12강.Actor-Critic: PPO

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- Code Ex.

Advantage GAE

• A
$$\pi$$
(s, a) = Q π (s, a) - V^{π} (s)

$$\longrightarrow$$
 V $\pi(s) = \sum_a \pi(a|s)Q \pi(s, a)$

- If A(s, a1) is +, relatively good action, if bad action
 - Mean advantage is 0:

$$E^{\pi}[A^{\pi}(s, a)|s] = \sum_{\alpha} \pi(a|s)[Q^{\pi}(s, a) - V^{\pi}(s)] = V^{\pi}(s) - V^{\pi}(s) = 0$$

• The mean gradient is the same, but the sample mean gradient variance is low because $Q^{\pi\theta}(s,a)$ - $V^{\pi\theta}(s) < Q^{\pi\theta}(s,a)$

•
$$\nabla_{\theta} J(\theta) = \sum_{a} \pi_{\theta}(a|s) Q^{\pi\theta}(s,a) \nabla_{\theta} log \pi_{\theta}(a|s)$$

= $\sum_{a} \pi_{\theta}(a|s) [Q^{\pi\theta}(s,a) - V^{\pi\theta}(s)] \nabla_{\theta} log \pi_{\theta}(a|s)$

•
$$\nabla_{\theta} J(\theta) \approx \frac{1}{n} \sum_{(s,a,r,s')} sg\left(Q^{\pi\theta}(s,a)\right) \nabla_{\theta} log \pi_{\theta}(a|s)$$
 High variance
$$\approx \frac{1}{n} \sum_{(s,a,r,s')} sg\left(Q^{\pi\theta}(s,a) - \bigvee^{\pi\theta}(s)\right) \nabla_{\theta} log \pi_{\theta}(a|s)$$
 Low variance

Adv. expressed by the value function:

$$A^{\pi}(s, a) = r + V^{\pi}(s') - V^{\pi}(s)$$

→ 1-step TD error!

Adv. expressed by the action-value function:

A
$$\pi(s, a) = Q \pi(s, a) - \sum_b \pi(b|s) Q^{\pi}(s, b)$$

or
A $\pi(s, a) = r + \gamma Q \pi(s', a') - \sum_b \pi(b|s) Q^{\pi}(s, b)$

Actor loss expressed by the value function Adv.:

$$L_{actor}(\theta) = -\frac{1}{n} \sum_{(s,a,r,s')} sg\left(r + \gamma V^{\pi\theta}(s') - V^{\pi\theta}(s)\right) \log \pi_{\theta}(a|s)$$

$$\nabla_{\theta} L_{actor}(\theta) \approx \hat{E} \left[A^{\pi\theta}(s,a) \nabla_{\theta} log \pi_{\theta}(a|s)\right]$$
Could be n-step TD target!

Actor loss expressed by the action-value function Adv.:

$$L_{actor}(\theta) = -\frac{1}{n} \sum_{(s,a,r,s')} sg(Q^{\pi}(s,a) - \sum_{b} \pi(b|s) Q^{\pi}(s,b)) \log \pi_{\theta}(a|s)$$

$$Or$$

$$L_{actor}(\theta) = -\frac{1}{n} \sum_{(s,a,r,s')} sg(r + \gamma Q^{\pi}(s',a') - \sum_{b} \pi(b|s) Q^{\pi}(s,b)) \log \pi_{\theta}(a|s)$$

Could be n-step TD target!

```
Initialize 	heta of the parameterized policy \pi_{	heta} and value function V_{	heta} and learning rate \eta.
While True
    Collect a trajectory of length L, \tau = (s_t, a_t, r_{t+1}, \cdots, s_{t+L_1}, a_{t+L-1}, r_{t+L}, s_{t+L}).
    L_{critic}(\theta) = L_{actor}(\theta) = L_{exp}(\theta) = 0
    For i \in 0: L-1
        L_{critic}(\theta) \leftarrow L_{critic}(\theta) + (r_{t+i} + \gamma \cdot sg(V_{\theta}(s_{t+1+i})) - V_{\theta}(s_{t+i}))^2
        L_{actor}(\theta) \leftarrow L_{actor}(\theta) - sg(r_{t+i} + \gamma V_{\theta}(s_{t+1+i}) - V_{\theta}(s_{t+i})) \log \pi_{\theta}(a_{t+i}|s_{t+i})
         L_{exp}(\theta) \leftarrow L_{exp}(\theta) - H(\pi_{\theta}(\cdot|s_{t+i}))
    L_{total}(\theta) = c_1 L_{critic}(\theta) + c_2 L_{actor}(\theta) + c_3 L_{exp}(\theta)
    \theta \leftarrow \theta - \eta \nabla_{\theta} L_{total}(\theta)
```

Initialize heta of the parameterized policy $\pi_{ heta}$ and value function $V_{ heta}$ and learning rate η . While True

Collect a trajectories of length
$$\underline{L}, \{\tau_1, \tau_2, \cdots, \tau_n\}$$
. Multiple trajectories from paralleled environments
$$L_{critic}(\theta) = L_{actor}(\theta) = L_{exp}(\theta) = 0$$
 Multiple trajectories from paralleled environments
$$\underline{For} \ \tau \in \{\tau_1, \tau_2, \cdots, \tau_n\}$$
 For $i \in 0 : L-1$
$$L_{critic}(\theta) \leftarrow L_{critic}(\theta) + \left(r_{t+1+i} + \gamma \cdot sg(V_{\theta}(s_{t+1+i})) - V_{\theta}(s_{t+i})\right)^2$$

$$L_{actor}(\theta) \leftarrow L_{actor}(\theta) - \left(r_{t+1+i} + \gamma \cdot sg(V_{\theta}(s_{t+1+i})) - V_{\theta}(s_{t+i})\right) \log \pi_{\theta}(a_{t+i}|s_{t+i})$$

$$L_{exp}(\theta) \leftarrow L_{exp}(\theta) - H(\pi_{\theta}(\cdot|s_{t+i}))$$

$$L_{total}(\theta) = c_1 L_{critic}(\theta) + c_2 L_{actor}(\theta) + c_3 L_{exp}(\theta)$$

$$\theta \leftarrow \theta - \eta/n \nabla_{\theta} L_{total}(\theta)$$

GAE

•
$$A_n^{\pi}(s_t, a_t) = r_{t+1} + \gamma r_{t+2} + ... + r_n + V^{\pi}(s_{t+n}) - V^{\pi}(s_t)$$

