# First Year Mathematics tutoring for Natural Sciences Week 5: Further introduction to the Complex Space

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Something else for the class

- Foundations
- $\textbf{2} \ \, \mathsf{Complex} \ \, \mathsf{space} \ \, \mathsf{as} \ \, \mathbb{R}^2$
- Something else for the class
- Remainder of the class

## Reading List or Recap

Foundations

- Wikipedia or other relevant key-word searches:
  - Euclidean distance
  - Normed vector space
  - Isometry
  - Root of unity
- Figure 21 of the lecture note:

Figure 21 gives a geometrical interpretation of multiplication, as described by (70). The special case of multiplication by i corresponds simply to rotation by  $90^{\circ}$  anti-clockwise. Taking the complex conjugate of z corresponds to reflection in the x axis.

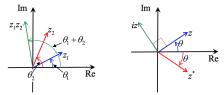


Figure 21: Argand diagram showing multiplication (left) and complex conjugates (right).

# Complex space as $\mathbb{R}^2$

$$(\mathbb{C}, |\cdot|) \cong (\mathbb{R}^2, ||\cdot||_2) \tag{1}$$

- The idea of  $(\mathbb{C}, |\cdot|)$  and  $(\mathbb{R}^n, ||\cdot||_n)$
- The idea of isometric isomorphism and the beauty about it
- Sidetrack (pure entertainment, not covered in class): Even more fun thing about its application to Economics:

You probably don't wanna click here if you wish to skip this entertainment, which is not necessarily that fun.

## Implication to 2D Geometry and the concept of $f: \mathbb{R}^2 \to \mathbb{R}$

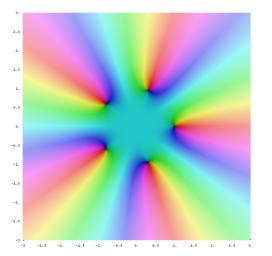


Figure: Plot of  $z^5-1$  in which a zero is represented by the color black. Courtesy: Wikipedia page for the Root of unity

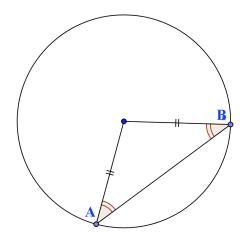


Figure: Isosceles triangle in a circle. Courtesy: GeoGebra

Extension: formula for the distance AB.



### Remainder of the class

- Warm Up: Jack to demonstrate F19.
- Quick points regarding F9 and F17.
- Main Teaching Point: F16