

Bright Sky Model

We want to create a better model for the moon.

```
In [1]: %pylab inline
```

Populating the interactive namespace from numpy and matplotlib

```
In [26]: import os, glob, sys, fnmatch
import numpy as np
import pandas as pd
import seaborn as sns
import pandas as pd
from astropy.io import fits

import astropy.table
import astropy.units as u
from astropy.time import Time
import corner
import seaborn as sns

import sklearn.linear_model
import specsim.atmosphere
from scipy import interpolate
import statsmodels.api as sm
from lmfit import models, Parameters, Parameter, Model
from scipy.optimize import curve_fit

import speclite
import astropy.units as u

from matplotlib.font_manager import FontProperties
font = FontProperties()
font.set_family('serif')
font.set_size('small')
```

Define Data

First, look at bright photometric data. Bright is defined as $2.5 \times$ mean dark level, which is $2.79 \times 10^{-17} \text{ erg/cm}^2/\text{s}/\text{\AA}$

```
In [3]: data = astropy.table.Table.read('data/good_data.fits')
```

```

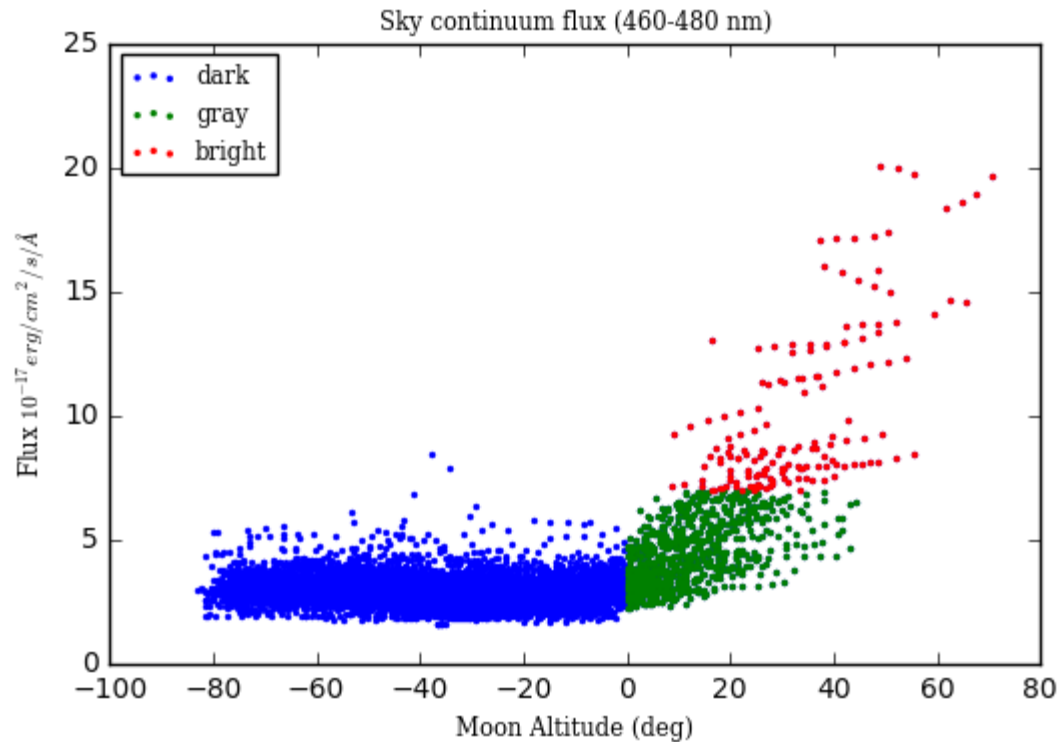
In [4]: def make_data_dict(data = data, plot = False):
        gray_level = 2.5*2.79
        gray = np.where((data['MOON_ALT']>0)&(data['SKY_VALUE']<gray_level))
        bright = np.where((data['MOON_ALT']>0)&(data['SKY_VALUE']>gray_level))

        if plot:
            plt.figure()
            plt.scatter(data['MOON_ALT'], data['SKY_VALUE'], s = 2, color='blue')
            plt.scatter(data['MOON_ALT'][gray], data['SKY_VALUE'][gray], s = 2, color='green')
            plt.scatter(data['MOON_ALT'][bright], data['SKY_VALUE'][bright], s = 2, color='red')
            plt.legend(loc='upper left', prop=font)
            plt.xlabel("Moon Altitude (deg)", fontproperties = font)
            plt.ylabel("Flux  $10^{-17}$  erg/cm2/s/Å", fontproperties = font)
            plt.title("Sky continuum flux (460-480 nm)", fontproperties = font)

        return {'good': data, 'gray': data[gray], 'bright': data[bright]}

data_dict = make_data_dict(plot=True)

