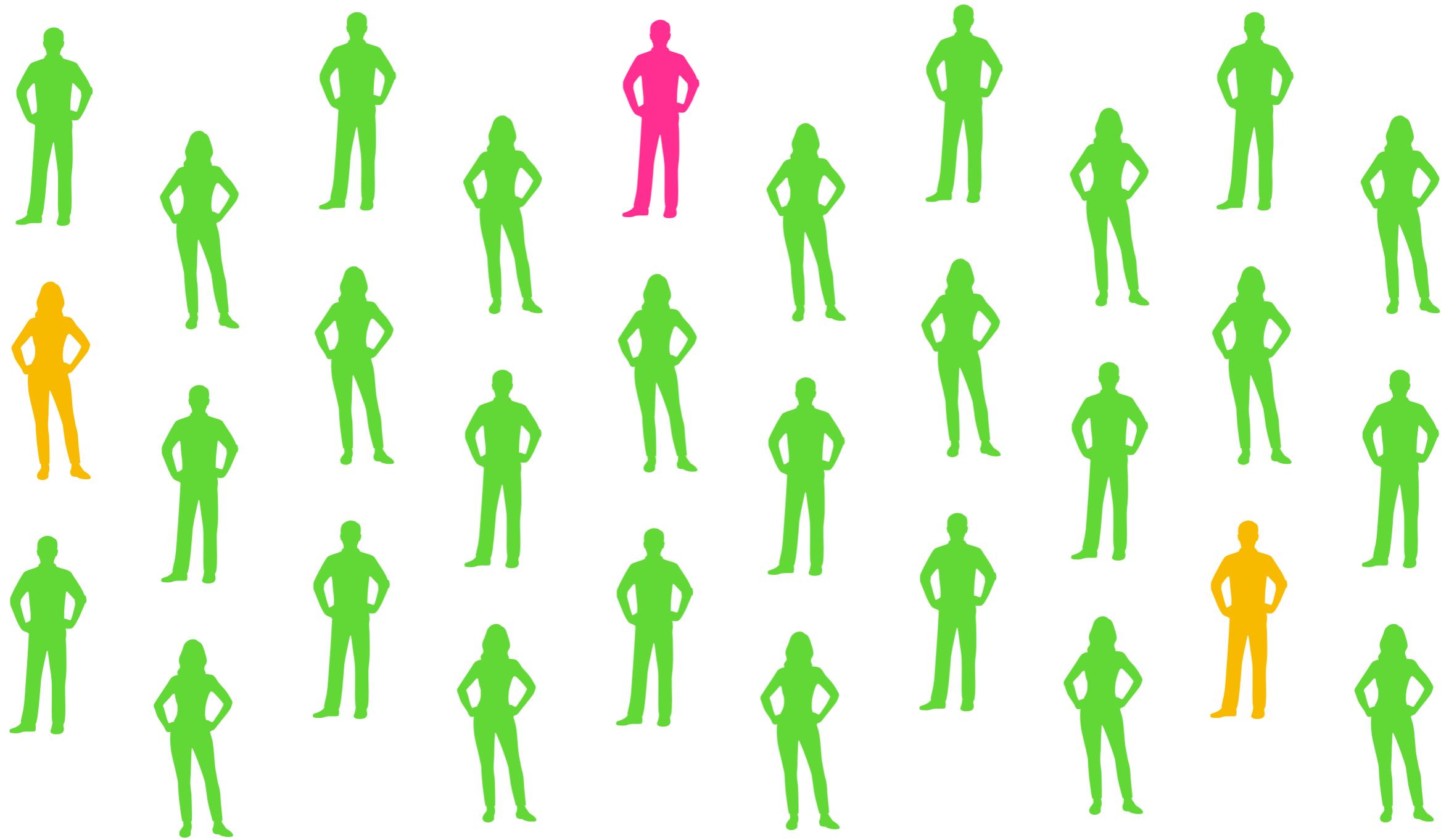
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Herd immunity

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Central question

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Can a population
self-organize
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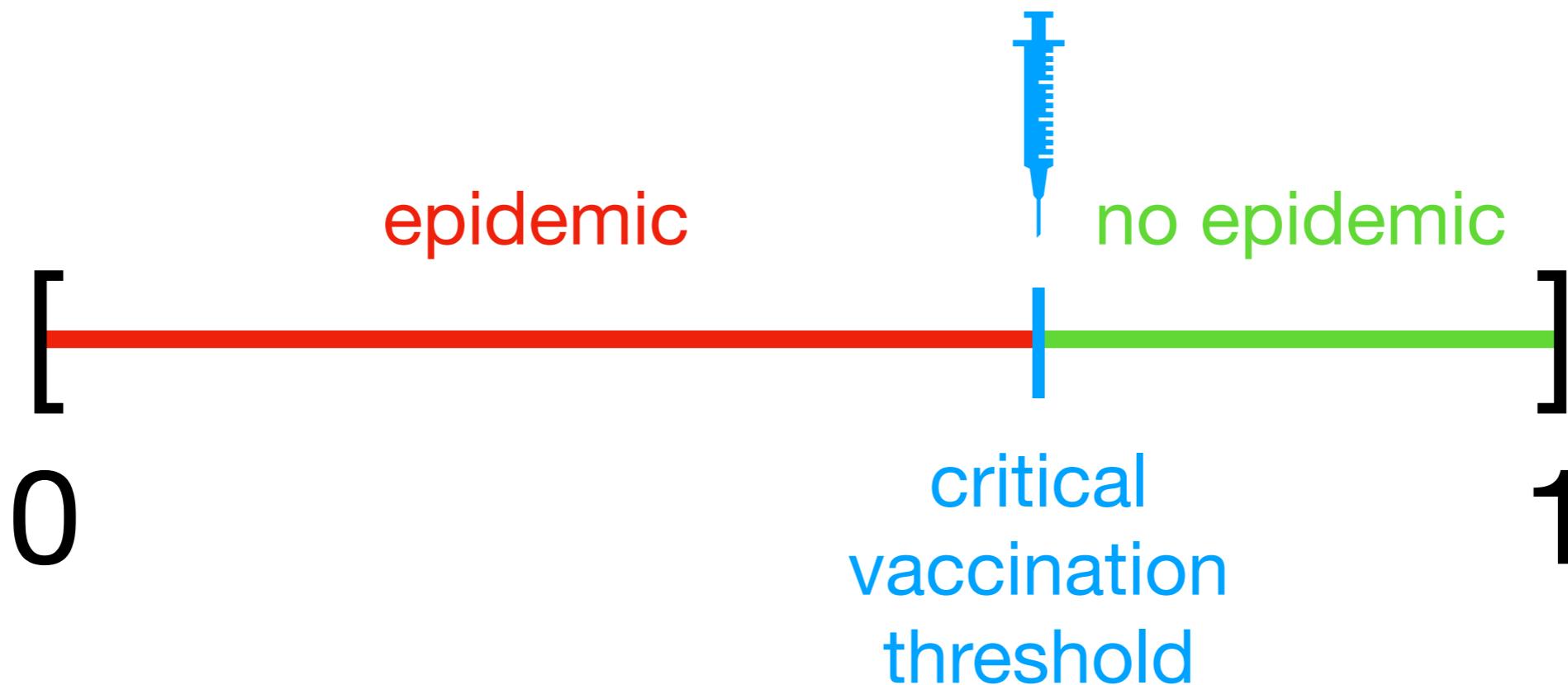
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- Game-theoretic approach

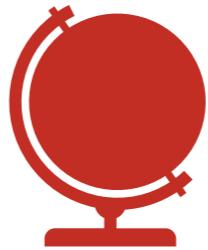
Previous result

- Game-theoretic approach
- Assumes perfect, global information



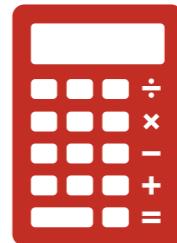
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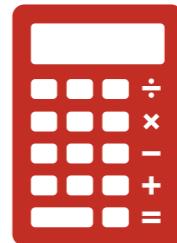
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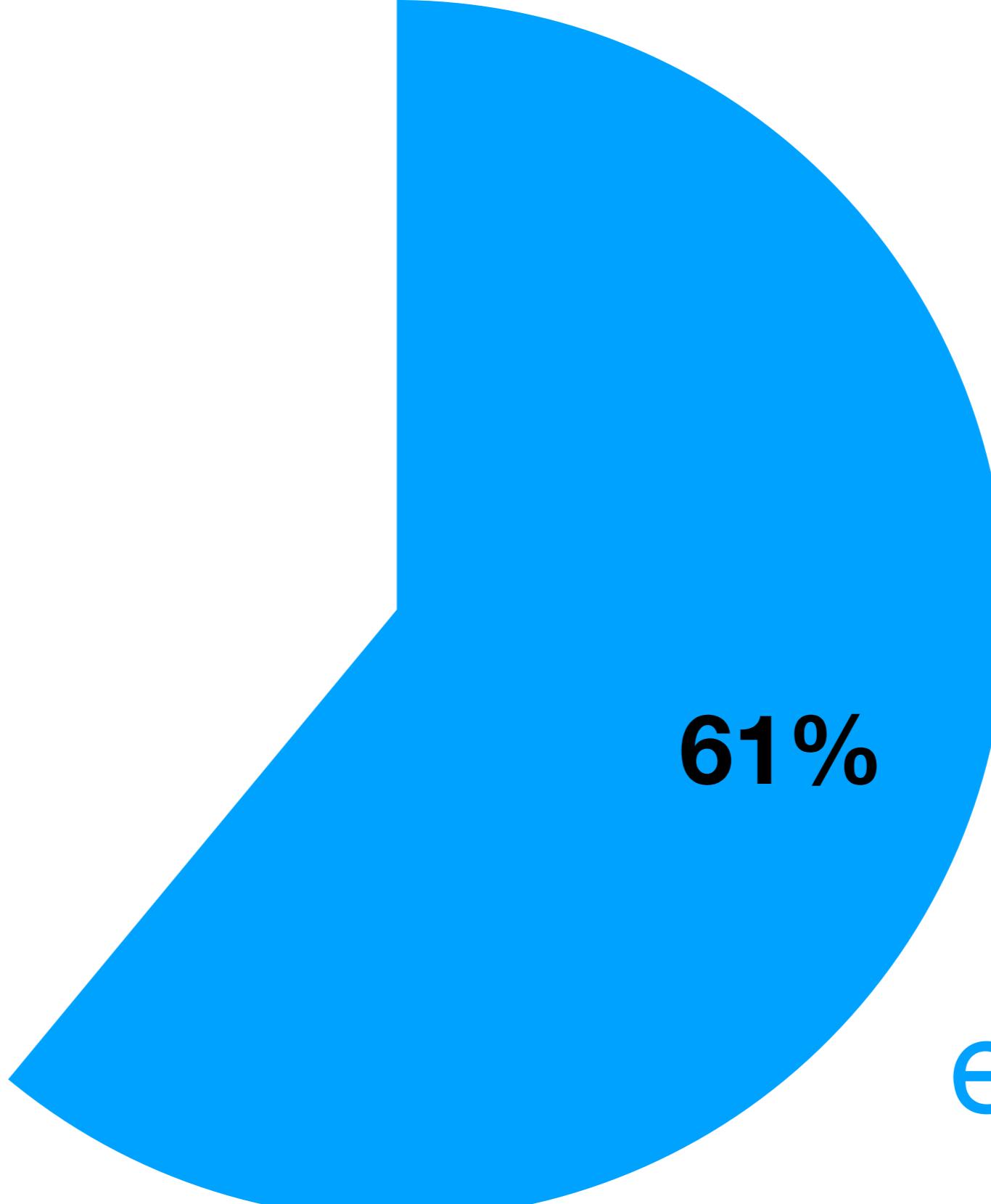
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Previous result

- Game-theoretic approach
- Assumes perfect, global information
 - Probability of getting sick
- Implicitly involves "rational" behavior
- Free-riding problem