N-step TD target

$$= \delta_t^{(n)}$$
N-step TD error

- $A_n(s_t, a_t) = r_{t+1} + \gamma r_{t+2} + ... + r_n + V_{\theta}^{\pi}(s_{t+n}) V_{\theta}^{\pi}(s_t)$
 - True value function is unknown. We use learnt value function
 - As n grows, the estimation become closer to the true value
 - But variance grows because $r_{t+1} < r_{t+1} + \gamma r_{t+2} + ... + r_n$
 - Mixing various n size, we can find a sweet spot that outputs both precise estimation and low variance
 - → TD(lambda)

GAŁ

•
$$A_{GAE(\gamma,\lambda)}(s_t, a_t) = (1-\lambda)(A_1(s_t, a_t) + \lambda A_2(s_t, a_t) + \lambda^2 A_3(s_t, a_t) + ...)$$

• δ_t $\delta_t + \lambda \delta_{t+1}$ $\delta_t + \gamma \delta_{t+1} + \gamma^2 \delta_{t+1}$

- A_{n} (st, at) = $\delta_{t} + \gamma \delta_{t+1} + \gamma^{2} \delta_{t+1} + ... + \gamma^{n-1} \delta_{t+n}$ We want $\lambda + \lambda^{2} + ... + \lambda^{n-1}$ to be 1, so multiply (1λ)
- $A_{GAE(\gamma \lambda)}(s_t, a_t) = \delta_t + (\gamma \lambda)\delta_{t+1} + (\gamma \lambda)^2 \delta_{t+2} + \cdots$
 - If $\lambda' = 0 : 1$ -step
 - If $\lambda \to 1$: As λ grows, $A_{GAE(\gamma \lambda)}(s_t, a_t)$ is closer to the true Return

GAE

```
Initialize 	heta of the parameterized policy \pi_{	heta} and value function V_{	heta} and learning rate \eta.
While True
    Collect a trajectory of length L, \tau = (s_t, a_t, r_{t+1}, \cdots, s_{t+L_1}, a_{t+L-1}, r_{t+L}, s_{t+L}).
    L_{critic}(\theta) = L_{actor}(\theta) = L_{exp}(\theta) = 0
    For i \in 0: L-1
        L_{critic}(\theta) \leftarrow L_{critic}(\theta) + (r_{t+i} + \gamma \cdot sg(V_{\theta}(s_{t+1+i})) - V_{\theta}(s_{t+i}))^2
         L_{actor}(\theta) \leftarrow L_{actor}(\theta) - sg(A_{GAE(\gamma,\lambda)}(s_{t+i}, a_{t+i})) \log \pi_{\theta}(a_{t+i}|s_{t+i})
         L_{exp}(\theta) \leftarrow L_{exp}(\theta) - H(\pi_{\theta}(\cdot|s_{t+i}))
    L_{total}(\theta) = c_1 L_{critic}(\theta) + c_2 L_{actor}(\theta) + c_3 L_{exp}(\theta)
    \theta \leftarrow \theta - \eta \nabla_{\theta} L_{total}(\theta)
```

GAE

Initialize heta of the parameterized policy $\pi_{ heta}$ and value function $V_{ heta}$ and learning rate η . While True

```
Collect a trajectories of length L, \{\tau_1, \tau_2, \cdots, \tau_n\}. L_{critic}(\theta) = L_{actor}(\theta) = L_{exp}(\theta) = 0 For \tau \in \{\tau_1, \tau_2, \cdots, \tau_n\} For i \in 0 : L - 1 L_{critic}(\theta) \leftarrow L_{critic}(\theta) + \left(r_{t+1+i} + \gamma \cdot sg(V_{\theta}(s_{t+1+i})) - V_{\theta}(s_{t+i})\right)^2 L_{actor}(\theta) \leftarrow L_{actor}(\theta) - sg(A_{GAE(\gamma,\lambda)}(s_{t+i}, a_{t+i})) \log \pi_{\theta}(a_{t+i}|s_{t+i}) L_{exp}(\theta) \leftarrow L_{exp}(\theta) - H(\pi_{\theta}(\cdot|s_{t+i})) L_{total}(\theta) = c_1 L_{critic}(\theta) + c_2 L_{actor}(\theta) + c_3 L_{exp}(\theta) \theta \leftarrow \theta - \eta/n \nabla_{\theta} L_{total}(\theta)
```

Monte-Carlo PG Off-policy PG Off-policy AC

Monte-Carlo Policy Gradient

•
$$J(\theta) = \sum_{a} \pi_{\theta}(a|s) Q^{\pi\theta}(s,a)$$

$$\mathbb{X}$$
 Off-policy $\begin{cases} \pi_b : \text{collects data} \\ \pi_t : \text{learns target policy} \end{cases}$

Objective :

- $e = (s_0, a_0, r_1, s_1, s_{T-1}, a_{T-1}, r_T, s_T)$
- $p(e|s_0) = \pi_{\theta}(a_0|s_0)p(s_1|s_0, a_0) \ \pi_{\theta}(a_1|s_1)p(s_2|s_1, a_1) \ \dots \ \pi_{\theta}(a_{T-1}|s_{T-1})p(sT|sT_1 \ a_{T-1})$
- $R(e) = r1 + \gamma r2 + ... + \gamma^{n-1} r_T$

$$J(\theta|s_0) = \sum_{e} p_{\theta}(e|s_0) R(e)$$

Monte-Carlo Policy Gradient

```
• J(\theta|s_0) = \sum_{e} (p_{\theta}(s_1|s_0) \pi_{\theta}(a_0|s_0)

p_{\theta}(s_2|s_0) \underline{sg}(\pi_{\theta}(a_0|s_0))

\vdots stop gradient

p_{\theta}(s_T|s_0) \underline{sg}(\pi_{\theta}(a_0|s_0)) R(e)
```

