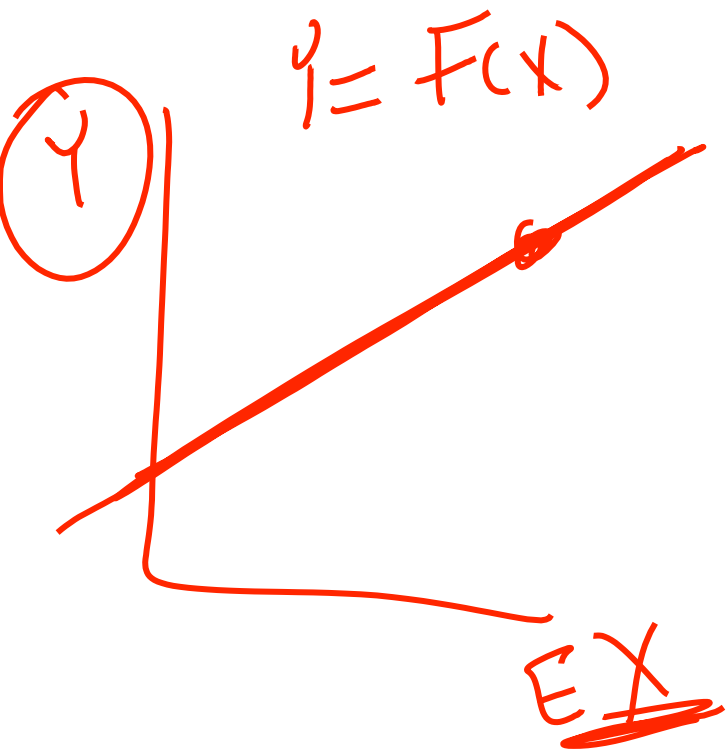


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Categorical Models



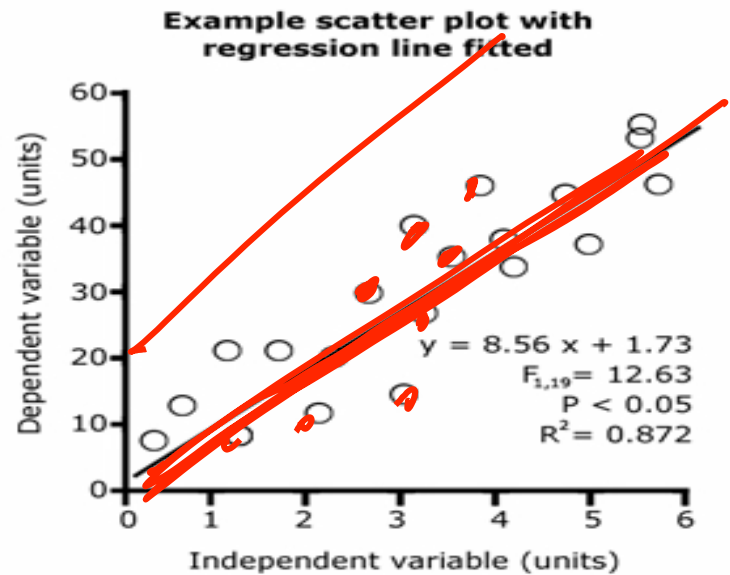


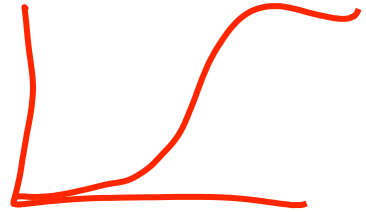
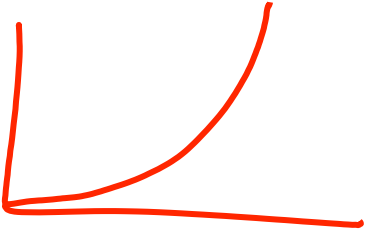
Linear Models



Fitting Lines to Data







Non Linear Models



$$y_1 = \underbrace{a_1}_{\text{Big}} x_1 + \underbrace{a_2}_{\text{Big}} x_2$$

Big Coefficient



Model Thinking

Scott E Page

Model Thinking

Scott E Page



Categorical Models



Amazon



“Lump to Live”