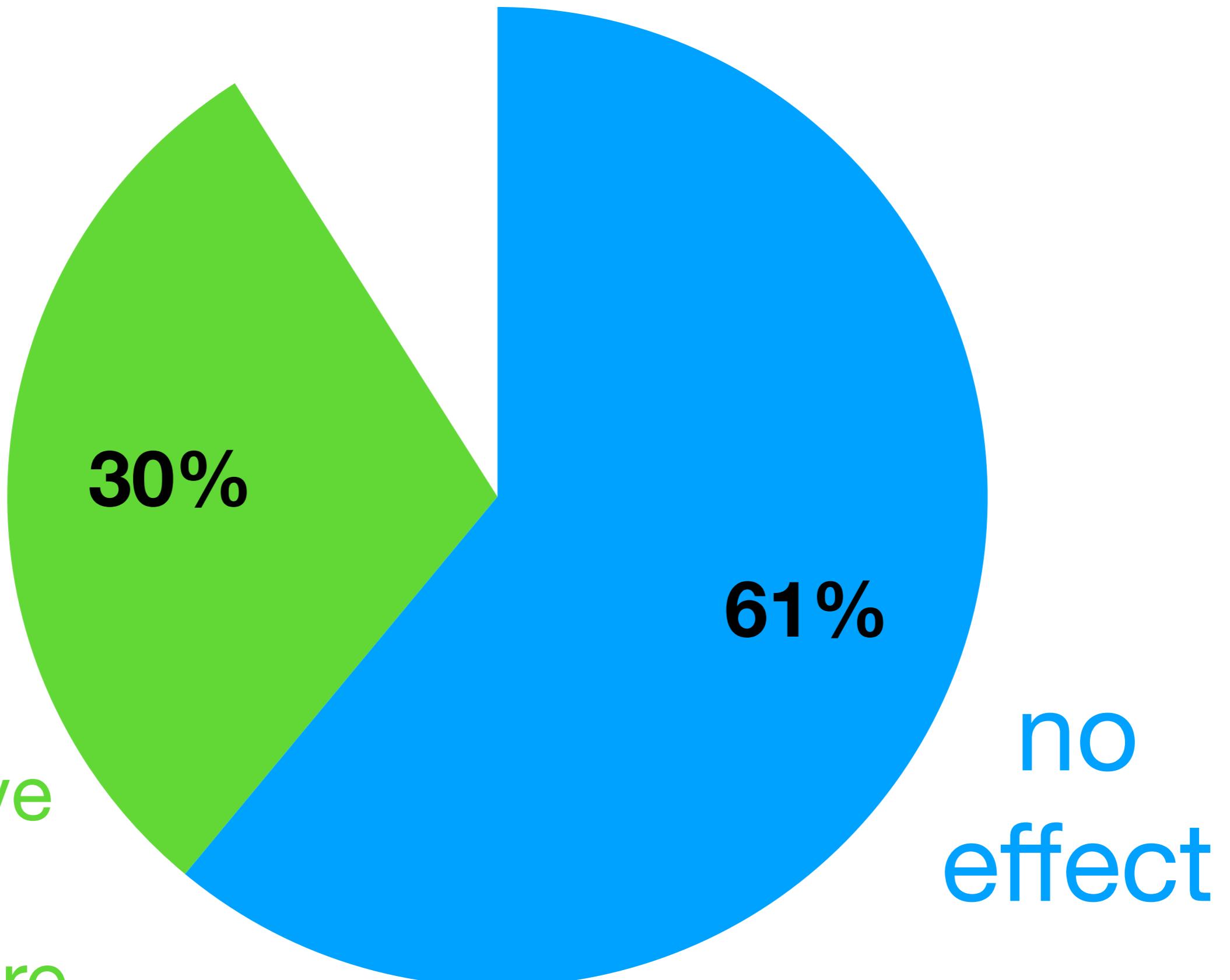


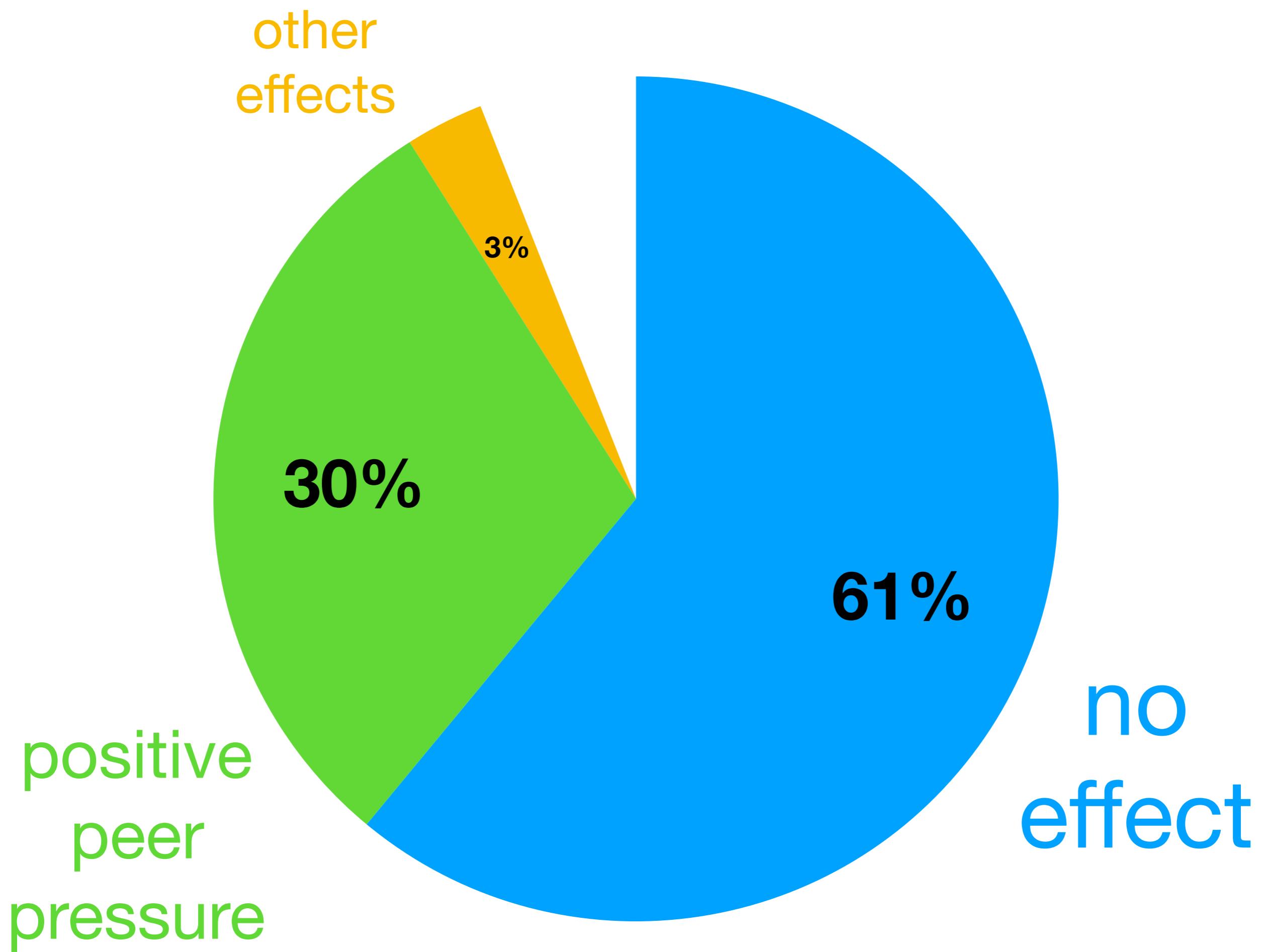


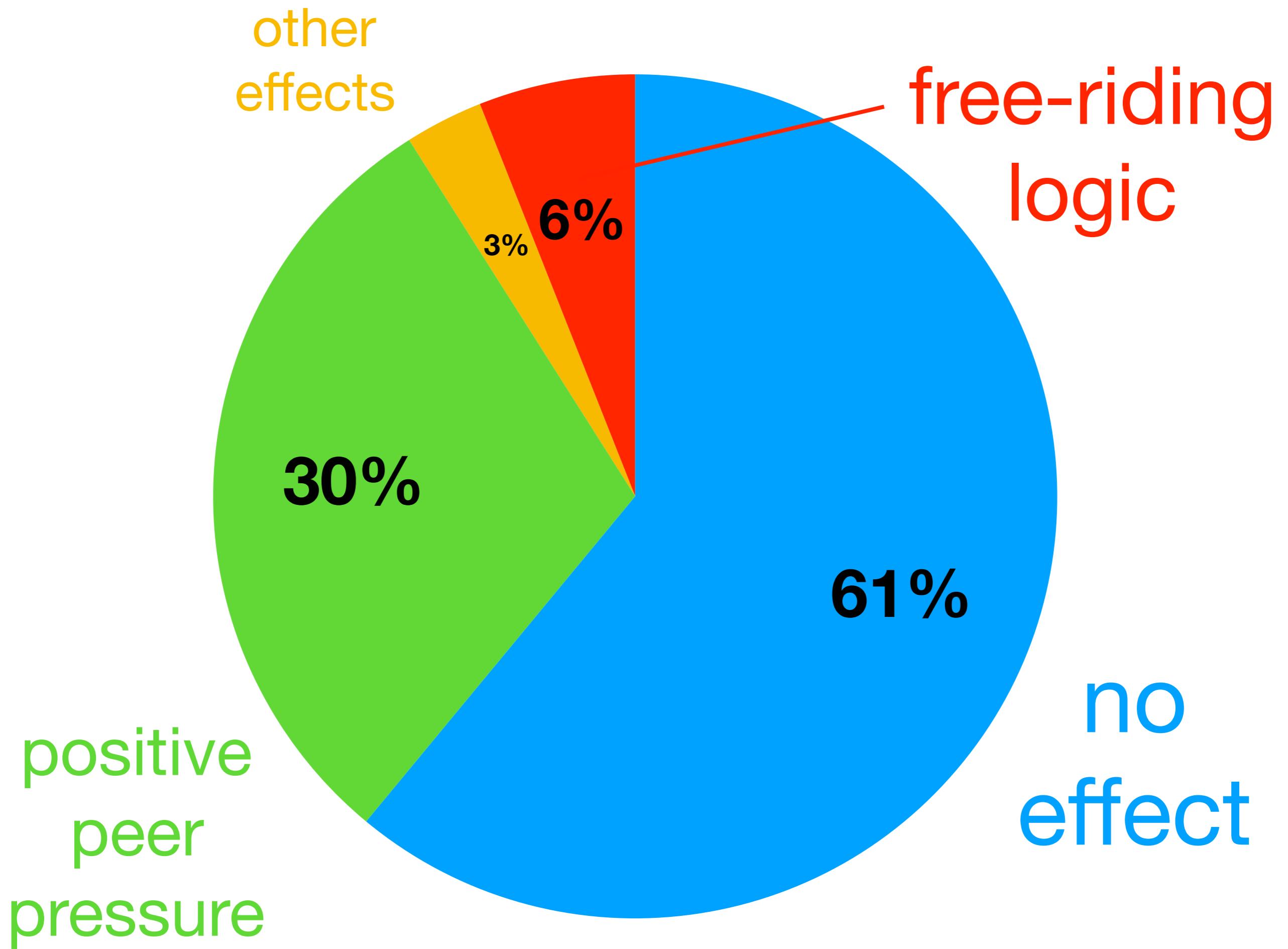
61%

no
effect

positive
peer
pressure







Decision-making framework

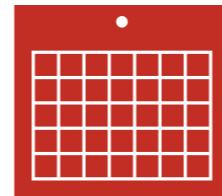
Decision-making framework

- Local (individual-based) information

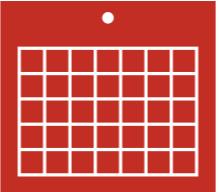


Decision-making framework

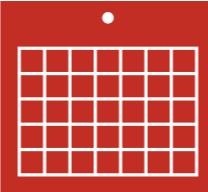
- Local (individual-based) information
- Discrete, annual flu seasons



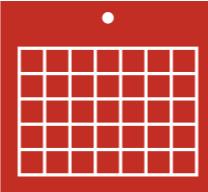
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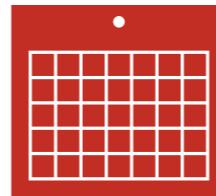
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(with disease or vaccine) 

