

# 1 Formal Reasoning

## 1.1 Truth tables

1. If I have money, then I can but a ticket and if I can buy a ticket, then I arrive on time.
2.  $D \wedge \neg B \rightarrow \neg A$

## 1.2 Automata

1. No
2. No
3. Yes
4. No
5. Yes

# 2 Probability theory

$$p(\text{ill}) = 0.01$$

$$p(\text{not ill}) = 1 - p(\text{ill}) = 1 - 0.01 = 0.99$$

$$p(+ \mid \text{ill}) = 0.90$$

$$p(+ \mid \text{not ill}) = 1 - p(+ \mid \text{ill}) = 1 - 0.90 = 0.10$$

$$p(+) = p(+ \mid \text{ill})p(\text{ill}) + p(+ \mid \text{not ill})p(\text{not ill})$$

$$p(+) = 0.90 \cdot 0.01 + 0.10 \cdot 0.99 = 0.108$$

$$p(\text{ill} \mid +) = \frac{0.99 \cdot 0.01}{0.108} \approx 0.083$$

# 3 Programming

## 3.1 PC

1. 3
2. 8

### 3.2 PC2

1. 0 1 4 9 16 25
2. 10

## 4 Machine Learning

| $b$  | $k_0$ | $k_1$ | $w_0$ | $w_1$ | $x$   | output |
|------|-------|-------|-------|-------|-------|--------|
| 1    | 0     | 0     | 1     | 1     | 0     | 1      |
| 0.5  | 1     | 0     | 0.80  | 0.25  | 1.4   | 1      |
| -0.5 | 1     | 1     | 0.90  | 0.50  | 0.90  | 1      |
| -1   | 1     | 0     | 0.60  | 0.40  | 0.40  | 0      |
| -1   | 1     | 1     | 0.70  | 0.25  | -0.05 | 0      |

- 1.
2. This is not possible. Because a single layer perceptron, as the one used here, can only separate the inputs linearly. And this combination of inputs cannot be separated linearly. This becomes clear when drawing a graph with all inputs on their.
3. Such a perceptron would have at least two layers. Then the weights and bias need to be adjusted accordingly such that the perceptron resembles an NXOR-gate.