ECE 47300:	Midterm	1	(Spring	2023).	Version:	C
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Instructions

Please fill out this cover page but do NOT start until instructed to do so.

What is your full name and Purdue ID (10-digit number)?
Name (please PRINT, no cursive):
Purdue ID (10 digits):
Honor Pledge Signature:
• Total number of points: 100 (Roughly 50 questions or subquestions)
• Question format notes
 Circular checkboxes are for multiple choice (i.e., a single correct answer) Square checkboxes are for select all questions (i.e., possibly multiple correct answers).
- Only put your answer in the boxes like
 No partial credit: Every (sub-)question is all or nothing credit. Thus, you must get the answer exactly right to get credit for the question (including SELECT ALL questions). No partial credit will be given.
Number Format: When giving numbers as short answers, please give in standard decimal notation

- Number Format: When giving numbers as short answers, please give in standard decimal notation with preceding "0." for decimals if needed but no trailing 0s (e.g., "0.15", "2.9", "0.001", "100" but NOT "0.15000" NOR ".15" NOR ".001" NOR "6.0").
- Honor Pledge: I assert that I have not received any information about this exam and will not share any exam content with anyone else, even after the exam. I understand that any violation of this will result in a failing grade for the whole class (not just this exam).

1.	(2 points) Select all the reasons that it	
	(2 points) Select all the reasons that dimensionality reduction may be helpful: Noise reduction via reconstruction	
	Visualization	
	Lower computational costs	
2.		
	(2 points) What was the main strength(s) of the first wave of AI called "Handcrafted Knowledge" according to DARPA's perspective (e.g. chess, TurboTax, rule-based scheduling systems)? Select all	
	□ Perceiving	
	□ Abstracting	
	Reasoning	
	□ Learning	
3.	(2 points) Assuming that A, B, C, D are 3×3 matrices, which of the following statements are ALWAYS true? Select all that apply.	
	$\Box A(B+C) = AB + CA$	
	$\Box (AB)^T = A^T B^T$	
	$\blacksquare A$ is not singular if and only if $rank(A) = 3$	
4.	(2 points) Numpy has two types of 1D arrays: column vectors and row vectors.	
	○ True	λ
	False	/ \
5.	(2 points) If $X = \begin{bmatrix} 1 & -2 \\ -3 & 1 \end{bmatrix}$ what is $ X _F^2$?	
	Answer: 15	
6.	(2 points) What is the ℓ_{∞} -norm of the vector $\mathbf{x} = [-1, -2, 3, -5, -4, 3, -9, 1]$ (i.e., what is $\ \mathbf{x}\ _{\infty}$)?	
	Answer: 9	
7.	(2 points) If $X_c = USV^T$ is the SVD decomposition of the centered matrix and $\Sigma_x = \frac{1}{n} X_c^T X_c$ is the covariance matrix whose eigendecomposition is $Q\Lambda Q^T$, which of the following are solutions of the principal component vectors for the dataset X_c (i.e., W^*)?	
	$\ \square \ U_{1:k}$	
	$\ \square \ S_{1:k}$	
	$\ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ $	
	$Q_{1:k}$	
	$\ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ $	