Broccoli

Grasshopper

Banana

Candy Bar

Orange

Asparagus

Pear

Strawberry



Calories

Pear 100-

Cake 250-

Apple 90

Banana 110/

Pie 350

Mean = 180

Pear $100 - 180 = \text{180}$

Cake $250 - 180 = \text{70}$

Apple $90 - 180 = \text{90}$

Banana $110 - 180 = \text{70}$

Pie $350 - 180 = \text{170}$

480

Pear $(100-180)^2$

Cake $(250-180)^2$

Apple $(90-180)^2$

Banana $(110-180)^2$

Pie $(350-180)^2$

$$(\underline{100} - \underline{180})^2 = \underline{6400}$$

$$(\underline{250} - \underline{180})^2 = 4900$$



| | |
|---------------|-----------------------|
| - Pear | $(100-180)^2 = 6400$ |
| - <u>Cake</u> | $(250-180)^2 = 4900$ |
| - Apple | $(90-180)^2 = 8100$ |
| - Banana | $(110-180)^2 = 4900$ |
| - <u>Pie</u> | $(350-180)^2 = 28900$ |

Total Variation = 53,200

90
100
110

250
350

FRUIT

DESSERT

mean = 100

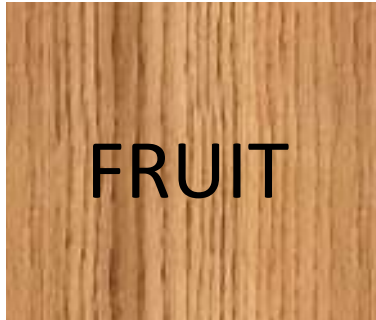
$$\begin{aligned}(90 - 100)^2 &= 100 \\ (100 - 100)^2 &= 0 \\ (110 - 100)^2 &= 100\end{aligned}$$

mean 300

$$\begin{aligned}(250 - 300)^2 &= 2500 \\ (350 - 300)^2 &= 2500 \\ \hline 5000\end{aligned}$$



$$\text{mean} = 180$$
$$V = \$3,200$$



Mean = 100



Mean = 300

Variation = 200

Variation = 5000



Total Variation = 53,200

Fruit Variation = 200

Dessert Variation = 5000
5200

How much did I explain?

$$\frac{53,200 - 5,200}{53,200} = \frac{48,000}{53,200}$$



R-Squared

% Variation Explained

$$1 - 5200/53,200$$

90.2%

$$\frac{48,000}{53,200}$$



R-Squared

R-squared near 1
model explains a
lot

R-squared near 0
model explains
little



FRUIT

DESSERT

VEG

GRAIN





Equestrian

Photo Simon Howden

Correlation

is not

Causation



Model Thinking

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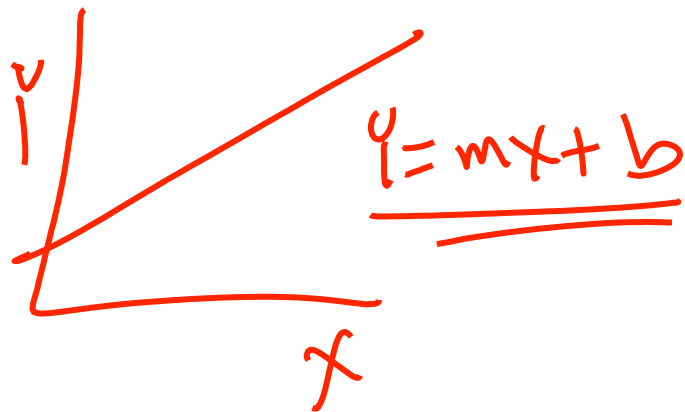
Model Thinking

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X

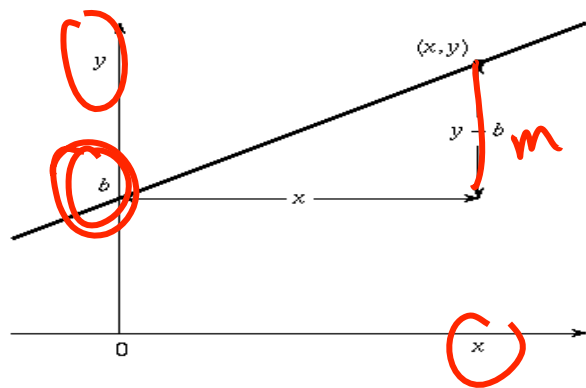
$$Y = F(X)$$



Linear Models



$$y = mx + b$$



Linear Model vs Line

X = Independent Variable

Y = Dependent Variable

Y depends on X





X = Length of Diagonal

Y = Cost of TV

Linear Model:

$$\text{Cost} = 15 * \text{Length} + 100$$

$$Y = 5X$$

Sign: does Y increase or decrease in X?

