!pip install pandas Show hidden output import pandas as pd import statsmodels.api as sm df = pd.read_csv('dataset.csv', encoding='cp1252') print(df.columns) Show hidden output 3 print(df[['Human Development Index (HDI) ', 'Gender Inequality Index', 'Life expectancy at birth (years)', 'Population age 15-64 years (millions)', 'Gross national income (GNI) per capita (2017 PPP \$)']].dtypes) Human Development Index (HDI) object Gender Inequality Index object Life expectancy at birth (years) object Population age 15-64 years (millions) object Gross national income (GNI) per capita (2017 PPP \$) object dtype: object # Convert columns to numeric, forcing errors to NaN $df['Human\ Development\ Index\ (HDI)\ '] = pd.to_numeric(df['Human\ Development\ Index\ (HDI)\ '], errors='coerce')$ df['Gender Inequality Index'] = pd.to_numeric(df['Gender Inequality Index'], errors='coerce') df['Life expectancy at birth (years)'] = pd.to_numeric(df['Life expectancy at birth (years)'], errors='coerce') df['Population age 15-64 years (millions)'] = pd.to_numeric(df['Population age 15-64 years (millions)'], errors='coerce') df['Gross national income (GNI) per capita (2017 PPP \$)'] = pd.to_numeric(df['Gross national income (GNI) per capita (2017 PPP \$)'], errors='coerce') # Drop rows with NaN values df = df.dropna(subset=['Human Development Index (HDI) ', 'Gender Inequality Index', 'Life expectancy at birth (years)', 'Population age 15-64 years (millions)', 'Gross national income (GNI) per capita (2017 PPP \$)']) # Define your independent variables with the correct column names X = df[['Human Development Index (HDI)',]'Gender Inequality Index', 'Life expectancy at birth (years)', 'Population age 15-64 years (millions)']] # Add a constant to the model (intercept) $X = sm.add_constant(X)$ # Define your dependent variable y = df['Gross national income (GNI) per capita (2017 PPP \$)'] # Fit the model model = sm.OLS(y, X).fit() # Print the summary print(model.summary()) **₹ OLS Regression Results** Dep. Variable: Gross national income (GNI) per capita (2017 PPP \$) R-squared: 0.684

Model: OLS Adj. R-squared: 0.676
https://colab.research.google.com/drive/1Tgpmw.luQyLbw.n2fz-pOEB6HxIZB7aFmR#scrollTo=-NlUqgSGAHPa

Method: Least Squares F-statistic: 84.85 Thu, 15 Aug 2024 Prob (F-statistic): 3.12e-38 Date: Time: 17:00:42 Log-Likelihood: -1741.0 No. Observations: 162 AIC: 3492. Df Residuals: 157 BIC: 3508. Df Model: 4

Covariance Type: nonrobust

coef std err t P>|t| [0.025 0.975]

const 4862.5341 2.08e+04 0.233 0.816 -3.63e+04 4.6e+04 Human Development Index (HDI) 0.000 4.65e+04 1.25e+05 8.552e+04 1.98e+04 4.329 **Gender Inequality Index** -3.777e+04 1.21e+04 -3.120 0.002 -6.17e+04 -1.39e+04 Life expectancy at birth (years) -458.8253 311.848 -1.471 0.143 -1074.784 157.134 Population age 15-64 years (millions) -6.5676 9.707 8.239 -0.797 0.427 -22.842

 Omnibus:
 70.466
 Durbin-Watson:
 1.495

 Prob(Omnibus):
 0.000
 Jarque-Bera (JB):
 255.494

 Skew:
 1.676
 Prob(JB):
 3.31e-56

 Kurtosis:
 8.158
 Cond. No.
 3.18e+03

Kurtosis: 8.158 Cond. No. 3.18e+03

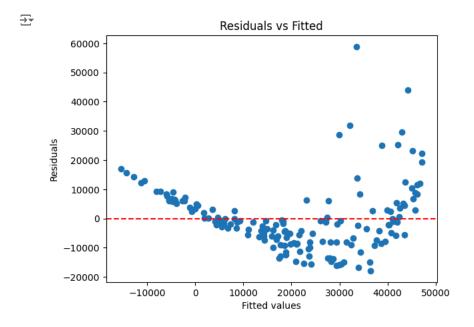
Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

