# Source finding demo

### 1. Initialisation

#### imports:

```
In [1]:

*matplotlib ipympl
from matplotlib import pyplot as plt
from matplotlib import colors
import numpy as np
from astropy.io import fits
#from astropy.table import QTable
from numba import njit
from photutils import segmentation as segm
from scipy.spatial import ConvexHull
```

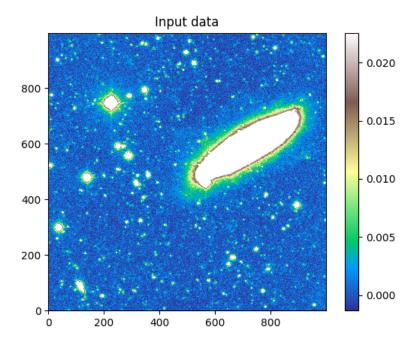
## 2. Read data

#### select one dataset:

\_\_\_\_

#### visual inspection:

data



# 3. Find mode

#### cumulative mass:

#### density peak (mode of the probability distribution):

Here we have a couple of free parameters:

Find maximum:

```
In [10]:
    x_top = np.interp((1+delta)*m, cumulative_mass, sorted_data)
    x_mid = np.interp(m, cumulative_mass, sorted_data)
    x_bot = np.interp((1-delta)*m, cumulative_mass, sorted_data)
    rho_top = delta * m / (x_top - x_mid)
    rho_bot = delta * m / (x_mid - x_bot)
    peak = np.nanargmin((rho_top - rho_bot) ** 2)
    data_mode = x_mid[peak]
```

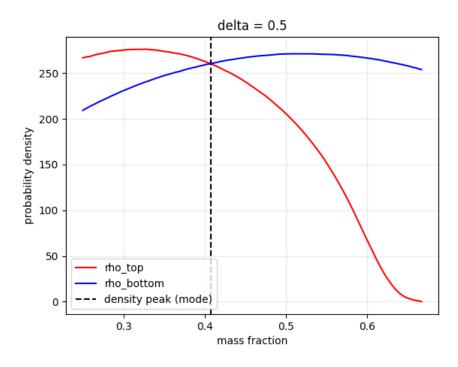
```
In [11]:
    plt.close('density')
    fig = plt.figure('density')
    ax = fig.subplots()

ax.plot(m, rho_top, 'r-', label='rho_top')
    ax.plot(m, rho_bot, 'b-', label='rho_bottom')
    ax.axvline(m[peak], c='k', ls='--', label='density peak (mode)')

ax.grid(alpha=.25)
    ax.legend()
    ax.set_xlabel('mass fraction')
    ax.set_ylabel('probability density')
    ax.set_title(f'delta = {delta}')

Out[11]: Text(0.5, 1.0, 'delta = 0.5')
```

