

# DEVELOPMENT OF A NEW THERMOCHEMISTRY CODE FOR MULTIPHYSICS SIMULATIONS OF NUCLEAR MATERIALS

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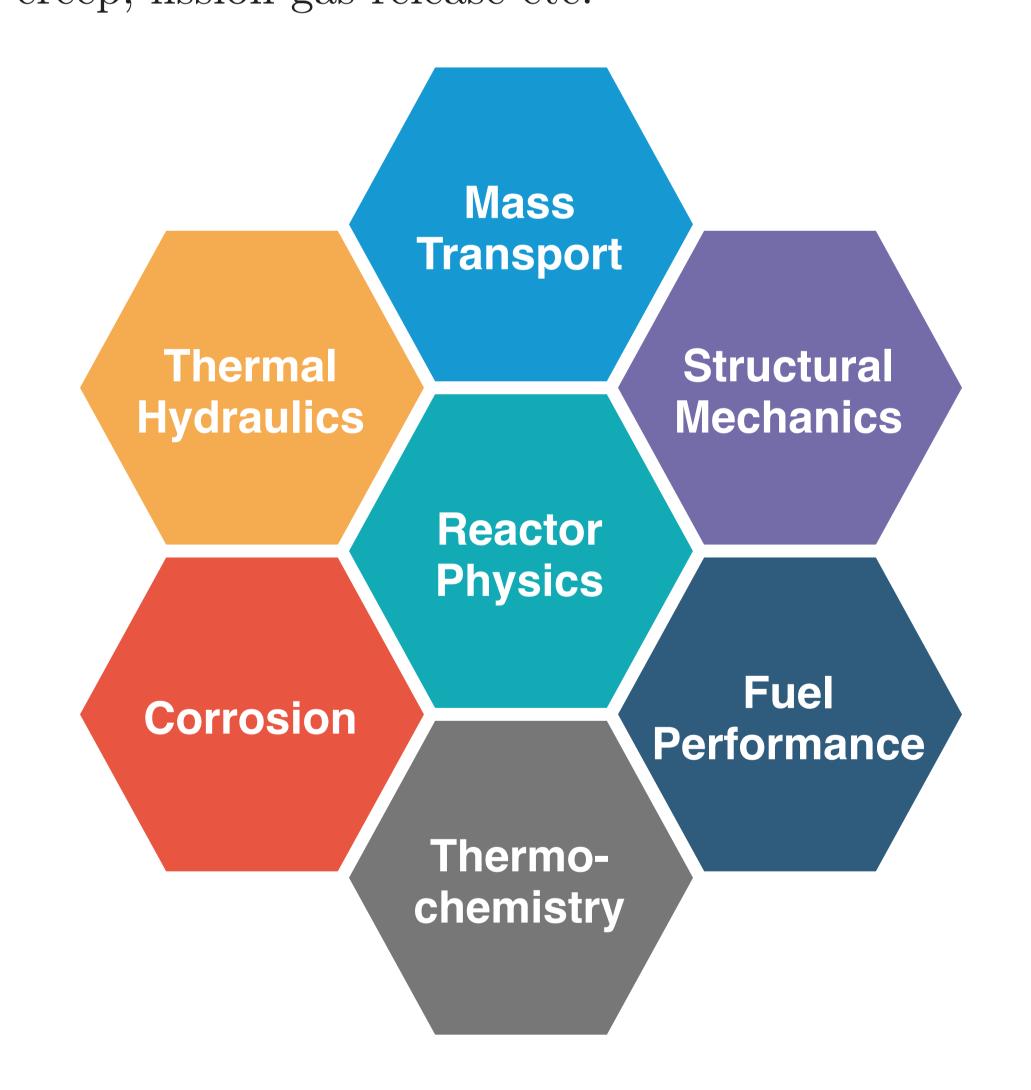


# OBJECTIVES

Recently, there has been an increasing interest in direct coupling of thermodynamic computations with multiphysics codes such as INL's MOOSE. A new thermochemistry code is being developed to provide rapid access to thermodynamic databases and perform thermochemical calculations for a range of different materials including nuclear fuels. This poster describes the preliminary work done in this direction and plans for developing capabilities of practical interest to the nuclear industry.