Decision-making framework

- Local (individual-based) information



- Discrete, annual flu seasons



- Decisions made between each season
- Next decision based on outcome of last decision made

- Winning = not having a bad experience
(with disease or vaccine)



- Win-stay, lose-shift

Notation

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p_{crit}	critical vaccination threshold to achieve herd immunity

Year n

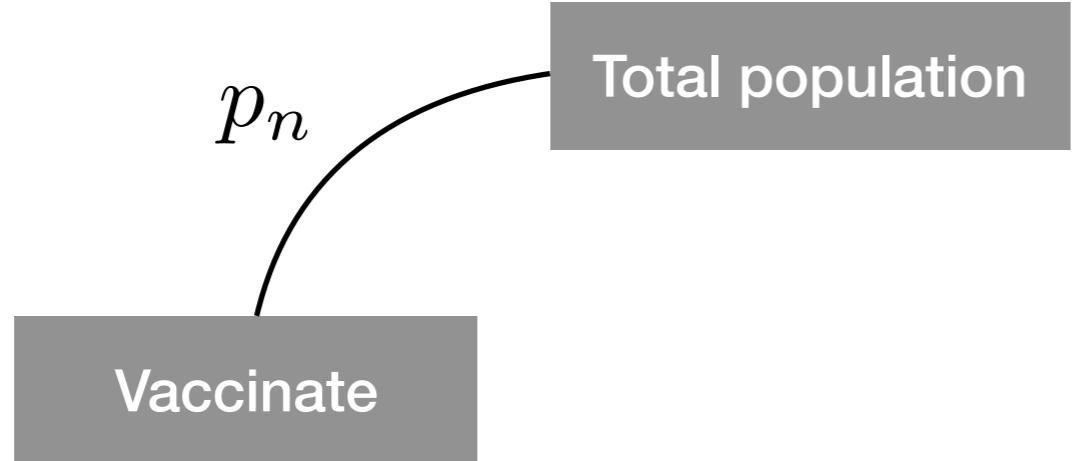
Total population

Year $n+1$

- Vaccinate
- Don't vaccinate

$$p_{n+1} =$$

Year n



Year $n+1$

- Vaccinate
- Don't vaccinate

$$p_{n+1} = \quad + p_n \quad + p_n$$

Year n

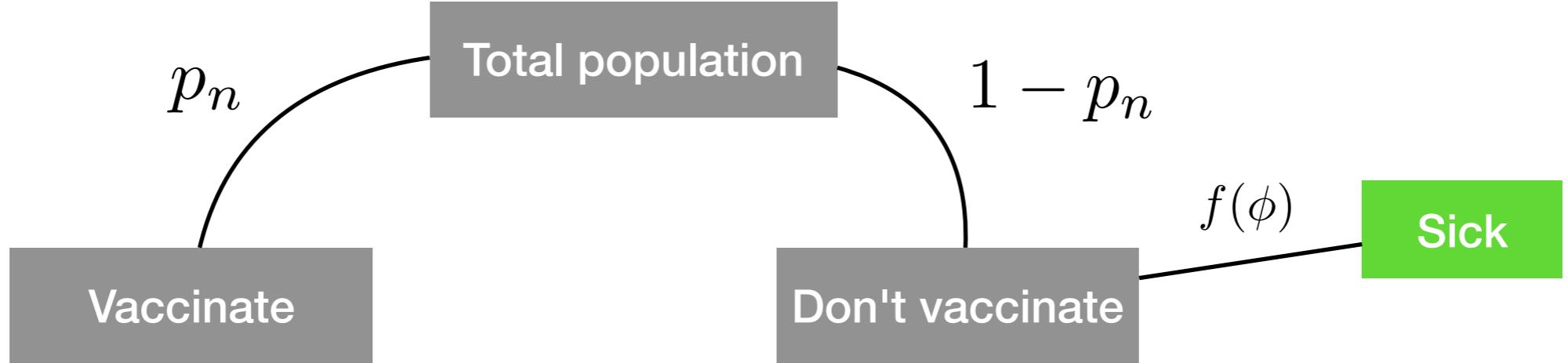


Year $n+1$

- Vaccinate
- Don't vaccinate

$$p_{n+1} = (1 - p_n) + p_n + p_n$$

Year n

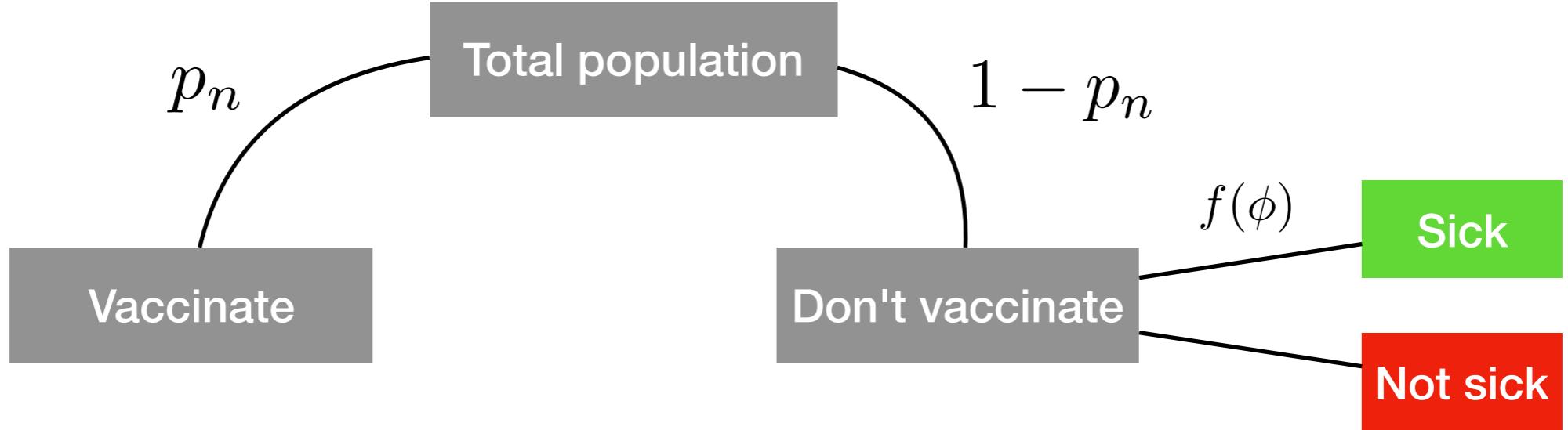


Year $n+1$

- Vaccinate
- Don't vaccinate

$$p_{n+1} = (1 - p_n) \frac{\phi(sp_n)}{1 - sp_n} + p_n$$

Year n

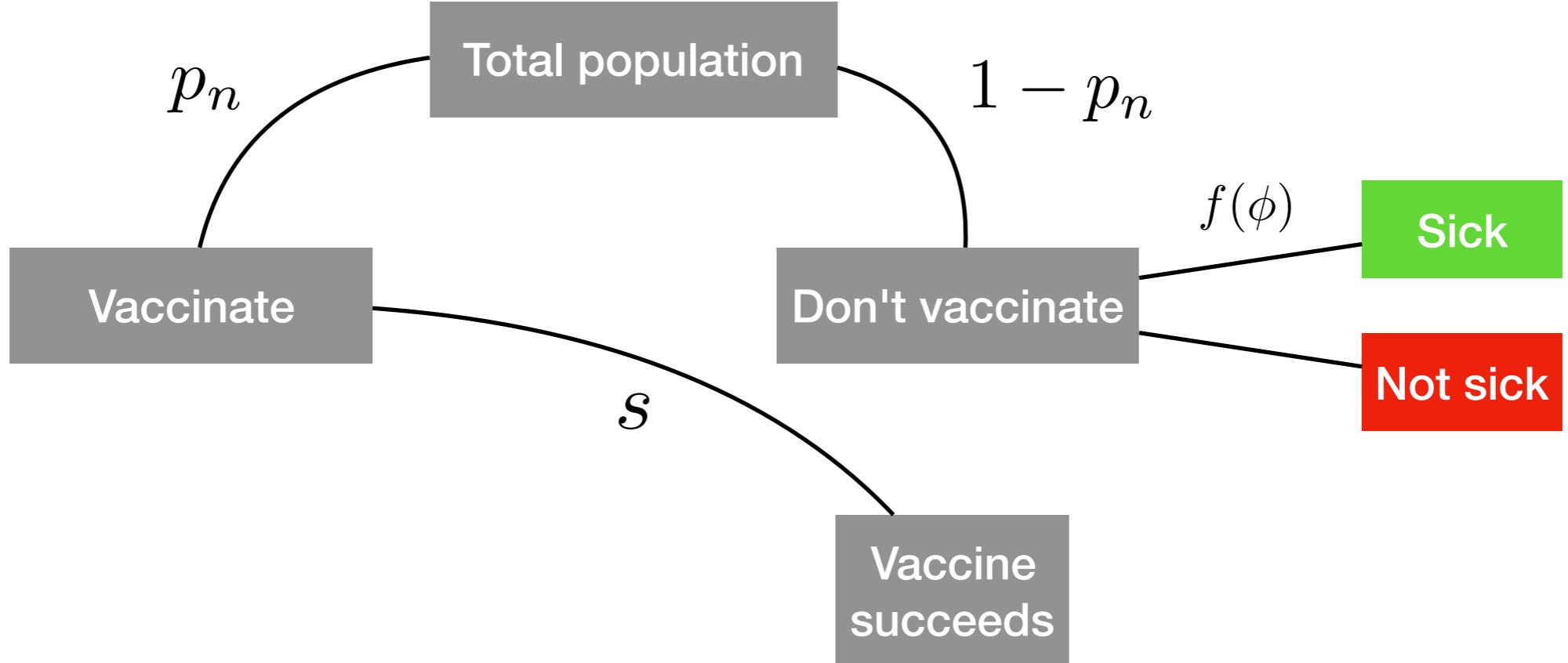


Year $n+1$

- Vaccinate (green square)
- Don't vaccinate (red square)