density



#### estimate source threshold:

```
In [12]:
    m_background = 2 * m[peak]
    m_signal = 1 - m_background
    threshold_guess = np.interp(m_background, cumulative_mass, sorted_data)

    m_above = 1 - cumulative_mass
    m_symmetric_above = np.interp(2 * data_mode - sorted_data, sorted_data, cumulative_mass, left=0.)
    left = np.where(sorted_data < data_mode)
    m_symmetric_above[left] = m_background - cumulative_mass[left]
    m_signal_above = m_above - m_symmetric_above
    purity = m_signal_above / (m_above+1e-30)
    purity[-1] = 1

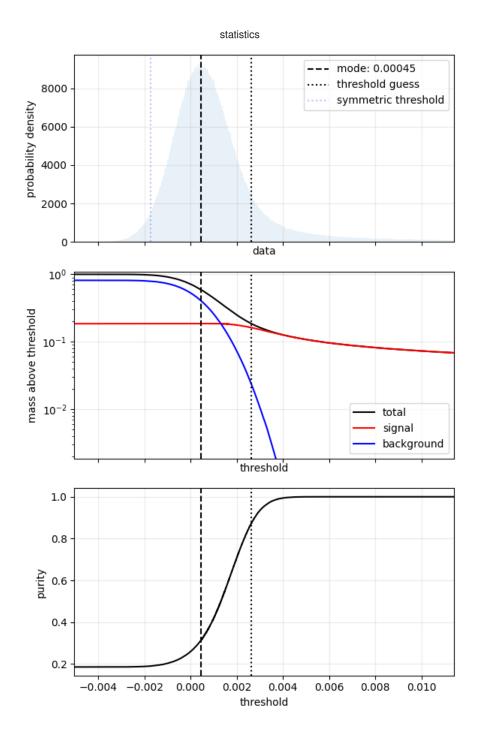
In [13]:

print(f'data_mode = {data_mode}')
    print(f'threshold_guess = {threshold_guess}, m_signal = {m_signal}')

data_mode = 0.0004482927539949746
    threshold_guess = 0.0026369258242411905, m_signal = 0.1855188521855189</pre>
```

```
In [14]:
                              L = max(data mode-sorted data[0], threshold guess-data mode)
                               plt.close('statistics')
                               fig = plt.figure('statistics', figsize=(6, 9))
                               fig.set tight layout(True)
                               ax = fig.subplots(nrows=3, sharex=True)
                               # density:
                               ax[0].hist(sorted\_data, \ bins=np.linspace(sorted\_data[0], \ data\_mode \ + \ 5*L, \ int(np.sqrt(data.size))), \ all interpretations and the second of the 
                              ax[0].axvline(data_mode, c='k', ls='--', label=f'mode: {data_mode:.2g}')
ax[0].axvline(threshold_guess, c='k', ls=':', label='threshold_guess')
ax[0].axvline(2*data_mode-threshold_guess, c='b', ls=':', alpha=.25, label='symmetric threshold')
                               ax[0].grid(alpha=.25)
                               ax[0].legend()
                               ax[0].set_xlabel('data')
                               ax[0].set_ylabel('probability density')
                               # mass:
                               ax[1].plot(sorted_data, m_above, 'k-', label='total')
                               ax[1].plot(sorted_data, m_signal_above, 'r-', label='signal')
ax[1].plot(sorted_data, m_symmetric_above, 'b-', label='background')
ax[1].axvline(data_mode, c='k', ls='--')
                               ax[1].axvline(threshold_guess, c='k', ls=':')
                               ax[1].grid(alpha=.25)
ax[1].legend(loc='lower right')
ax[1].set_xlabel('threshold')
                               \#ax[1].set xlim(sorted data[0], data mode + <math>5*L)
                               ax[1].set_ylabel('mass above threshold')
                               ax[1].set_yscale('log')
                               ax[1].set_ylim(1e-2*m_signal, 1.1)
                               # purity:
                               ax[2].plot(sorted_data, purity, 'k-')
ax[2].axvline(data_mode, c='k', ls='--')
                               ax[2].axvline(threshold_guess, c='k', ls=':')
                               ax[2].grid(alpha=.25)
                               #ax[2].legend()
                               ax[2].set_xlabel('threshold')
                               ax[2].set_ylabel('purity')
                               ax[0].set_xlim(sorted_data[0], data_mode + 2*L)
```

0ut[14]: (-0.0050287372432649136, 0.011402352748514751)



# 3. Hierarchical Overdensity Tree (HOT)

routine definition:

