

**LISTS**

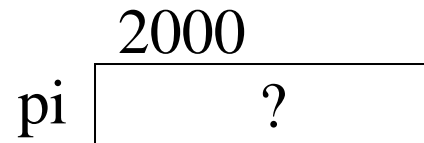
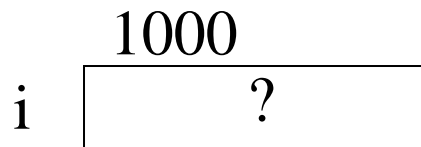
# Introduction

- Array
  - successive items located at fixed distance apart
- disadvantage
  - data movements during insertion and deletion
  - waste space in storing  $n$  ordered lists of varying size
- possible solution
  - linked list

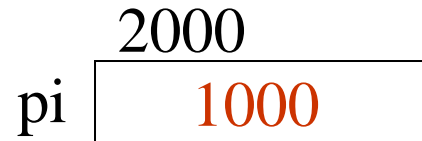
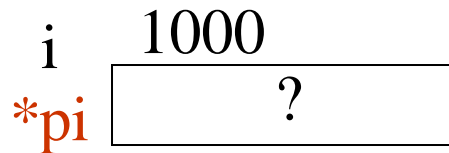
# Pointer Review (1)

## Pointer Can Be Dangerous

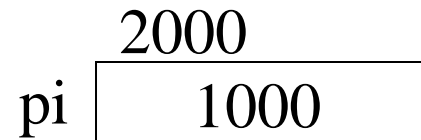
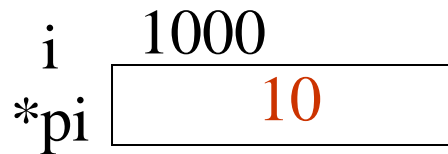
```
int i, *pi;
```



```
pi = &i;
```



```
i = 10 or *pi = 10
```

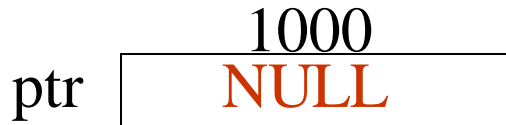


- Set to NULL
- Explicit typecasts

## Pointer Review (2)

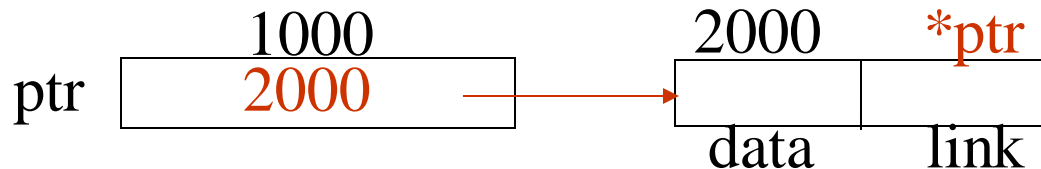
```
typedef struct list_node *list_pointer;  
typedef struct list_node {  
    int data;  
    list_pointer link;  
}
```

```
list_pointer ptr = NULL;
```