$$p_{n+1} = (1 - p_n) \frac{\phi(sp_n)}{1 - sp_n} + p_n$$

Year n

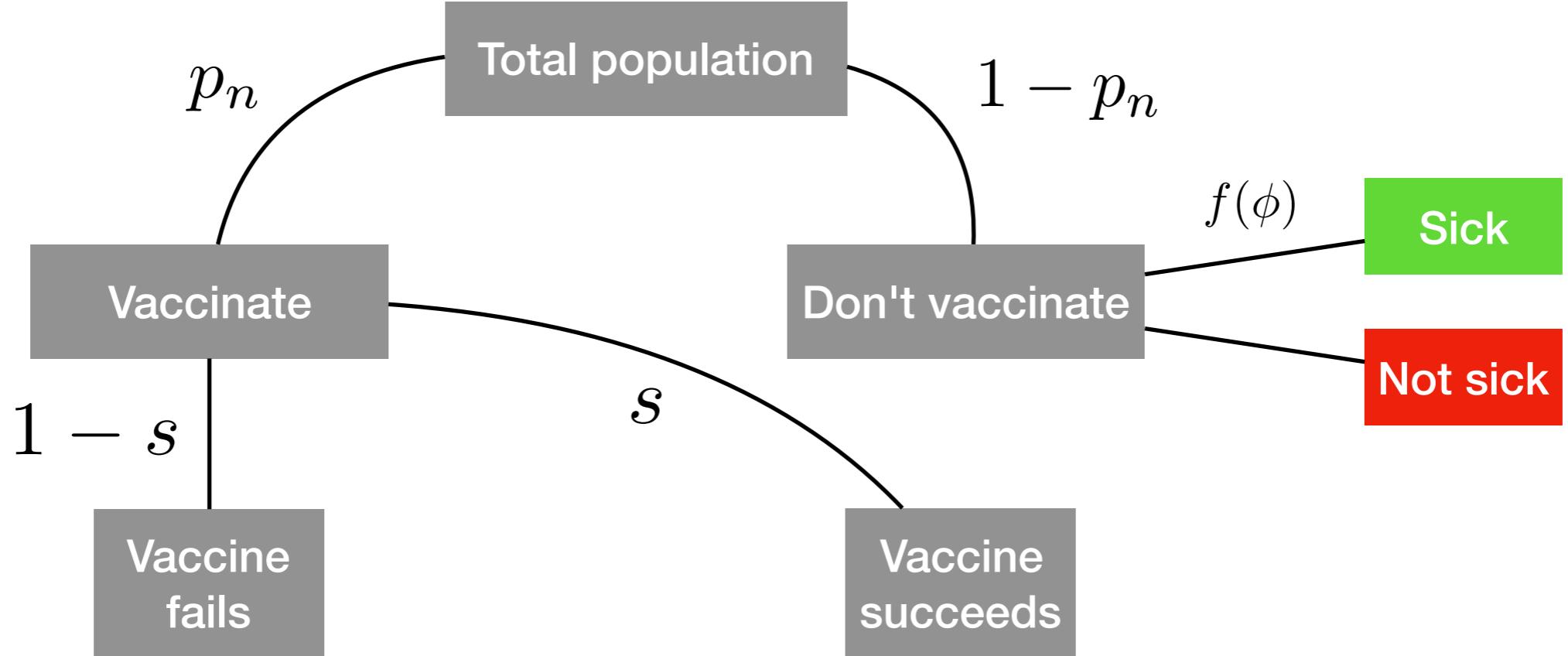


Year $n+1$

- Vaccinate
- Don't vaccinate

$$p_{n+1} = (1 - p_n) \frac{\phi(sp_n)}{1 - sp_n} + p_n$$

Year n

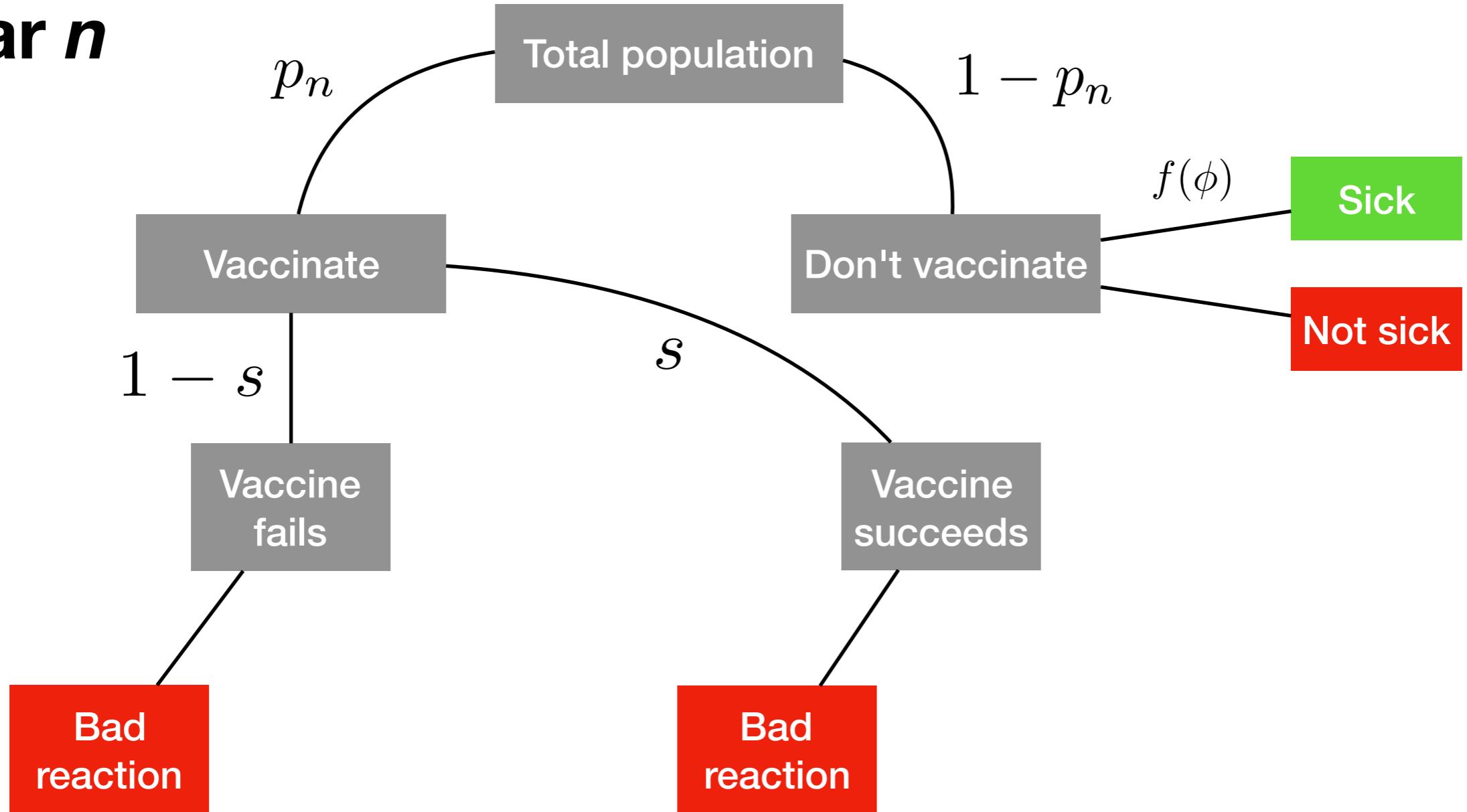


Year $n+1$

- Vaccinate
- Don't vaccinate

$$p_{n+1} = (1 - p_n) \frac{\phi(s p_n)}{1 - s p_n} + p_n s + p_n (1 - s)$$

Year n

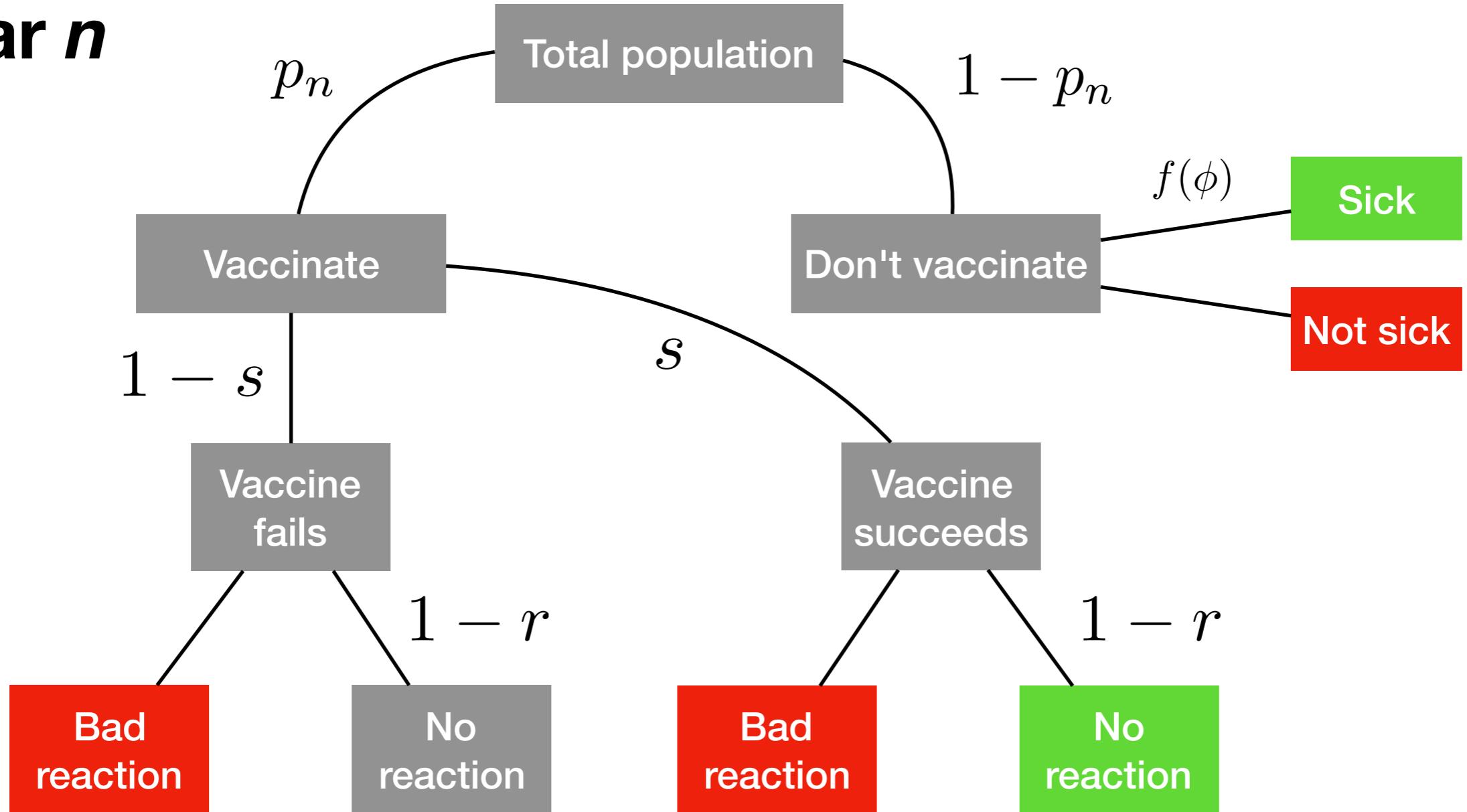


Year $n+1$

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Year n

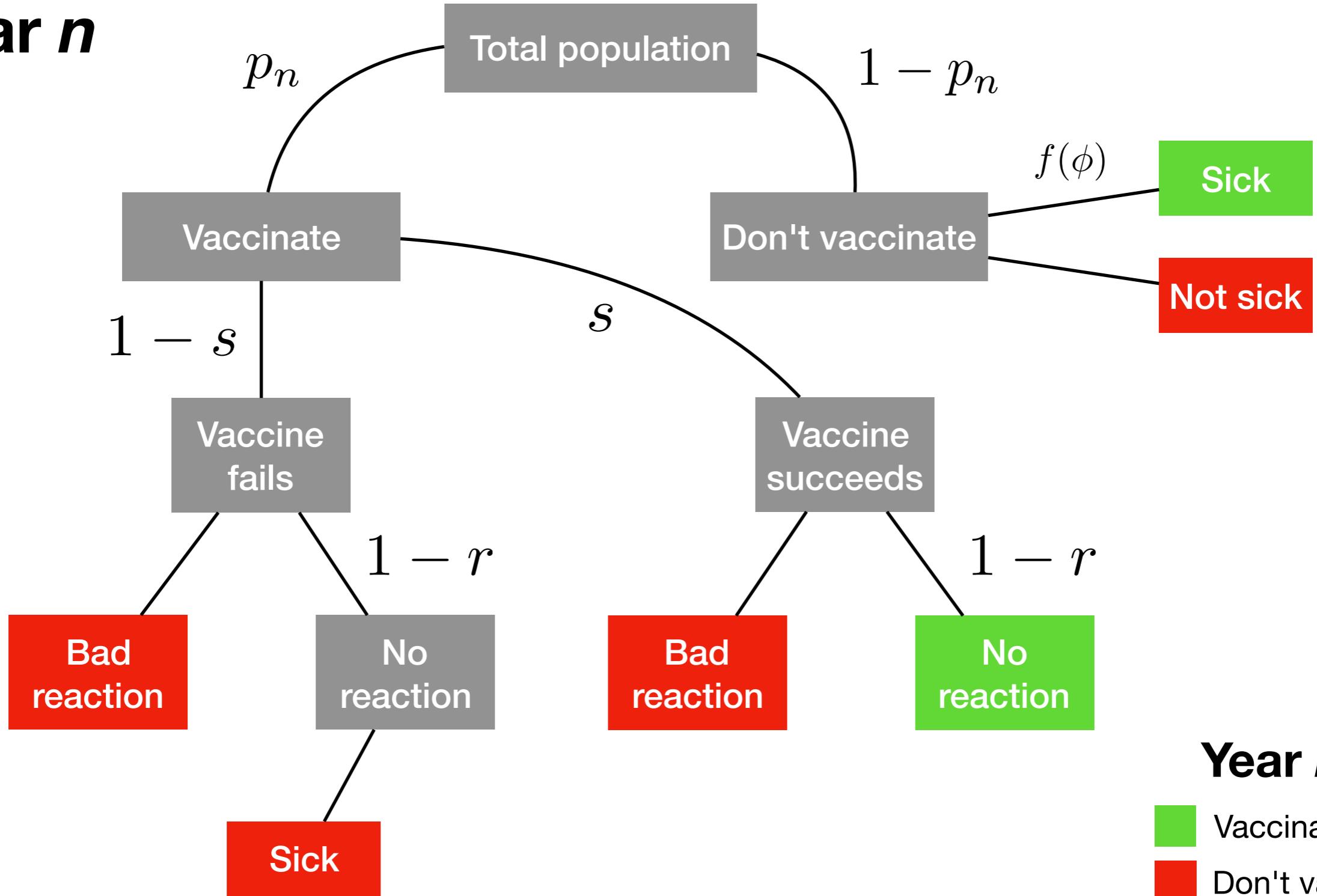


Year $n+1$

- Vaccinate
- Don't vaccinate

$$p_{n+1} = (1 - p_n) \frac{\phi(sp_n)}{1 - sp_n} + p_n s(1 - r) + p_n(1 - s)(1 - r)$$