```



```
In [5]: # Add in clouds/photometricity
cloud_data = np.load('clouds/phot_rec.npy')
def get_cloud_data(line):
    df = pd.DataFrame(cloud_data)
    clouds = df[(df['STARTTAI'] <= line['TAI-BEG']) & (df['ENDTAI'] > line['TAI-END'])]
    if len(clouds) == 0:
        clouds = df[(df['STARTTAI'] < line['TAI-END']) & (df['ENDTAI'] > line['TAI-BEG'])]
    if len(clouds) == 0:
        clouds = 0.5
    return clouds

In [6]: clouds = [get_cloud_data(line) for line in data]
data['PHOTO'] = astropy.table.Column(np.hstack(clouds).astype(np.float64))
data_dict = make_data_dict()

In [7]: def photometric_cut(data = data):
    phot_data = data[data['PHOTO'] == 1]
    phot_data_dict = make_data_dict(data = phot_data)
    return phot_data_dict
phot_data_dict = photometric_cut()
```

How good is a linear regression model?

These results are only from the photometric bright nights. The linear regression fit is pretty good. It helps me identify components important to the moon model

```

In [8]: def linear_regression(data_name = 'bright', data_dict = data_dict):
        data = data_dict[data_name]
        #features = ['MOON_ILL', 'MOON_ALT', 'MOON_SEP', 'AIRMASS', 'AZ', 'SU
        features = ['MOON_ILL', 'MOON_ALT', 'MOON_SEP', 'AIRMASS', 'SUN_MOON_
                    'ECL_LON', 'ECL_LAT', 'GAL_LAT', 'SEASON', 'HOUR', 'MOON_
                    'PRESSURE', 'SUN_ALT', 'DUSTB', 'MOON_LAT', 'MOON_LON', '
                    'WINDS25M', 'GUSTS', 'HUMIDITY', 'MOON_D']

        X = []
        for feat in features:
            X.append(data[feat])
        X = np.column_stack(X)

        y = data['SKY_VALUE']
        print(X.shape, y.shape)

        sm.OLS.exog_names = features
        results = sm.OLS(y, X).fit()

        params = results.params
        model = np.dot(X, params)

        print(results.summary())

        xmin, xmax = np.percentile(model, (1, 99))
        ymin, ymax = np.percentile(y - model, (1, 99))
        plt.hist2d(model, y-model, bins=(50,50), cmap=plt.cm.jet)
        plt.colorbar()
        plt.xlim(xmin, xmax)
        plt.ylim(ymin, ymax)
        plt.xlabel("Model flux", fontproperties=font)
        plt.ylabel("Data - Model (residuals)", fontproperties=font)
        plt.title("Residual plot for Linear Regression Model")
        linear_regression(data_name='bright', data_dict = phot_data_dict)

```

```
(86, 22) (86,)
```

OLS Regression Results

```

=====
=====
Dep. Variable:                  y      R-squared:
0.997
Model:                        OLS      Adj. R-squared:
0.997
Method:                    Least Squares      F-statistic:
1137.
Date:                Wed, 24 Jan 2018      Prob (F-statistic):
1.51e-74
Time:                15:17:34      Log-Likelihood:
-62.224
No. Observations:                86      AIC:
168.4
Df Residuals:                64      BIC:
222.4