Magnitude: how much does Y increase for each one unit increase in X?




$$\text{Cost} = 15 * \text{Length} + 100$$

Predict

Understand Data



$$\text{Cost} = 15 * \text{Length} + 100$$

30 inch TV?

$$C = 15(30) + 100$$

$$450 + 100$$

$$\$550$$



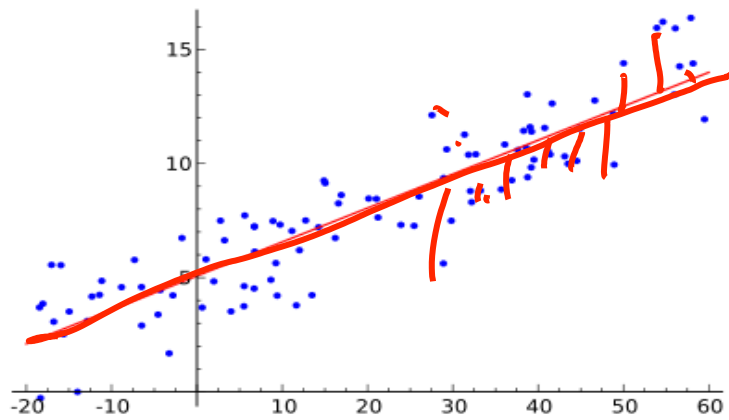
$$\text{Cost} = 15 * \text{Length} + 100$$

100 inch TV?

$$C = 15(100) + 100$$

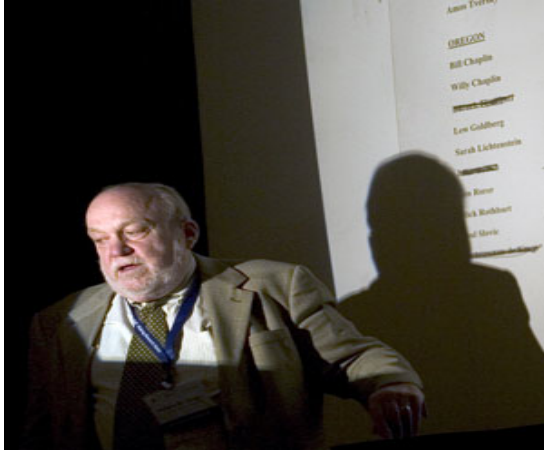
~~\$~~1600





www.wikimedia.org





Robyn Dawes 1979: “The Robust Beauty of Improper Linear Models in Decision Making”



43 bank loan officers predict which 30 of 60 firms would go bankrupt. They see financial statements.

Bankers: 75 % accurate

Linear Model: ratio of assets to liabilities 80%



Mehl (1954) 20
studies of clinicians

Sawyer (1966) 45
studies of predictions
in the social world.

Experts ~~NEVER~~ did
significantly better



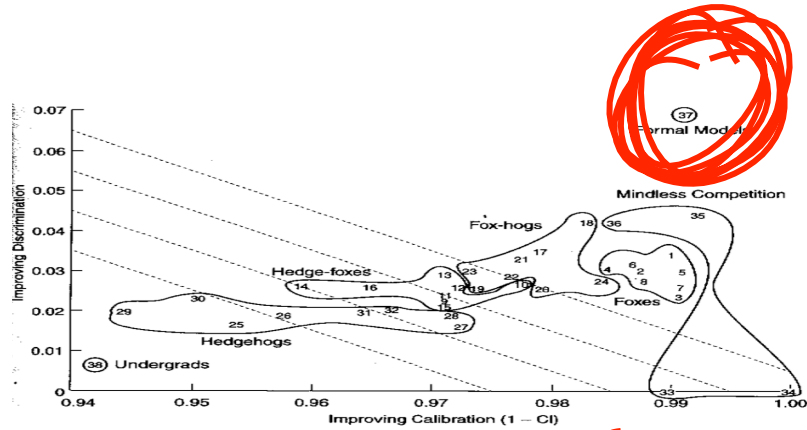


Figure 3.2. How thoroughly foxes and fox-hog hybrids (first and second generation) make short-term and long-term decisions on cognitive style scales.