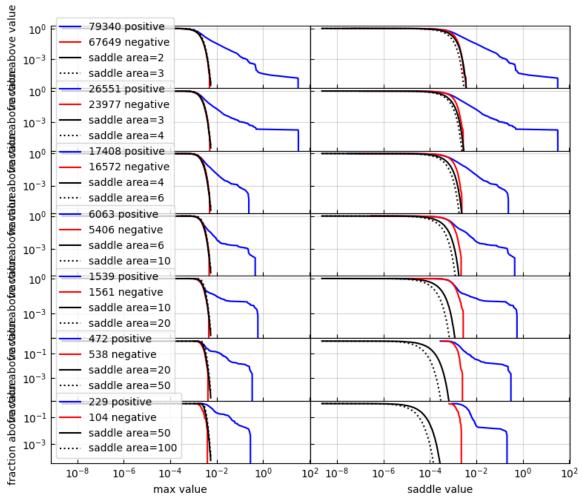
```
In [15]:
          @njit
          def hot(data, threshold=-np.inf):
              """Hierarchical Overdenity Tree (HOT)"""
              flat_data = data.flatten()
              strides = np.array(data.strides)//data.itemsize
              label = np.zeros(data.size, dtype=np.int64)
              n labels = 0
              parent = np.zeros(data.size, dtype=np.int64)
              area = np.zeros(data.size, dtype=np.int64)
              max value = np.zeros like(flat data)
              saddle_value = np.full_like(max_value, threshold)
              saddle_area = np.zeros(data.size, dtype=np.int64)
              for pixel in np.argsort(flat_data)[::-1]: # decreasing order
                   pixel_value = flat_data[pixel]
                   if np.isnan(pixel_value):
                      continue
                   if pixel_value < threshold:</pre>
                      break
                  neighbour_parents = []
                  for stride in strides:
                      if pixel >= stride:
                           p = label[pixel-stride]
                           while p > 0:
                               pp = parent[p]
                               if pp == p:
                                   break
                               else:
                                  p = pp
                           if p > 0 and p not in neighbour_parents:
                               neighbour_parents.append(p)
                      if pixel+stride < flat_data.size:</pre>
                           p = label[pixel+stride]
                           while p > 0:
                               pp = parent[p]
                               if pp == p:
                                   break
                               else:
                           if p > 0 and p not in neighbour_parents:
                               neighbour_parents.append(p)
                  neighbour_parents = np.array(neighbour_parents)
                  n_parents = neighbour_parents.size
                   \overrightarrow{\mathbf{if}} n parents == 0:
                       n_labels += 1
                       selected_parent = n_labels
                       parent[n_labels] = n_labels
                      max_value[n_labels] = pixel_value
                  elif n_parents == 1:
                      selected_parent = neighbour_parents[0]
                  else:
                      selected_parent = neighbour_parents[np.argmax(area[neighbour_parents])]
                      for p in neighbour_parents:
                           parent[p] = selected_parent
                           if saddle_area[p] == 0:
                               saddle_value[p] = pixel_value
saddle_area[p] = area[p]+1
                      #saddle area[selected parent] -= 1
                  label[pixel] = selected_parent
                  area[selected_parent] += 1
                   #saddle area[selected parent] += 1
                  if saddle_area[selected_parent] == 0:
                      saddle_value[selected_parent] = pixel_value
              n_src = np.count_nonzero(label)
              indep = np.where(parent[:n_labels+1] == np.arange(n_labels+1))
              print(f'{n_labels} overdensities found:'
                    f'{n_src} "pixels" ({int(100*n_src/data.size)}%),',
                     f'{indep[0].size -1} independent regions')
              area[0] = saddle_area[0] = data.size-n_src
              saddle_area[indep] = area[indep]
              max_value[0] = saddle_value[0] = threshold
              catalog = (parent[:n_labels+1],
                         area[:n labels+1],
                          max_value[:n_labels+1],
                          saddle_value[:n_labels+1],
                          saddle_area[:n_labels+1],
```

```
return label.reshape(data.shape), catalog
```

