

# Fair Convex Partitions of Convex Polygons

Paritosh Borkar(pb2982) and Vineet Kamat(vvk1199)

## Summary

We will be tackling open problem 67 from the list of open problems provided. The problem talks about whether a given convex polygon can be divided into  $n$  convex pieces of equal areas and perimeters, where  $n$  is a natural number. This problem has solutions for some values of  $n$ . This problem has been partially solved for  $n = p^k$  where  $p$  is a prime number and  $k$  is an integer.

A fair partition of a convex polygon is described as partitions that have equal areas and perimeters. A fair partition is convex if the pieces are also convex.

We would also like to create an online tool that finds partitions as mentioned above, for any random convex polygon.

## Timeline

| Week # | Deliverables  | Artifacts  |
|--------|---|--|
| 4      | Dive deep into the scope of the solutions of the problem.   |  |
| 5      | Recreate the known solutions ourselves and create the framework for an online tool for demonstrating these solutions. | - Week 6 presentation document                       |
| 6      | Present the overview of the project. Start developing new approaches to solving the problem.                          |  |
| 7      | Test new approaches to tackle the problem for different values of $n$ .   | - Experiment results document                        |
| 8      | Continue with testing new methods. Create an online tool that finds a partition of a polygon for the known solutions. | - Online tool to demonstrate the problem's solutions |
| 9      | Make UI improvements on the online tool. If alternative or new solutions are found, update the online tool.           |  |
| 10     | Present work done so far on the project and steps to wrap up the project.   | - Week 10 progress presentation document             |
| 11     | Document our findings and report any failures or successes achieved during the entire process.                        | - Final project document                             |
| 12     | Final presentation  | - Final presentation document                        |

## Work Distribution

### PARITOSH

- Responsible for researching the problem and figuring out the scope and extent of the solutions to the problem.
- Responsible for testing new approaches to solving the problem.
- Responsible for updating the final project document.

### VINEET

- Responsible for creating the online tool for demonstrating the solutions to the problem.
- Responsible for researching new improvements to existing solutions.
- Responsible for updating the final project document.

## Sources

<http://cs.smith.edu/~jorourke/TOPP/P67.html#Problem.67>

[https://parasol.tamu.edu/~amato/Courses/620/openProblems/csce620-openProblem-P67\\_FairPartitioning\\_NicolasCastet.pdf](https://parasol.tamu.edu/~amato/Courses/620/openProblems/csce620-openProblem-P67_FairPartitioning_NicolasCastet.pdf)

<https://arxiv.org/abs/0812.2241> for  $2^k$  partitions

<https://arxiv.org/abs/1011.4762v2> for  $p^k$  partitions where  $p$  is any prime number

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