Model Thinking

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Model Thinking

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Fitting Lines to Data

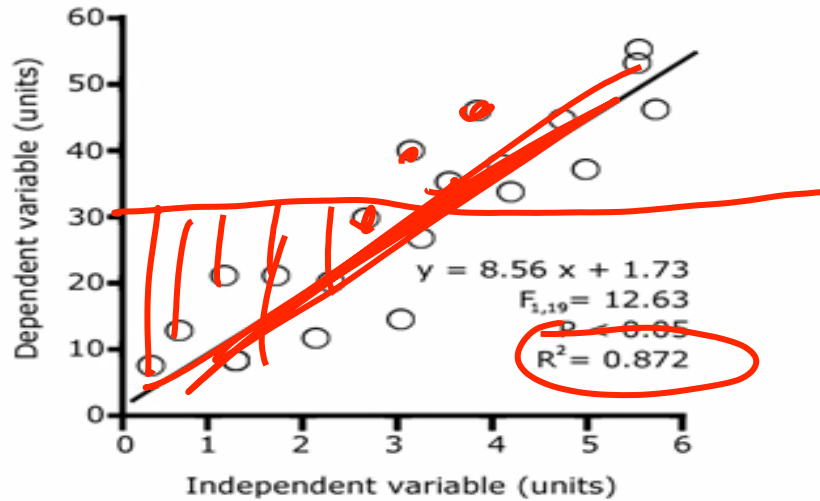


R-squared:

% Variation Explained



Example scatter plot with regression line fitted



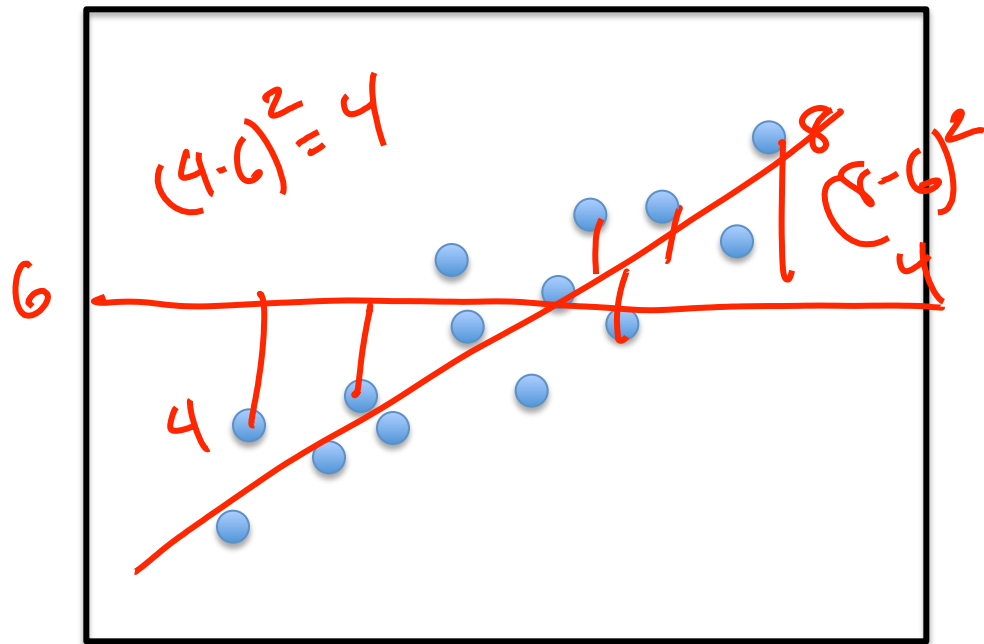
R-Squared

% Variation Explained

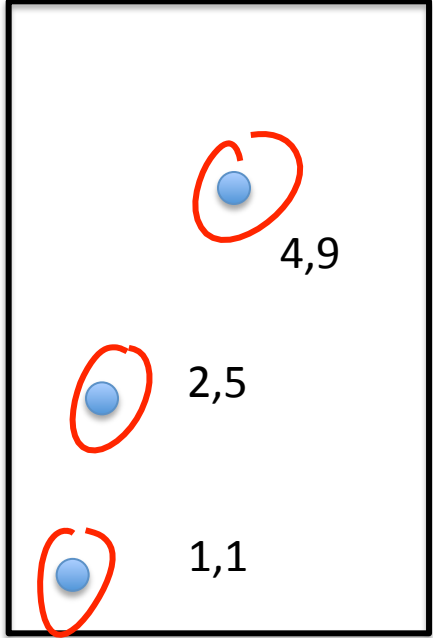
$$1 - 5200/53,200$$

90.2%





Shoe
Size



Grade

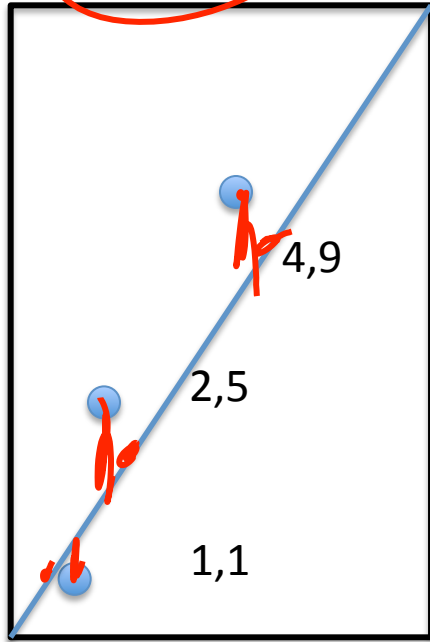


Variation?

