

Phase Field (University of Florida)

Gibbs Energy Minimiser (This Work)

$$G = \sum_j h_j g_j + W g(\eta_j)$$

$$c_i = \sum_j h_j c_{ij}$$

$$\frac{\partial G_j}{\partial c_{ij}} = \frac{\partial G_{j'}}{\partial c_{ij'}}$$

$$\frac{\partial c_i}{\partial t} = \nabla \cdot M_i \nabla \left(\frac{\partial g_{\text{loc}}}{\partial c_i} - \kappa_i \nabla^2 c_i + \frac{\partial E_d}{\partial c_i} \right)$$

$$\frac{\partial \eta_j}{\partial t} = -L \left(\frac{\partial g_{\text{loc}}}{\partial \eta_j} - \kappa_j \nabla^2 \eta_j + \frac{\partial E_d}{\partial \eta_j} \right)$$

$$G = \sum_{\phi=1}^{\Phi} n_{\phi} \sum_{i=1}^{N_{\phi}} x_i \mu_{ij}$$

$$b_j = \sum_{\phi=1}^{\Phi} n_{\phi} \sum_{i=1}^{N_{\phi}} x_i \nu_{ij}$$

$$\mu_i = \sum_{j=1}^C \nu_{ij} \Gamma_j$$

$$\frac{1}{\chi_i} = \left(\frac{\partial^2 G}{\partial n_i^2} \right)_{T,P,n_{j \neq i}}$$

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