[2] The condition number is large, 3.18e+03. This might indicate that there are strong multicollinearity or other numerical problems.

import matplotlib.pyplot as plt

plt.scatter(model.fittedvalues, model.resid)
plt.axhline(y=0, color='r', linestyle='-')
plt.xlabel('Fitted values')
plt.ylabel('Residuals')
plt.title('Residuals vs Fitted')
plt.show()

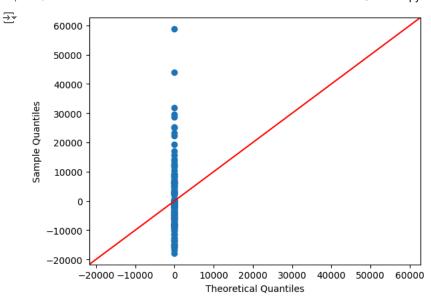


from statsmodels.stats.diagnostic import het_breuschpagan

test = het_breuschpagan(model.resid, model.model.exog)
labels = ['LM Statistic', 'LM Test p-value', 'F-Statistic', 'F-Test p-value']
print(dict(zip(labels, test)))

Fy (LM Statistic': 8.669127461722518, 'LM Test p-value': 0.06992328095234364, 'F-Statistic': 2.2191437851999827, 'F-Test p-value': 0.06935281133931234

sm.qqplot(model.resid, line ='45') plt.show()



 $from\ statsmodels.stats.outliers_influence\ import\ variance_inflation_factor$

```
vif_data = pd.DataFrame()
vif_data["feature"] = X.columns
vif_data["VIF"] = [variance_inflation_factor(X.values, i) for i in range(len(X.columns))]
print(vif_data)
```

Check the unique categories in the HDI Group column hdi_groups = df['HDI Group'].unique() print(hdi_groups) print(f"Number of HDI categories: {len(hdi_groups)}")

('Very high' 'High' 'Medium' 'Low')
Number of HDI categories: 4

df['HDI Group'] = pd.Categorical(df['HDI Group'], categories=['Low', 'Medium', 'High', 'Very high'], ordered=True)

- # Now create dummy variables, ensuring 'Low' is the reference category df = pd.get_dummies(df, columns=['HDI Group'], drop_first=True)
- # Check which dummy variables were created print(df.columns)