• $\nabla_{\theta} J(\theta|s_0) = \sum_{e} \pi_{\theta}(a_0|s_0) p(e|s_0, a_0) R(e) \nabla_{\theta} log \pi_{\theta}(a_0|s_0)$ $\approx \hat{E} [R(e)\nabla_{\theta} log \pi_{\theta}(a_0|s_0)]$ • $\nabla_{\theta} J(\theta|s_t) \approx \hat{E} [R(e_t)\nabla_{\theta} log \pi_{\theta}(a_t|s_t)]$

Off-policy Policy Gradient

•
$$J(\theta|s_0) = \sum_{e} p_{\theta}(e|s_0) R(e)$$

= $\sum_{e} p_{b}(e|s_0) \frac{p_{\theta}(e|s_0)}{p_{b}(e|s_0)} R(e)$

 $\mbox{$\times$ Off-policy} \ \begin{cases} \pi_b : \mbox{behavior policy that collects data} \\ \pi_{\theta} : \mbox{learns target policy} \end{cases}$

Importance sampling ratio

$$\begin{split} \bullet \ \nabla_{\theta} J(\theta | s_0) &= \sum_{e} p_b(e | s_0) \frac{p_{\theta}(e | s_0)}{p_b(e | s_0)} R(e) \ \nabla_{\theta} log \pi_{\theta}(a_0 | s_0) \\ &\approx \widehat{E} \ \begin{bmatrix} p_{\theta}(e | s_0) \\ p_b(e | s_0) \end{bmatrix} R(e) \nabla_{\theta} log \pi_{\theta}(a_0 | s_0)] \\ &\xrightarrow{\pi_{\theta}(a_0 | s_0) p(s_1 | s_0, a_0) \dots \pi_{\theta}(a_T - 1 | s_T - 1) p(sT | sT_1, a_{T-1}) \\ \pi_{\theta}(a_0 | s_0) p(s_1 | s_0, a_0) \dots \pi_{\theta}(a_T - 1 | s_T - 1) p(sT | sT_1, a_{T-1}) \end{bmatrix} \\ &\xrightarrow{\pi_{\theta}(a_0 | s_0) \dots \pi_{\theta}(a_T - 1 | s_T - 1) \\ \pi_{\theta}(a_0 | s_0) \dots \pi_{\theta}(a_T - 1 | s_T - 1)} \longrightarrow \end{split} \end{split}$$
 This value could be a very big! Instable learning problem due to high variance.

Off-policy Actor-Critic

- Actor Objective(1-step TD):
- $J(\theta) = \sum_{a} \sum_{s'} p(s'|s,a) \pi_{\theta}(a|s) \left(r + \gamma V^{\pi\theta}(s')\right)$ $\approx \widehat{E}^{\pi\theta} \left[r + \gamma V^{\pi\theta}(s')\right]$ $\approx \widehat{E}^{\pi\theta'} \left[\frac{\pi_{\theta}(a|s)}{\pi_{\theta'}(a|s)} \left(r + \gamma V^{\pi\theta}(s')\right) \nabla_{\theta} \log \pi_{\theta}(a|s)\right]$

 \Re Off-policy $\pi_{\theta'}$: old policy that collected data π_{θ} : learns target policy

•
$$\nabla_{\theta}J(\theta|s_{0}) = \sum_{a}\sum_{s'}p(s'|s,a)\pi_{\theta}(a|s)\left(r + \gamma V^{\pi\theta}(s')\right)\nabla_{\theta}log\pi_{\theta}(a|s)$$

$$\approx \widehat{\mathbb{E}}^{\pi\theta}\left[(r + \gamma V^{\pi\theta}(s'))\nabla_{\theta}log\pi_{\theta}(a|s)\right]$$

$$= \sum_{a}\sum_{s'}p(s'|s,a)\pi_{\theta'}(a|s)\frac{\pi_{\theta}(a|s)}{\pi_{\theta},(a|s)}\left(r + \gamma V^{\pi\theta}(s')\right)\nabla_{\theta}log\pi_{\theta}(a|s)$$

$$\approx \widehat{\mathbb{E}}^{\pi\theta'}\begin{bmatrix}\frac{\pi_{\theta}(a|s)}{\pi_{\theta'}(a|s)}(r + \gamma V^{\pi\theta}(s'))\nabla_{\theta}log\pi_{\theta}(a|s)\end{bmatrix}$$
This value could be a very big!! Instable learning problem due to high variance.

Off-policy Actor-Critic

What about Critic Objective?

•
$$L(\theta) = \sum_{a} \sum_{s'} p(s'|s, a) \pi_{\theta}(a|s) \left((r + \gamma \cdot \operatorname{sg}(V^{\pi\theta}(s'))) - V^{\pi\theta}(s) \right)^{2}$$

$$\approx \widehat{E}^{\pi\theta} \left[\left((r + \gamma \cdot \operatorname{sg}(V^{\pi\theta}(s'))) - V^{\pi\theta}(s) \right)^{2} \right]$$

$$= \sum_{a} \sum_{s'} p(s'|s, a) \pi_{\theta'}(a|s) \frac{\pi_{\theta}(a|s)}{\pi_{\theta'}(a|s)} \left(r + \gamma \cdot \operatorname{sg}(V^{\pi\theta}(s')) - V^{\pi\theta}(s) \right)^{2}$$

$$\approx \widehat{E}^{\pi\theta'} \left[\frac{\pi_{\theta}(a|s)}{\pi_{\theta'}(a|s)} \left(r + \gamma \cdot \operatorname{sg}(V^{\pi\theta}(s')) - V^{\pi\theta}(s) \right)^{2} \right]$$

This value could be a very big!! instable learning problem due to high variance.

