
Example 4.18

1. According to the Chomsky hierarchy, CFG is type _____ grammar.
2. The grammar where production rules are in the format of $\{A \text{ string consists of at least one non-terminal}\} \rightarrow \{A \text{ string of terminals and/or non-terminals}\}$ is _____ grammar in particular.
3. The grammar $S \rightarrow aSb/bSc/C$ produces the string _____.
4. Finding a derivation for a string from a given grammar is called _____.
5. The tree representation of deriving a context-free language from a given context grammar is called _____.
6. A parse tree construction is only possible for _____ grammar.
7. The root of the parse tree of a given context-free language is represented by the _____ of the corresponding CFG.
8. A CFG G is said to be _____ if there exists some $w \in L(G)$ that has at least two distinct parse trees.
9. A CFL L is said to be _____ if all its grammars are ambiguous.
10. The CFG where a non-terminal ' A ' as a leftmost symbol appears alternatively at the time of derivation either immediately or through some other non-terminal definitions is called _____ grammar.
11. To avoid the problem of backtracking, we need to perform _____.
12. In a CFG, the symbols which do not produce any terminal string is called _____.
13. In a CFG, the symbols which cannot be reached at any time starting from the start symbol are called _____.
14. In a CFG, non-generating symbols and non-reachable symbols are both called _____ symbol.
15. In a CFG, the production in the form non-terminal \rightarrow single non-terminal is called _____.
16. In a CFG, a production in the form $NT \rightarrow \epsilon$ is called _____.
17. Normalizing a CFG should not hamper the _____ power of the grammar.

18. A CFG where all the productions of the grammar are in the form
 Non-terminal \rightarrow string of exactly two non-terminals
 Non-terminal \rightarrow single terminal
 is called --- normal form.
19. A CFG where all the productions of the grammar are in the form
 Non-terminal \rightarrow (single terminal)(string of non-terminals)
 Non-terminal \rightarrow single terminal
 is called --- normal form.
20. Context-free languages are not closed under --- and --- .
21. --- is used to prove that certain sets are not context free.

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22. $a^n b^n c^n$, where $n \geq 1$, is not --- language but --- language.
23. If the length of the longest path of the directed graph generated from a CFG is n , then the longest
 string generated by the grammar is --- .
24. A language L generated from a given CFG is finite if there are no --- in the directed graph generated from the production rules of the given CFG.

1 picture

Answers:

- | | | |
|-------------------------------------|-----------------------------------|--------------------------------|
| 1. Two | 2. context-free | 3. $WCW^R \mid W \in (a, b)^*$ |
| 4. parsing | 5. parse tree | 6. context-free |
| 7. start symbol | 8. ambiguous | 9. inherently ambiguous |
| 10. left recursive | 11. left factoring | 12. non-generating symbols |
| 13. non-reachable symbols | 14. useless | 15. unit production |
| 16. null production | 17. language generating | 18. Chomsky |
| 19. Greibach | 20. intersection, complementation | 21. Pumping lemma for CFL |
| 22. context free, context sensitive | 23. 2^n | 24. cycles |

Exercise

1. Construct a CFG for the following.
 - a) $a^n a^m$, where $n > 0$ and $m = n + 1$
 - b) $a^n b a^m$, where $m, n > 0$
 - c) $a^n b^n c^m$, where $n > 0$ and $m = n + 1$
 - d) $L = (011 + 1) * (01)^*$
 - e) $L = \{Set\ of\ all\ integers\}$

2. a) Construct the string 0110001 from the grammar

$$\begin{aligned}
 S &\rightarrow AB \\
 A &\rightarrow 0A/1B/0 \\
 B &\rightarrow 1A/0B/1
 \end{aligned}$$

By using

- i) Leftmost derivation
- ii) Rightmost derivation

- b) Construct the string $baaabba$ from the grammar

$$\begin{aligned}
 S &\rightarrow AaB/AbB \\
 A &\rightarrow Sa/b \\
 B &\rightarrow Sb/a
 \end{aligned}$$

