

1. a) 12-bit binary representation of -142_{10}

$$\begin{aligned} -142_{10} &= -0b\ 0000\ 1000\ 1110 \\ &= -0b\ 1111\ 0111\ 0001 + 1 \\ &= \mathbf{0b\ 1111\ 0111\ 0010} \end{aligned}$$

- b) 12-bit binary: $119 + (-142)$

$$\begin{aligned} 119_{10} &= 0b\ 0000\ 0111\ 0111 \\ -142_{10} &= 0b\ 1111\ 0111\ 0010 \\ 119 + (-142) &= -23 \\ &= \mathbf{0b\ 1111\ 1110\ 1001} \end{aligned}$$

- c) Smallest number of bits that can correctly represent the signed binary of 56841_{10}

$$\begin{aligned} 56841_{10} &= 0b\ 0\ 1101\ 1110\ 0001\ 0010 \\ 16\ \text{bits} + 1\ (\text{signed}) &= \mathbf{17\ \text{minimum bits.}} \end{aligned}$$

- d) Unsigned hexadecimal of 56841_{10}

$$\begin{aligned} 56841_{10} &= 0b\ 1101\ 1110\ 0001\ 0010\ (\text{unsigned}) \\ &= \mathbf{0x\ DE12} \end{aligned}$$

2. Using the 32-bit IEEE-754 standard:

- a) Binary of 572.375_{10} :

$$\begin{aligned} 572.375_{10} &= 0b\ 0010\ 0011\ 1100\ .\ 0110 \\ &= (-1)^1 * 1.0001111000110 * 2^9 \end{aligned}$$

$$S = 0$$

$$\text{Fraction} = 0\ 0011\ 1100\ 0110$$

$$\text{Exp} = 9 + 127 = 136 = 0b\ 1000\ 1000\ (\text{single})$$

$$= 9 + 1023 = 1032 = 0b\ 100\ 0000\ 1000\ (\text{double})$$

$$= \mathbf{0b\ 0\ 1000\ 1010\ 000\ 1111\ 0001\ 1000\ 0000\ 0000\ (\text{single})}$$

$$\begin{aligned} &= \mathbf{0b\ 0\ 100\ 0000\ 1000\ 0\ 0011\ 1100\ 0110\ 0000\ 0000\ 0000\ 0000\ 0000\ 0000\ 0000\ 0000} \\ &\mathbf{0000\ 000\ (\text{double})} \end{aligned}$$

- b) Most negative floating-point number in 32-bit IEEE-754 format

$$\begin{aligned} x &= (-1)^1 * (1 + 2^{23}) * 2^{(254-127)} \\ &= -340282346638528859811704183484516925440 \\ &= \mathbf{-3.402823 * 10^{38}} \end{aligned}$$

c) Binary representation

S=1

Fraction = 111 1111 1111 1111 1111 1111

Exp = 127 + 127 = 254 = 0b 1111 1110

= **0b 1 1111 1110 111 1111 1111 1111 1111**

3. Decimal 472.2

- a. Why can't we use 32-bit IEEE 754 to represent 472.2 accurately?

Same reason why we can't represent 1/3 in decimals accurately. 0.2 has a repeating mantissa (1100) when represented in binary.

- b. Can we use 64-bit IEEE-754 instead?

No, repeating mantissa (1100) will keep on repeating throughout history.

4. Given Register values:

.text

\$t1 = 0x0004

\$s0 = 0x01A7

\$a1 = 0x6B20

\$sp = 0x8034

.code

```
addi    $sp, $sp, -4           ; $sp = 0x8030
sw      $s0, 0($sp)           ; store address of stack pointer (word) to $s0
add     $s0, $zero, $zero      ; $s0 = 0x0000
add     $t1, $s0, $a1          ; $t1 = 0x0000 + 0x6B20
```

Result:

\$t1 = 0x6B20

\$s0 = 0x0000

\$a1 = 0x6B20

\$sp = 0x8030

5. a) see prime_number.c

b) see run.sh

c) I checked. It looks like it works.

d) More command added to run.sh

e) out of the 8 registers for x86 (eax, ebx, ecx, edx, esi, edi, ebp, esp), it only used:

eax, edx

f) more code added to run.sh

g) Out of the 32 registers for MIPS architecture, it only used:

\$0 (zero), \$31 (return address), \$sp (stack pointer) and \$2 (return value)