$$\begin{array}{l} \text{G} \quad \text{S} \\ (1, 1) \quad (1-5)^2 = 16 \\ (2, 5) \quad (5-5)^2 = 0 \\ (4, 9) \quad (9-5)^2 = 16 \\ \hline 15/3 = 5 \quad (32) \end{array}$$

$$Y=2X$$

Shoe
Size



Grade

$$Y=2X$$

32

$(X, Y, 2X)$

$(1, 1, 2)$

$$(2-1)^2 = 1$$

$(2, 5, 4)$

$$(4-5)^2 = 1$$

$(4, 9, 8)$

$$(8-9)^2 = 1$$

3

$$1 - \frac{3}{32} =$$

$$90.4\%$$

$(1,1,2)$

$(2,5,4)$

$(4,9,8)$

R-Squared



$$Y = mX + b$$

$$x=1 \quad (m+b \cdot 1)^2 = (m^2 + 2mb + b^2 - 2m - 2b + 1)$$

$$x=2 \quad (2m+b-5)^2$$

$$(4m+b-9)^2$$

$$21m^2 + 14mb + 3b^2 - 94m - 30b + 81$$

$$b = -1$$

$$m = 8/3$$

Total
Variation

X, Y, MODEL

(1, 1, 5/3)

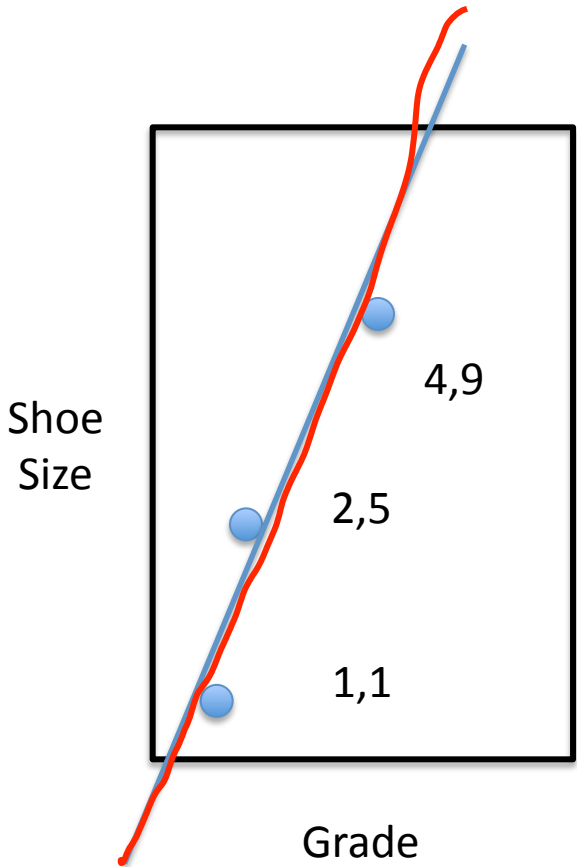
(2, 5, 13/3)

(4, 9, 29/3)

R-Squared

$$1 - \frac{4/3}{32}$$

0.90



Model Thinking

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Model Thinking

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R-Squared: 0.72
Standard Error: 24.21
Observations: 50

| | Coeff | SE | P-value |
|-----------|-------|----|---------|
| Intercept | 25 | 2 | 0.000 |
| X1 | 20 | 1 | 0.000 |
| X2 | 10 | 4 | 0.014 |



$$Y = mx + b$$

$$Y = \underline{m_1 x_1} + \underline{m_2 x_2} + b$$

Multiple Variables



Y = Test Score

T = Teacher Quality

Z = Class Size

$$Y = \underbrace{cT}_{c > 0} + \underbrace{dZ}_{d < 0} + \underbrace{b}_{(b)}$$



$$Y = aX_1 + bX_2 + \textcircled{c}$$

coet

int

R-Squared:

0.72

Standard Error:

24.21

Observations:

50



Intercept

Coeff

25

SE

2

P-value

0.000

X1

20

1

0.000

X2

10

4

0.014




$$\underline{Y} = \underline{20}X_1 + \underline{10}X_2 + 25$$

Sign: does Y increase or decrease in X?



Magnitude: how much does Y increase for each one unit increase in X?