By using

- i) Leftmost derivation
- ii) Rightmost derivation

3. a) Find the parse tree for generating the string $abaabaa$ from the given grammar.

$$\begin{aligned}
 S &\rightarrow aAS/a \\
 A &\rightarrow bS
 \end{aligned}$$

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- b) Find the parse tree for generating the string $aabbaa$ from the given grammar.

$$S \rightarrow aAS/a$$

$$A \rightarrow SbA/SS/ba$$

4. Show that the following grammars are ambiguous.

- a) $S \rightarrow abSb/aAb/a$
 $A \rightarrow bS/aAAb$
- b) $E \rightarrow E + E/E * E/id$
- c) $S \rightarrow aB/bA$
 $A \rightarrow aS/bAA/a$
 $B \rightarrow bS/aBB/b$

5. Remove the useless productions from the following grammar

- a) $S \rightarrow AB/a$
 $A \rightarrow b$
- b) $S \rightarrow AB/AC$
 $A \rightarrow 0A1/1A0/0$
 $B \rightarrow 11A/00B/AB$
 $C \rightarrow 01C0/0D1$
 $D \rightarrow 1D/0C$

6. Remove the unit production from the following grammar:

- a) $S \rightarrow SaA$
 $A \rightarrow aB/B/b$
 $B \rightarrow bC/C/a$
 $C \rightarrow ab$
- b) $S \rightarrow Aa/B$
 $B \rightarrow A/bb$
 $A \rightarrow a/bc/B$

7. Remove the null production from the following grammar

- a) $S \rightarrow aAB$
 $A \rightarrow Bb$
 $B \rightarrow \epsilon$
- b) $S \rightarrow aA$
 $A \rightarrow bB$
 $B \rightarrow b$
 $B \rightarrow \epsilon$

8. Simplify the following CFG.

$$S \rightarrow AB/aB$$

$$A \rightarrow BC/B/a$$

$$B \rightarrow C$$

$$C \rightarrow b/ \epsilon$$

9. i) Convert the following left linear grammar into right linear grammar.

$$S \rightarrow Sab/Aa$$

$$A \rightarrow Abb/bb$$

- ii) Convert the following right linear grammar into left linear grammar.

$$S \rightarrow aaB/ab$$

$$B \rightarrow bB/bb$$

10. Convert the following linear grammar into regular grammar.

$$S \rightarrow 01B/0$$

$$B \rightarrow 1B/11$$

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11. Convert the following grammar into CNF.

a) $S \rightarrow AB$

$$A \rightarrow aA/a$$

$$B \rightarrow ab/bB/b$$

b) $S \rightarrow aSa/SSa/a$

12. Convert the following grammar into GNF.

a) $S \rightarrow Abb/a$

$$A \rightarrow aaA/B$$

$$B \rightarrow bAb$$

b) $S \rightarrow aSb/bSa/a/b$

13. Construct a DFA equivalent to the regular grammar.

a) $S \rightarrow aS/bA/b$

$$A \rightarrow aA/bS/a$$

b) $S \rightarrow bA/aB$

$$A \rightarrow bA/aS/a$$

$$B \rightarrow aB/bS/b$$

14. Prove that $L = a^n b^n c^2 n$ is not context free by using the pumping lemma for CFL.

15. Verify whether the languages generated by the following grammar are finite or not.

- a) $S \rightarrow aA$
 $A \rightarrow BC$
 $B \rightarrow SC/b$
 $C \rightarrow B/a$
- b) $S \rightarrow AB$
 $A \rightarrow C/a$
 $B \rightarrow AC/b$

16. Remove the left recursion from the following grammar and then perform left factoring.

$$E \rightarrow E + T \mid T \quad T \rightarrow T * F \mid F \quad F \rightarrow G^F \mid G \quad G \rightarrow id \mid (E)$$

17. Generate the string $id + id * id$ from the grammar

$$E \rightarrow E + E \quad E \rightarrow E * E \quad E \rightarrow id$$

where the precedence of operator is given as follows.

	+	*
+	>	<
*	>	<

Are you getting any ambiguity in the grammar?