Year n

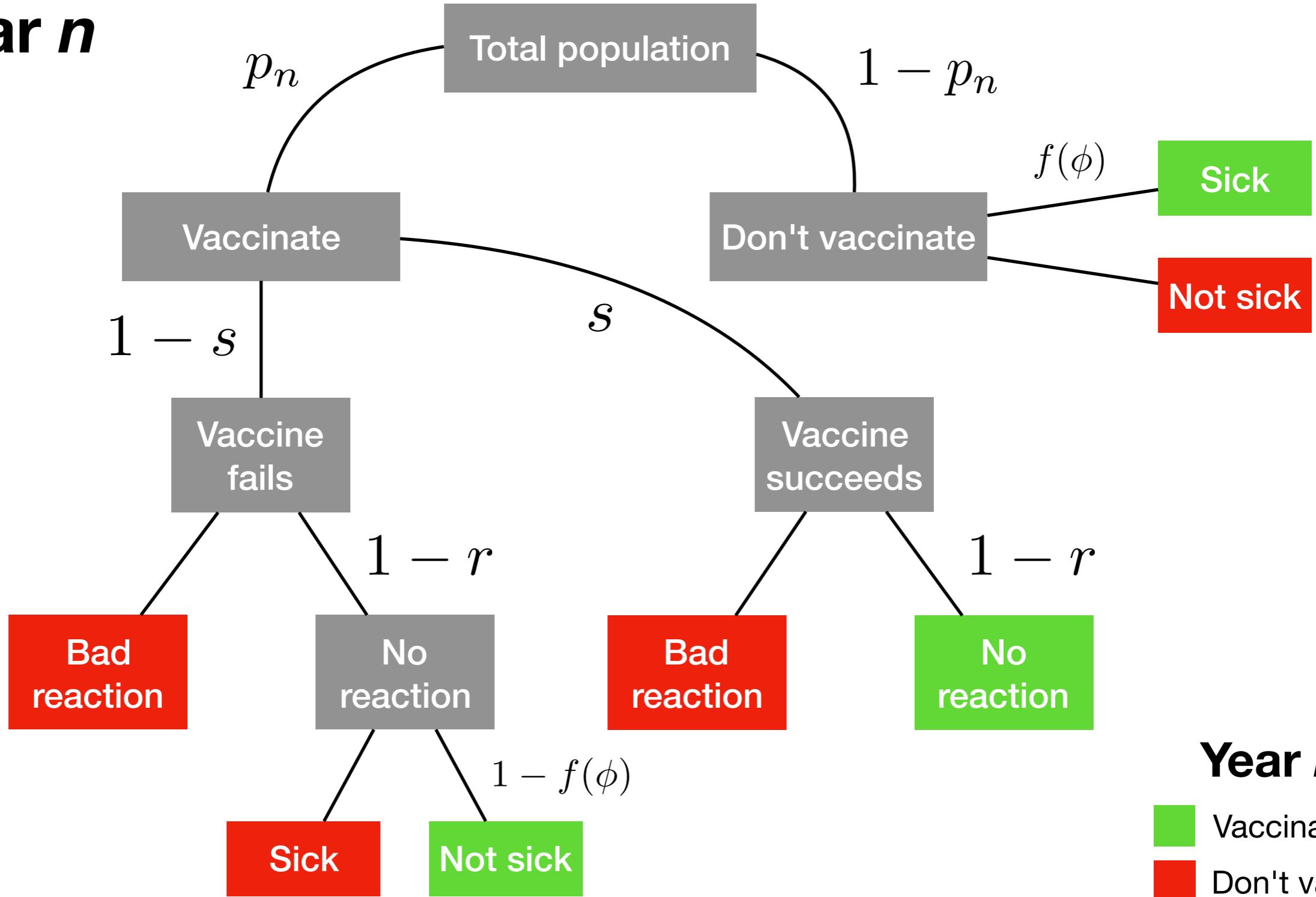


Year $n+1$

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Year n



Year $n+1$

- Vaccinate
- Don't vaccinate

$$p_{n+1} = (1 - p_n) \frac{\phi(sp_n)}{1 - sp_n} + p_n s(1 - r) + p_n(1 - s)(1 - r) \left[1 - \frac{\phi(sp_n)}{1 - sp_n} \right]$$

Central question

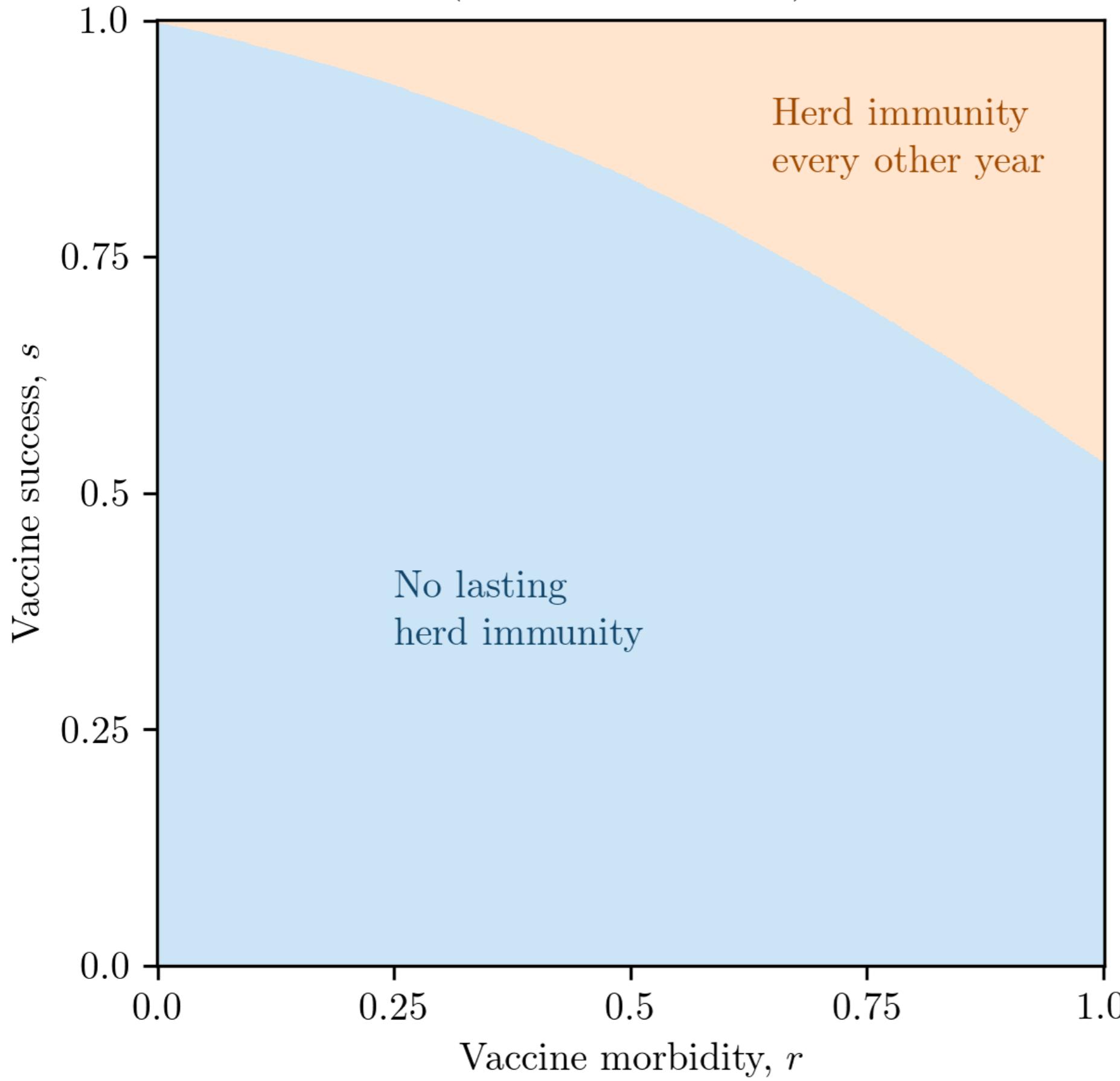
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Can a population
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Model results

