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All

Articles

Videos

Problems

Quiz

<< Prev

Next >>

Matrix Operations (Addition, Subtraction, Multiplication)

Matrices Addition

The addition of two matrices $A_{m \times n}$ and $B_{m \times n}$ gives a matrix $C_{m \times n}$. Here, m and n represents the number of rows and columns in the matrix respectively. The elements of C are sum of corresponding elements in A and B which can be shown as:

$$\begin{bmatrix} 1 & 2 \\ 4 & 5 \end{bmatrix} + \begin{bmatrix} 5 & 6 \\ 8 & 9 \end{bmatrix} = \begin{bmatrix} 6 & 8 \\ 12 & 14 \end{bmatrix}$$

Example: - $\text{mat1} = \{\{1, 2\}, \{3, 4\}\}$ $\text{mat2} = \{\{1, 2\}, \{3, 4\}\}$ $\text{mat1} + \text{mat2} = \{\{2, 4\}, \{6, 8\}\}$

The algorithm for addition of matrices can be written as:

```
for i in 1 to m
  for j in 1 to n
    cij = aij + bij
```

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<<

>>

```
#include <bits/stdc++.h>
using namespace std;

int main(){

    int N = 2, M = 2;
    int m1[N][M] = { { 1, 2 },
                     { 4, 5 } };
    int m2[N][M] = { { 5, 6 },
                     { 8, 9 } };
    int ans[N][M];

    // Traversing number of Rows
    for(int i = 0; i < N; i++)
    {
        // Traversing number of Columns
        for (int j = 0; j < M; j++)
        {
            ans[i][j] = m1[i][j] + m2[i][j];
        }
    }

    for (int i = 0; i < N; i++)
    {
        for (int j = 0; j < M; j++)
        {
            cout<<ans[i][j]<<" ";
        }
    }
}
```





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```
}  
cout<<endl;  
}  
  
}
```

Output

```
6 8  
12 14
```

Key points:

- Addition of matrices is commutative which means $A+B = B+A$
- Addition of matrices is associative which means $A+(B+C) = (A+B)+C$
- The order of matrices A, B and A+B is always same
- If order of A and B is different, A+B can't be computed
- The complexity of addition operation is $O(m*n)$ where $m*n$ is order of matrices

Matrices Subtraction

The subtraction of two matrices A_{m*n} and B_{m*n} gives a matrix C_{m*n} . Here, m and n represents the number of rows and columns in the matrix respectively. The elements of C are difference of corresponding elements in A and B which can be represented as:

$$\begin{bmatrix} 5 & 6 \\ 8 & 9 \end{bmatrix} - \begin{bmatrix} 1 & 2 \\ 4 & 5 \end{bmatrix} = \begin{bmatrix} 4 & 4 \\ 4 & 4 \end{bmatrix}$$

Example: - mat1 = {{1, 2}, {3, 4}} mat2 = {{1, 2}, {3, 4}} mat1 - mat2 = {{0, 0}, {0, 0}}

The algorithm for subtraction of matrices can be written as:

```
for i in 1 to m
  for j in 1 to n
    cij = aij - bij
```

C++

```
#include <bits/stdc++.h>
using namespace std;

int main(){

int N = 2, M = 2;
int m1[N][M] = { { 5, 6 },
                  { 8, 9 } };

int m2[N][M] = { { 1, 2 },
                  { 4, 5 } };

int ans[N][M];
```



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```
// Traversing number of Rows
for(int i = 0; i < N; i++)
{
    // Traversing number of Columns
    for (int j = 0; j < M; j++)
    {
        ans[i][j] = m1[i][j] - m2[i][j];
    }
}

for (int i = 0; i < N; i++)
{
    for (int j = 0; j < M; j++)
    {
        cout<<ans[i][j]<<" ";
    }
    cout<<endl;
}
}
```

Output

```
4 4
4 4
```

Key points:

- Subtraction of matrices is non-commutative which means $A-B \neq B-A$
- Subtraction of matrices is non-associative which means $A-(B-C) \neq (A-B)-C$
- The order of matrices A, B and A-B is always same
- If order of A and B is different, A-B can't be computed
- The complexity of subtraction operation is $O(m*n)$ where $m*n$ is order of matrices

Matrices Multiplication

The multiplication of two matrices A_{m*n} and B_{n*p} gives a matrix C_{m*p} . It means number of columns in A must be equal to number of rows in B to calculate $C=A*B$. To calculate element C_{11} , multiply elements of 1st row of A with 1st column of B and add them ($5*1+6*4$) which can be shown as:

$$\begin{bmatrix} 5 & 6 \\ 8 & 9 \end{bmatrix} * \begin{bmatrix} 1 \\ 4 \\ 2 \\ 5 \end{bmatrix} = \begin{bmatrix} 29 & 40 \\ 44 & 61 \end{bmatrix}$$

Example: - $\text{mat1} = \{\{1, 2\}, \{3, 4\}\}$ $\text{mat2} = \{\{1, 2\}, \{3, 4\}\}$ $\text{mat1} * \text{mat2} = \{\{7, 10\}, \{15, 22\}\}$

The algorithm for multiplication of matrices A with order $m*n$ and B with order $n*p$ can be written as:

```
for i in 1 to m
  for j in 1 to p
    cij = 0
    for k in 1 to n
      cij += aik*bkj
```

C++



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Videos



Problems



Quiz

<<

>>

```
#include <bits/stdc++.h>
using namespace std;

int main(){

    int M = 2, N = 2, P = 2;
    int m1[M][N] = { { 5, 6 },
                     { 8, 9 } };
    int m2[N][P] = { { 1, 2 },
                     { 4, 5 } };
    int ans[M][P];

    // Traversing number of Rows
    for(int i = 0; i < M; i++)
    {
        // Traversing number of Columns
        for (int j = 0; j < P; j++)
        {
            ans[i][j] = 0;

            for( int k = 0; k < N; k++ )
                ans[i][j] += m1[i][k] * m2[k][j];
        }
    }

    for (int i = 0; i < N; i++)
```





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```
{  
    cout<<ans[i][j]<<" ";  
}  
cout<<endl;  
}  
}
```

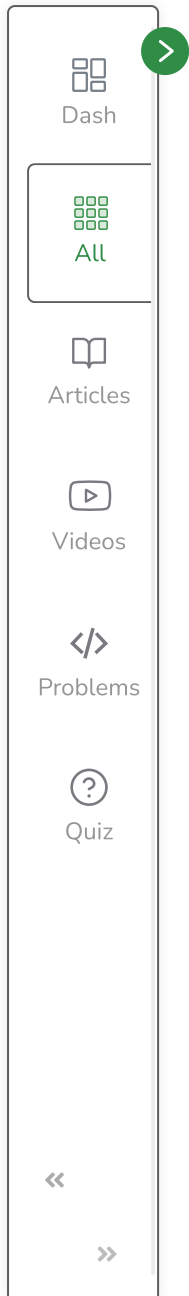
Output

```
29 40  
44 61
```

Key points:

- Multiplication of matrices is always non-commutative which means $A*B \neq B*A$
- Multiplication of matrices is associative which means $A*(B*C) = (A*B)*C$
- For computing $A*B$, the number of columns in A must be equal to number of rows in B
- Existence of $A*B$ does not imply existence of $B*A$
- The complexity of multiplication operation ($A*B$) is $O(m*n*p)$ where $m*n$ and $n*p$ are order of A and B respectively
- The order of matrix C computed as $A*B$ is $O(m*p)$ where $m*n$ and $n*p$ are order of A and B respectively

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