## normal and inverted catalogues:

```
In [16]:
            label, catalog = hot(data-data_mode, 0)
            segmentation = segm.SegmentationImage(label)
            parent = catalog[0]
            area = catalog[1]
            max_value = catalog[2]
            saddle_value = catalog[3]
            saddle_area = catalog[4]
            label_inv, catalog_inv = hot(data_mode-data, 0)
            segmentation_inv = segm.SegmentationImage(label_inv)
            parent inv = catalog inv[0]
            area_inv = catalog_inv[1]
            max value_inv = catalog_inv[2]
            saddle_value_inv = catalog_inv[3]
            saddle_area_inv = catalog_inv[4]
           152109 overdensities found: 592760 "pixels" (59%), 43525 independent regions
           135667 overdensities found: 407240 "pixels" (40%), 38478 independent regions
          I tried to predict the probability distribution of max_value and saddle value, given saddle_area. In the former, I more or less
          succeeded...
In [17]: | #'''
           plot_areas_edges = [2, 3, 4, 6, 10, 20, 50, 100]
            x bg = np.sort(data mode-data[data < data mode])</pre>
            P_bg = (np.arange(x_bg.size)+.5)/x_bg.size
            plt.close('selection model')
            fig = plt.figure('selection model', figsize=(8, 4+np.sqrt(len(plot_areas_edges))))
           ax = fig.subplots(nrows=len(plot_areas_edges)-1, ncols=2, squeeze=False,
                                 sharex=True, sharey='row',
gridspec_kw={'hspace': 0, 'wspace': 0})
            for axis in ax.flatten():
                 axis.tick_params(which='both', direction='in')
                 axis.grid(alpha=.5)
            fig.set_tight_layout(True)
            for i in range(len(plot_areas_edges)-1):
                ax[i, 0].set_ylabel('fraction above value')
ax[i, 0].set_yscale('log')
                n0 = plot_areas_edges[i]
                n1 = plot areas edges[i+1]
                 selected regions = np.where((saddle area >= n0) & (saddle area < n1))
                seleced_max = np.sort(max_value[selected_regions])
                 seleced_saddle = np.sort(saddle_value[selected_regions])
                 selected_regions_inv = np.where((saddle_area_inv >= n0) & (saddle_area_inv < n1))</pre>
                seleced_max_inv = np.sort(max_value_inv[selected_regions_inv])
                seleced_saddle_inv = np.sort(saddle_value_inv[selected_regions_inv])
                 f = np.arange(seleced_max.size)[::-1]/seleced_max.size
                ax[i, 0].plot(seleced_max, f, 'b-', label=f'{seleced_max.size} positive')
                 f = np.arange(seleced_max_inv.size)[::-1]/seleced_max_inv.size
                ax[i, 0].plot(seleced_max_inv, f, 'r-', label=f'{seleced_max_inv.size} negative')
ax[i, 0].plot(x_bg, 1-P_bg**n0, 'k-', label=f'saddle area={n0}')
ax[i, 0].plot(x_bg, 1-P_bg**n1, 'k:', label=f'saddle area={n1}')
                 f = np.arange(seleced_saddle.size)[::-1]/seleced_saddle.size
                ax[i, 1].plot(seleced_saddle, f, 'b-', label='positive')
                f = np.arange(seleced_saddle_inv.size)[::-1]/seleced_saddle_inv.size
ax[i, 1].plot(seleced_saddle_inv, f, 'r-', label='negative')
ax[i, 1].plot(x_bg, (1-P_bg)**n0, 'k-', label=f'saddle area={n0}')
ax[i, 1].plot(x_bg, (1-P_bg)**n1, 'k:', label=f'saddle area={n1}')
                 ax[i, 0].legend(loc='lower left')
                #ax[i, 0].set_ylim(1/n_regions, 1)
           ax[-1, 0].set_xlabel('max value')
ax[-1, 1].set_xlabel('saddle value')
            ax[-1, 0].set_xscale('log')
            \#ax[-1, 0].set\_xlim(x\_bg[-1]/100, x\_bg[-1])
```