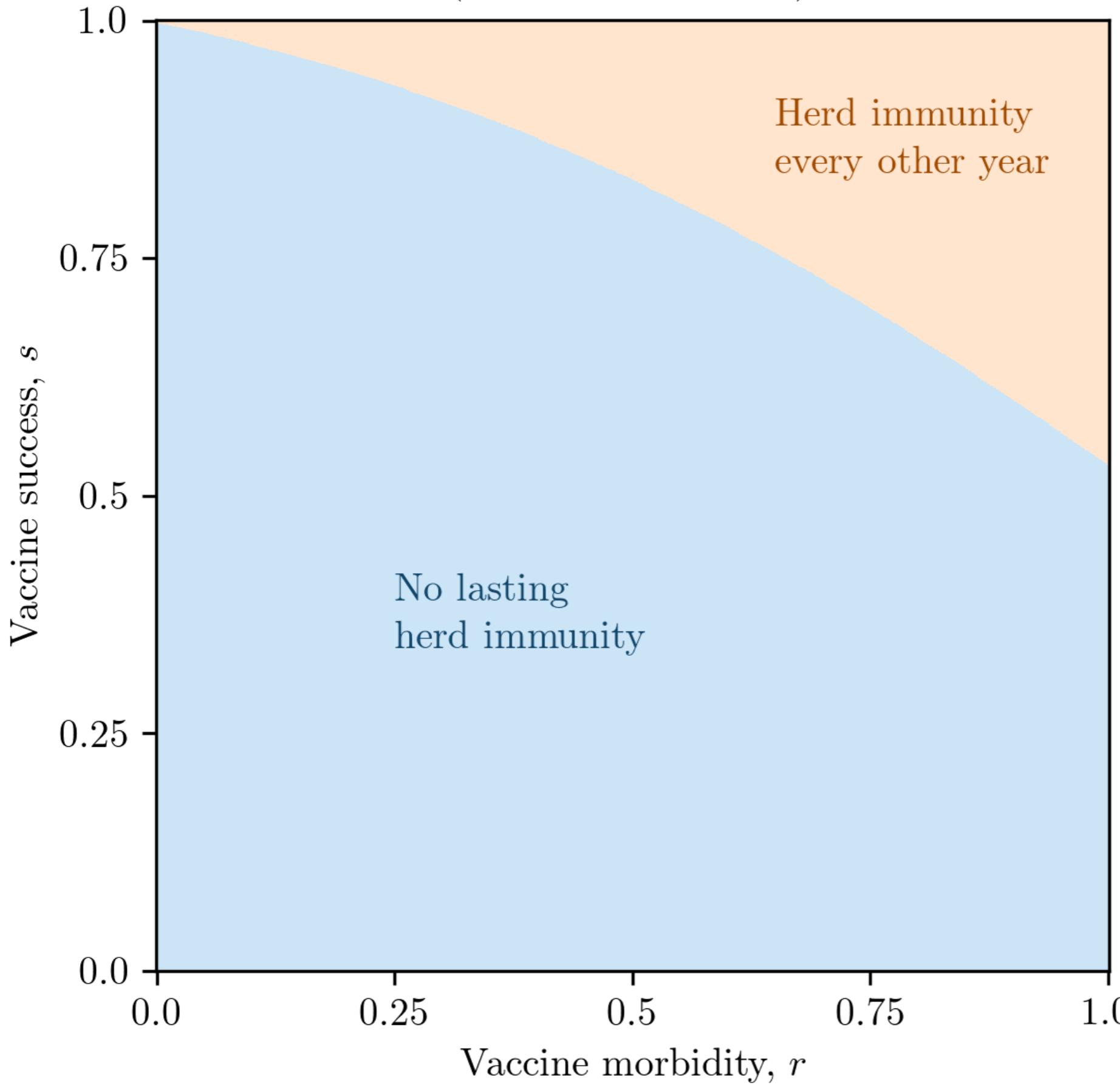
Long-term system behavior

$(\mathcal{R}_0 = 1.4, p_0 = 0)$



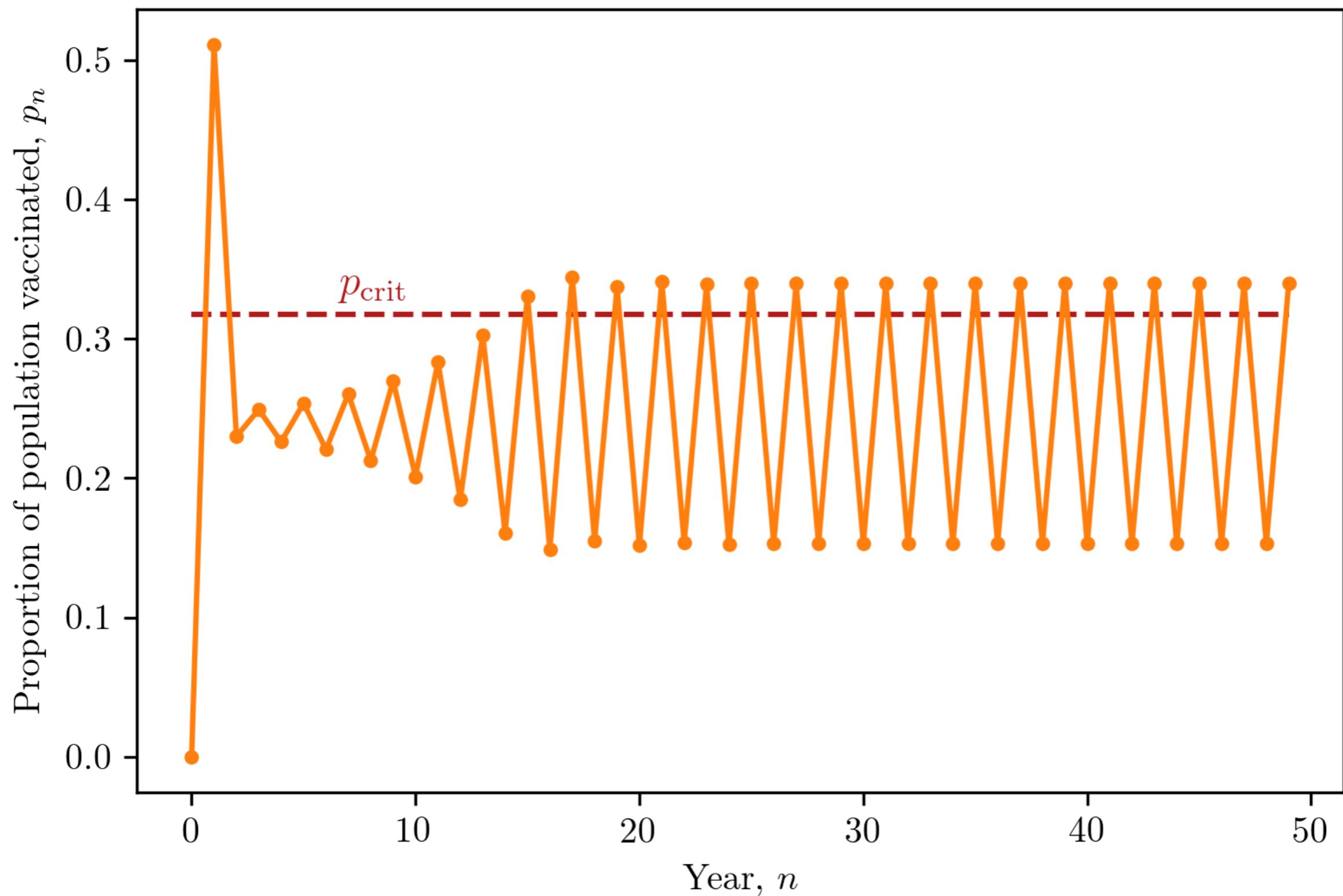
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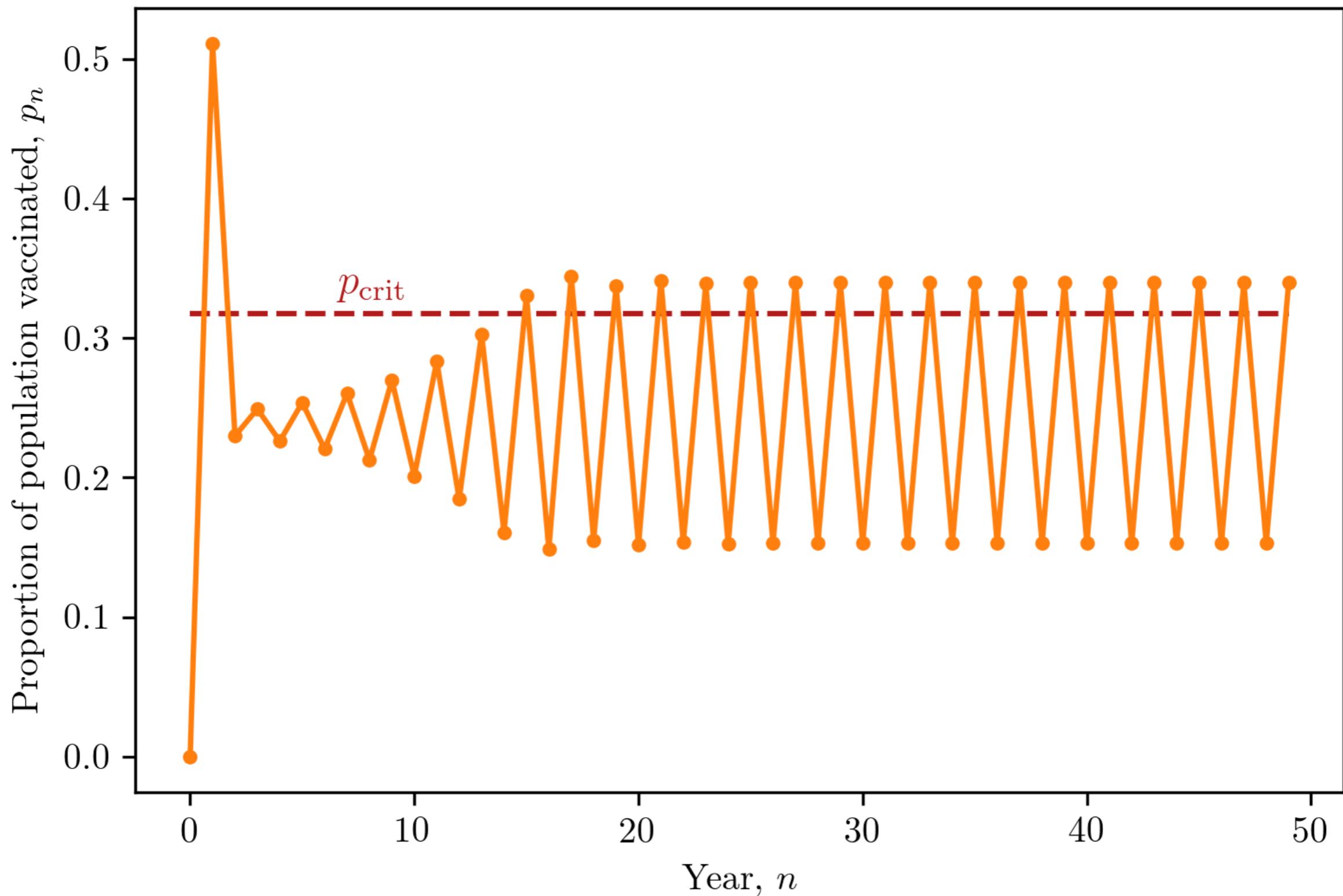


When there is
any cost to the
vaccine
(i.e. $r > 0$),
the system
cannot self-
organize into
herd immunity.

Vaccine coverage level over time
 $(\mathcal{R}_0 = 1.4, r = 0.55, s = 0.9)$



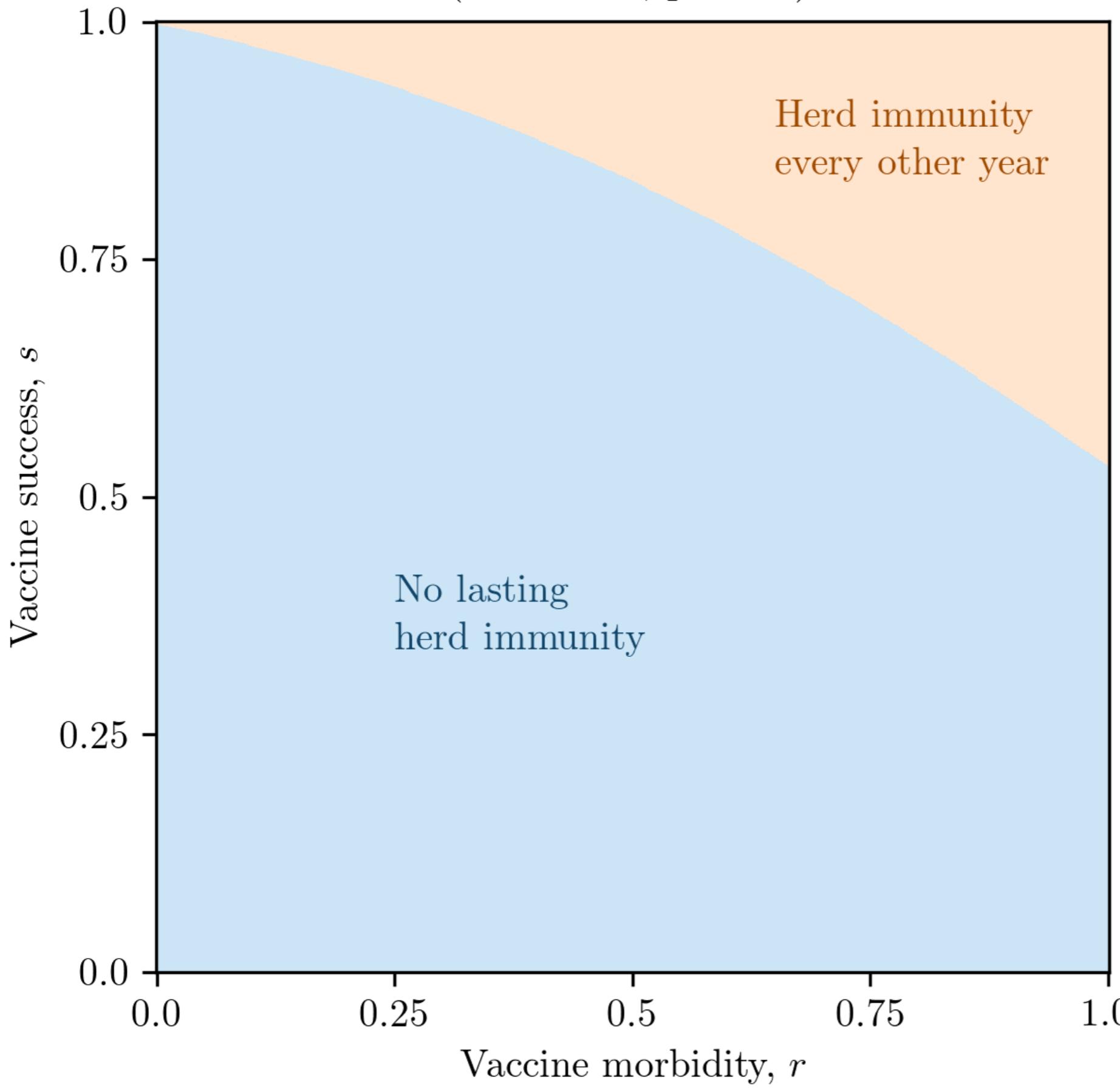
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Even with a **cost** and **imperfect** vaccine, can achieve herd immunity **every other year**.