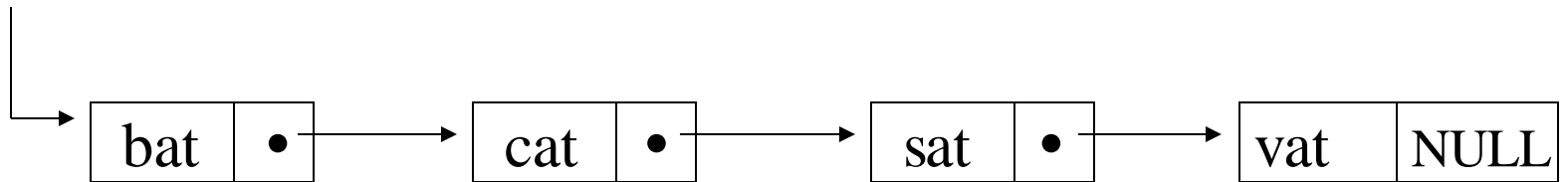


ptr->data ? (\*ptr).data

```
ptr = malloc(sizeof(list_node));
```

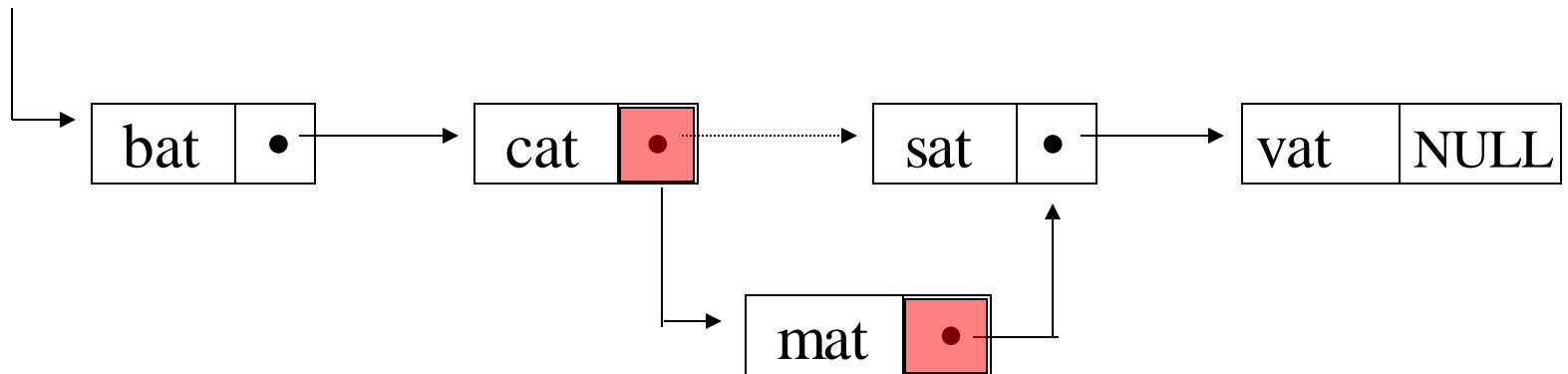


## 4.2 SINGLY LINKED LISTS

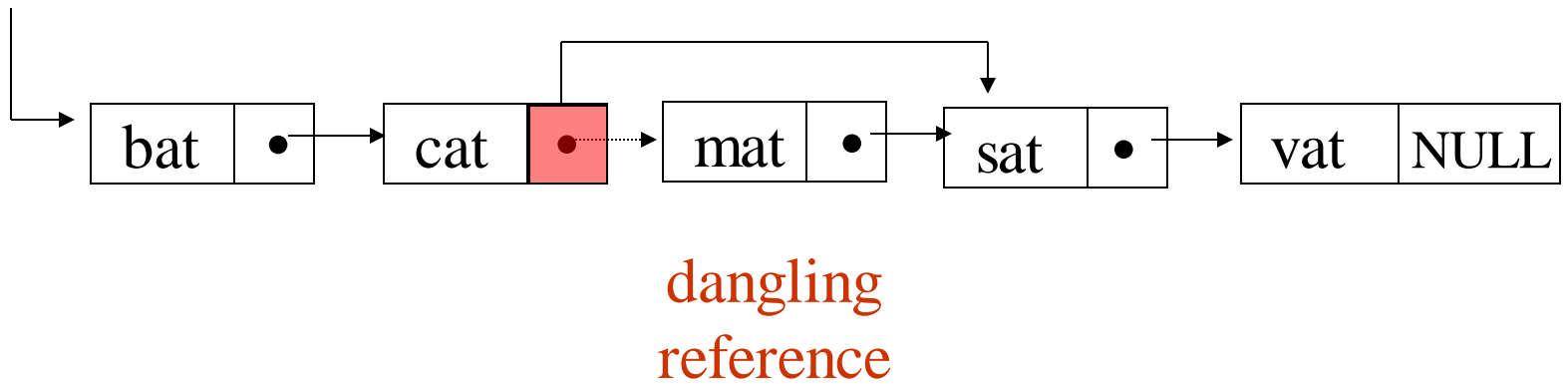


**\*Figure 4.1:** Usual way to draw a linked list

## Insertion



**\*Figure 4.2:** Insert mat after cat



**\*Figure 4.3:** Delete *mat* from list

## Example 4.1: create a linked list of words

### Declaration

```
typedef struct list_node *list_pointer;  
typedef struct list_node {  
    char data [4];  
    list_pointer link;  
};
```

### Creation

```
list_pointer ptr =NULL;
```

### Testing

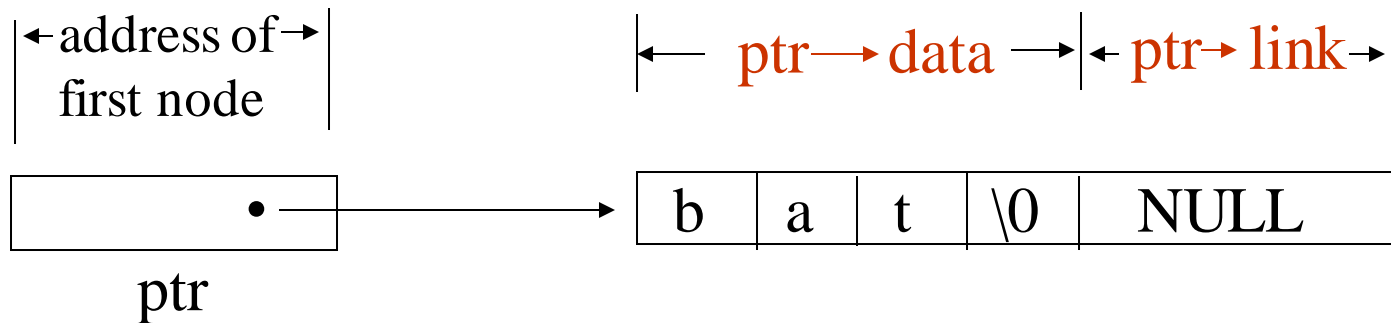
```
#define IS_EMPTY(ptr) (!(ptr))
```

### Allocation

```
ptr=(list_pointer) malloc (sizeof(list_node));
```

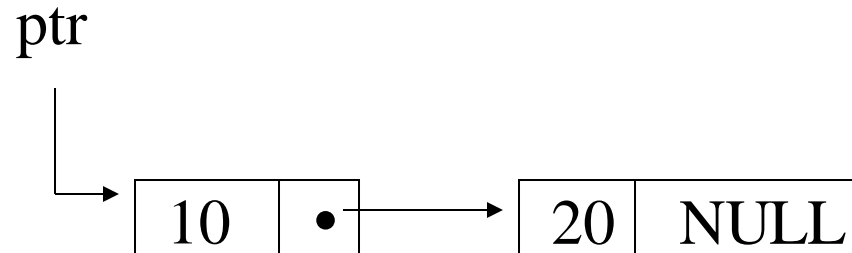


```
strcpy(ptr -> data, "bat");  
ptr -> link = NULL;
```



**\*Figure 4.4: Referencing the fields of a node(p.142)**

## Example: create a two-node list



```
typedef struct list_node *list_pointer;  
struct list_node {  
    int data;  
    list_pointer link;  
};  
list_pointer ptr = NULL
```

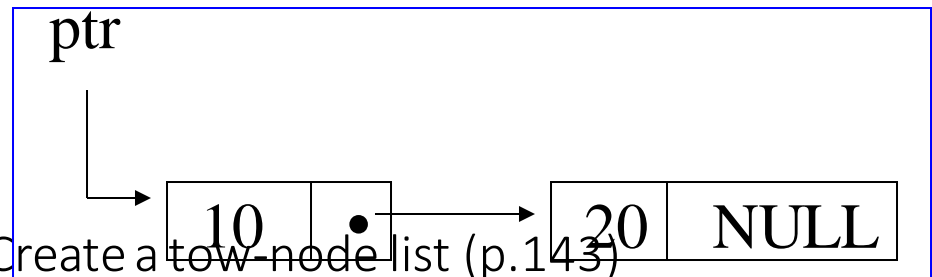
Example 4.2: (p.142)

```

list_pointer create2( )
{
/* create a linked list with two nodes */
list_pointer first, second;

first = (list_pointer) malloc(sizeof(list_node)); // new list_node;
second = (list_pointer) malloc(sizeof(list_node)); // new list_node
second -> link = NULL;
second -> data = 20;
first -> data = 10;
first -> link = second;
return first;
}