# 4. Object selection

#### estimate thresholds:

Compute upper hulls in log(max\_value) and log(saddle\_value) as a funtion of log(saddle area) for the "inverted" data:

```
In [18]:

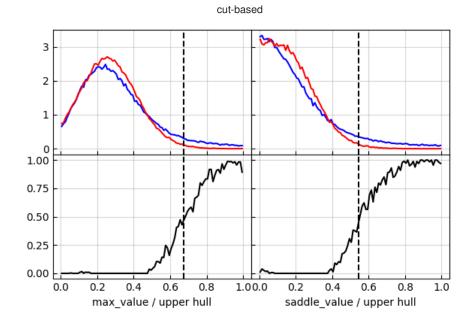
def upper_hull(x, y):
    """Compute upper hull"""

    points = np.array([x, y]).T
    hull = ConvexHull(points)
    i_max = np.argmax(x[hull.vertices])
    i_min = np.argmin(x[hull.vertices])
    if i_min > i_max:
        i = hull.vertices[i_max:i_min+1]
    else:
        i = np.concatenate([hull.vertices[i_max:], hull.vertices[:i_min+1]])
    srt = np.argsort(x[i])
    return x[i[srt]], y[i[srt]]

log_sarea_inv = np.log(saddle_area_inv[1:])
    log_svalue_inv = np.log(saddle_value_inv[1:])
    log_svalue_inv = np.log(saddle_value_inv[1:])
    max_hull_x, max_hull_y = upper_hull(log_sarea_inv, log_max_inv)
    saddle_hull_x, saddle_hull_y = upper_hull(log_sarea_inv, log_svalue_inv)
```

Let's go for a more aggressive threshold:

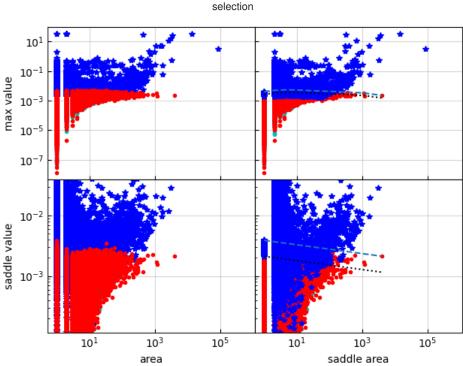
```
In [19]:
          log sarea = np.log(saddle area)
           log_max = np.log(max_value)
           log svalue = np.log(saddle value)
          max_cut = np.interp(log_sarea, max_hull_x, max_hull_y)
          max_cut_inv = np.interp(log_sarea_inv, max_hull_x, max_hull_y)
           saddle_cut = np.interp(log_sarea, saddle_hull_x, saddle_hull_y)
           saddle_cut_inv = np.interp(log_sarea_inv, saddle_hull_x, saddle_hull_y)
           cut\_bins = np.linspace(0, 1, 101)
           cut_mid = (cut_bins[1:] + cut_bins[:-1]) / 2
          \verb|max_hist|, \verb|cut_bins| = \verb|np.histogram| (\verb|np.exp|(log_max-max_cut|), \verb|bins=cut_bins|, \verb|density=True|)|
          max_hist_inv, cut_bins = np.histogram(np.exp(log_max_inv-max_cut_inv), bins=cut_bins, density=True)
          max_threshold = np.max(cut_mid[max_hist < 3*max_hist_inv])</pre>
           print(f'select objects above {100*max_threshold:.1f}% of max_value upper hull')
           saddle hist, cut bins = np.histogram(np.exp(log svalue-saddle cut), bins=cut bins, density=True)