Proximal Policy Optimization(PPO)

Overview

- PPO problem statement:
 - Q-learning is tricky,
 - vanilla PG is low in sample efficiency and unstable in learning
 - TRPO is stable but rather complex and unable to share parameters btw. value and policy
- PPO is On-policy learning alg., but uses Off-policy data and update multiple times per sample (high sample efficiency)

Overview

- PPO updates the policy conservatively
 - It stops the policy change too fast or dramatically
- The surrogate objective prevent the new policy from changing too far from the old policy
 - Importance Sampling ratio could be a very big!! (instable learning problem due to high variance)
 - Updating multiple times per sample worsen learning instabilities
 - An actor learning w/o well learnt critic adds instability (sub-optima convergence)

Method

- $L^{pg}(\theta) = \hat{E}_t [log\pi_{\theta}(a_t|st)\hat{A}_t]$
 - Multiple time updates should look good for learning
 - But, in fact, empirically, multiple updates cause dramatic change in policy that lead to instability in learning
- $\nabla_{\theta} L^{pg}(\theta) = \hat{E}_t [\nabla_{\theta} log \pi_{\theta}(a_t | st) \hat{A}_t]$
 - π_{θ} : stochastic policy
 - \hat{A}_t : advantage estimator at time step t

Method

• KL-divergence (Discrete distribution):

$$KL[p,q] = \sum_{x} p(x) \log \frac{p(x)}{q(x)} \ge 0$$

- measure of how much two distributions are different
- 0 if p = q. The greater KL-divergence is, the bigger the difference is
 - Want to increase value accuracy as much as possible while updating the policy very conservatively

Method

• TRPO Objective that limit the amount of change in Policy:

$$\begin{aligned} & \underset{\theta}{\text{maximize}} \, \hat{E}_t \big[\, \frac{\pi_{\theta}(at|st)}{\pi_{\theta old}(a_t|s_t)} \, \hat{A}_t \big] \\ & \qquad \qquad & \times \nabla_{\theta} \pi_{\theta}(a_0|s_0) \\ & \qquad & = \pi_{\theta}(a_0|s_0) \text{log} \nabla_{\theta} \pi_{\theta}(a_0|s_0) \\ & \longrightarrow & \nabla_{\theta} \, J(\theta) = \hat{E} \, \left[\frac{\nabla_{\theta} \pi(\text{at}|s_t)}{\pi_{\theta old}(\text{at}|s_t)} \, \hat{A}_t \big] \\ & \longrightarrow & \nabla_{\theta} \, J(\theta) = \hat{E}^{\pi \theta \text{old}} \big[\frac{\pi(\text{at}|s_t)}{\pi_{\theta old}(\text{at}|s_t)} \, \hat{A}_t \nabla_{\theta} log \pi_{\theta}(a_0|s_0) \big] \leftarrow \underset{\text{p.g.}}{\text{Equal to}} \end{aligned}$$

subject to
$$\hat{E}_t[KL[\pi_{\theta old}(\cdot | s_t), \pi_{\theta}(\cdot | s_t)]] \leq \delta$$

 \longrightarrow Allow the new policy to change by δ from the old policy

Objective

TRPO:

Stop a new policy become too different from the behavior policy $\pi_{\theta old}$

Setting β is difficult

• PPO:

$$L^{clip}(\theta) = \hat{E}_t \left[\min(rt(\theta) \hat{A}_{t_t} clip(r_t(\theta), 1 - \varepsilon, 1 + \epsilon) \hat{A}_t) \right]$$

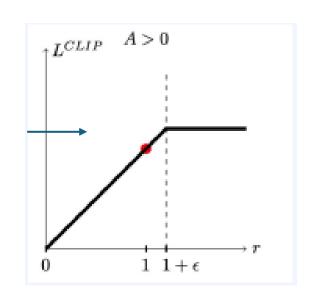
with
$$r_{t(\theta)} = \frac{\pi_{\theta(a_t|S_t)}}{\pi_{\theta old}(a_t|s_t)}$$
 , $1 > \varepsilon > 0$

if $rt(\theta) \le 1 - \varepsilon$, or $rt(\theta) \ge 1 + \varepsilon$ No gradient(no learning),

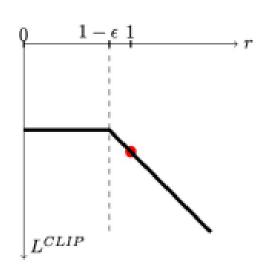
Objective

$$\begin{split} L^{clip}(\theta) = & \hat{E}_t \left[\min(rt(\theta) \, \hat{A}_{t,clip}(r_t(\theta), 1 - \varepsilon, 1 + \epsilon) \hat{A}_t \right] \\ with \, r_{t(\theta)} = & \frac{\pi_{\theta}(a_t | S_t)}{\pi_{\theta old}(a_t | S_t)} \text{ , } 1 > \varepsilon > 0 \end{split}$$

Loss does not grow = No gradient



Limit an action prob. to grow only $(1 \pm \varepsilon)$ times greater or smaller than previous policy (control policy to change only $\pm \varepsilon$ ratio)



A < 0

Objective

Maximize constraint off-policy gradient

$$L_t^{CLIP+VF+S}(heta) = \hat{\mathbb{E}}_tig[L_t^{CLIP}(heta) - c_1L_t^{VF}(heta) + c_2S[\pi_ heta](s_t)ig]$$
 Minimize loss bonus $L_t^{VF}(heta) = (V_ heta(s_t) - V_t^{targ})^2$ $S: ext{Entropy} \quad \hat{A}_t = A_t^{GAE(\gamma,\lambda)}$

Algorithm 1 PPO, Actor-Critic Style

```
Parallel learning  \begin{array}{ll} \textbf{for} \ \operatorname{iteration} = 1, 2, \dots, M \ \textbf{do} \\ & \text{Run policy } \pi_{\theta_{\operatorname{old}}} \ \text{in environment for } T \ \operatorname{timesteps} \\ & \operatorname{Compute advantage estimates } \hat{A}_1, \dots, \hat{A}_T \\ & \textbf{end for} \\ & \operatorname{Optimize surrogate } L \ \operatorname{wrt} \ \theta, \ \operatorname{with } K \ \operatorname{epochs and minibatch size } M \leq NT \\ & \theta_{\operatorname{old}} \leftarrow \theta \\ & \textbf{end for} \\ \end{array}
```