```



**\*Program 4.2:** Create a two-node list (p.143)

# List Insertion:

Insert a node after a specific node

```
void insert(list_pointer *ptr, list_pointer node)
{
    /* insert a new node with data = 50 into the list ptr after node */
    list_pointer temp;

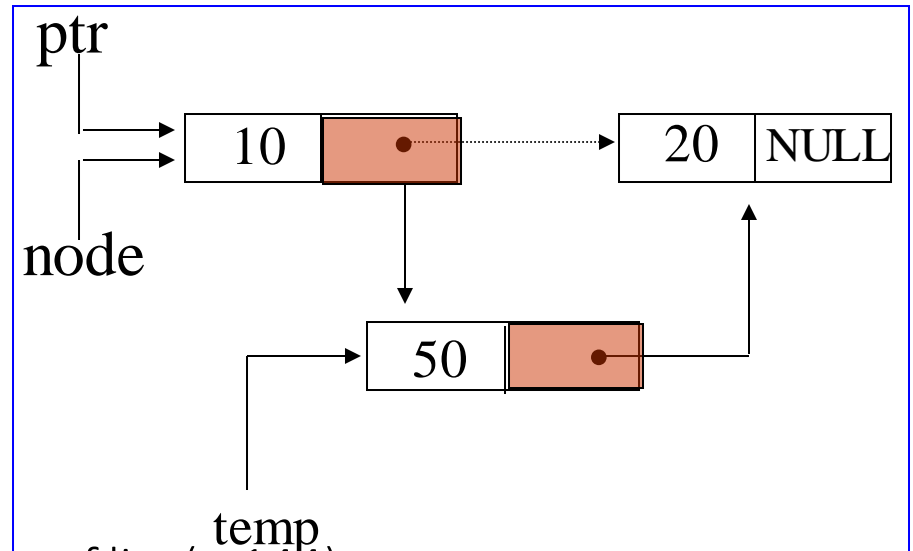
    temp = (list_pointer) malloc(sizeof(list_node));

    if (IS_FULL(temp)){
        cout<<"The memory is full\n";
        exit (1);
    }
```

```

temp->data = 50;
if (*ptr) { noempty list
    temp->link = node ->link;
    node->link = temp;
}
else { empty list
    temp->link = NULL;
    *ptr = temp;
}
}

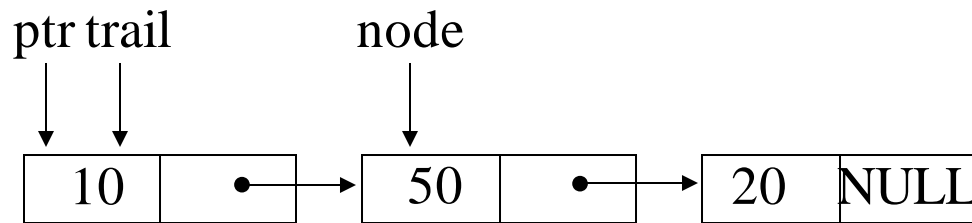
```



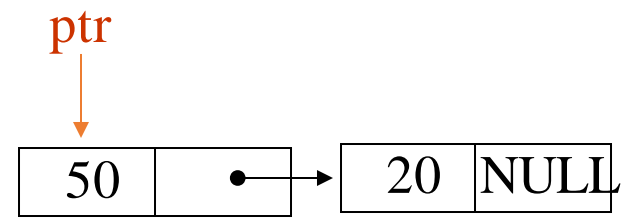
\*Program 4.3: Simple insert into front of list (p.144)

# List Deletion

Delete the first node.

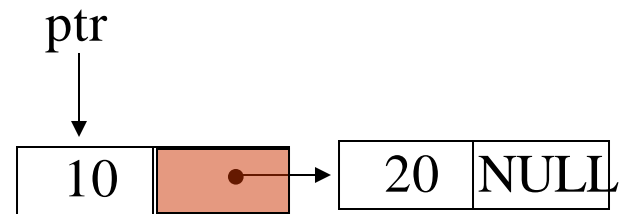
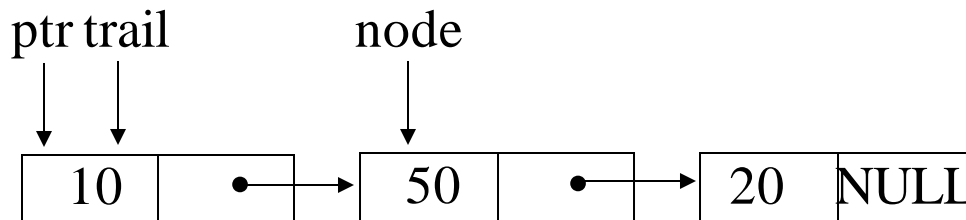


(a) before deletion



(b) after deletion

Delete node other than the first node.



```
void delete(list_pointer *ptr, list_pointer trail, list_pointer
node)
```

```
{
/* delete node from the list, trail is the preceding node
ptr is the head of the list */
```

```
if (trail)
```

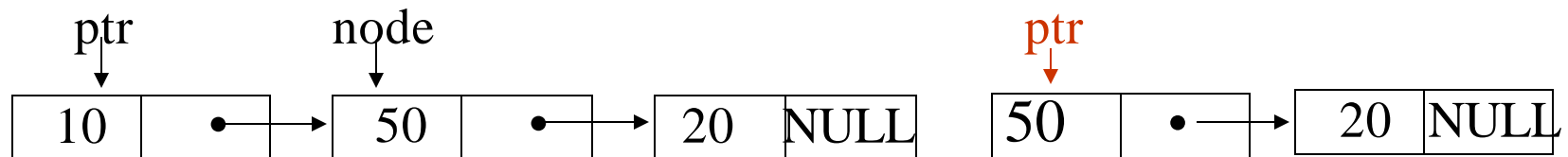
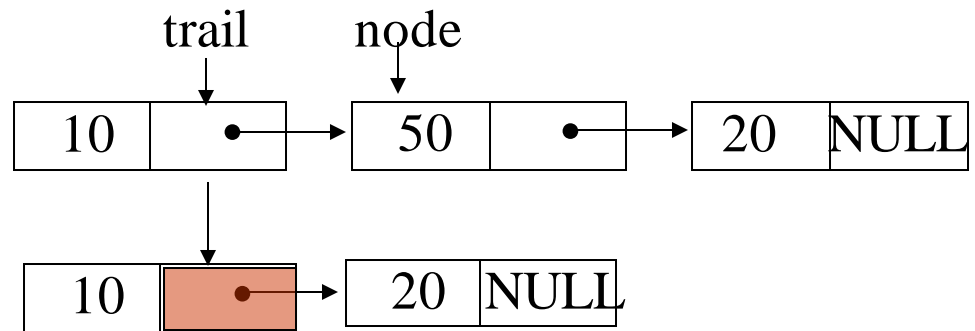
```
    trail->link = node->link;
```

```
else
```

```
    *ptr = (*ptr) ->link;
```

```
    free(node);
```

```
}
```



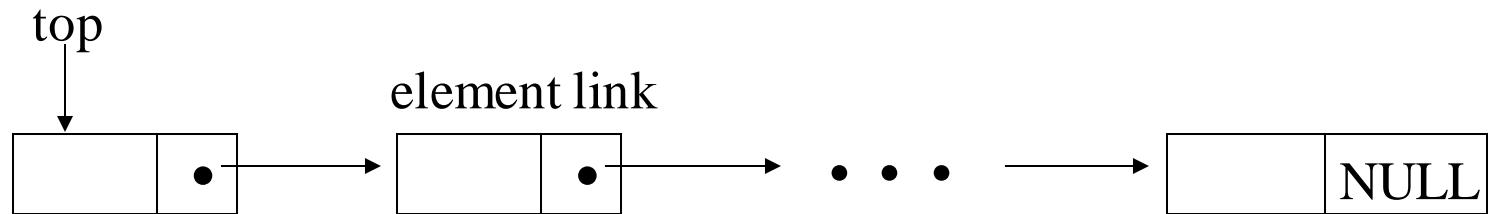
## Print out a list (traverse a list)

```
void print_list(list_pointer ptr)
{
    printf("The list contains: ");
    for ( ; ptr; ptr = ptr->link)
        printf("%4d", ptr->data);
    printf("\n");
}
```