           saddle hist inv, cut bins = np.histogram(np.exp(log_svalue_inv-saddle_cut_inv), bins=cut_bins, density
           saddle_threshold = np.max(cut_mid[saddle_hist < 3*saddle_hist_inv])</pre>
           #saddle_threshold = 1
           print(f'select objects above {100*saddle_threshold:.1f}% of saddle_value upper hull')
          select objects above 67.5% of max_value upper hull
          select objects above 54.5% of saddle_value upper hull
          /tmp/ipykernel 12997/3953992399.py:2: RuntimeWarning: divide by zero encountered in log
            log_max = np.log(max_value)
          tmp/ipykernel_12997/3953992399.py:3: RuntimeWarning: divide by zero encountered in log/
            log_svalue = np.log(saddle_value)
In [20]:
          plt.close('cut-based')
           fig = plt.figure('cut-based', figsize=(6, 4))
           ax = fig.subplots(nrows=2, ncols=2, squeeze=False,
                              sharex=True, sharey='row',
gridspec_kw={'hspace': 0, 'wspace': 0})
           for axis in ax.flatten():
               axis.tick_params(which='both', direction='in')
               axis.grid(alpha=.5)
           fig.set_tight_layout(True)
          ax[0, 0].plot(cut_mid, max_hist, 'b-')
          ax[0, 0].plot(cut_mid, max_hist_inv, 'r-')
ax[0, 0].axvline(max_threshold, c='k', ls='--')
           ax[1, 0].plot(cut_mid, np.clip(max_hist-max_hist_inv, 0, np.inf)/(max_hist+max_hist_inv), 'k-')
          ax[1, 0].axvline(max threshold, c='k', ls='--')
          ax[0, 1].plot(cut_mid, saddle_hist, 'b-')
          ax[0, 1].plot(cut_mid, saddle_hist_inv, 'r-')
ax[0, 1].axvline(saddle_threshold, c='k', ls='--')
           ax[1, 1].plot(cut mid, np.clip(saddle hist-saddle hist_inv), 0, np.inf)/(saddle hist+saddle hist_inv),
          ax[1, 1].axvline(saddle_threshold, c='k', ls='--')
           ax[1, 0].set_xlabel('max_value / upper hull')
          ax[1, 1].set_xlabel('saddle_value / upper hull')
0ut[20]: Text(0.5, 0, 'saddle_value / upper hull')
```