*	
(8.) (2 points) Suppose $x = [10, 5]^T$ and $w = [\frac{3}{5}, \frac{4}{5}]^T$ (note $ w _2 = 1$). What is the solution to $\arg \min_z x - y _2 = 1$).	
$\bigcirc z^* = 5$	
$\bigcirc z^* = 8$	1
$\bigcirc z^* = 11$	1
None of the above / Many possible solutions	
9. (2 points) Suppose $X_c \in \mathbb{R}^{100 \times 10}$ and X_c has a rank of 8. If we run PCA with $k = 6$ latent dimensions, what will be the PCA reconstruction error?	
Greater than 0	
\bigcirc 0	
○ Less than 0	
10. (2 points) Cross validation provides a good estimate of a model's performance even if the real-world test distribution of unseen data is different from the training dataset.	
○ True	R
2 points) The KNN algorithm uses less computation during training rather than test/inference time.	
True	
○ False	
12. (2 points) Let $\theta = [1, 5, 1, 0]^T$ be the parameters of a 3 dimensional linear regression model f_{θ} (where θ_4 is the intercept term). What is $f_{\theta}(\mathbf{x} + [1, 0, 3, 7]^T) - f_{\theta}(\mathbf{x})$?	
\bigcirc 1	
\bigcirc 2	
\bigcirc 3	
4	
 Impossible to know given the available information 	
 (2 points) Deep learning methods will always perform better than linear methods because they can model non-linear functions. 	0
○ True	
(2 points) Gradient descent will not converge to a local optimum for any fixed step size.	
True	
○ False	
15. (2 points) Stochastic gradient descent computes the full gradient as in gradient descent but then explicitly adds noise to make the gradient stochastic.	
O True	8
P.I.	~)

False

16.	(2 points) If $\lambda \geq 0$, R is a regularizer, θ is the model parameters, and \mathcal{D} is the training dataset, what is the regularized optimization problem?	
	$\bigcirc \min_{\theta} \mathcal{L}(\theta, \mathcal{D}) - \lambda R(\theta)$	
	$\bigcirc \min_{\theta} \mathcal{L}(\theta, \mathcal{D}) - \lambda R(\mathcal{D})$	
	$\bigcirc \min_{\theta} \mathcal{L}(\theta, \mathcal{D}) + \lambda R(\mathcal{D})$	
17.		
	(2 points) Which optimization problem is most likely to have exact zeros in the solution for θ ? Orange $\min_{\theta} \ y - X\theta\ _2^2$	
	$ \text{arg min}_{\theta} \ \mathbf{y} - X\theta \ _{2}^{2} + 10 \ \theta\ _{1}^{2} $ $ \text{arg min}_{\theta} \ \mathbf{y} - X\theta \ _{2}^{2} + 10 \ \theta\ _{2}^{1} $	
	$\bigcirc \arg \min_{\theta} \ \mathbf{y} - X\theta\ _{2}^{2} + 10\ \theta\ _{2}^{2}$ $\bigcirc \arg \min_{\theta} \ \mathbf{y} - X\theta\ _{2}^{2} + 10\ \theta\ _{\infty}^{3}$	
10		
18.	(2 points) Suppose f is a complex non-linear function (e.g., a deep model), and you know that the unique solution of $\arg\min_z f(z)$ is $z^*=5$, i.e., $\arg\min_z f(z)=5$. What is the solution of $\arg\min_v g(v)$, where $g(v)=3f(4v+3)-3$?	
	$\bigcirc v^* = -0.5$	
	$\bigcirc v^* = 0$	2
	$v^* = 0.5$	
	Knowing the solution given the information in the question is impossible.	
19.	(2 points) Suppose the input tensor is an CIFAR-10 image (32x32 size with 3 channels) and we apply a " 2×2 " convolution with 9 filters, no padding, and a stride of 1, how many channels will the output of the convolution have?	
	Answer: 9	
20.	(2 points) Suppose the input is a MNIST image ($28x28$ size with only 1 channel) and we perform a $3x3$ convolution with a padding of 1 on all sides and a stride of 1. What will be the width dimension of the output?	
	Answer: 28	
21.	(2 points) If we perform a 1D convolution where the input length is 6 and the filter/kernel is size 2 with no padding and a stride of 2, what will the length of the output be?	
	Answer: 3	

