

Pardis Sadatian Moghaddam

Panther ID: 002722641

**HW4:**

1. Consider loci 1 and 2. Suppose the allele for locus 1 is either A or a and the allele for locus 2 is either B or b. Suppose A and B are associated such that (1)  $p_{AB} = p_{ApB} + D1$ , (2)  $p_{Ab} = p_{Apb} - D2$ , (3)  $p_{aB} = p_{apB} - D3$ , and (4)  $p_{ab} = p_{apb} + D4$ . Can you show that  $D1 = D2 = D3 = D4$ ?

$$p_{AB} = p_{ApB} + D1$$

$$p_{Ab} = p_{Apb} - D2$$

$$p_{aB} = p_{apB} - D3$$

$$p_{ab} = p_{apb} + D4$$

$$D1 = p_{AB} - p_{ApB}$$

$$P A = p_{AB} + p_{Ab}$$

$$p B = p_{AB} + p_{aB}$$

$$p a = p_{ab} + p_{aB}$$

$$p b = p_{ab} + p_{Ab}$$

$$D2 = p_{Apb} - p_{Ab} = p_A(1 - p_B) - p_{Ab} = p_A - p_{ApB} - p_{Ab} = p_{AB} + p_{Ab} - p_{ApB} - p_{Ab} = p_{AB} - p_{ApB}$$

$$\Rightarrow D2 = p_{AB} - p_{ApB}$$

So, we can say  $D1=D2$

$$D3 = p_{aB} - p_{apB} = p_{aB} - (1-p_A)p_B = p_{aB} - p_B + p_{ApB} = p_{aB} - [p_{AB} + p_{aB}] + p_{ApB} = -p_{AB} + p_{ApB} = -D1$$

$$\Rightarrow D1 = p_{ApB} - p_{AB}$$

So, we can say  $D1 = D3$

$$D4 = p_{apb} - p_{ab} = (1-p_A)(1-p_B) - p_{ab} = 1 - p_B - p_A + p_{ApB} - p_{ab} = p_b - p_A + p_{ApB} - p_{ab} = p_{ab} + p_{Ab} - p_A + p_{ApB} - p_{ab} = p_{Ab} - p_A + p_{ApB} = p_{Ab} - p_{AB} - p_{Ab} + p_{ApB} = -p_{AB} + p_{ApB}$$

$$\Rightarrow D1 = p_{ApB} - p(AB)$$

## 2. Consider the following two SNPs.

• SNP1: Case—40A,160C,Control—20A,180C,

• SNP2: Case—20A,180C,Control—10A,190C.

Can you compute the relative risk and the odds ratio for the two SNPs? Which SNP has a higher risk?

### Case 1

	Case	Control
A	40 (p)	20 (q)
C	160 (r)	180 (s)

$$\text{Relative risk} \Rightarrow RR = [40/(160+180)]/[20/(40+20)] = 1.416$$

$$\text{Odds ratio} \Rightarrow OR = [40/160]/[20/180] = 1.37$$

$RR > 1$  and  $OR > 1$  exposure is positively associated with disease.

## Case 2

	Case	Control
A	20 (p)	10 (q)
C	180 (r)	190 (s)

Relative risk =>  $RR = [p/(p+q)] / [r/(r+s)] = [20/(20+10)] / [180/(180+190)] = 1.37$

Odds ratio =>  $OR = [p/q] / [r/s] = [20/10] / [180/190] = 2.11$

**By comparing RR and OD in both cases, we can say case 1 has the higher risk.**

- Given a set of 6 haplotypes over 11 SNPs, find the minimum size subset of tag SNP which will distinguish all haplotypes

the subset consists of SNPs:\_\_\_\_\_

0,1,2,3,4,5,6,7,8,9,10

(0,1,0,1,0,1,0,1,0,1,0)

(0,1,1,0,1,0,1,0,0,0,0)

(0,0,0,1,0,1,0,0,1,1,1)

(1,0,1,1,0,1,0,1,1,0,1)

(1,0,1,0,1,0,0,1,1,0,1)

(1,0,0,0,1,0,1,0,1,1,1)

$r_i(k)$  => as the allele of the i-th SNP in the k-th haplotype.

We can partition 11 SNPs in to 3 blocks:

$r_1, \dots, r_3$

$r_4, \dots, r_7$

$r_8, \dots, r_{11}$

For  $r_1, \dots, r_3$  is selected we should consider two things:

$r_1=0$ , we predict  $r_1, \dots, r_3 = 010$  and  $011$  and  $000$  as the tag SNP; We predict the whole.

For  $r_1=1$ , we predict  $r_1, \dots, r_3 = 101$  as the tag SNP; This one can predict 3 out of 6 so it is more than 50%.

For  $r_4, \dots, r_7$  is selected we should consider two things:

$r_1=0$ , we predict  $r_4, \dots, r_7 = 0101$  as the tag SNP; We predict the whole with this tag.

For  $r_1=1$ , we predict  $r_4, \dots, r_7 = 1010$  as the tag SNP; This one can predict 5 out of 6 so it is more than 80%.

For  $r_8, \dots, r_{11}$  is selected we should consider two things:

$r_1=0$ , we predict  $r_8, \dots, r_{11} = 0111$  as the tag SNP; We predict the whole with this tag.

For  $r_1=1$ , we predict  $r_4, \dots, r_7 = 1101$  as the tag SNP; This one can predict 5 out of 6 so it is more than 66%.