Policy Loss

To get GAE, $\delta_t = R_{t+1} \gamma V(s_{t+1}) - V(st)$

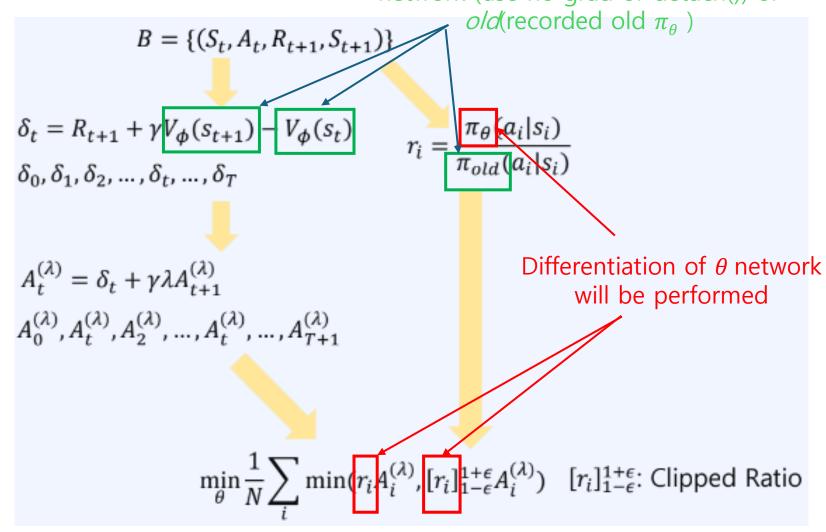
$$A_{t}^{(\lambda)}$$

$$= \sum_{k=0} (\gamma \lambda)^{k} \delta_{t+k}$$

$$= \delta_{t} + \gamma \lambda \sum_{k=0} (\gamma \lambda)^{k} \delta_{t+1+k}$$

$$= \delta_{t} + \gamma \lambda A_{t+1}^{(\lambda)}$$

There's no differentiation of φ network (use no grad or detach()) or



Value Loss

$$B = \{(S_t, A_t, R_{t+1}, S_{t+1})\}$$

$$G_t = \sum_i \gamma^k R_{t+k}$$

$$\min_{\phi} \frac{1}{N} \sum_i \frac{1}{2} \left(G_i - V_{\phi}(s_i)\right)^2$$

Differentiation of φ network will be performed

- Return Definition:
 - $G_t = \sum_{k=0} \gamma^k R_{t+1+k}$
 - recursive: $G_t = Rt_{+1} \gamma G_{t+1}$
- Return Calculation (Backward):
 - $G_{t+1} = 0$
 - From t = T to t= 0, compute $G_t = Rt_{+1} \gamma G_{t+1}$

Pseudo Code:PPO

Algorithm 1 PPO-Clip

- 1: Input: initial policy parameters θ_0 , initial value function parameters ϕ_0
- 2: **for** k = 0, 1, 2, ... **do**
- 3: Collect set of trajectories $\mathcal{D}_k = \{\tau_i\}$ by running policy $\pi_k = \pi(\theta_k)$ in the environment.
- 4: Compute rewards-to-go \hat{R}_t .
- 5: Compute advantage estimates, \hat{A}_t (using any method of advantage estimation) based on the current value function V_{ϕ_k} .
- 6: Update the policy by maximizing the PPO-Clip objective:

$$\theta_{k+1} = \arg\max_{\theta} \frac{1}{|\mathcal{D}_k|T} \sum_{\tau \in \mathcal{D}_k} \sum_{t=0}^{T} \min\left(\frac{\pi_{\theta}(a_t|s_t)}{\pi_{\theta_k}(a_t|s_t)} \underline{A^{\pi_{\theta_k}}(s_t, a_t)}, \ g(\epsilon, \underline{A^{\pi_{\theta_k}}(s_t, a_t)})\right),$$

typically via stochastic gradient ascent with Adam.

7: Fit value function by regression on mean-squared error:

$$\phi_{k+1} = \arg\min_{\phi} \frac{1}{|\mathcal{D}_k|T} \sum_{\tau \in \mathcal{D}_k} \sum_{t=0}^T \left(V_{\phi}(s_t) - \underline{\hat{R}_t} \right)^2,$$

typically via some gradient descent algorithm.

8: end for

2 NN, θ, φ

The same policy but old

Note fitting V requires no target policy (On-policy learning)

Performance comparison

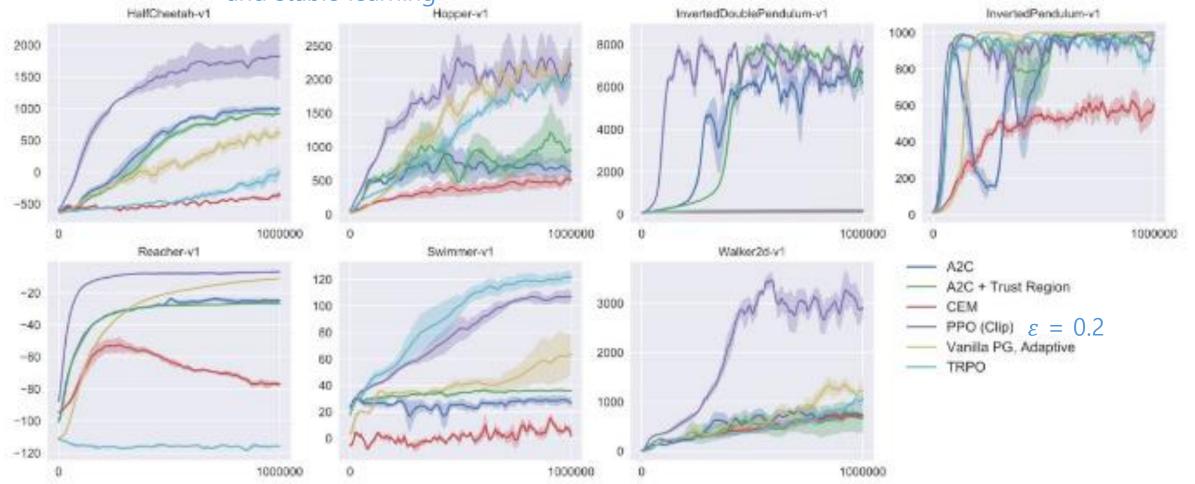
```
No clipping or penalty: L_t(\theta) = r_t(\theta) \hat{A}_t Clipping: L_t(\theta) = \min(r_t(\theta) \hat{A}_t, \text{clip}(r_t(\theta)), 1 - \epsilon, 1 + \epsilon) \hat{A}_t KL penalty (fixed or adaptive) L_t(\theta) = r_t(\theta) \hat{A}_t - \beta \text{ KL}[\pi_{\theta_{\text{old}}}, \pi_{\theta}]
```