22. You are given a Python function to classify tweets as "spam", "not-spam", or "toxic". Provide this function's predictions for each Tweet below. def classify_tweet(tweet): spam_words = ['free', 'buy', 'cheap', 'discount', 'limited', 'offer', 'sale'] toxic_words = ['hate', 'killer', 'attack', 'terrific', 'abuse', 'bully', 'hurt', 'racist'] spam_word_count = 0 for word in tweet: if word in spam_words: spam_word_count += 1 if word in toxic_words: return 'toxic' if spam_word_count > 1: return 'spam' else: return 'not spam' (a) (1 point) It's a limited-time offer, so buy now! $(True\ label = spam,\ Predicted\ label =$ Spam (b) (1 point) Best deal with a huge discount on the purchase of this iPhone. $(True\ label=spam,\ Predicted\ label=$ not spam (c) (1 point) That was a killer performance. $(True\ label=not\ spam,\ Predicted\ label=$ toxic (d) (1 point) They did a terrific job painting my house. $(\mathit{True\ label} = \mathit{not\ spam},\, \mathit{Predicted\ label} =$ toxic (3 points) What words should be added or removed (if any) from the above lists to make the classifier accurate on all the samples above? (One or more may be left blank.) Add to spam-words deal Add to • Remove killer from toxic-words • Remove terrific from toxic - words



23. Recall the following equation from the Power Iteration method for calculating PCA of sparse matrices $v^{(i)} = X^T(Xv^{(i-1)}) - \mu(\mathbf{1}^T(Xv^{(i-1)})) - (X^T\mathbf{1})(\mu^Tv^{(i-1)}) + \mu(\mathbf{1}^T\mathbf{1})(\mu^Tv^{(i-1)})$ We initialize the variables in the following manner:

X is of shape (n, d)
v = np.random.randn(X.shape[1])
one_vec = np.ones(X.shape[0])
mu = np.array(np.mean(X, axis=0)).squeeze()

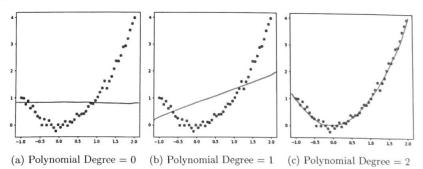
Write the shapes in terms of "n" and "d" where the format of the shape should be "(a, b)" for 2D arrays or "(a,)" for 1D arrays.

- (a) (1 point) Shape of v:
- (b) (1 point) Shape of one_vec: (N₃)
- (c) (1 point) Shape of mu:
- (d) (2 points) Shape of $\mu(\mathbf{1}^T\mathbf{1})(\mu^Tv^{(i-1)})$:
- (e) (2 points) Shape of $X(\mu(\mathbf{1}^T\mathbf{1})(\mu^Tv^{(i-1)})X^T\mathbf{1})$: Invalid
- 24. Suppose the following are matrices and their shapes.

X:(100,50), Y:(50,1), Z:(100,1)

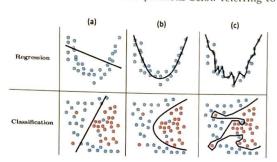
If the operation is valid, write the shape of the output in the format "(a,b)". If the operation is not valid, write "Invalid".

- (a) (2 points) $X^T Z Y$: Invalid
- (b) (2 points) $X^T(ZY^T)$: (50,50)
- (c) (2 points) $XYZ^TX^T(ZY^T)$: Invalid
- (d) (2 points) $XYZ^TX(ZY^T)$: Invalid
- 25. We want to fit the given data with varying degrees of the polynomial, i.e., the prediction $\hat{y} = \theta_0 + \theta_1 x + \theta_2 x^2 + ... + \theta_d x^d$.
 - (a) (6 points) For each box below, draw the approximate fitted polynomial for the given polynomial degree.



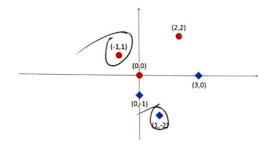
(b) (1 point) Which degree will likely generalize the best to new data? d = 2

26. We have learned model generalization. Solve the questions below referring to the following figure.



- (a) (2 points) Select one that correctly diagnoses (a)-(c)
 - \bigcirc (a) overfitting, (b) overfitting, (c) underfitting
 - (a) underfitting, (b) just right (c) overfitting
 - (a) just right, (b) overfitting (c) overfitting
 - (a) underfitting, (b) overfitting (c) overfitting
- (b) (2 points) Select all that correctly describe (a)
- - High training error
 - \square Low training error
 - High testing error
 - ☐ Low testing error
- (c) (2 points) Select all that correctly describe (c)
 - ☐ High training error
 - Low training error
 - High testing error
 - \square Low testing error

27. Let red circles denote class 1 and let blue diamonds denote class 2. In this question, we would like to select the best value of k using cross validation where the number of folds is equal to the number of points (i.e., leave-one-out cross validation). The CV accuracy for k=3 neighbors is 3/6. You will have to compute the CV accuracy for k=1 and k=5 in the next questions. (Note that all points are at integer locations.)



