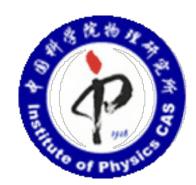
# Topological Quantum Chemistry and its applications in materials search

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http://edu.iphy.ac.cn/moreintro.php?id=1250



### Check any material by yourself

The open-source code *VASP2Trace* and end-user button *CheckTopologicalMat* are available online at <a href="http://www.cryst.ehu.es/cryst/checktopologicalmat">http://www.cryst.ehu.es/cryst/checktopologicalmat</a>.

- 1. Obtain the eigenstates at several k-points. (VASP)
- 2. Compute the irreps from the eigenstates. ("irvsp", "vasp2trace")
- a. Download and "vasp2trace": www.cryst.ehu.es/cryst/checktopologicalmat, which includes a folder of "max\_KPOINTS\_VASP/" and a source code of "src\_trace\_v1.tar.gz"
  - b. For more versions of "vasp2trace", please refer to <a href="https://github.com/zjwang11/irvsp">https://github.com/zjwang11/irvsp</a>.
- 3. Solve the compatibility relations: semimetal or Insulator. ("checktopologicalmat").

Insulator: check If it's can be decomposed into a sum of EBRs.

(Yes: Trivial No: Topological)

Topological: Compute the symmetry indicators

Ref: Vergniory, M.G., et al., "A complete catalogue of high-quality topological materials", Nature, 566, 480-485 (2019)

### www.cryst.ehu.es/cryst/checktopologicalmat

#### **Check Topological Mat**

#### **Check Topological Mat.**

Given a file that contain the eigenvalues at each maximal k-vec of a space group, the program gives the set of irreducible representations at each maximal k-vec (time-reversal is assumed). Then, using the compatibility relations and the set of Elementary Band Representations (EBRs), it checks whether the set of bands can be put as linear combinations of EBRs. This (self-explanatory) file shows the format of the file to be uploaded in the menu on the right:

#### File\_Description

You can download examples of input files here:

Example\_Ag1Ge1Li2 Example\_Ag1O2Sc1
Example\_B2Ca3Ni7 Example\_of\_Bad\_File
Example\_Ba3Ca1O9Pu2

You can generate the "trace.txt" file in your own computer using VASP and this program (fortran).

#### vasp2trace

Read the "README.pdf" file for help on the use of vasp2trace. If you are using "Check Topological Mat." and/or "vasp2trace" programs in the preparation of an article, please cite this reference:

M.G. Vergniory, L. Elcoro, C. Felser, N. Regnault, B.A. Bernevig, Z. Wang Nature(2019) **566**, 480-485. doi:10.1038/s41586-019-0954-4

Upload your traces.txt file (see the help in the column on the left).

Show

选取文件 未选择文件

### Ex: Bi2Se3

- ➤ 1. The SG number(166) and crystal structure.

  (run "Phonopy" to make sure the POSCAR is given in a standard setting.)
- 2. Get the high-symmetry k points for that SG (166).
   (Vasp2trace/max\_KPOINTS\_VASPKPOINTS\_166.txt).
- > 3. Run "VASP", to obtain the eigen-states(WAVECAR) at those kpoints. (check the symmetry operators in OUTCAR, simply by counting the total number of the operators)
- ➤ 4. Run "vasp2trace" that you have just installed locally in the folder. (trace.txt would be generated automatically)
- 5. Upload "trace.txt" and press the button.

### Step 1:

- \$ phonopy --tolerance 0.01 --symmetry -c POSCAR
- \$ vim PPOSCAR
- \$ cp PPOSCAR POSCAR

```
/anaconda3/bin/phonopy --tolerance 0.01 --symmetry -c POSCAR
phonopy version: 1.13.2
space group type: 'R-3m'
space grup number: 166
point group type: '-3m'
space group operations:
- rotation: # 1
 - [ 1, 0 , 0]
 - [ 0, 1, 0]
 - [ 0, 0 , 1]
 translation: [ 0.00000, 0.00000, 0.00000 ]
- rotation: # 2
 -[-1, 0, 0]
 -[0,-1,0]
 -[0, 0, -1]
 translation: [ 0.00000, 0.00000, 0.00000 ]
```

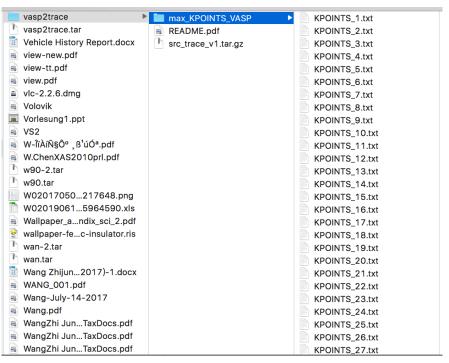
#### "POSCAR"

```
generated by phonopy
     1.0
       2.0690000000000000
                         1.1945377069533354
                                             9.5466666571200012
                         1.1945377069533354
      -2.0690000000000000
                                             9.5466666571200012
      0.00000000000000000
                         -2.3890754139066708
                                             9.5466666571200012
6 Bi Se
         3
8 Direct
    0.6009999996010008 0.6009999996010008
                                       0.6009999996010009
    0.3990000003989990 0.3990000003989991
                                       0.3990000003989989
11
    0.793999997940036 0.793999997940036 0.793999997940036
    0.2060000002059964 0.2060000002059964 0.2060000002059964
```

<sup>&</sup>quot;PPOSCAR" 13L, 560C

### Step 2:

\$ cp xx/vasp2trace/max\_KPOINTS\_VASP/KPOINTS\_166.txt KPOINTS.high



### Step 3:

#### Follow REDME in the folder VASP2trace

- a. Run the scf calcualtion in vasp
- b. Run the band calculation in vasp with KPOINTS.high
- \$ vim OUTCAR; :/ irot

```
399 Automatic generation of k-mesh.
    Space group operators:
401
     irot
                                               n x
                                                             n y
                                                                           n z
                 det(A)
                               alpha
                                                                                                    tau y
                                                                                                                  tau z
                                                                                       tau x
402
              1.000000
                            0.000000
                                          1.000000
                                                        0.00000
                                                                      0.000000
                                                                                   0.00000
                                                                                                 0.00000
                                                                                                               0.00000
             -1.000000
403
                            0.000000
                                          1.000000
                                                        0.000000
                                                                      0.000000
                                                                                   0.000000
                                                                                                 0.000000
                                                                                                               0.000000
404
              1.000000
                          180.000000
                                          0.866025
                                                        0.500000
                                                                      0.000000
                                                                                   0.000000
                                                                                                 0.000000
                                                                                                               0.00000
             -1.000000
                          180.000000
                                                        0.500000
                                                                      0.00000
                                                                                   0.00000
                                                                                                 0.00000
                                                                                                               0.00000
405
                                          0.866025
406
              1.000000
                          120.000000
                                          0.000000
                                                        0.000000
                                                                    -1.000000
                                                                                   0.00000
                                                                                                 0.00000
                                                                                                               0.00000
407
             -1.000000
                          120,000000
                                          0.000000
                                                        0.000000
                                                                    -1.000000
                                                                                   0.000000
                                                                                                 0.000000
                                                                                                               0.000000
408
              1.000000
                          179.999999
                                          0.000000
                                                        1.000000
                                                                      0.000000
                                                                                   0.000000
                                                                                                 0.000000
                                                                                                               0.000000
409
             -1.000000
                          179.999999
                                          0.000000
                                                        1.000000
                                                                      0.000000
                                                                                   0.000000
                                                                                                 0.000000
                                                                                                               0.000000
410
              1.000000
                          120.000000
                                          0.00000
                                                        0.000000
                                                                      1.000000
                                                                                   0.00000
                                                                                                 0.00000
                                                                                                               0.00000
411
             -1.000000
                          120,000000
                                          0.000000
                                                        0.000000
                                                                      1,000000
                                                                                   0.000000
                                                                                                 0.000000
                                                                                                               0.000000
       10
412
       11
              1.000000
                          180.000000
                                          0.866025
                                                       -0.500000
                                                                      0.000000
                                                                                   0.000000
                                                                                                 0.000000
                                                                                                               0.000000
413
       12
             -1.000000
                          180.000000
                                          0.866025
                                                       -0.500000
                                                                      0.000000
                                                                                   0.000000
                                                                                                 0.000000
                                                                                                               0.00000
414
```

415 Subroutine IBZKPT returns following result:

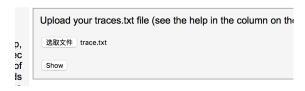
### Step 4:

\$ vasp2trace / vasp2trace \$nele

```
28
 1
 2
    12
 3
                           0
                                    0.000000
                                                 0.000000
                                                              0.000000
                                                                           1.000000
                                                                                        0.00000
                                                                                                     0.000000
                                                                                                                  0.0000
                        0
                              1
 5
                     0
                         0
                           0
                                    0.000000
                                                 0.000000
                                                              0.000000
                                                                           1.000000
                                                                                        0.000000
                                                                                                     0.000000
                                                                                                                  0.0000
 6
                                    0.000000
                                                 0.000000
                                                              0.000000
                                                                           0.000000
                                                                                        0.000000
                                                                                                     0.500000
                                                                                                                  0.8660
               0
                        0
 7
               0
                           1
                                    0.000000
                                                 0.000000
                                                              0.000000
                                                                           0.000000
                                                                                        0.000000
                                                                                                     0.500000
                                                                                                                  0.8660
 8
                                    0.000000
                                                 0.000000
                                                              0.000000
                                                                           0.500000
                                                                                       -0.866025
                                                                                                     0.000000
                                                                                                                  0.0000
                        0
                           1
 9
                          -1
                                    0.000000
                                                 0.000000
                                                              0.000000
                                                                           0.500000
                                                                                       -0.866025
                                                                                                     0.000000
                                                                                                                  0.0000
                        0
10
                     0
                           0
                                    0.000000
                                                 0.000000
                                                              0.000000
                                                                           0.000000
                                                                                        0.000000
                                                                                                     1.000000
                                                                                                                  0.0000
                        0
11
                                    0.000000
                                                 0.000000
                                                              0.000000
                                                                           0.000000
                                                                                        0.000000
                                                                                                     1.000000
                                                                                                                  0.0000
           0
                  0
                     0
                        0
                           0
12
               0
                     1
                            0
                                    0.000000
                                                 0.000000
                                                              0.000000
                                                                           0.500000
                                                                                        0.866025
                                                                                                     0.000000
                                                                                                                  0.0000
           0
                  0
13
                                    0.000000
                                                                                                     0.000000
                                                                                                                  0.0000
                                                 0.000000
                                                              0.000000
                                                                           0.500000
                                                                                        0.866025
                                    0.000000
                                                 0.000000
                                                              0.000000
                                                                           0.000000
                                                                                        0.000000
                                                                                                    -0.500000
                                                                                                                  0.8660
14
               0
                     0
                       -1
                           0
15
     0
        0
               0
                 1
                     0
                           0
                                    0.000000
                                                 0.000000
                                                              0.000000
                                                                           0.000000
                                                                                        0.000000
                                                                                                    -0.500000
                                                                                                                  0.8660
16
     4
17
       0.000000
                    0.00000
                                 0.000000
18
       0.500000
                    0.500000
                                 0.500000
19
       0.500000
                    0.500000
                                 0.000000
20
       0.000000
                    0.500000
                                 0.000000
21
    12
22
             2
                  3
                             5
                                                  9
                                                       10
                                                                 12
                        4
                                  6
                                                           11
23
        2
            -9.773922
                           2.000000
                                       0.000000
                                                    2.000000
                                                                 0.000000
                                                                              0.000000
                                                                                           0.000000
                                                                                                        0.000000
                                                                                                                     0.0
24
    3
             -8.564873
                                                                                                        0.000000
                           2.000000
                                       0.000000
                                                    -2.000000
                                                                 0.00000
                                                                              0.000000
                                                                                           0.000000
                                                                                                                     0.0
```

### Step 5:

#### pological Mat



#### Result of the analysis of the uploaded structure

- The material is a topological insulator.
- List of topological indices:

```
z2w,1=0
```

z2w,2=0

z2w.3=0

z4=3

- The material belongs to the strong topological class: 6
- Clicking on See the irreps you can see the details about the number of bands and the identified irreps at each maximal k-vector.
- The set of bands can be put as linear combination of Elementary Band Representations (EBR) and parts of decomposable EBRs with integer positive coefficients. Click on Linear Combinations to get some possible linear combinations of EBRs and partial EBRs.
- Click on Subgroups to check the topological character of the structure in each of its (translationengleiche) subgroups.

### Take-home message

Obtain the eigenstates at maximal high-symmetry k-points in VASP.
 Download the klist for all space groups:
 <u>https://github.com/zjwang11/irvsp/tree/master/max\_KPOINTS\_VASP.</u>

2. Compute the irreps from the eigenstates. ("vasp2trace" or "irvsp") Download and install "vasp2trace":

<a href="https://github.com/zjwang11/irvsp/blob/master/src\_trace\_v1.tar.gz">https://github.com/zjwang11/irvsp/blob/master/src\_trace\_v1.tar.gz</a>.

ref.: <a href="https://arxiv.org/abs/2002.04032">https://arxiv.org/abs/2002.04032</a>

 Solve the compatibility relations: semimetal or Insulator. ("checktopologicalmat"): <a href="http://www.cryst.ehu.es/cryst/checktopologicalmat">http://www.cryst.ehu.es/cryst/checktopologicalmat</a>.

 Insulator: check If it's can be decomposed into a sum of EBRs.

 (Yes: Trivial
 No: Topological)

 Topological: compute the symmetry indicators

ref: Vergniory, M.G., et al., Nature, 566, 480-485 (2019)

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## Thanks for your attention!