- Test for 7 robotic task in Mujoco (continuous domain!)
- 1M step updates
- Test with multiple β , d_{targ} , various ε
- Policy: 64 hidden unit, 2 layer MLP, tanh activation, with output of Gaussian (mean, std)

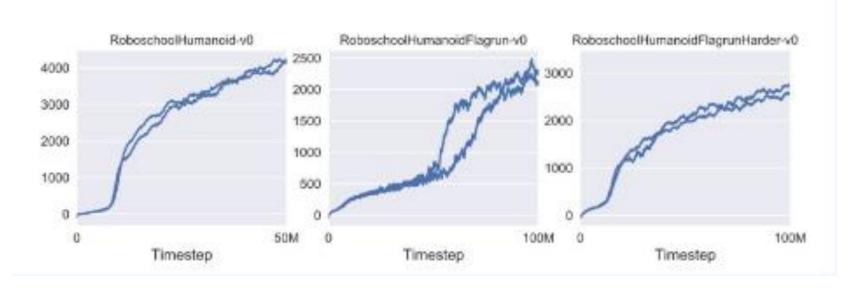
- No parameter sharing, no entropy bonus
- 3 random seed
- avg. score for the last 100 before the end
- Normalization 0~1
- No clipping & KL penalty is -0.39
- Clipping score is 0.82

algorithm	avg.	${\bf normalized\ score}$
No clipping or penalty		-0.39
Clipping, $\epsilon = 0.1$		0.76
Clipping, $\epsilon = 0.2$		0.82
Clipping, $\epsilon = 0.3$		0.70
Adaptive KL $d_{\text{targ}} = 0.003$		0.68
Adaptive KL $d_{\text{targ}} = 0.01$		0.74
Adaptive KL $d_{\text{targ}} = 0.03$		0.71
Fixed KL, $\beta = 0.3$		0.62
Fixed KL, $\beta = 1$.		0.71
Fixed KL, $\beta = 3$.		0.72
Fixed KL, $\beta = 10$.		0.69

PPO shows sample efficiency and stable learning



- High-dimensional continuous control test of PPO: 3D humanoid
 - 1. RoboschoolHumannoid: moving forward
 - 2. RoboschoolHumanoidFlagrun: moving forward with moving target every 200 timestep
 - 3. RoboschoolHumanoidFlagranHarder: throw a cube to the robot tumble and stand-up again



• Learning in Atari domain:

Hyperparameter	Value		
Horizon (T)	128		
Adam stepsize	$2.5 \times 10^{-4} \times \alpha$		
Num. epochs	3		
Minibatch size	32×8		
Discount (γ)	0.99		
GAE parameter (λ)	0.95		
Number of actors	8		
Clipping parameter ϵ	0.1 imes lpha		
VF coeff. c_1 (9)	1		
Entropy coeff. c_2 (9)	0.01		

The number of games out of 48

	A2C	ACER	PPO	Tie
(1) avg. episode reward over all of training	1	18	30	0
(2) avg. episode reward over last 100 episodes	1	28	19	1

Code Ex.1

- configuration.py
- utils.py
- agent.py
- train.py
- eval.py

Code Ex.1

• 'Cartpole' Env.: move a cart (black) such that it balances a pendulum (brown) without moving too far from the center.

• State:

- The agent observes current position and velocity of the cart, as well as angle and velocity of the pole
- cart position, cart velocity, pole angle, pole angular velocity

Action:

- 0: push the cart left
- 1: push the cart right
- Reward:+1 for every step

configuration.py

```
from utils import AttrDict
config = AttrDict(
   gamma=0.99,
   lam=0.95,
   eps clip=100,
   k epoch=4,
   1r=1e-4,
                             Critic loss constant
   c1=1,
                             actor loss constant
   c2=0.5,
                             Exploration loss constant (entropy loss constant)
   c3=1e-3,
                             Parallel environment to collect trajectories
   num env=8,
                             Length of a trajectory
    seq length=16,
                             Learning from a batch that contains 64 trajectories
   batch size=64,
   minibatch size=16,
   hidden size=128,
   train env steps=1000000,
   num_eval_episode=100,
```

train.py

```
import torch
import datetime
import numpy as np
from utils import create env
from agent import Agent
from configuration import config
from collections import deque
from torch.utils.tensorboard import SummaryWriter
if name == ' main ':
   env list = [create env(config) for in range(config.num env)]
    agent = Agent(env list[0], config)
   agent.set optimizer()
    assert config.batch size % config.num env == 0
   dt now = datetime.datetime.now()
   logdir = f"logdir/{dt_now.strftime('%y-%m-%d_%H-%M-%S')}"
   writer = SummaryWriter(logdir)
    score que = deque([], maxlen=config.num eval episode)
   count_step_que = deque([], maxlen=config.num eval episode)
    score = 0
   count step = 0
    s_list = [env.reset() for env in env_list]
   score_list = [0 for env in env_list]
   count_step_list = [0 for env in env_list]
```