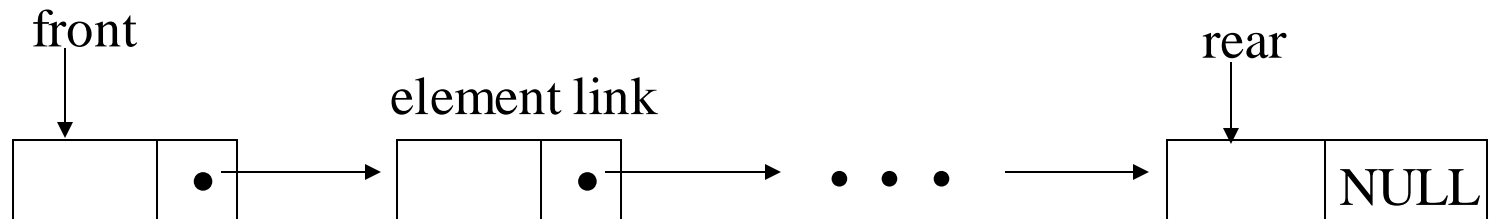
\*Program 4.5: Printing a list (p.146)



## 4.3 DYNAMICALLY LINKED STACKS AND QUEUES



(a) Linked Stack



(b) Linked queue

**\*Figure 4.10: Linked Stack and queue (p.147)**

## Push in the linked stack

```
void add(stack_pointer *top, element item)
{
    /* add an element to the top of the stack */
    stack_pointer temp =
        (stack_pointer) malloc (sizeof (stack));
    if (IS_FULL(temp)) {
        fprintf(stderr, "The memory is full\n");
        exit(1);
    }
    temp->item = item;
    temp->link = *top;
    *top = temp;
}
```

\*Program 4.6: Add to a linked stack (p.149)

## pop from the linked stack

```
element delete(stack_pointer *top) {  
    /* delete an element from the stack */  
    stack_pointer temp = *top;  
    element item;  
    if (IS_EMPTY(temp)) {  
        fprintf(stderr, "The stack is empty\n");  
        exit(1);  
    }  
    item = temp->item;  
    *top = temp->link;  
    free(temp);  
    return item;  
}
```

\*Program 4.7: Delete from a linked stack (p.149)

## enqueue in the linked queue

```
void addq(queue_pointer *front, queue_pointer *rear, element item)
{ /* add an element to the rear of the queue */
    queue_pointer temp =
        (queue_pointer) malloc(sizeof (queue));
    if (IS_FULL(temp)) {
        fprintf(stderr, " The memory is full\n");
        exit(1);
    }
    temp->item = item;
    temp->link = NULL;
    if (*front) (*rear) -> link = temp;
    else *front = temp;
    *rear = temp; }
```

dequeue from the linked queue (similar to push)

```
element deleteq(queue_pointer *front) {  
    /* delete an element from the queue */  
    queue_pointer temp = *front;  
    element item;  
    if (IS_EMPTY(*front)) {  
        fprintf(stderr, "The queue is empty\n");  
        exit(1);  
    }  
    item = temp->item;  
    *front = temp->link;  
    free(temp);  
    return item;  
}
```

# Polynomials

$$A(x) = a_{m-1}x^{e_{m-1}} + a_{m-2}x^{e_{m-2}} + \dots + a_0x^{e_0}$$

## Representation

```
typedef struct poly_node *poly_pointer;
```

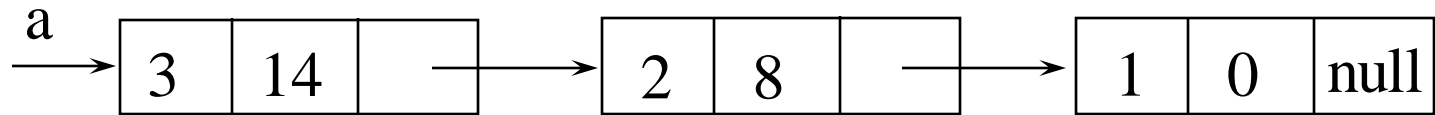
```
typedef struct poly_node {  
    int coef;  
    int expon;  
    poly_pointer link;  
};
```