### INTRODUCTION

Nuclear reactors are highly complex multiscale, multiphysics systems with strong coupling between various phenomena such as temperature, creep, fission gas release etc.



Idaho National Laboratory's **Multiphysics Ob**ject Oriented Simulation Environment (MOOSE) provides the computational foundation for performing multiphysics simulations suitable in such problems and a new MOOSE-based application called Yellowjacket is under development to model corrosion and fuel problems.

The thermochemistry solver within Yellowjacket will use Gibbs Energy Minimisation to provide material properties and boundary conditions such as the phase distribution and chemical potentials in molten salts.

# THERMODYNAMIC EQUILIBRIUM

Thermochemical equilibrium calculations are based on minimising the integral Gibbs energy of a closed system at constant temperature and hydrostatic pressure.

• Integral Gibbs energy of the system

$$G = RT \left( \sum_{\lambda=1}^{\Lambda} n_{\lambda} \sum_{i=1}^{N_{\lambda}} x_{i(\lambda)} \tilde{\mu}_{i} + \sum_{\omega=1}^{\Omega} n_{\omega} \tilde{\mu}_{\omega} \right)$$

• Chemical potential of ideal phase species

$$\tilde{\mu}_i = \tilde{g}_{i(\lambda)}^0 + \ln(x_{i(\lambda)})$$

• Chemical potential of non-ideal phase species

$$\tilde{\mu}_i = \tilde{g}_{i(\lambda)}^0 + \tilde{g}_{i(\lambda)}^{ex} + \ln(x_{i(\lambda)})$$