Gender Inequality Index float64
Life expectancy at birth (years) float64
Population age 15-64 years (millions) float64
HDI Group_Medium bool
HDI Group_ligh bool
HDI Group_very high bool
dtype: object

```
# Convert the columns to numeric, forcing errors to NaN (which can then be handled)
df['Gender Inequality Index'] = pd.to_numeric(df['Gender Inequality Index'], errors='coerce')
df['Life expectancy at birth (years)'] = pd.to_numeric(df['Life expectancy at birth (years)'], errors='coerce')
df['Population age 15-64 years (millions)'] = pd.to_numeric(df['Population age 15-64 years (millions)'], errors='coerce')
# Convert boolean columns to numeric
df['HDI Group_Medium'] = df['HDI Group_Medium'].astype(int)
df['HDI Group_High'] = df['HDI Group_High'].astype(int)
df['HDI Group_Very high'] = df['HDI Group_Very high'].astype(int)
# Check the data types to ensure all are numeric
print(df[['Gender Inequality Index',
      'Life expectancy at birth (years)',
      'Population age 15-64 years (millions)',
      'HDI Group_Medium', 'HDI Group_High', 'HDI Group_Very high']].dtypes)
Gender Inequality Index
                                         float64
      Life expectancy at birth (years)
                                         float64
      Population age 15-64 years (millions) float64
      HDI Group_Medium
                                          int64
      HDI Group_High
                                        int64
      HDI Group_Very high
                                          int64
      dtype: object
# Drop rows with NaN values
df = df.dropna(subset=['Gender Inequality Index',
               'Life expectancy at birth (years)',
              'Population age 15-64 years (millions)',
               'HDI Group_Medium', 'HDI Group_High', 'HDI Group_Very high'])
# Define your independent variables
X = df[['Gender Inequality Index',
     'Life expectancy at birth (years)',
     'Population age 15-64 years (millions)'.
     'HDI Group_Medium', 'HDI Group_High', 'HDI Group_Very high']]
# Add a constant to the model (intercept)
X = sm.add\_constant(X)
# Define your dependent variable
y = df['Gross national income (GNI) per capita (2017 PPP $)']
# Fit the model
model = sm.OLS(y, X).fit()
# Print the summary of the model
print(model.summary())
<del>_</del>_
                                   OLS Regression Results
                      Gross national income (GNI) per capita (2017 PPP $) R-squared:
                                                                                                     0.736
      Dep. Variable:
      Model:
                                                    OLS Adj. R-squared:
                                                                                    0.726
      Method:
                                              Least Squares F-statistic:
                                                                                     72.09
      Date:
                                           Thu, 15 Aug 2024 Prob (F-statistic):
                                                                                     2.41e-42
                                               17:00:43 Log-Likelihood:
      Time:
                                                                                   -1726.3
      No. Observations:
                                                       162 AIC:
                                                                                   3467
      Df Residuals:
                                                      155 BIC:
                                                                                  3488.
      Df Model:
                                                      6
      Covariance Type:
                                                   nonrobust
                                        std err
                                                     t
                                                          P>|t|
                                                                   [0.025
                                 -5428.5966 1.97e+04
                                                          -0.275
                                                                    0.784 -4.44e+04 3.36e+04
      Gender Inequality Index
                                       -3.498e+04 1.05e+04
                                                                -3.339
                                                                          0.001 -5.57e+04 -1.43e+04
      Life expectancy at birth (years)
                                         461.6654 254.551
                                                                1.814
                                                                          0.072
                                                                                   -41.171
                                                                                              964.501
      Population age 15-64 years (millions) -0.0110
                                                                                   -15.150
                                                                                              15.128
                                                       7.664
                                                                -0.001
                                                                          0.999
      HDI Group_Medium
                                       -3306.5352 3199.464
                                                                 -1.033
                                                                           0.303 -9626.715 3013.644
      HDI Group_High
                                      -3446.7064 3860.354
                                                               -0.893
                                                                         0.373 -1.11e+04 4178.988
      HDI Group_Very high
                                       1.558e+04 5214.288
                                                                 2.988
                                                                          0.003 5278.007 2.59e+04
      Omnibus:
                              60.766 Durbin-Watson:
                                                                  1.878
      Prob(Omnibus):
                                0.000 Jarque-Bera (JB):
                                                                 230.338
                                                          9.61e-51
                             1.390 Prob(JB):
      Skew:
```

Kurtosis: 8.138 Cond. No. 2.99e+03

Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

[2] The condition number is large, 2.99e+03. This might indicate that there are

strong multicollinearity or other numerical problems.

df = pd.read_csv('dataset.csv', encoding='cp1252')

Reorder the HDI Group to make 'Very High' the reference category

df['HDI Group'] = pd.Categorical(df['HDI Group'], categories=['Very high', 'Low', 'Medium', 'High'], ordered=True)

Create dummy variables again, this time 'Very High' will be the reference category (and thus not included in the dummy variables) df = pd.get_dummies(df, columns=['HDI Group'], drop_first=True)

Check to see which columns were created print(df.columns)

Show hidden output

Check the data types of all relevant columns

print(df[['Gender Inequality Index',

'Life expectancy at birth (years)',

'Population age 15-64 years (millions)',

'HDI Group_Low', 'HDI Group_Medium', 'HDI Group_High',

'Gross national income (GNI) per capita (2017 PPP \$)']].dtypes)