coef	expon	link
------	-------	------

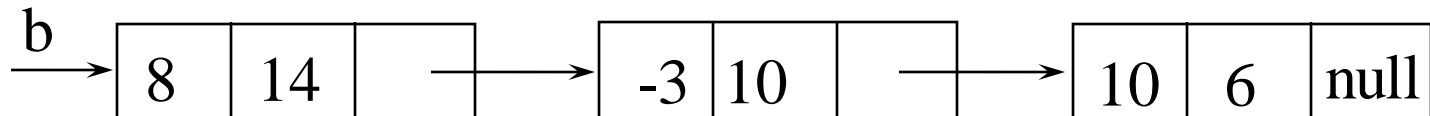
```
poly_pointer a, b, c;
```

## Examples

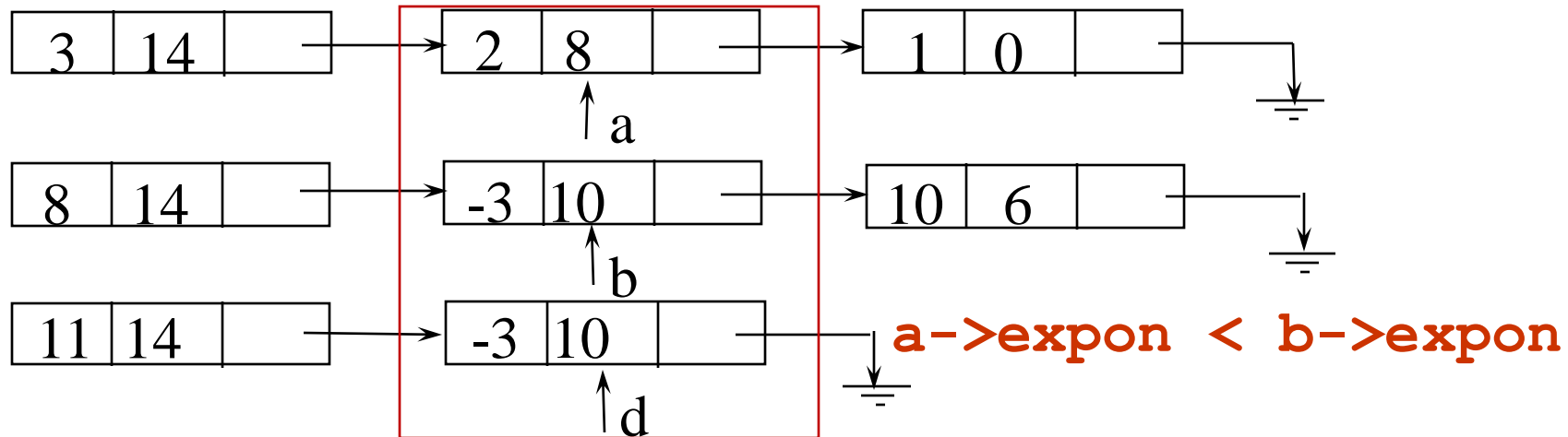
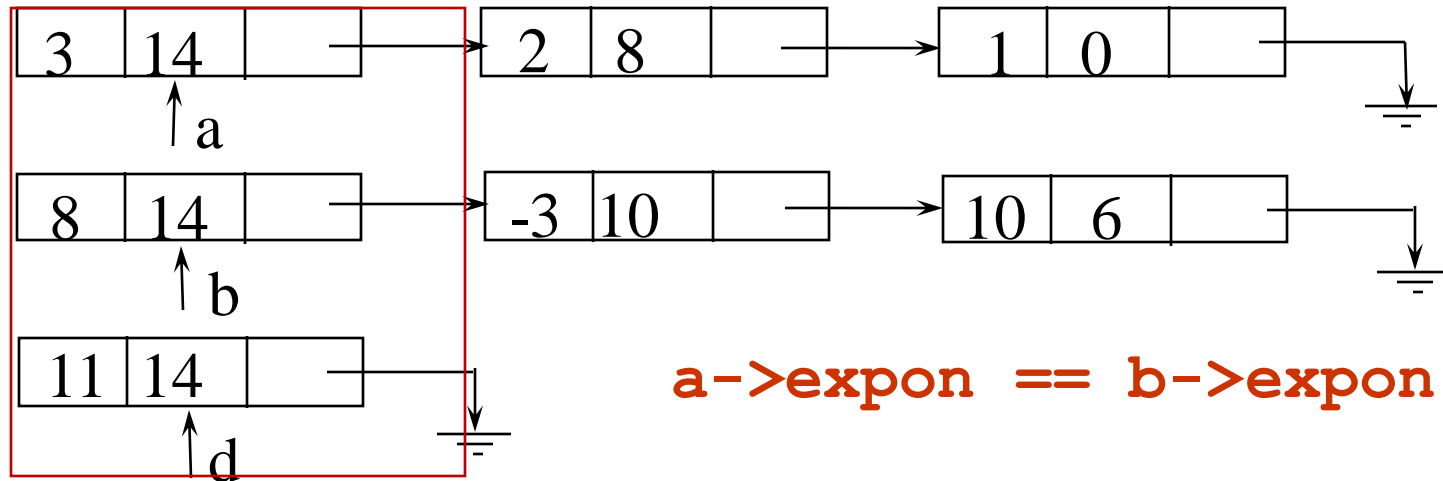
$$a = 3x^{14} + 2x^8 + 1$$



$$b = 8x^{14} - 3x^{10} + 10x^6$$

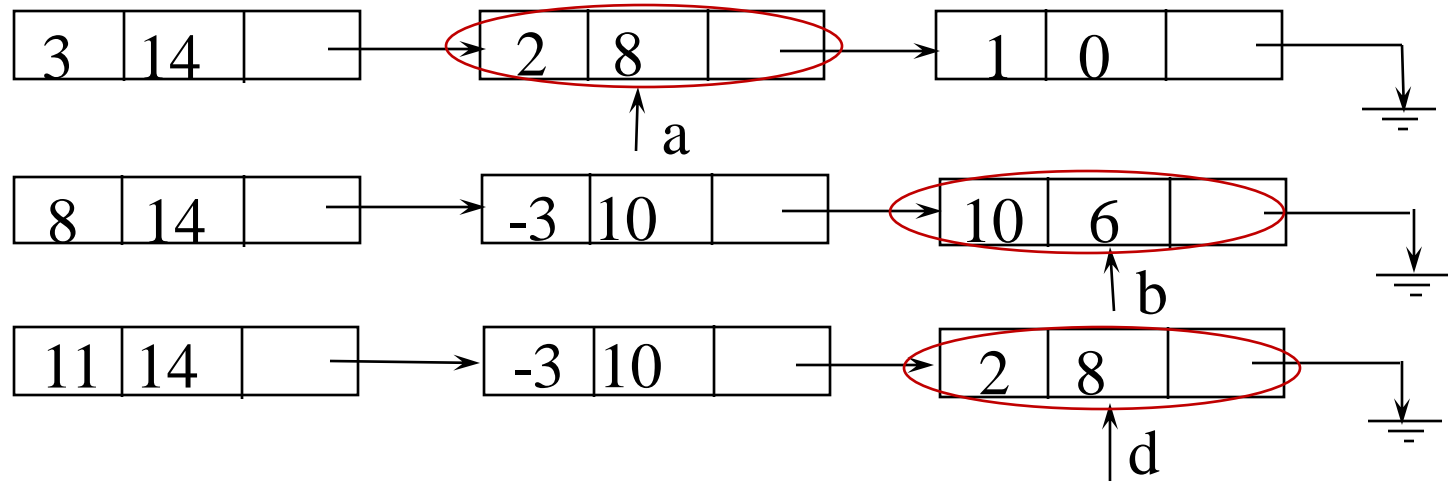


# Adding Polynomials





## Adding Polynomials (*Continued*)



**a->expon > b->expon**

# Algorithm for Adding Polynomials

```
poly_pointer padd(poly_pointer a,  
                  poly_pointer b)  
{  
}  
  
void attach(int coefficient, int exponent,  
            poly_pointer *ptr)  
{  
}
```

## Attach a Term

```
void attach(int coefficient, int exponent,  
            poly_pointer *ptr)  
{  
    /* create a new node attaching to the node  
       pointed to by ptr.  
       ptr is updated to point to this new node.  
    */  
  
}
```

## Attach a Term

```
void attach(float coefficient, int exponent,
            poly_pointer *ptr)
{
    /* create a new node attaching to the node pointed to
       by ptr.
       ptr is updated to point to this new node. */

    poly_pointer temp;
    temp = (poly_pointer) malloc(sizeof(poly_node));

}
```