Vector environments
One agent

train.py

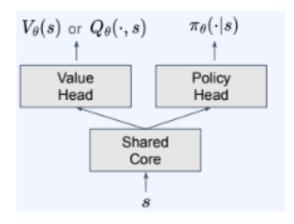
from pi

```
num iteration = int(config.train env steps / config.num env / config.seq length)
          for step iteration in range(num iteration):
                                                              Parallelized environments shares config.train env steps load
               for i env in range(config.num env):
                                                              One agent plays in multiple environments
                   env = env list[i env]
                   s = s list[i env]
                   for in range(config.seq_length):
                                                              Trajectory rollout until seg length
                      pi, a = agent.action(s)
pi is behavior policy
                      s next, r, done, info = env.step(a)
a is an action sampled
                      agent.add to batch(s, pi, a, r, s next, done)
                                                                           Put the behavior policy
                                                                            into a trajectory in batch
                       s = s next
                       score list[i env] += r
                       count step list[i env] += 1
                       s list[i env] = s
                       if done:
                           s = env.reset()
                           s list[i env] = s
                           score que.append(score list[i env])
                           count step que.append(count step list[i env])
                           score list[i env] = 0
                           count_step list[i env] = 0
                           break
```

agent.py

return return seq

```
class Agent (nn.Module):
   def init (self, env, config):
        super(). init ()
        self.config = config
       d state = env.observation space.shape[0]
       n action = env.action space.n
        self.encoder = nn.Sequential(
            nn.Linear(d state, self.config.hidden size),
           nn.ELU(),
           nn.Linear(self.config.hidden size, self.config.hidden size),
           nn.ELU()
        self.value head = nn.Sequential(
            nn.Linear(self.config.hidden size, self.config.hidden size),
           nn.ELU(),
            nn.Linear(self.config.hidden size, 1)
        self.policy head = nn.Sequential(
            nn.Linear(self.config.hidden size, self.config.hidden size),
           nn.ELU(),
            nn.Linear(self.config.hidden size, n action),
           nn.Softmax(dim=-1)
        self.batch = deque([], maxlen=config.batch size) # list of episodes
```



batch size is 64 trajectories Each trajectory has seq. length 16

agent.py

```
def crate trajectory(self):
                                           A trajectory dictionary
    trajectory = {
        'state': list(),
        'pi old': list(),
                                           We'll record the behavior policy every time step the agent act.
        'action': list(),
        'reward': list(),
        'state next': list(),
        'done': list(),
    return trajectory
                                                                  Add a sample to the batch
def add to batch(self, s, pi old, a, r, s next, done):
   if (
            len(self.batch) == 0
                                                                          When a seq. is full
            or len(self.batch[-1]['state']) == self.config.seq length
                                                                          Create a new seq.
        ):
        trajectory = self.crate trajectory()
                                                                          Add the seq. to the batch
        self.batch.append(trajectory)
    if not done:
        length to append = 1
    else:
        # When the trajectory is done before it is full, append the last data until the end
        length to append = self.config.seq length - len(self.batch[-1]['state'])
    for in range(length to append):
        self.batch[-1]['state'].append(s)
        self.batch[-1]['pi old'].append(pi old)
        self.batch[-1]['action'].append(a)
        self.batch[-1]['reward'].append(r)
        self.batch[-1]['state next'].append(s next)
        self.batch[-1]['done'].append(done)
```

```
def set optimizer(self):
    self.optim = torch.optim.Adam(
        self.parameters(),
        lr=self.config.lr
def forward(self, x):
    h enc = self.encoder(x)
   value = self.value head(h enc)
   pi = self.policy_head(h_enc)
    return pi, value
def action(self, x):
    # used when sampling an action for a state
   with torch.no grad():
        x = torch.from numpy(x).float().reshape(1, -1)
       pi, value = self.forward(x)
       a = torch.distributions.Categorical(pi).sample().item()
        pi = pi.numpy().squeeze(0) # (n action)
    return pi, a
```

Action sample using pi distribution

```
def train(self):
   for k in range(self.confiq.k epoch):
                                                                          Train repeating k epoch with minibatch size
       minibatch = random.sample(self.batch, self.config.minibatch size)
        state seg array = np.array([trajectory['state'] for trajectory in minibatch]) # (n batch, n seg, *dim state)
       pi old seq array = np.array([trajectory['pi old'] for trajectory in minibatch]) # (n batch, n seq, n action)
        action seg array = np.array([trajectory['action'] for trajectory in minibatch], dtype=np.int64) # (n batch, n seg)
        reward_seq_array = np.array([trajectory['reward'] for trajectory in minibatch]) # (n batch, n seq)
        state next seg array = np.array([trajectory['state next'] for trajectory in minibatch]) # (n batch, n seg, *dim state)
        done seg array = np.array([trajectory['done'] for trajectory in minibatch]) # (n batch, n seg)
        state seg tensor = torch.from numpy(
            state seg array
                                                                    To insert into NN
        ).float().transpose(0, 1) # (n_seq, n batch, *dim states)
       pi old seg tensor = torch.from numpy(pi old seg array).transpose(0, 1) # (n seg, n batch, n action)
        action seg tensor = torch.from numpy(action seg array).transpose(0, 1) # (n seg, n batch)
        reward seq tensor = torch.from numpy(reward seq array).float().transpose(0, 1) # (n seq, n batch)
        state next seg tensor = torch.from numpy(
           state next seg array
        ).float().transpose(0, 1) # (n seq, n batch, *dim states)
        done seq tensor = torch.from numpy(done seq array).float().transpose(0,1) # (n seq, n batch)
        # mask for updating policy, until the transition that its done is True
                                                                                   Mask for updating policy
        update mask = done seq tensor.roll(1, dims=0) # (n seq, n batch)
       update mask[0, :] = 0  # (n seq, n batch)
        update mask = 1 - update mask # (n seq, n batch)
```