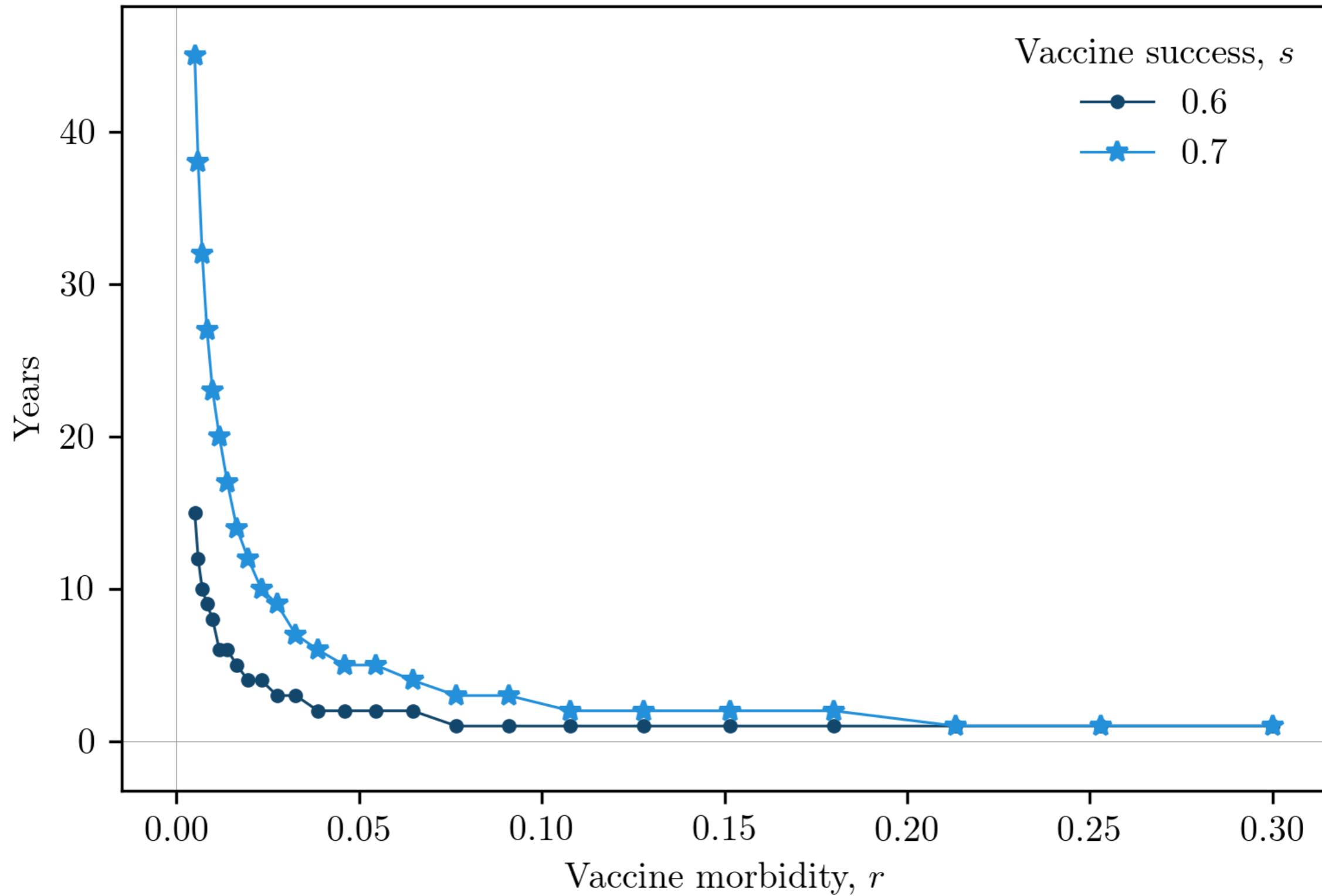
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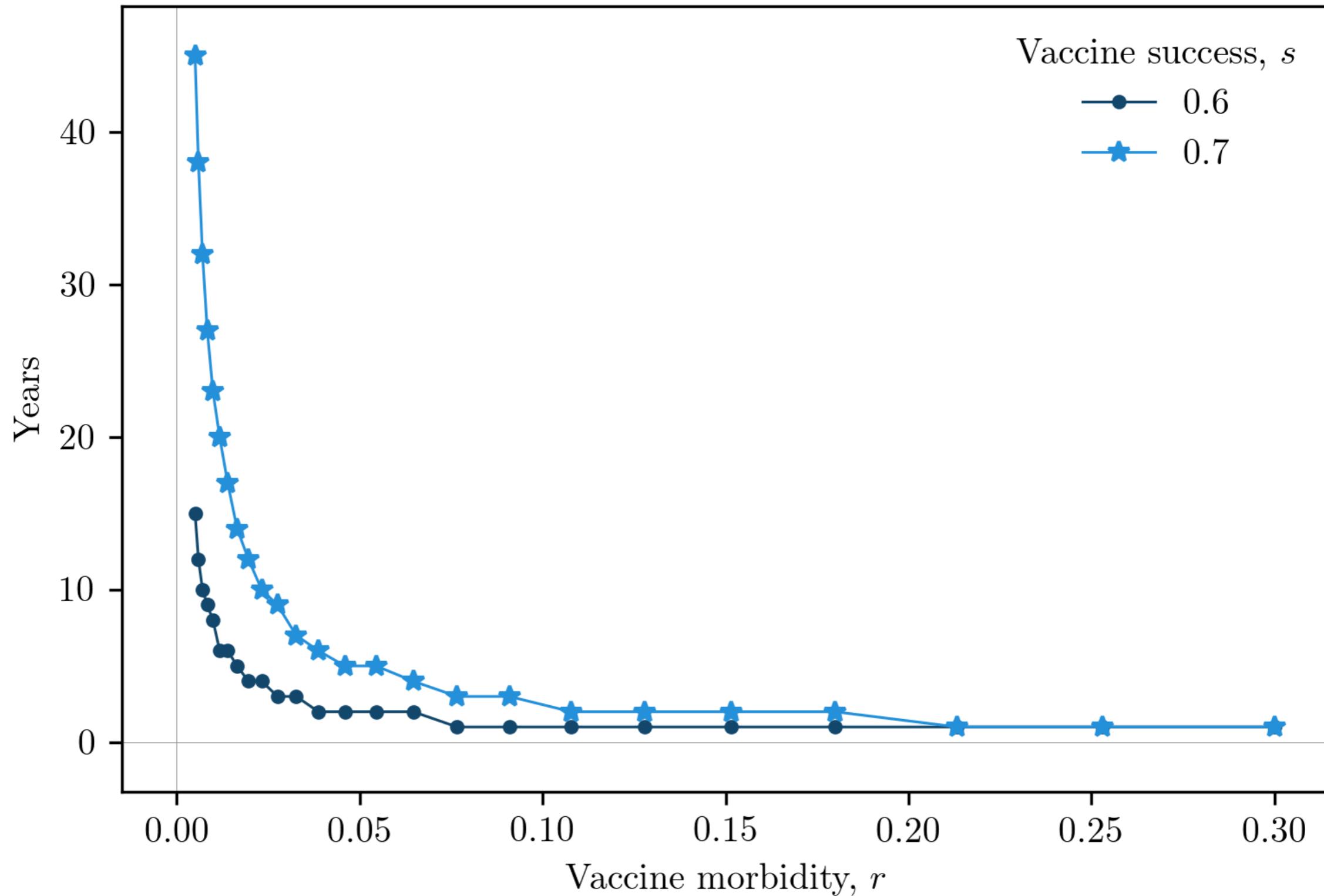


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Number of years spent in HI interval during transient period
 $(\mathcal{R}_0 = 1.4, p_0 = 0)$