# Attach a Term

```
void attach(float coefficient, int exponent,
            poly_pointer *ptr)
{
    /* create a new node attaching to the node pointed to
       by ptr.
       ptr is updated to point to this new node. */

    poly_pointer temp;
    temp = (poly_pointer) malloc(sizeof(poly_node));

    temp->coef = coefficient;
    temp->expon = exponent;
}
```

# Attach a Term

```
void attach(float coefficient, int exponent,
            poly_pointer *ptr)
{
    /* create a new node attaching to the node pointed to
       by ptr.
       ptr is updated to point to this new node. */

    poly_pointer temp;
    temp = (poly_pointer) malloc(sizeof(poly_node));

    temp->coef = coefficient;
    temp->expon = exponent;

    (*ptr)->link = temp;
    *ptr = temp;
}
```

# Algorithm for Adding Polynomials

```
poly_pointer padd(poly_pointer a, poly_pointer b)  
{  
    poly_pointer c, rear, temp;  
    int sum;  
  
    //create a dummy node  
    rear =(poly_pointer)malloc(sizeof(poly_node)) ;  
    c= rear;
```

```
while (a && b) {  
    switch (COMPARE(a->expon, b->expon)) {  
        ...  
        case 0: /* a->expon == b->expon */  
            sum = a->coef + b->coef;  
            if (sum) attach(sum, a->expon, &rear);  
            a = a->link;    b = b->link;  
            break;  
        ...  
    }  
}
```



```

while (a && b) {
    switch (COMPARE(a->expon, b->expon)) {
        case -1: /* a->expon < b->expon */
            attach(b->coef, b->expon, &rear);
            b = b->link;
            break;

        case 0: /* a->expon == b->expon */
            sum = a->coef + b->coef;
            if (sum) attach(sum, a->expon, &rear);
            a = a->link;      b = b->link;
            break;

        case 1: /* a->expon > b->expon */
            attach(a->coef, a->expon, &rear);
            a = a->link;
    }
}

```

```
/* copy rest of list a and then list b*/  
for (; a; a = a->link)  
    attach(a->coef, a->expon, &rear);  
  
for (; b; b=b->link)  
    attach(b->coef, b->expon, &rear);  
  
rear->link = NULL;
```

...

```
}
```

```
/* copy rest of list a and then list b*/  
for (; a; a = a->link)  
    attach(a->coef, a->expon, &rear);  
for (; b; b=b->link)  
    attach(b->coef, b->expon, &rear);  
rear->link = NULL;
```

```
//delete extra initial node;  
temp = c;  c = c->link;  free(temp);  
return c;
```

```
}
```

# Erasing Polynomials

$$e(x) = a(x) * b(x) + d(x)$$

```
... .
polypointer a, b, d, e;
.
.
.
a=readPoly();
/*read b and d polynomials */
... .

temp=pmult(a,b);
e=padd(temp, d);
printPoly(e);
..
```

# Erasing Polynomials

$$e(x) = a(x) * b(x) + d(x)$$

```
... .
polypointer a, b, d, e;
.
.
.
a=readPoly();
/*read b and d polynomials */
... .

temp=pmult(a,b);
e=padd(temp, d);
printPoly(e);
. .
/* Erase temp */
```

# Erasing Polynomials

```
void erase(poly_pointer *ptr)
{
    poly_pointer temp;

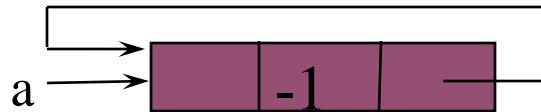
    while(*ptr)
    { temp = *ptr;
      *ptr = (*ptr)-> link

      free(temp) ;
    }
}
```

Head Node

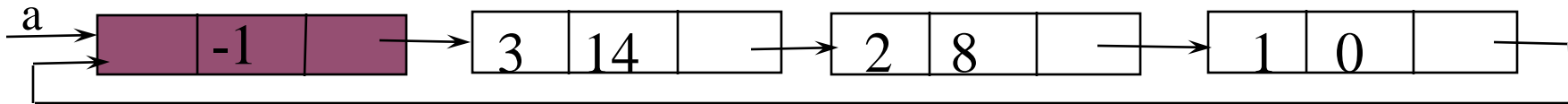
Represent polynomial as circular list.

(1) zero



Zero polynomial

(2) others



$$a = 3x^{14} + 2x^8 + 1$$

## Another Padd

```
poly_pointer cpadd(poly_pointer a, poly_pointer b)
{
    poly_pointer startA, c, lastC;
    int sum, done = FALSE;

    startA = a;
    a = a->link;
    b = b->link;

    c = get_node();
    c->expon = -1;    lastC = c;
```

Set expon field of head node to -1.



## Another Padd (*Continued*)

```
do {
    switch (COMPARE(a->expon, b->expon)) {
        case -1: attach(b->coef, b->expon, &lastC);
                b = b->link;
                break;

        case 0: if (startA == a) done = TRUE;
                else {
                    sum = a->coef + b->coef;
                    if (sum) attach(sum, a->expon, &lastC);
                    a = a->link;    b = b->link;
                }
                break;

        case 1: attach(a->coef, a->expon, &lastC);
                a = a->link;
    }
} while (!done);
```

## Another Padd (*Continued*)

```
lastC->link = c;  
return c;  
}
```

Link last node to first

## Additional List Operations

```
typedef struct list_node *list_pointer;  
typedef struct list_node {  
    char data;  
    list_pointer link;  
};
```

# **Operations For Chains**

**Invert** single linked lists

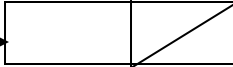
**Concatenate** two linked lists

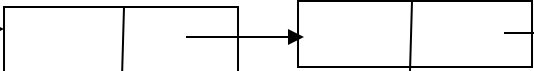
# Invert Single Linked Lists

Use two extra pointers: middle and trail.

```
list_pointer invert(list_pointer lead)
{
    list_pointer middle, trail;
    middle = NULL;
    while (lead) {
        trail = middle;
        middle = lead;
        lead = lead->link;
        middle->link = trail;
    }
    return middle;
}
```

0: null

1: lead → 

≥2: lead →  ...