```

Now, we want to create a better more physical model

```
In [11]: wavelength = np.linspace(3550, 9350, (9350-3550)*10)*u.Angstrom
sky_unit = 1e-17 * u.erg / (u.cm**2 * u.s * u.Angstrom * u.arcsec**2)
area = 1 * u.arcsec ** 2
```

```
In [12]: #moon spectrum
moon_s = np.loadtxt('/Users/parkerf/Research/SkyModel/DESI_Sky/solar_spectra/moon_spectra.txt')
moon_s = interpolate.interpld(moon_s[:,1], moon_s[:,2], bounds_error=False)
moon_spectrum = moon_s(wavelength)* u.erg/ (u.cm**2 * u.s * u.Angstrom * u.arcsec**2)

#extinction curve
ext_c = np.loadtxt('/Users/parkerf/Research/SkyModel/DESI_Sky/ZenithalExtinctionCoefficients.txt')
ext_c = interpolate.interpld(ext_c[:,0], ext_c[:,1], bounds_error=False)
extinction_coefficient = ext_c(wavelength)
```

```
In [18]: moon_zenith = 90-data['MOON_ALT']
data['MOON_ZENITH'] = astropy.table.Column(moon_zenith.astype(np.float64))
# Compute the pointing zenith angle in degrees.
obs_zenith = 90 - data['ALT']
data['OBS_ZENITH'] = astropy.table.Column(obs_zenith.astype(np.float64))

mphase = np.arccos(2 * data['MOON_ILL'] - 1) / np.pi
data['MPHASE'] = astropy.table.Column(mphase.astype(np.float32))

helio_lon = data['ECL_LON'] - data['SUN_LON']
data['HELIO_LON'] = astropy.table.Column(np.array(helio_lon).astype(np.float64))
```

Calculate Values for Moon Brightness

```
In [14]: # Calculate the V-band extinction of the moon spectrum.
_vband = speclite.filters.load_filter('bessell-V')
V = _vband.get_ab_magnitude(moon_spectrum, wavelength)
extinction = 10 ** (-extinction_coefficient / 2.5)
Vstar = _vband.get_ab_magnitude(
    moon_spectrum * extinction, wavelength)
_vband_extinction = Vstar - V
```

```
In [19]: #Calculate the wavelength-dependent extinction of moonlight
# scattered once into the observed field of view.
idx = np.where((wavelength>4600*u.Angstrom)&(wavelength<4800*u.Angstrom))
ext = np.array(extinction_coefficient)

scattering_airmass = np.array((
    1 - 0.96 * np.sin(data['MOON_ZENITH']) ** 2) ** (-0.5))
data['scatt_airmass'] = astropy.table.Column(scattering_airmass.astype(np.float32))
```

```
In [20]: RAWV = []
MEAN_EXT = []
for item in data:
    extinction = (10 ** ((-ext * item['scatt_airmass']) / 2.5) *
        (1 - 10 ** (-ext * item['AIRMASS'] / 2.5)))
    surface_brightness = moon_spectrum * extinction

    # Renormalized the extincted spectrum to the correct V-band magnitude
    raw_V = _vband.get_ab_magnitude(
        surface_brightness, wavelength) * u.mag
    RAWV.append(raw_V.value)

    idx = np.where((wavelength>4400*u.Angstrom)&(wavelength<4800*u.Angstrom))
    MEAN_EXT.append(np.mean(extinction[idx]))

data['raw_V'] = astropy.table.Column(np.array(RAWV).astype(np.float32))
data['mean_ext'] = astropy.table.Column(np.array(MEAN_EXT).astype(np.float32))
```

