SOLUTION OF LINEAR EQUATIONS BY GAUSS JACOBI & GAUSS-SIEDEL METHOD

SCILAB ALGORITHM

```
// gauss Jacobi method and gauss siedel method
clc;clear;
a=[3 -1 1;-1 4 1;-1 1 5]
b = [20;6;7]
n=length(b)
c=0
for i=1:n
  s=0
  for j=1:n
    if j∼=i
      s=s+a(i,j)
    end
  end
  if(a(i,i)>s)
    c=c+1
  else break
  end
end
if c==n then
  disp('matrix is diagonally dominant')
  disp('matrix is diagonally not dominant')
end
x=input('Initial guess of first value ');
y=input('Initial guess of second value');
z=input('initial guess of third value ');
n=input('Enter no. of iterations')
  x(i+1)=(b(1,1)-(a(1,2)*y(i))-(a(1,3)*z(i)))/a(1,1)
  y(i+1)=(b(2,1)-a(2,1)*x(i+1)-a(2,3)*z(i))/a(2,2)
  z(i+1)=(b(3,1)-a(3,1)*x(i+1)-a(3,2)*y(i+1))/a(3,3)
  if (abs(x(i+1)-(x(i)))<0.001) & (abs(y(i+1)-(y(i)))<0.001) & (abs(z(i+1)-(z(i)))<0.001)
    break
  end
end
disp("No. of iteration",i,x(i),y(i),z(i))
iter = 0:i
scf(0)
plot(iter, x(1:i+1), 'ro-')
plot(iter, y(1:i+1), 'gs-')
<u>plot(iter, z(1:i+1), 'b^-')</u>
<u>legend("x","y","z")</u>
xlabel("Iteration")
vlabel("Value")
title("Convergence of Gauss-Seidel Method")
xgrid()
```

Python

```
#Gauss-jacobi & Gauss-Siedel
import numpy as np
import matplotlib.pyplot as plt
A = np_array([[3, -1, 1],
                                   [-1, 4, 1],
                                    [-1, 1, 5]], dtype=float)
b = np.array([20, 6, 7], dtype=float)
n = len(b)
c = 0
for i in range(n):
          S=0
          for j in range(n):
                 if j != i:
                    s=s+A[i,j]
          if (A[i,i]>s):
                  c += 1
          else:
                   break
if c == n:
         print("Matrix is diagonally dominant")
else:
         print("Matrix is diagonally not dominant")
x0 = float(input("Initial guess of first value: "))
v0 = float(input("Initial guess of second value: "))
z0 = float(input("Initial guess of third value: "))
max iter = int(input("Enter number of iterations: "))
x vals = [x0]
y vals = [y0]
z vals = [z0]
for i in range(max_iter):
          x \text{ new} = (b[0] - (A[0,1]*y \text{ vals}[-1]) - (A[0,2]*z \text{ vals}[-1])) / A[0,0]
          y \text{ new} = (b[1] - A[1,0]*x \text{ new} - A[1,2]*z \text{ vals}[-1]) / A[1,1]
          z_{new} = (b[2] - A[2,0]*x_{new} - A[2,1]*y_{new}) / A[2,2]
          x vals append(x new)
          v vals append(v new)
          z vals.append(z new)
          if (abs(x_vals[-1] - x_vals[-2]) < 0.001 and
                    abs(y_vals[-1] - y_vals[-2]) < 0.001 and
                     abs(z \ vals[-1] - z \ vals[-2]) < 0.001):
                     break
print(f"No. of iterations = {i+1}")
print(f''x = \{x_vals[-1]:.4f\}, y = \{y_vals[-1]:.4f\}, z = \{z_vals[-1]:.4f\}, z = \{z_vals
1]:.4f}")
iterations = list(range(len(x_vals)))
plt.figure(figsize=(8,6))
plt.plot(iterations, x_vals, marker='o', label='x')
plt.plot(iterations, y_vals, marker='s', label='y')
plt.plot(iterations, z_vals, marker='^', label='z')
plt.xlabel("Iteration")
plt.ylabel("Value")
plt.title("Convergence of Gauss-Seidel Method")
plt.legend()
plt_grid(True)
plt.show()
```