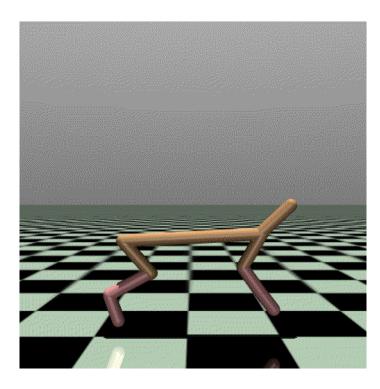
```
[P(a1),p(a2)], V(s_t)
pi, value = self.forward(state_seq_tensor) # (n_seq, n_batch, n_action), (n_seq, n_batch, 1)
_, value_next = self.forward(state_next_seq_tensor) # (n_seq, n_batch, 1)
                                                                                                                  V(S_{+\perp 1})
value = value.squeese(-1) # (n seq, n batch)
value next = value next.squeeze(-1) # (n seq, n batch)
delta = reward seq tensor + self.config.qamma * (1 - done seq tensor) * value next - value
                                                                                                                 \hat{A}_t is GAE that uses
gae = calc_return_seq_tensor(self.config.lam * self.config.gamma, update mask * delta.detach())
                                                                                                                 N-step TD target
pi_chosen = pi.gather(dim=-1, index=action_seq_tensor.unsqueege(-1)) # (n_seq, n_batch, 1)
pi chosen = pi chosen.squeese(-1) # (n seq, n batch)
pi_old_chosen = pi_old_seq_tensor.gather(dim=-1, index=action_seq_tensor.unsqueeze(-1)) # (n_seq, n batch, 1)
pi old chosen = pi old chosen.squeeze(-1) # (n seq, n batch)
value target = (
                                                                                    Value target
    reward_seg_tensor
    + self.config.gamma * (1 - done seg tensor) * value next.detach()
) # (n seq, n batch)
                                                                                    Critic loss(L^{VF})
loss critic = torch.mean(update mask * (value target - value) ** 2)
                                                                                    r_{t(\theta)} = \frac{\pi_{\theta(a_t|S_t)}}{\pi_{\theta_0|d}(a_t|S_t)}
r = pi_chosen / pi_old_chosen
loss actor = -torch.mean(
    update mask * torch.min(
         gae * torch.clip(r, 1 - self.config.eps_clip, 1 + self.config.eps_clip)
                                                                            Actor loss Lcl^{ip}(\theta) = \hat{E}_t \left[ \min(rt(\theta) \hat{A}_t \ clip(r_t(\theta), 1 - \varepsilon, 1 + \epsilon) \hat{A}_t) \right]
```

agent.py

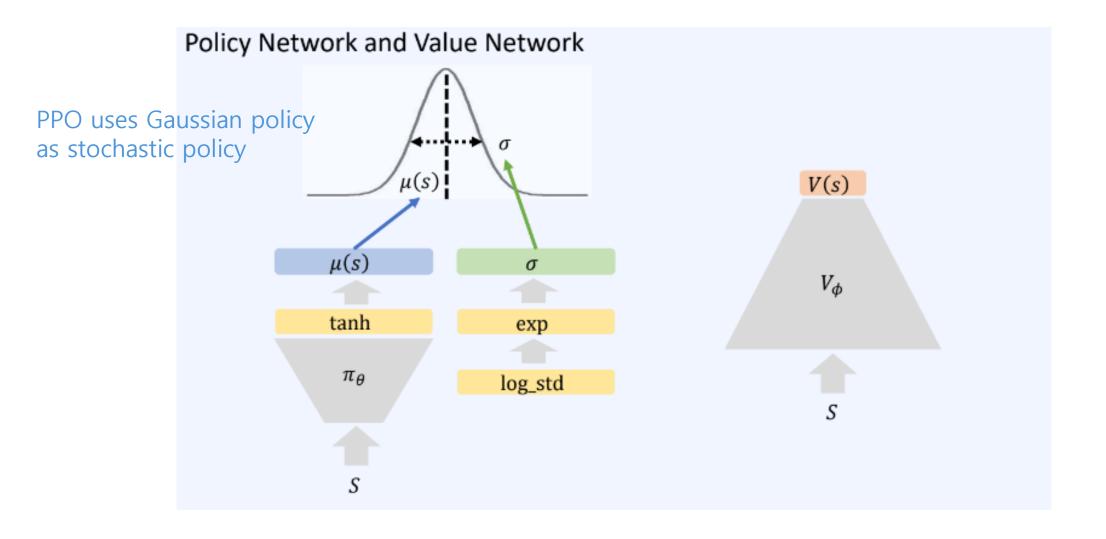
```
loss exp = -torch.mean(
Entropy bonus
                         update mask
                         * torch.sum(-pi * torch.log(pi + 1e-15), dim=-1) # (n seg, n batch, n action) -> (n seg, n batch)
Add all loss
                     loss = self.config.c1 * loss critic + self.config.c2 * loss actor + self.config.c3 * loss exp
and make actor
critic loss
                     loss critic avg = loss critic * self.config.seg length * self.config.minibatch size / update mask.sum()
                     entropy avg = -loss exp * self.config.seg length * self.config.minibatch size / update mask.sum()
                     self.optim.zero grad()
                     loss.backward()
Gradient descent
                     self.optim.step()
  Throw away
                 self.batch.clear()
   the batch
                 return loss critic aug.detach().item(), entropy aug.detach().item()
```

Code Ex.2

- Upload 'proximal_policy_optimizatin.ipynb' file onto Colab
- The notebook includes 'Mujoco' environment, 'Half Cheetah'
- State(17):
 - (body parts) position,
 - (roter, axis) angle or velocity
- Action(6):
 - Torque on 6 roters (-1~1)
- Reward:
 - Forward_reward: moving-forward reward
 - ctrl_cost: penalty in taking too large action



Continuous Action



Collecting episodes

- Initial sampling
 - $S_0 \sim d(\cdot)$
- Action sampling from Policy
 - $\mu_t = \pi_{\theta}(s)$
 - $\varepsilon \sim N(o, I)$: Noisiness for exploration
 - $a_t = \mu + \sigma \varepsilon_t$:Reparameterization trick
- Simulation learnt std.
 - $s_{t+1} r_{t+1} d_{t+1} = \text{env.step}(a_t)$
 - Next_staté
 - Reward
 - Done, terminal information