Calculate values for Zodiacal light

```
In [23]: leinert_lookup = '/Users/parkerf/Research/SkyModel/BOSS_Sky/Model/fiber_lookup.dat'
ZodiLookup = np.load(leinert_lookup)
S10 = 1.28*10**(-9) #erg/cm2/s/sr/A @ 500nm
sr = 4.25*10**(10) #arcsec^2/sr
fiber_area = np.pi
```

```
In [24]: hdu = fits.open('ftp://ftp.stsci.edu/cdbs/current_calspec/sun_reference.fits')
sun_spectrum = hdu[1].data
hdu.close()
sun_wave = sun_spectrum['WAVELENGTH']/10. #nm
sun_flux = sun_spectrum['FLUX'] #erg/s/cm2/A
sun_spectrum = interpolate.interpld(sun_wave, sun_flux, bounds_error=False, fill_value=0)
#relative to 500nm
nm_500 = [np.abs(500.-w) for w in sun_wave]
nm_id = np.argmin(nm_500)
relative_sun_flux = sun_flux[sun_wave[nm_id]]
```

```
In [25]: ZODI = []
for line in data:
    lamb = np.argmin([np.abs(np.abs(line['HELIO_LON'])-lon) for lon in lon_list])
    beta = np.argmin([np.abs(np.abs(line['ECL_LAT'])-lat) for lat in lat_list])
    BASE_ZODI = ZodiLookup[2][lamb][beta]

    IO = BASE_ZODI*S10*(fiber_area/sr)
    flux = relative_sun_flux*IO*10**17
    zodi_spect = interpolate.interpld(sun_wave*10, flux, bounds_error=False, fill_value=0)
    ext = 10 ** (-extinction_coefficient * line['AIRMASS'] / 2.5)
    zodi_flux = zodi_spect(wavelength)*ext*u.erg/ (u.cm**2 * u.s * u.angstrom)
    idx = np.where((wavelength>4600*u.angstrom)&(wavelength<4800*u.angstrom))
    ZODI.append(np.mean(zodi_flux[idx]).value)
data['ZODI'] = astropy.table.Column(np.array(ZODI).astype(np.float32))
```

```
In [27]: data_dict = make_data_dict()
phot_data_dict = photometric_cut()
this_data = np.random.choice(phot_data_dict['bright'],1)
```

```

In [32]: def bright_sky_model(X, A, B, C, D, E, a1, a2, a3, a4, a5, a6, a7, a8, a9, a10,
    moon_ill, moon_sep, moon_alt, airmass, Xmoon, raw_V, mean_ext, zodi):

    #The following is from the specsim.atmosphere model with constant
    abs_alpha = 180. * moon_ill
    m = -a1 + a2 * abs_alpha + a3 * abs_alpha ** 4

    # Calculate the illuminance of the moon outside the atmosphere in
    # foot-candles (eqn. 8).
    Istar = 10 ** (-0.4 * (m + a4))

    # Calculate the scattering function (eqn.21).
    rho = moon_sep #separation_angle.to(u.deg).value
    f_scatter = (10 ** a5 * (a6 + np.cos(np.deg2rad(rho)) ** 2) +
                  10 ** (a7 - rho / a8))

    # Calculate the V-band moon surface brightness in nanoLamberts.
    B_moon = (f_scatter * Istar *
              10 ** (-0.4 * _vband_extinction * Xmoon) *
              (1 - 10 ** (-0.4 * (_vband_extinction * airmass))))

    # Convert from nanoLamberts to to mag / arcsec**2 using eqn.19 of
    # Garstang, "Model for Artificial Night-Sky Illumination",
    # PASP, vol. 98, Mar. 1986, p. 364 (http://dx.doi.org/10.1086/131111)
    _scattered_V = ((20.7233 - np.log(B_moon / 34.08)) / 0.92104 *
                    u.mag / (u.arcsec ** 2))

    idx = np.where((wavelength>4600*u.Angstrom)&(wavelength<4800*u.Angstrom))
    surface_brightness = np.mean(moon_spectrum[idx]) * mean_ext

    area = 1 * u.arcsec ** 2

    surface_brightness *= 10 ** (
        -(_scattered_V * area - raw_V * u.mag) / (2.5 * u.mag))

    moon = (surface_brightness*10**17).value
    sky = A*zodi + moon #+ B*pressure + C*dust +D*airtemp + E*dewpoint
    return moon