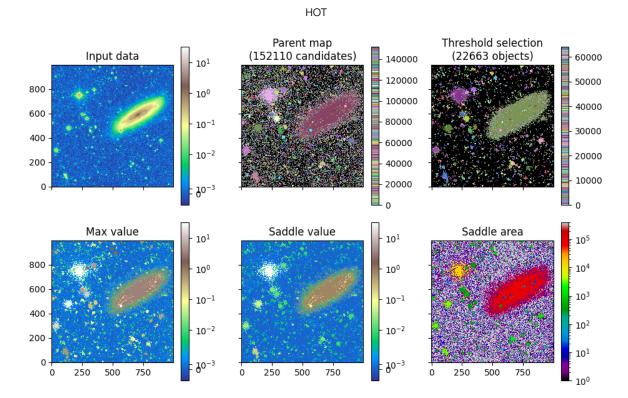
# apply threshod-based selection criteria:

22663 overdensities pass the selection criteria

```
In [22]:
           plt.close('selection')
           fig = plt.figure('selection')
           ax = fig.subplots(nrows=2, ncols=2, squeeze=False,
                                sharex=True, sharey='row',
                                gridspec_kw={'hspace': 0, 'wspace': 0})
           for axis in ax.flatten():
                axis.tick_params(which='both', direction='in')
                axis.grid(alpha=.5)
           fig.set_tight_layout(True)
           ax[0, 0].set_ylabel('max value')
           ax[0, 0].set_yscale('log')
ax[0, 0].plot(catalog[1], catalog[2], 'c.')
           ax[0,\ 0].plot(catalog[1][selected],\ catalog[2][selected],\ 'b*')
           ax[0, 0].plot(catalog_inv[1], catalog_inv[2], 'r.')
           ax[1, 0].set_ylabel('saddle value')
ax[1, 0].set_yscale('log')
           ax[1, 0].plot(catalog[1], catalog[3], 'c.')
           ax[1, 0].plot(catalog[1][selected], catalog[3][selected], 'b*')
           ax[1, 0].plot(catalog_inv[1], catalog_inv[3], 'r.')
           ax[-1, 0].set_xlabel('area')
           ax[-1, 0].set_xscale('log')
           ax[0, 1].plot(catalog[4], catalog[2], 'c.')
           ax[0, 1].plot(catalog_inv[4], catalog_inv[2], 'r.')
           ax[0,\ 1].plot(catalog[4][selected],\ catalog[2][selected],\ 'b*')
           ax[0, 1].plot(np.exp(max\_hull\_x), np.exp(max\_hull\_y), '--')\\
           ax[0, 1].plot(np.exp(max_hull_x), max_threshold*np.exp(max_hull_y), 'k:')
           ax[1, 1].plot(catalog[4], catalog[3], 'c.')
ax[1, 1].plot(catalog_inv[4], catalog_inv[3], 'r.')
           ax[1, 1].plot(catalog[4][selected], catalog[3][selected], 'b*')
#ax[1, 1].plot(nn, cut_saddle, 'k--')
           ax[1, 1].plot(np.exp(saddle_hull_x), np.exp(saddle_hull_y), '--')
ax[1, 1].plot(np.exp(saddle_hull_x), saddle_threshold*np.exp(saddle_hull_y), 'k:')
           ax[1,\ 1].set\_ylim(.1*saddle\_threshold*np.exp(np.min(saddle\_hull\_y)),\ 10*np.exp(np.max(saddle\_hull\_y)))
           ax[-1, 1].set_xlabel('saddle area')
           ax[-1, 1].set_xscale('log')
```



```
In [23]:
          plt.close('HOT')
          fig = plt.figure('HOT', figsize=(9.5, 6))
          fig.set_tight_layout(True)
          ax = fig.subplots(nrows=2, ncols=3, sharex=True, sharey=True)
          delta = threshold_guess-data_mode
          ax[0, 0].set_title('Input data')
          im = ax[0, 0].imshow(
              data-data_mode,
              interpolation='nearest', origin='lower', cmap='terrain',
              norm = colors.SymLogNorm(vmin=-delta, linthresh=3*delta, vmax=np.max(data-data_mode)),
          cb = fig.colorbar(im, ax=ax[0, 0])
          ax[0, 1].set_title(f'Parent map\n({parent.size} candidates)')
          im = ax[0, 1].imshow(
              segmentation.
              interpolation='nearest', origin='lower', cmap=segmentation.make_cmap(seed=123),
          cb = fig.colorbar(im, ax=ax[0, 1])
          ax[0, 2].set_title(f'Threshold selection\n({selected[0].size} objects)')
          im = ax[0, 2].imshow(
              thresold selection,
              interpolation='nearest', origin='lower', cmap=thresold selection.make cmap(seed=123),
          cb = fig.colorbar(im, ax=ax[0, 2])
          ax[1, 0].set_title('Max value')
          im = ax[1, 0].imshow(
              max value[label],
              interpolation='nearest', origin='lower', cmap='terrain',
              norm = colors.SymLogNorm(vmin=-delta, linthresh=3*delta, vmax=np.max(data-data_mode)),
          cb = fig.colorbar(im, ax=ax[1, 0])
          ax[1, 1].set_title('Saddle value')
          im = ax[1, 1].imshow(
              saddle_value[label],
              interpolation='nearest', origin='lower', cmap='terrain',
              norm = colors.SymLogNorm(vmin=-delta, linthresh=3*delta, vmax=np.max(data-data_mode)),
          cb = fig.colorbar(im, ax=ax[1, 1])
          ax[1, 2].set_title('Saddle area')
          im = ax[1, 2].imshow(
              saddle area[label],
              interpolation='nearest', origin='lower', cmap='nipy spectral', norm=colors.LogNorm(),
          cb = fig.colorbar(im, ax=ax[1, 2])
```