VARIATION R^2

Sign

magnitude

P-value

Model Thinking

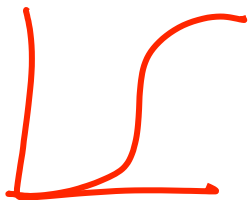
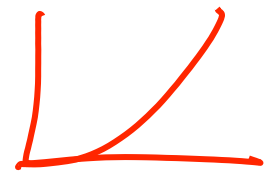
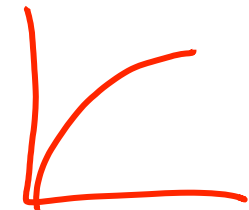
Scott E Page



Model Thinking

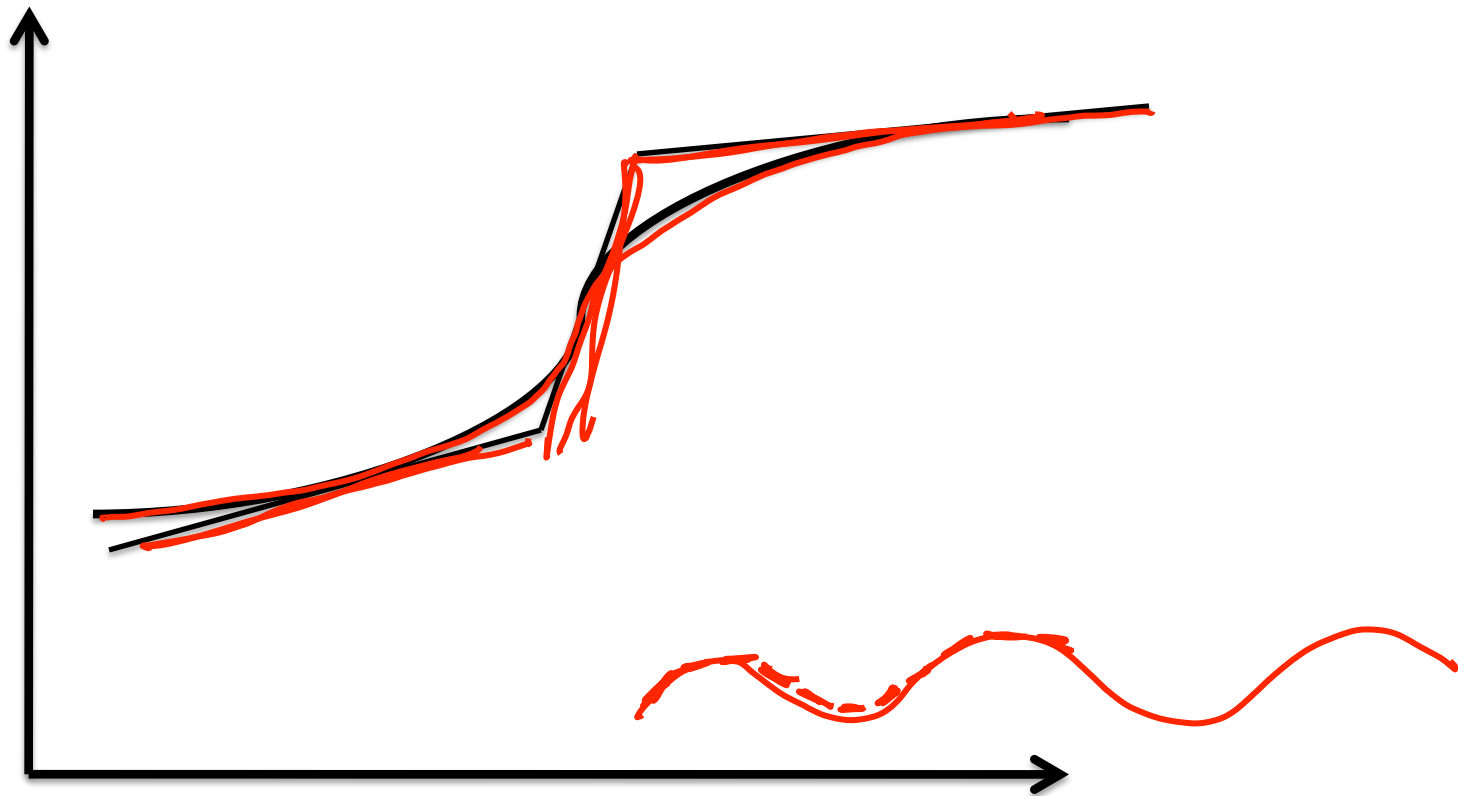
Scott E Page



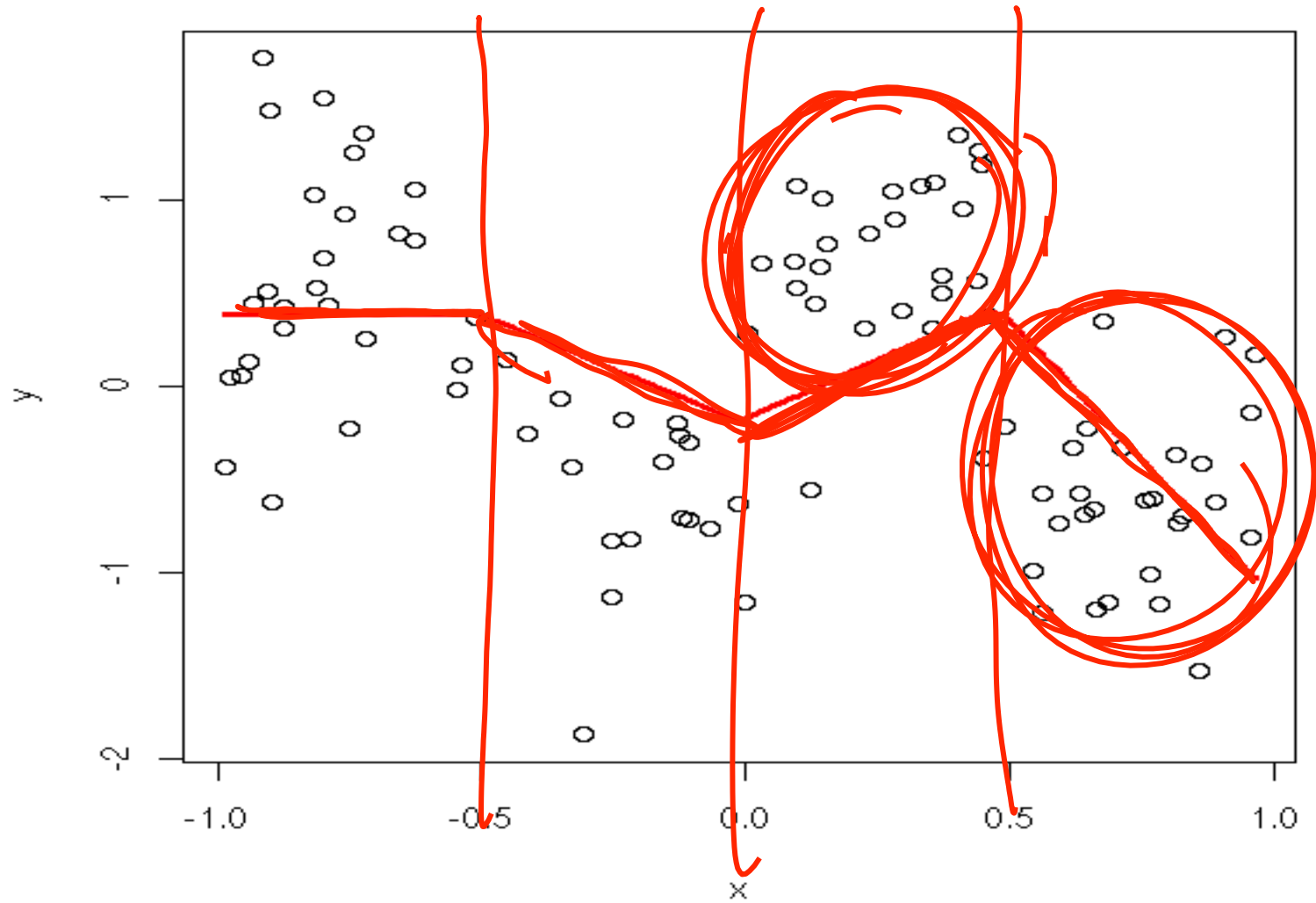


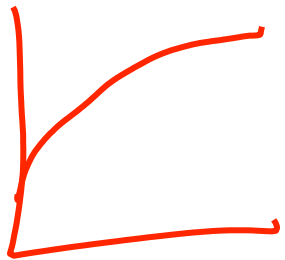
Non Linear





M





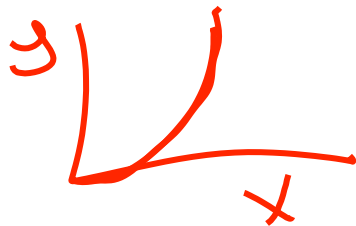
$$y = m\sqrt{x} + b$$

$$y = mz + b$$

$$z = \sqrt{x}$$

$$z = x^2$$

$$y = mz + b$$



Non Linear Terms



Model Thinking

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Model Thinking

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$$Y = (a_1)X_1 + (a_2)X_2 + b$$