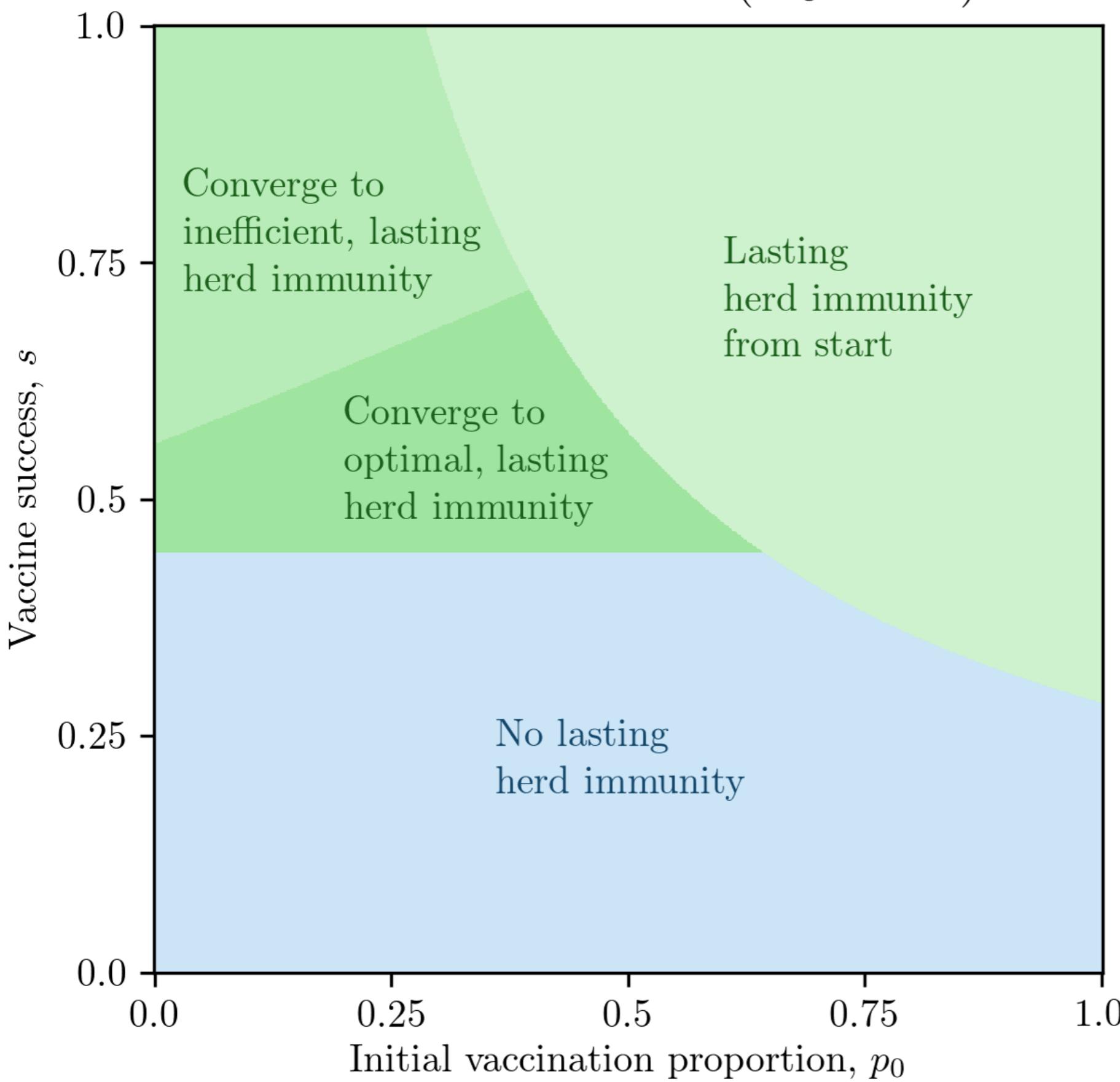


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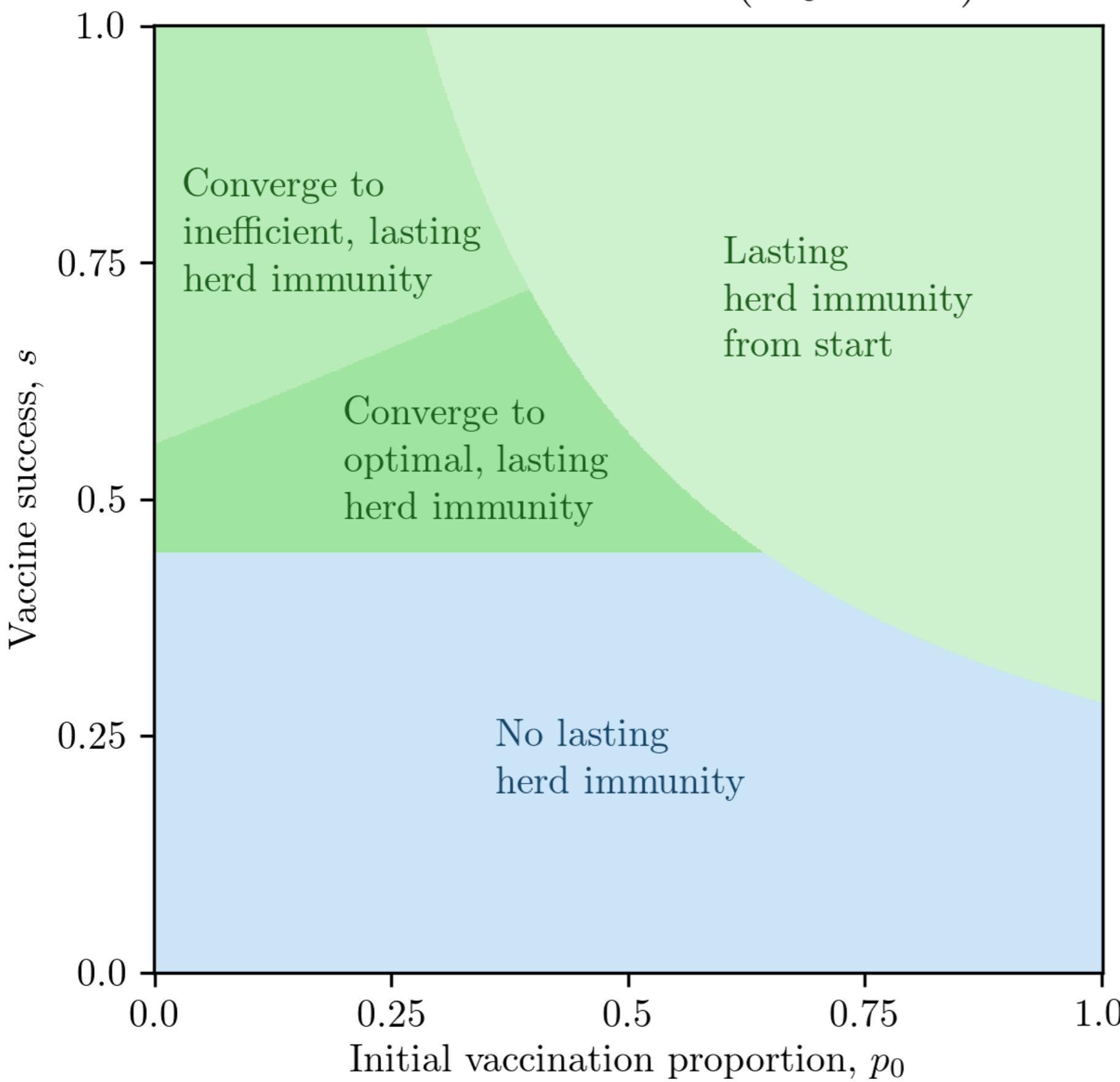


Long transients in the herd immunity interval
open the door for public health **interventions**.

Long-term system behavior with no vaccine cost ($\mathcal{R}_0 = 1.4$)

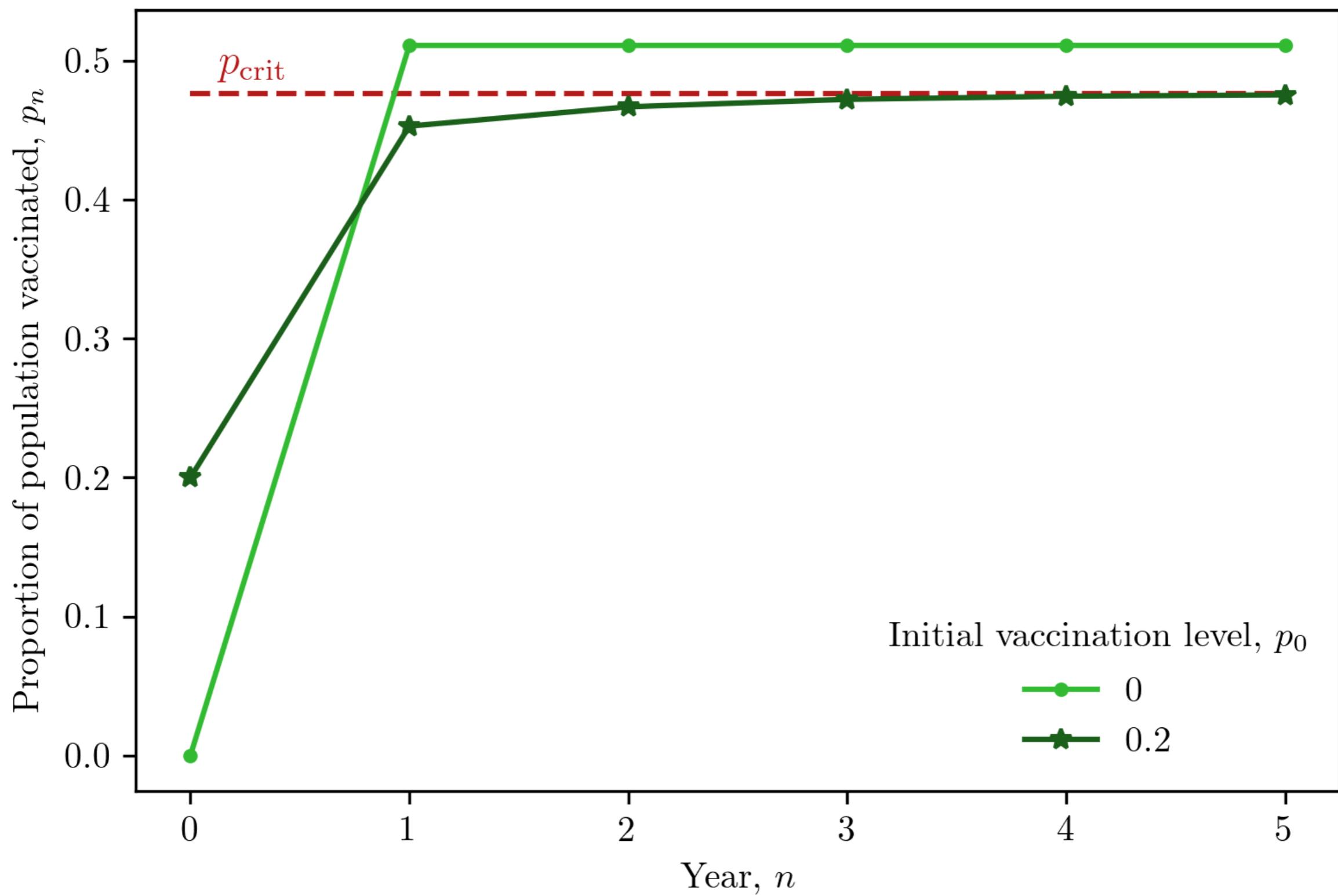


Long-term system behavior with no vaccine cost ($\mathcal{R}_0 = 1.4$)

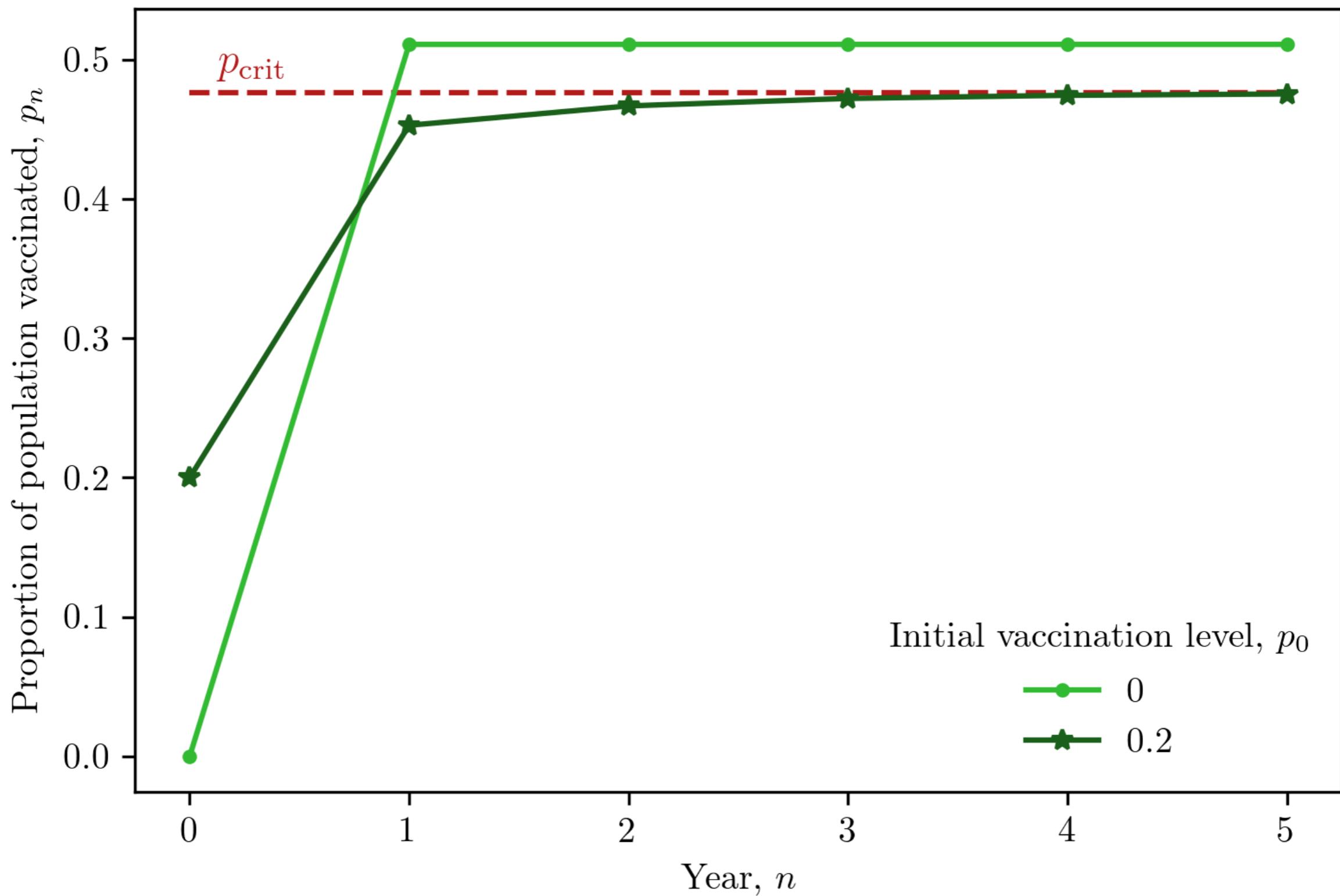


Self-organized herd immunity can be achieved (with no vaccine cost) even if the vaccine is only moderately effective.

Vaccine coverage level over time
 $(\mathcal{R}_0 = 1.4, r = 0, s = 0.6)$



Vaccine coverage level over time
 $(\mathcal{R}_0 = 1.4, r = 0, s = 0.6)$



**Inefficient herd immunity results from an overreaction
& optimal from gradual learning.**



Thank you!



Thank you!



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