## Concatenate Two Lists

```
list_pointer concatenate(list_pointer  
                        ptr1, list_pointer ptr2)
```

```
{
```

```
//Note: One or both the pointers may be NULL
```

```
.....
```

```
}
```

## Concatenate Two Lists

```
list_pointer concatenate(list_pointer
                        ptr1, list_pointer ptr2)
{
    list_pointer temp;
    if (IS_EMPTY(ptr1)) return ptr2;
    else {
        .....
    }
    return ptr1;
}
```

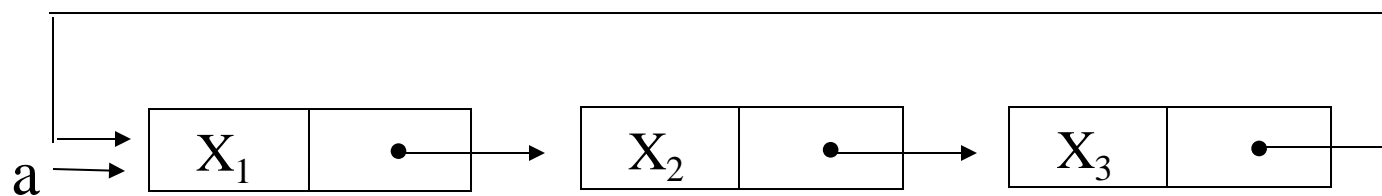
## Concatenate Two Lists

```
list_pointer concatenate(list_pointer
                        ptr1, list_pointer ptr2)
{
    list_pointer temp;
    if (IS_EMPTY(ptr1)) return ptr2;
    else {
        if (!IS_EMPTY(ptr2)) {
            for (temp=ptr1; temp->link; temp=temp->link) ;
            temp->link = ptr2;
        }
        return ptr1;
    }
}
```



## 4.5.2 Operations For Circularly Linked List

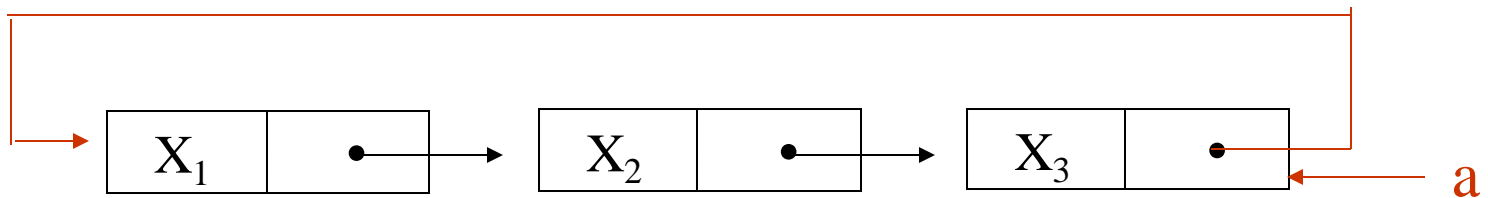
What happens when we insert a node to the front of a circular linked list?



Problem: move down the whole list.

\*Figure 4.16: Example circular list (p.165)

A possible solution:



Note a pointer points to the last node.

**\*Figure 4.17:** Pointing to the last node of a circular list (p.165)

# Operations for Circular Linked Lists

`insertFront()`

`insertRear()`

`length()`

# Operations for Circular Linked Lists

**insertFront()**

insertRear()

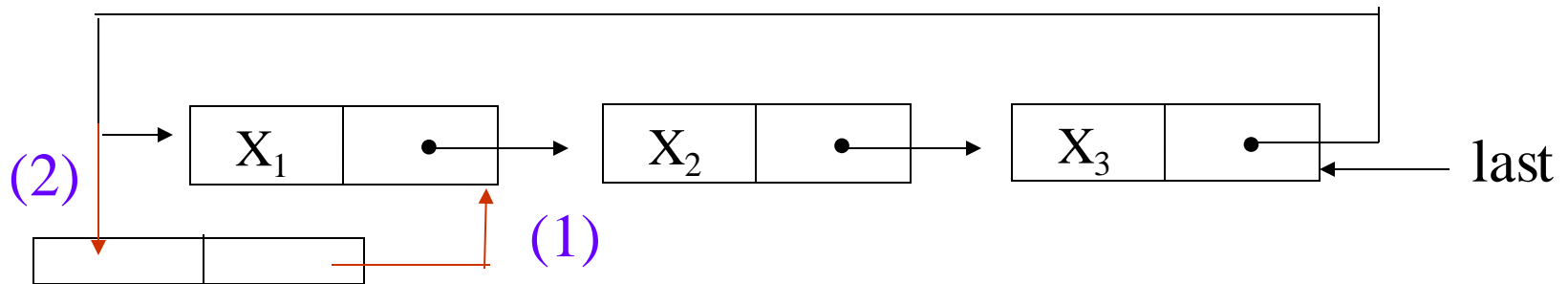
length()

```
void insertFront (list_pointer *last,  
list_pointer node)  
{  
    //Note: *last may be null  
}
```

# Operations for Circular Linked Lists

```
void insertFront (list_pointer *last, list_pointer  
node)
```

```
{  
    if (IS_EMPTY(*last)) {  
        *last= node;  
        node->link = node;  
    }  
    else {  
        node->link = (*last)->link; (1)  
        (*last)->link = node;      (2)  
    }  
}
```



# Operations for Circular Linked Lists

`insertFront()`

**`insertRear()`**

`length()`

```
void insertRear (list_pointer *last,  
list_pointer node)  
{  
    //Note: *last may be null  
}
```

# Operations for Circular Linked Lists

insertFront()

**insertRear()**

length()

```
void insertRear (list_pointer *last,  
list_pointer node)  
{  
    //Note: *last may be null  
    // same as insertFront except  
    *last = node; //in else  
}
```

# Operations for Circular Linked Lists

`insertFront()`

`insertRear()`

**`length()`**

```
void length(list_pointer last)
{
    //Note: last may be null
}
```



## Length of Linked List

```
int length(list_pointer last)
{
    list_pointer temp;
    int count = 0;

    if (last) {
        temp = last;
        do {
            count++;
            temp = temp->link;
        } while (temp!=last);
    }

    return count;
}
```

## 4.8 Doubly Linked List

Move in forward and backward direction.

Singly linked list (*in one direction only*)

How to get the preceding node during deletion or insertion?

Using 2 pointers

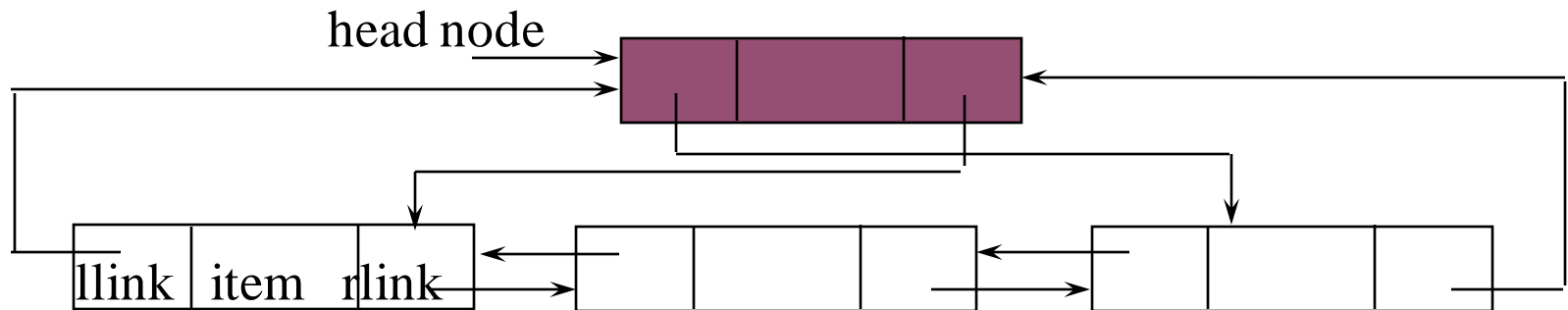
Node in doubly linked list consists of:

1. *left link field* (llink)
2. *data field* (item)
3. *right link field* (rlink)

# Doubly Linked Lists

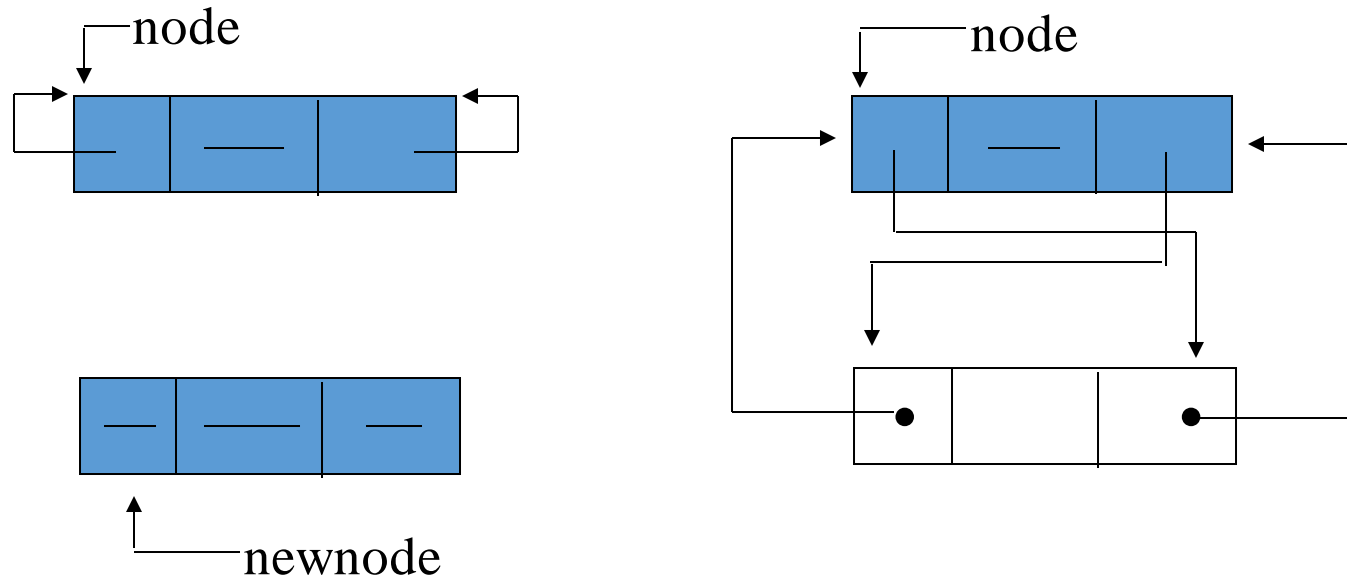
```
typedef struct node *node_pointer;  
typedef struct node {  
    node_pointer llink;  
    element item;  
    node_pointer rlink;  
}
```

ptr  
= ptr->rlink->llink  
= ptr->llink->rlink





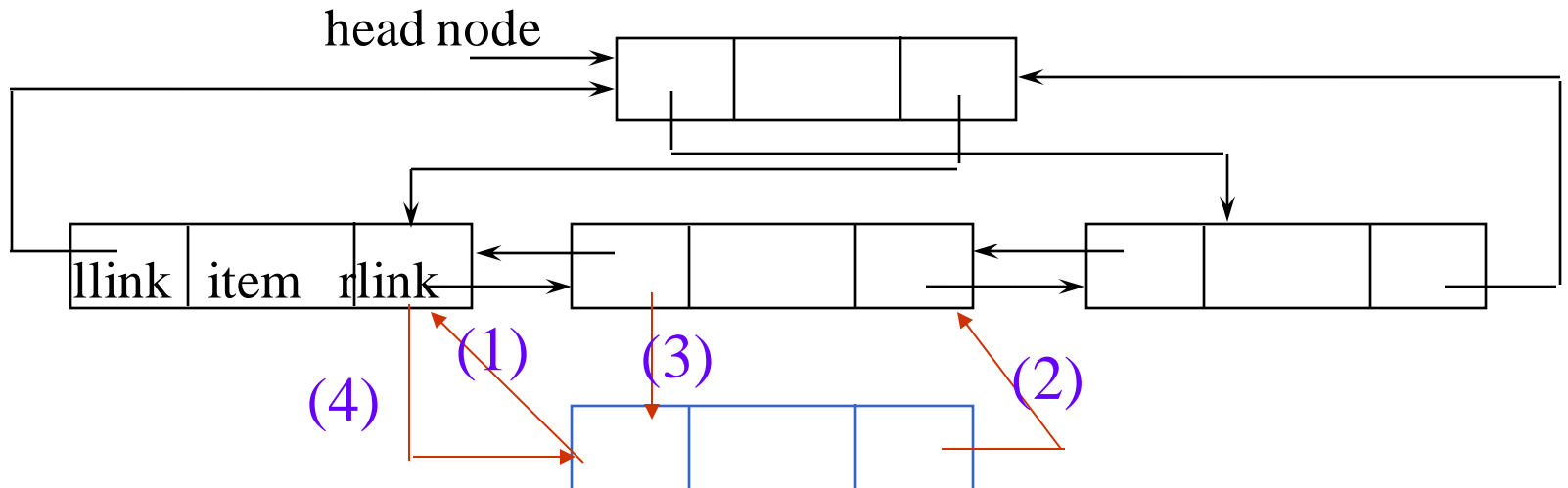
**\*Figure 4.24: Empty doubly linked circular list with head node (p.180)**



**\*Figure 4.25:** Insertion into an empty doubly linked circular list (p.181)

# Insert

```
void dininsert(node_pointer node, node_pointer newnode)
{
    (1) newnode->llink = node;
    (2) newnode->rlink = node->rlink;
    (3) node->rlink->llink = newnode;
    (4) node->rlink = newnode;
}
```



# Delete

```
void ddelete(node_pointer node, node_pointer deleted)
{
    if (node==deleted) printf("Deletion of head node
                             not permitted.\n");
    else {
        (1) deleted->llink->rlink= deleted->rlink;
        (2) deleted->rlink->llink= deleted->llink;
        free(deleted);
    }
}
```