Gender Inequality Index object Life expectancy at birth (years) object Population age 15-64 years (millions) object HDI Group_Low bool HDI Group_Medium HDI Group_High bool

Gross national income (GNI) per capita (2017 PPP \$) object

dtype: object

Convert the columns to numeric, forcing errors to NaN (which can then be handled)

df['Gender Inequality Index'] = pd.to_numeric(df['Gender Inequality Index'], errors='coerce')

df['Life expectancy at birth (years)'] = pd.to_numeric(df['Life expectancy at birth (years)'], errors='coerce')

df['Population age 15-64 years (millions)'] = pd.to_numeric(df['Population age 15-64 years (millions)'], errors='coerce')

Convert boolean columns to numeric

df['HDI Group_Medium'] = df['HDI Group_Medium'].astype(int)

df['HDI Group_High'] = df['HDI Group_High'].astype(int)

df['HDI Group_Low'] = df['HDI Group_Low'].astype(int)

df['Gross national income (GNI) per capita (2017 PPP \$)'] = pd.to_numeric(df['Gross national income (GNI) per capita (2017 PPP \$)'], errors='coerce')

Drop rows with NaN values or handle them appropriately

df = df.dropna(subset=['Gender Inequality Index',

'Life expectancy at birth (years)',

'Population age 15-64 years (millions)',

'HDI Group_Low', 'HDI Group_Medium', 'HDI Group_High',

'Gross national income (GNI) per capita (2017 PPP \$)'])

Verify that all columns are now numeric

print(df[['Gender Inequality Index',

'Life expectancy at birth (years)',

'Population age 15-64 years (millions)',

'HDI Group_Low', 'HDI Group_Medium', 'HDI Group_High',

'Gross national income (GNI) per capita (2017 PPP \$)']].dtypes)

Gender Inequality Index float64 Life expectancy at birth (years) float64 Population age 15-64 years (millions) float64 HDI Group_Low int64 HDI Group_Medium int64 HDI Group_High int64

Gross national income (GNI) per capita (2017 PPP \$) float64

dtype: object

```
# Define your independent variables
```

X = df[['Gender Inequality Index',

'Life expectancy at birth (years)',

'Population age 15-64 years (millions)',

'HDI Group_Low', 'HDI Group_Medium', 'HDI Group_High']]

Add a constant to the model (intercept)

 $X = sm.add_constant(X)$

Define your dependent variable

y = df['Gross national income (GNI) per capita (2017 PPP \$)']

Fit the model

model = sm.OLS(y, X).fit()

Print the summary of the model

print(model.summary())

OLS Regression Results

Dep. Variable: Gross national income (GNI) per capita (2017 PPP \$) R-squared: 0.736 Model: OLS Adj. R-squared: 0.726 Method: 72.09 Least Squares F-statistic: Date: Thu, 15 Aug 2024 Prob (F-statistic): 2.41e-42 17:12:17 Log-Likelihood: -1726.3 Time: 162 AIC: No. Observations: 3467. Df Residuals: 155 BIC: 3488. Df Model: 6 Covariance Type: nonrobust

coef std err t P>|t| [0.025 0.975]

1.015e+04 2.11e+04 0.481 0.631 -3.15e+04 5.18e+04 const **Gender Inequality Index** 0.001 -5.57e+04 -1.43e+04 -3.498e+04 1.05e+04 -3.339Life expectancy at birth (years) 461.6654 254.551 1.814 0.072 -41.171 964.501 Population age 15-64 years (millions) -0.0110 7.664 -0.001 0.999 -15.150 15.128 HDI Group_Low -1.558e+04 5214.288 -2.988 0.003 -2.59e+04 -5278.007 HDI Group_Medium -1.888e+04 4001.807 -4.719 0.000 -2.68e+04 -1.1e+04 HDI Group_High -1.902e+04 2828.801 -6.725 0.000 -2.46e+04 -1.34e+04

 Omnibus:
 60.766
 Durbin-Watson:
 1.878

 Prob(Omnibus):
 0.000
 Jarque-Bera (JB):
 230.338

 Skew:
 1.390
 Prob(JB):
 9.61e-51

 Kurtosis:
 8.138
 Cond. No.
 3.10e+03

Notes:

[1] Standard Errors assume that the covariance matrix of the errors is correctly specified.