The Big Coefficient



Evidence Based_____

Medicine

Philanthropy

Education

Management



Construct Model

Gather Data

Identify important variables

Change those variables



Big Data





Gather Data

Find Pattern

Identify important variables

Change those variables



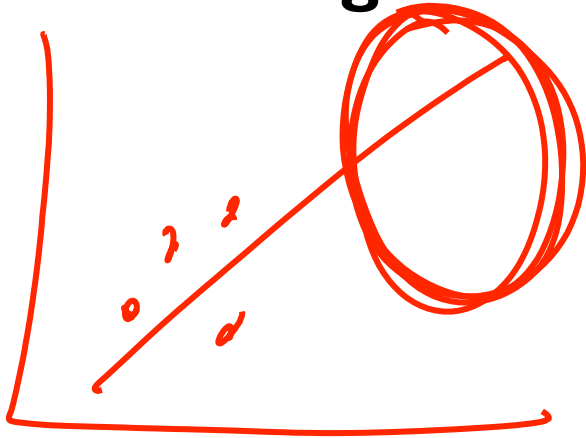
Big data does not
obviate the uses of
models

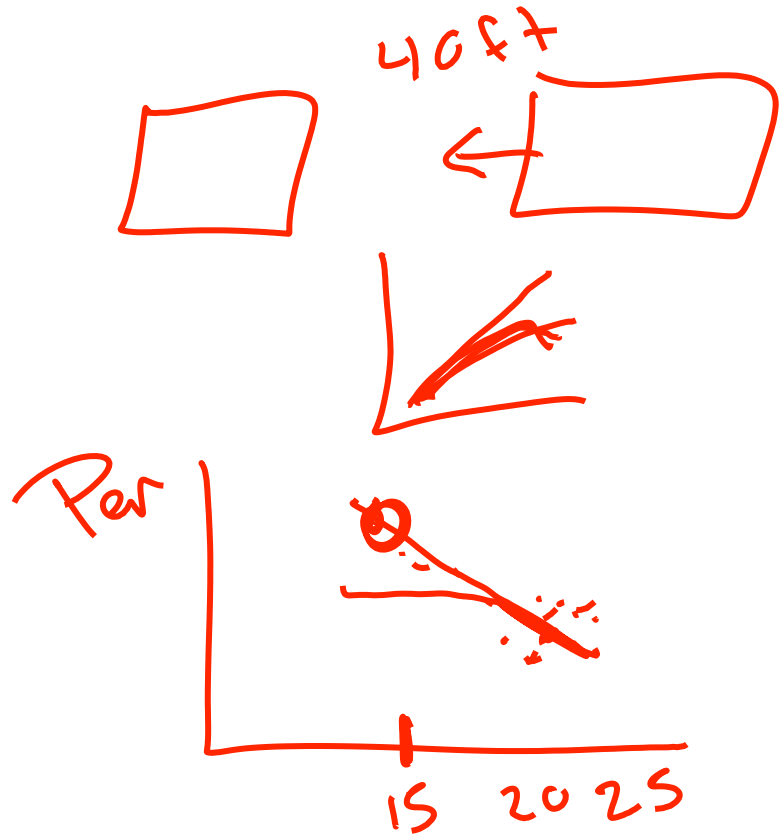


Correlation
is not
Causation



Linear models tell sign
and magnitude of
changes in independent
variables **within data
range**





Feedbacks



Multiple Peaks



The New Reality



Big Coefficient

Tax Cigarettes

New Reality

Universal Health Care



Big Coefficient

Increase HOV Lanes

New Reality

Rail System



Big Coefficient

Oat Bran Pretzels

New Reality

Fitness Regimine



American Jobs Act

1. Tax Cuts to Help America's Small Businesses Hire and Grow

- Cutting the payroll tax
- Payroll tax holiday for new workers and higher wages
- 100% expensing

2. Rebuilding and Modernizing America

- Subsidies to hire veterans
- Save 280,000 teachers jobs
- Infrastructure and infrastructure bank
- Modernize Schools and buildings
- High speed wireless

3. Pathways to Work

- Rewrite unemployment insurance
- \$4000 tax credit for new employees

4. Tax Relief

- Cuts in payroll taxes
- Allowing more refinancing



Interstate Highway System

41,000 miles of roads

\$25 billion

CPI: \$207 Billion today

Mile: \$10 million a mile

\$410 Billion



Model Thinking

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