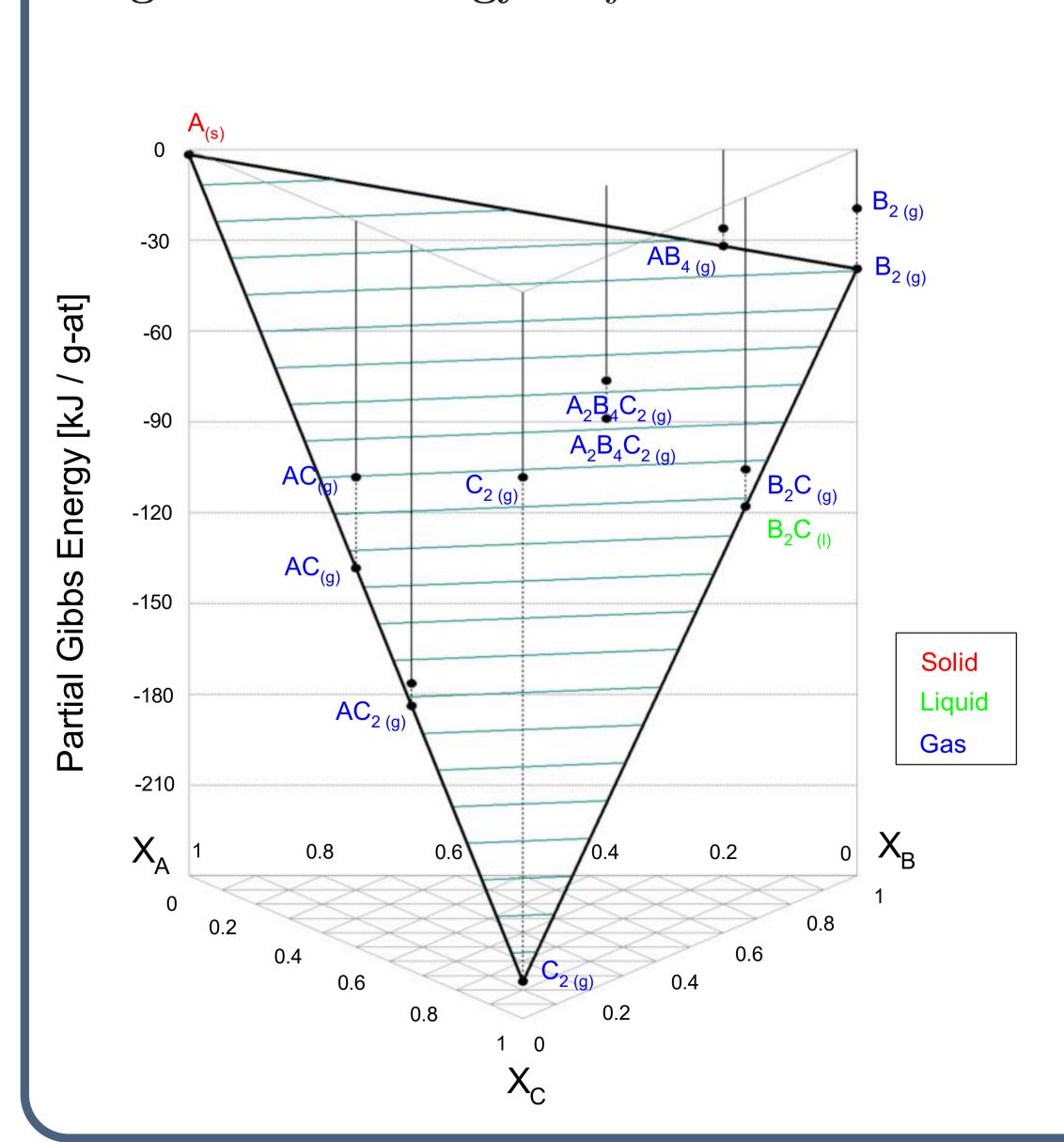
#### COMPUTATIONAL FRAMEWORK Read and verify the data file and store the Gibbs energy coefficient of Read the parameters - temperature, pressure and composition from other Input using levelling method **YELLOW** Find the stable phases by minimising Gibbs Energy the Gibbs energy of the non-ideal **JACKET** Apply non-convex optimisation Chem Poten Global schemes to find the global minimum for complex systems Moles - Phases Output Moles - Species Solver Pass back the output such as chemical potential, Gibbs energy, Output etc. to other codes Gibbs Energy

# Coding Tools

- Environment: MOOSE
- Language: C++
- Data File Format: ChemSage (\*.dat)
- Library: PETSc/Tao, LAPACK
- Documentation: MooseDocs
- Testing: CIVET

# GIBBS ENERGY MINIMISATION

From a numerical point of view, the objective of computing thermochemical equilibria is to **determine** a unique combination of phases and their composition that yields a global minimum in the integral Gibbs energy subject to various linear and non-linear equality and inequality constraints.



## Necessary conditions

Conservation of mass

$$b_j = \sum_{\lambda=1}^{\Lambda} n_{\lambda} \sum_{i=1}^{N_{\lambda}} x_{i(\lambda)} \nu_{i,j} + \sum_{\omega=1}^{\Omega} n_{\omega} \nu_{\omega}$$

• Gibbs' phase rule

$$F = C - \Phi + 2$$

• Gibbs' criterion

$$\mu_i = \sum_{j=1}^C \nu_{i,j} \Gamma_j$$

#### Sufficient condition

• Integral Gibbs energy at global minimum

$$\pi_{\lambda} = \min_{\lambda} \sum_{i=1}^{N_{\lambda}} x_{i(\lambda)} \left( \mu_{i(\lambda)} - \sum_{j=1}^{C} a_{i,j} \Gamma_{j} \right)$$

# CONCLUSION

The new MOOSE based app, Yellowjacket, is aimed at developing corrosion modelling capability for advanced reactors and will help in improving multiphysics simulations for nuclear reactor materials by coupling thermochemistry computations with continuum and meso-scales models.

### ACKNOWLEDGEMENT

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