- (a) (4 points) Compute the CV accuracy for k = 1 neighbors in KNN:
 - \bigcirc 0
 - \bigcirc 1/6
 - 2/6
 - \bigcirc 3/6
 - \bigcirc 4/6
 - \bigcirc 5/6
 - \bigcirc 1
- (b) (4 points) Compute the CV accuracy for k = 5 neighbors in KNN:
 - **0**
 - $\bigcirc 1/6$
 - O 2/6
 - \bigcirc 3/6
 - \bigcirc 4/6
 - \bigcirc 5/6
 - \bigcirc 1
- (c) (1 point) What is the best k:
 - $\bigcirc k = 1$

 - $\bigcirc k = 5$



).	Suppose we want to train a deep learning model by using 1000 training samples. Caraining setting.	Choose the appropriate
	(a) (1 point) Given batch size of 10, what is the number of mini batches?10	
	100	
	O 1,000	
	○ 10,000	
	○ 100,000	
	(b) (1 point) If we want to train the model for 100 epochs, how many times the training sample?	model will go over each
	O 10	
	100	
	○ 1,000 ○ 10,000	
	\bigcirc 10,000 \bigcirc 100,000	
		the However the
2	 Assume that the goal of the code below is to compute the covariance matrix c current code below contains a bug. 	orrectly. However, the
	# Assume X is a 2D numpy array	
	n. d = X.shape	# (a) -
	<pre>x_center = X.mean(axis****). zero_centered_data = X - x_center</pre>	# (b)
	cov = (1/n) * np.dot(zero_centered_data.T, zero_centered_data)	# (c)
	(a) (2 points) Which line will raise an error?	
	(a) (2 points) Which has also also (a)	
	(b)	
	(c)	
	(b) (2 points) Which line should be changed to correctly compute the covariant	ice matrix?
	(a)	
	○ (b)	
	○ (c)	



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Suppose we want to train a 1D linear regression model using a mean squared error (MSE) objective. For simplicity, we will assume that the model does not include a shift/bias term and is simply $f_{\theta}(x) = \theta x$, where both θ and x are scalars. The training data is two points (note that X only has 1 column since

$$X = \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} = \begin{bmatrix} 1.0 \\ 2.0 \end{bmatrix} \quad \text{and} \quad y = \begin{bmatrix} y_1 \\ y_2 \end{bmatrix} = \begin{bmatrix} 2.0 \\ 5.0 \end{bmatrix}$$
 (1)

(a) (2 points) Assuming that $\theta = 1$, what is the gradient of the parameters for sample 1?

$$\nabla_{\theta}\ell(y_1, f_{\theta}(x_1)) = \boxed{-2} \tag{2}$$

(b) (2 points) Assuming that $\theta = 1$, what is the gradient of the parameters for sample 2?

$$\nabla_{\theta}\ell(y_2, f_{\theta}(x_2)) = \boxed{-12}$$

(c) (2 points) Assuming that $\theta = 1$ at the current iteration and the step size is $\eta = 0.2$, what is the updated θ after one step of gradient descent?

$$\theta^{\text{new}} = \boxed{2.4}$$

(d) (2 points) Assuming that $\theta = 1$ at the current iteration, the step size is $\eta = 0.1$, and the batchsize is 1 (where the first sample is in the first batch), what is the updated θ after one step of stochastic gradient descent?

$$\theta^{\text{new}} = 1.2$$



$$\frac{2}{20}\left(0n-y\right)^{2}=2\left(0n-y\right)m$$