```



```
In [33]: my_data = phot_data_dict['bright']
p0 = 1, 1, 1, 1, 1, 12.73, 0.025, 4*10**(-9), 16.57, 5.36, 1.06, 6.15,
xx = (my_data['MOON_ILL'], my_data['MOON_SEP'], my_data['MOON_ALT'],
      my_data['scatt_airmass'], my_data['raw_V'], my_data['mean_ext'],
      my_data['PRESSURE'], my_data['DUSTB'], my_data['AIRTEMP'], my_data['SKY_VALUE'])
popt, pcov = curve_fit(bright_sky_model, xx, my_data['SKY_VALUE'], p0)

/Users/parkerf/anaconda3/lib/python3.5/site-packages/ipykernel/__main__.py:10: RuntimeWarning: overflow encountered in power
/Users/parkerf/anaconda3/lib/python3.5/site-packages/ipykernel/__main__.py:20: RuntimeWarning: invalid value encountered in multiply
/Users/parkerf/anaconda3/lib/python3.5/site-packages/scipy/optimize/minpack.py:715: OptimizeWarning: Covariance of the parameters could not be estimated
category=OptimizeWarning)
```

```
In [30]: print(p0)
print(popt)

(1, 1, 1, 1, 1, 12.73, 0.025, 4e-09, 16.57, 5.36, 1.06, 6.15, 40.0)
[ 1.00000000e+00  1.00000000e+00  1.00000000e+00  1.00000000e+00
 1.00000000e+00 -2.37544188e+02 -4.84908534e-02  1.20063607e-08
-2.28078738e+02  6.21961954e+00  6.58817916e-01  5.63404504e+00
 1.29500833e+00]
```

```

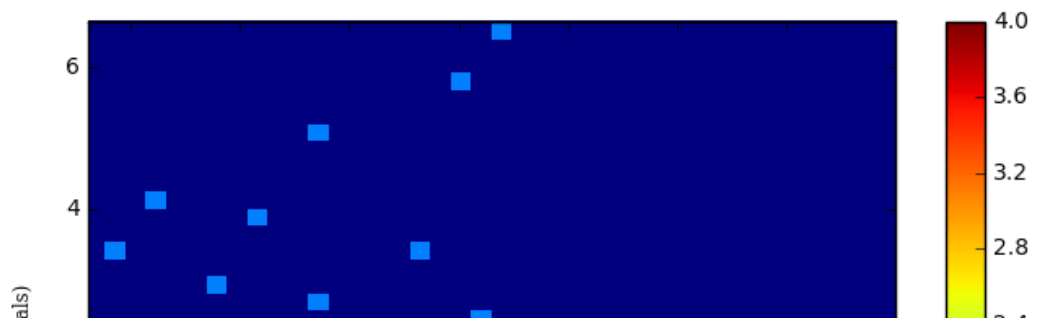
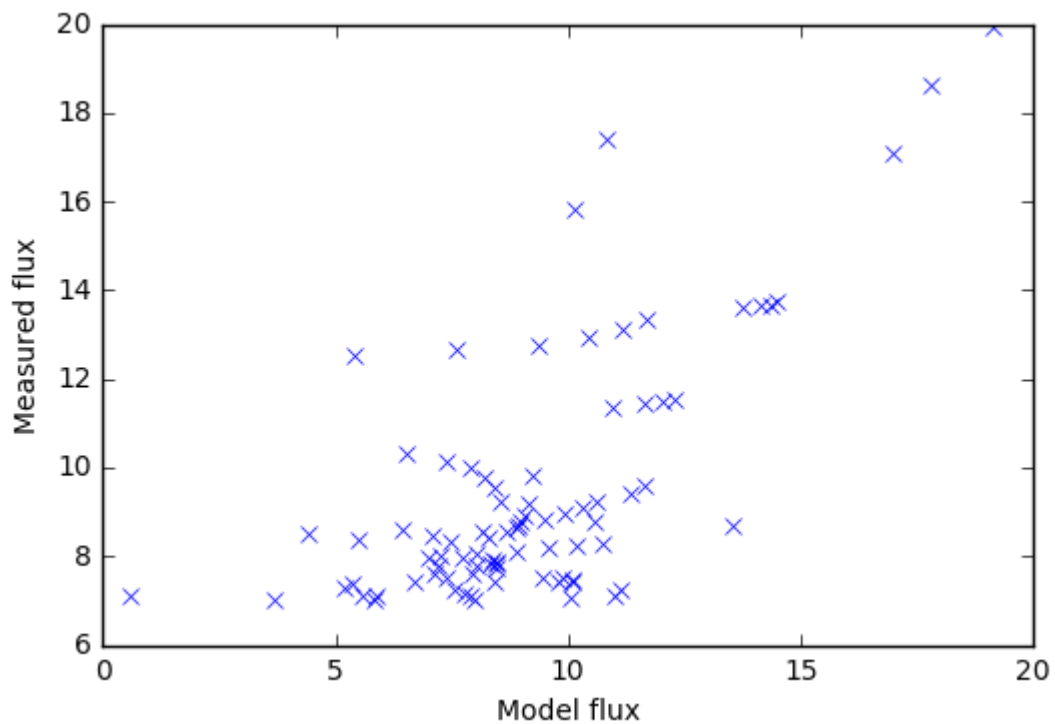
In [36]: model = bright_sky_model(xx, *popt)
         res = my_data['SKY_VALUE']-model

         plt.figure()
         plt.plot(model, my_data['SKY_VALUE'],'x')
         plt.xlabel("Model flux")
         plt.ylabel("Measured flux")
         fig, ax = plt.subplots(1, figsize=(8,6))

         xmin, xmax = np.percentile(model, (1, 99))
         ymin, ymax = np.percentile(res, (1, 99))
         plt.hist2d(model, res,bins=(50,50), cmap=plt.cm.jet)
         plt.colorbar()
         plt.xlim(xmin, xmax)
         plt.ylim(ymin, ymax)
         plt.xlabel("Model flux",fontproperties=font)
         plt.ylabel("Data - Model (residuals)",fontproperties=font)

```

Out[36]: <matplotlib.text.Text at 0x12137cac8>



In []: