Topological Quantum Chemistry and its applications

Zhijun Wang(王志俊)

中科院.物理所

Check any material by yourself

The open-source code VASP2Trace and end-user button CheckTopologicalMat are available online at http://www.cryst.ehu.es/cryst/checktopologicalmat.

- 1. Obtain the eigenstates at several k-points. (VASP)
- 2. Compute the irreps from the eigenstates. ("irvsp", "vasp2trace")
 - a. Download "vasp2trace": www.cryst.ehu.es/cryst/checktopologicalmat, which includes a folder of "max_KPOINTS_VASP/" and a source code of "src_trace_v1.tar.gz"
 - b. Install "vasp2trace" with the source: vasp2trace/src_trace_v1.tar.gz
- 3. Solve the compatibility relations: semimetal or Insulator. ("checktopologicalmat").

Insulator: check If it's can be decomposed into a sum of EBRs.

(Yes: Trivial No: Topological)

Topological: Compute the symmetry indicators

Ref: Vergniory, M.G., et al., "A complete catalogue of high-quality topological materials", Nature, 566, 480-485 (2019)

www.cryst.ehu.es/cryst/checktopologicalmat

Check Topological Mat

Check Topological Mat.

Given a file that contain the eigenvalues at each maximal k-vec of a space group, the program gives the set of irreducible representations at each maximal k-vec (time-reversal is assumed). Then, using the compatibility relations and the set of Elementary Band Representations (EBRs), it checks whether the set of bands can be put as linear combinations of EBRs. This (self-explanatory) file shows the format of the file to be uploaded in the menu on the right:

File_Description

You can download examples of input files here:

Example_Ag1Ge1Li2 Example_Ag1O2Sc1
Example_B2Ca3Ni7 Example_of_Bad_File
Example_Ba3Ca1O9Pu2

You can generate the "trace.txt" file in your own computer using VASP and this program (fortran).

vasp2trace

Read the "README.pdf" file for help on the use of vasp2trace. If you are using "Check Topological Mat." and/or "vasp2trace" programs in the preparation of an article, please cite this reference:

M.G. Vergniory, L. Elcoro, C. Felser, N. Regnault, B.A. Bernevig, Z. Wang Nature(2019) **566**, 480-485. doi:10.1038/s41586-019-0954-4

Upload your traces.txt file (see the help in the column on the left).

Show

选取文件 未选择文件

Ex: Bi2Se3

- ➤ 1. The SG number(166) and crystal structure.

 (run "Phonopy" to make sure the POSCAR is given in a standard setting.)
- 2. Get the high-symmetry k points for that SG (166).
 (Vasp2trace/max_KPOINTS_VASPKPOINTS_166.txt).
- > 3. Run "VASP", to obtain the eigen-states(WAVECAR) at those kpoints. (check the symmetry operators in OUTCAR, simply by counting the total number of the operators)
- ➤ 4. Run "vasp2trace" that you have just installed locally in the folder. (trace.txt would be generated automatically)
- 5. Upload "trace.txt" and press the button.

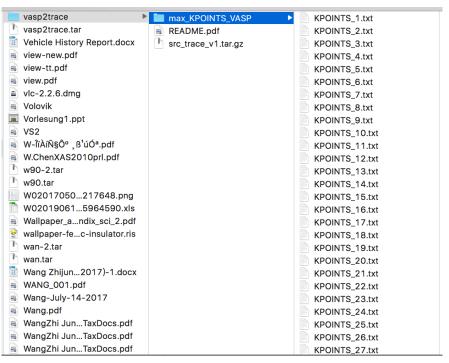
Step 1:

- \$ phonopy --tolerance 0.01 --symmetry -c POSCAR
- \$ cp PPOSCAR POSCAR

```
/anaconda3/bin/phonopy --tolerance 0.01 --symmetry -c POSCAR
phonopy version: '1.13.2'
space group type: 'R-3m'
space group number: 166
point group type: '-3m'
space group operations:
- rotation: # 1
 - [ 1, 0 , 0]
 - [ 0, 1 , 0]
 - [ 0, 0 , 1]
 translation: [ 0.00000, 0.00000, 0.00000 ]
- rotation: # 2
 -[-1, 0, 0]
 - [0, -1, 0]
 - [0, 0, -1]
 translation: [ 0.00000, 0.00000, 0.00000 ]
```

Step 2:

\$ cp xx/vasp2trace/max_KPOINTS_VASP/KPOINTS_166.txt KPOINTS.high



Step 3:

Follow REDME in the folder VASP2trace

- a. Run the scf calcualtion in vasp
- b. Run the band calculation in vasp with KPOINTS.high
- \$ vim OUTCAR; :/ irot

415

```
399 Automatic generation of k-mesh.
    Space group operators:
401
     irot
                                               n x
                                                             n y
                                                                           n z
                 det(A)
                               alpha
                                                                                                    tau y
                                                                                                                  tau z
                                                                                       tau x
402
              1.000000
                            0.000000
                                          1.000000
                                                        0.00000
                                                                      0.000000
                                                                                   0.00000
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             -1.000000
403
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404
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408
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412
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413
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             -1.000000
                          180.000000
                                          0.866025
                                                       -0.500000
                                                                      0.000000
                                                                                   0.000000
                                                                                                 0.000000
                                                                                                               0.00000
414
```

Subroutine IBZKPT returns following result:

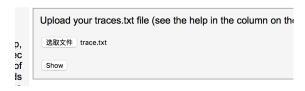
Step 4:

\$ vasp2trace / vasp2trace \$nele

```
28
 1
 2
    12
 3
                           0
                                    0.000000
                                                 0.000000
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                                                                           1.000000
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 7
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                                    0.000000
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                                                                                                     0.500000
                                                                                                                  0.8660
 8
                                    0.000000
                                                 0.000000
                                                              0.000000
                                                                           0.500000
                                                                                       -0.866025
                                                                                                     0.000000
                                                                                                                  0.0000
                        0
                           1
 9
                          -1
                                    0.000000
                                                 0.000000
                                                              0.000000
                                                                           0.500000
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                                                                                                     0.000000
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10
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11
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12
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13
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                                                                                                                  0.8660
14
               0
                     0
                       -1
                           0
15
     0
        0
               0
                 1
                     0
                           0
                                    0.000000
                                                 0.000000
                                                              0.000000
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16
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17
       0.000000
                    0.00000
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18
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                    0.500000
                                 0.500000
19
       0.500000
                    0.500000
                                 0.000000
20
       0.000000
                    0.500000
                                 0.000000
21
    12
22
             2
                  3
                             5
                                                  9
                                                       10
                                                                 12
                        4
                                  6
                                                           11
23
        2
            -9.773922
                           2.000000
                                       0.000000
                                                    2.000000
                                                                 0.000000
                                                                              0.000000
                                                                                           0.000000
                                                                                                        0.000000
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24
    3
             -8.564873
                                                                                                        0.000000
                           2.000000
                                       0.000000
                                                    -2.000000
                                                                 0.00000
                                                                              0.000000
                                                                                           0.000000
                                                                                                                     0.0
```

Step 5:

pological Mat



Result of the analysis of the uploaded structure

- The material is a topological insulator.
- List of topological indices:

```
z2w,1=0
```

z2w,2=0

z2w.3=0

z4=3

- The material belongs to the strong topological class: 6
- Clicking on See the irreps you can see the details about the number of bands and the identified irreps at each maximal k-vector.
- The set of bands can be put as linear combination of Elementary Band Representations (EBR) and parts of decomposable EBRs with integer positive coefficients. Click on Linear Combinations to get some possible linear combinations of EBRs and partial EBRs.
- Click on Subgroups to check the topological character of the structure in each of its (translationengleiche) subgroups.

Take-home message

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欢迎各位学生学者联系我们(<u>wzj@iphy.ac.cn</u>),来本组学习访问!!

Thanks for your attention!