[2] The condition number is large, 3.1e+03. This might indicate that there are

strong multicollinearity or other numerical problems.

Create interaction terms between HDI groups and GII

 $df['Interaction_Low_GII'] = df['HDI\ Group_Low'] \ * \ df['Gender\ Inequality\ Index']$

 $df['Interaction_Medium_GII'] = df['HDI\ Group_Medium'] \ *\ df['Gender\ Inequality\ Index']$

 $df['Interaction_High_GII'] = df['HDI\ Group_High'] * df['Gender\ Inequality\ Index']$

Define the independent variables including the interaction terms

X = df[['Gender Inequality Index',

'Life expectancy at birth (years)',

'Population age 15-64 years (millions)',

'HDI Group_Low', 'HDI Group_Medium', 'HDI Group_High',

'Interaction_Low_GII', 'Interaction_Medium_GII', 'Interaction_High_GII']]

Add a constant to the model (intercept)

 $X = sm.add_constant(X)$

Define the dependent variable

y = df['Gross national income (GNI) per capita (2017 PPP \$)']

Fit the model

model = sm.OLS(y, X).fit()

Print the summary of the model print(model.summary())

 $\overline{\mathbf{T}}$

OLS Regression Results

Dep. Variable: Gross national income (GNI) per capita (2017 PPP \$\) R-squared: 0.772

Model: OLS Adj. R-squared: 0.759

Method: Least Squares F-statistic: 57.34

 Date:
 Thu, 15 Aug 2024
 Prob (F-statistic):
 2.04e-44

 Time:
 17:35:01 Log-Likelihood:
 -1714.4

 No. Observations:
 162 AIC:
 3449.

 Df Residuals:
 152 BIC:
 3480.

 Df Model:
 9

Covariance Type: nonrobust

coef std err t P>|t| [0.025 0.975]

const 2.169e+04 2.04e+04 1.061 0.291 -1.87e+04 6.21e+04 **Gender Inequality Index** 0.000 -1.1e+05 -5.49e+04 -8.243e+04 1.39e+04 -5.926Life expectancy at birth (years) 408.8524 245.086 1.668 0.097 -75.362 893.067 Population age 15-64 years (millions) 2.6840 0.368 0.713 -11.714 17.082 7.288 HDI Group_Low -4.933e+04 1.55e+04 -3.184 0.002 -7.99e+04 -1.87e+04 HDI Group_Medium 0.000 -7.1e+04 -2.48e+04 -4.788e+04 1.17e+04 -4.096HDI Group_High -3.845e+04 6541.483 -5.878 0.000 -5.14e+04 -2.55e+04 Interaction Low GII 8.987e+04 2.81e+04 3.194 0.002 3.43e+04 1.45e+05 Interaction_Medium_GII 9.03e+04 2.66e+04 3.401 0.001 3.78e+04 1.43e+05 Interaction_High_GII 7.989e+04 2.07e+04 3.869 0.000 3.91e+04 1.21e+05

 Omnibus:
 80.198
 Durbin-Watson:
 2.145

 Prob(Omnibus):
 0.000
 Jarque-Bera (JB):
 477.270

 Skew:
 1.714
 Prob(JB):
 2.30e-104

 Kurtosis:
 10.678
 Cond. No.
 5.27e+03

Autosis. 10.070 Collativo. 5.276-05

Notes

- [1] Standard Errors assume that the covariance matrix of the errors is correctly specified.
- [2] The condition number is large, 5.27e+03. This might indicate that there are $\,$