5. Mode filter

```
In [24]:
          @njit
          def mode_filter(data):
               flat_data = data.flatten()
              mode = np.empty_like(flat_data)
count = np.empty_like(flat_data)
               strides = np.array(data.strides)//data.itemsize
               neighbours = np.empty(2*len(strides)+1, dtype=np.int64)
               counts = np.empty_like(neighbours)
               n_{changes} = 0
               for pixel in range(flat_data.size):
                   #print('>', pixel)
                   neighbours[0] = flat_data[pixel]
                   counts[0] = 1
                   n_neighbours = 1
                   for stride in strides:
                       if pixel >= stride:
                            #print(-stride)
                           value = flat_data[pixel-stride]
                           n = 0
                           while True:
                                if value == neighbours[n]:
                                    counts[n] += 1
                                    break
                                else:
                                    n += 1
                                    if n == n_neighbours:
                                         neighbours[n] = value
                                         counts[n] = 1
                                         n_{\text{neighbours}} += 1
                                         break
                       if pixel+stride < flat data.size:</pre>
                            value = flat_data[pixel+stride]
                            #print(stride, value)
                           n = 0
                           while True:
                                if value == neighbours[n]:
                                    counts[n] += 1
                                    break
                                else:
                                    n += 1
                                    if n == n_neighbours:
                                         neighbours[n] = value
                                         counts[n] = 1
                                         n_{neighbours} += 1
                                         break
                   best = np.argmax(counts[:n_neighbours])
                   if counts[best] == counts[0]: # just in case
                       best = 0
                   else:
                       n_{changes} += 1
                   #print(f'> pixel {pixel} moves from {neighbours[0]} to {neighbours[best]} (out of {n_neighbour
                   mode[pixel] = neighbours[best]
                   count[pixel] = counts[best]
               return mode.reshape(data.shape), count.reshape(data.shape), n_changes
In [26]:
          filtered_labels = np.copy(valid_labels)
          n_old = \overline{0}
          n = filtered_labels.size
          while n != n_old:
               n \text{ old } = \overline{n}
               filtered_labels, c, n = mode_filter(filtered_labels)
               print(n, 'changes')
         85612 changes
          22109 changes
         6211 changes
         1899 changes
         643 changes
         255 changes
         120 changes
         71 changes
         55 changes
          52 changes
         50 changes
         48 changes
         47 changes
         47 changes
```

```
In [27]:
           final labels = np.copy(filtered labels)
           unique_labels = np.unique(filtered_labels)
           n_final_labels = unique_labels.size
           for i, lbl in enumerate(unique_labels):
               final_labels[final_labels == lbl] = i
           final_selection = segm.SegmentationImage(final_labels)
In [28]:
           plt.close('filtered')
           fig = plt.figure('filtered', figsize=(10, 5))
ax = fig.subplots(nrows=1, ncols=2, squeeze=False,
                               sharex=True, sharey='row',
gridspec_kw={'hspace': 0, 'wspace': 0})
           for axis in ax.flatten():
                axis.tick_params(which='both', direction='in')
               axis.grid(alpha=.5)
           fig.set_tight_layout(True)
           ax[0, 0].set_title('Input data')
           im = ax[0, 0].imshow(
               data-data_mode,
               interpolation='nearest', origin='lower', cmap='terrain',
               norm = colors.SymLogNorm(vmin=-delta, linthresh=3*delta, vmax=np.max(data-data_mode)),
           cb = fig.colorbar(im, ax=ax[0, 0])
cb.ax.axhline(0, c='k', ls=':')
           cb.ax.axhline(threshold_guess-data_mode, c='k', ls='--')
           ax[0, 1].set\_title(f'Final \ selection \ map\n(\{n\_final\_labels\} \ objects)')
           im = ax[0, 1].imshow(
               final_selection,
                interpolation='nearest', origin='lower', cmap=final_selection.make_cmap(seed=123),
           cb = fig.colorbar(im, ax=ax[0, 1])
```

#### Final selection map Input data (4271 objects) 4000 10<sup>1</sup> 3500 800 10<sup>0</sup> 3000 2500 600 $10^{-1}$ 2000 400 1500 $10^{-2}$ 200 1000 500 200 400 600 800

filtered

In [ ]: