

An overview of : A model independent calibration of quasars



Xiaolei Li, Ryan E. Keeley, Arman Shafieloo, Xiaogang Zheng, Shou Cao, Marek Biesiada, Zong-Hong Zhu⁵

Resources:
github.com/parsa-ghafour/Conferences_and_Seminars

At a glance:

Foreword	Base relation	Data sets	Calibration	Results
Important characteristics of quasars	Relation between the log of their ultraviolet (UV) and X-ray luminosities	Quasar sample (Training data set)	Unanchored luminosity distance	Model independent calibration results for the quasar parameters
Quasars as standardized candles	Free parameters	Supernovae Ia sample (Test data set)	Generating a set of cosmological functions	$\log(D_L H_0)$ - redshift relation
Base relation	Hyper parameters		GP regression	Residuals of the observed $\log(F_X)$ values with respect to the predicted $\log(F_X)$
Correlation between the Base relation and the cosmological distances			Reconstruct the expansion history	
			Likelihood	The linear relation between $\log(L_{UV})$ and $\log(L_X)$
			LINMIX_ERR	
			MCMC analysis	

Foreword:

Quasars

- Are luminous persistent sources
- Can be observed up to redshifts of $z \approx 7.5$ (Mortlock et al. 2011)
- Might be able to fill the redshift gap between the farthest observed Type Ia Supernovae and CMB (Scolnic et al. 2017)

Farthest SN Ia: $z \approx 2.3$ (ESA/Hubble, David O. Jones et al.)
CMB: higher redshift

Quasars can be used as
standardized candles

Calibrate the
largest quasar
sample

Constraining the
parameters of the
Base relation

There is a strong correlation
between the parameters
characterizing the quasar
luminosity relation and the
cosmological distances

Base relation:

Quasars have also been used as standard candles whose standardization relies on the linear relation between the log of their ultraviolet (UV) and X-ray luminosities:

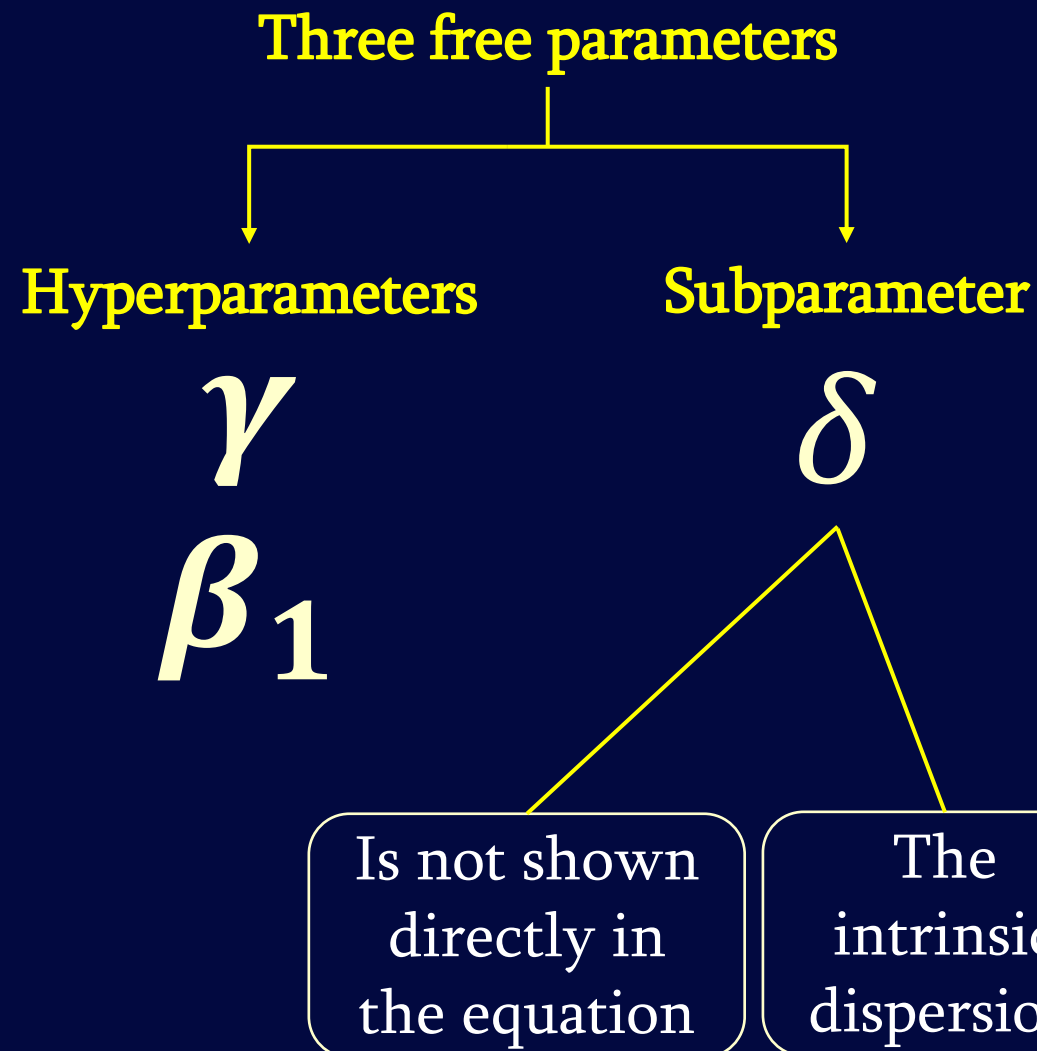
(Risaliti & Lusso 2015, 2017; Lusso & Risaliti 2016, 2017; Risaliti & Lusso 2019; Salvestrini et al. 2019; Lusso et al. 2019, 2020; Lusso 2020; Khadka & Ratra 2020a, b; Liu et al. 2020a, b, c; Geng et al. 2020; Zheng et al. 2021).

$$\log(L_X) = \gamma \log(L_{UV}) + \beta_1$$

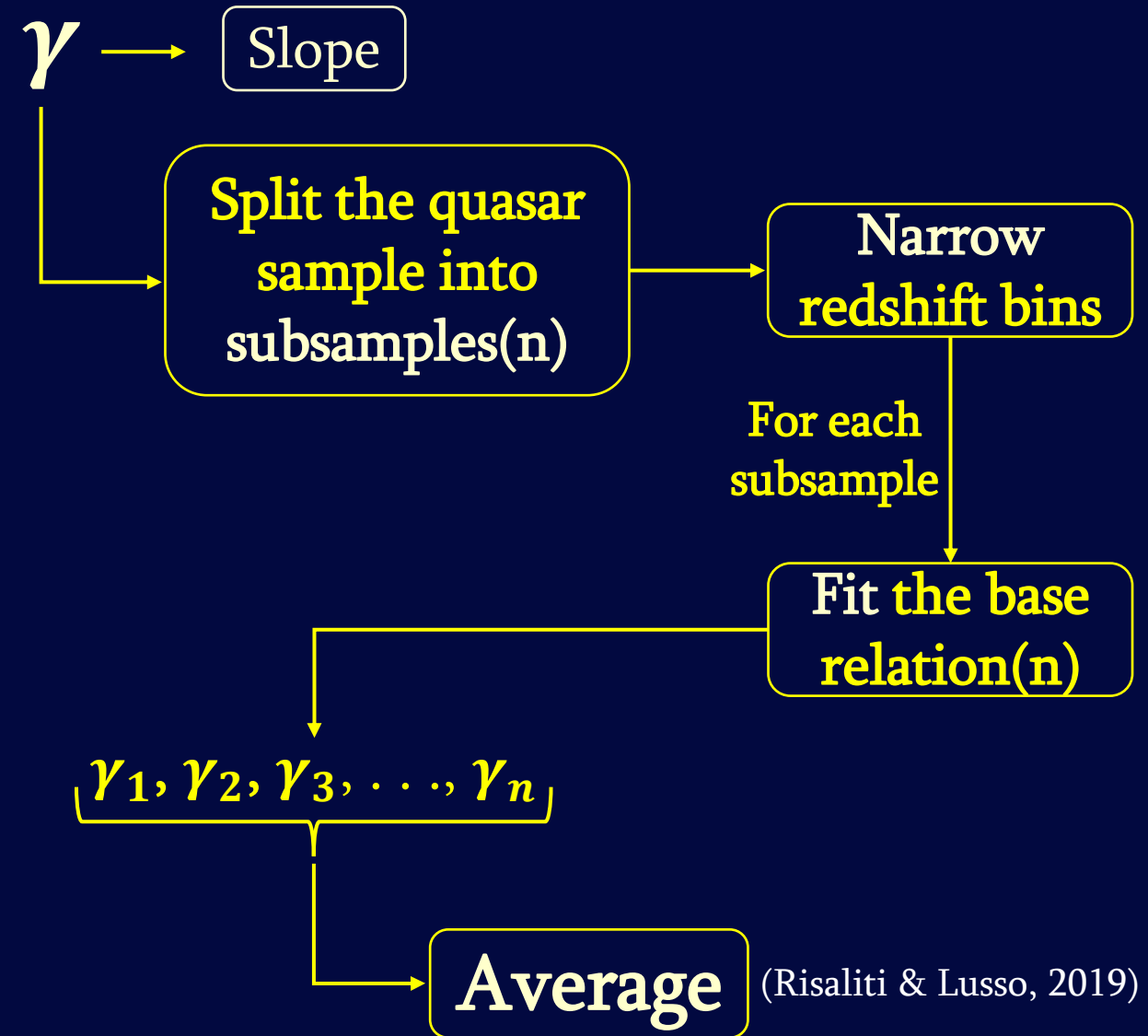
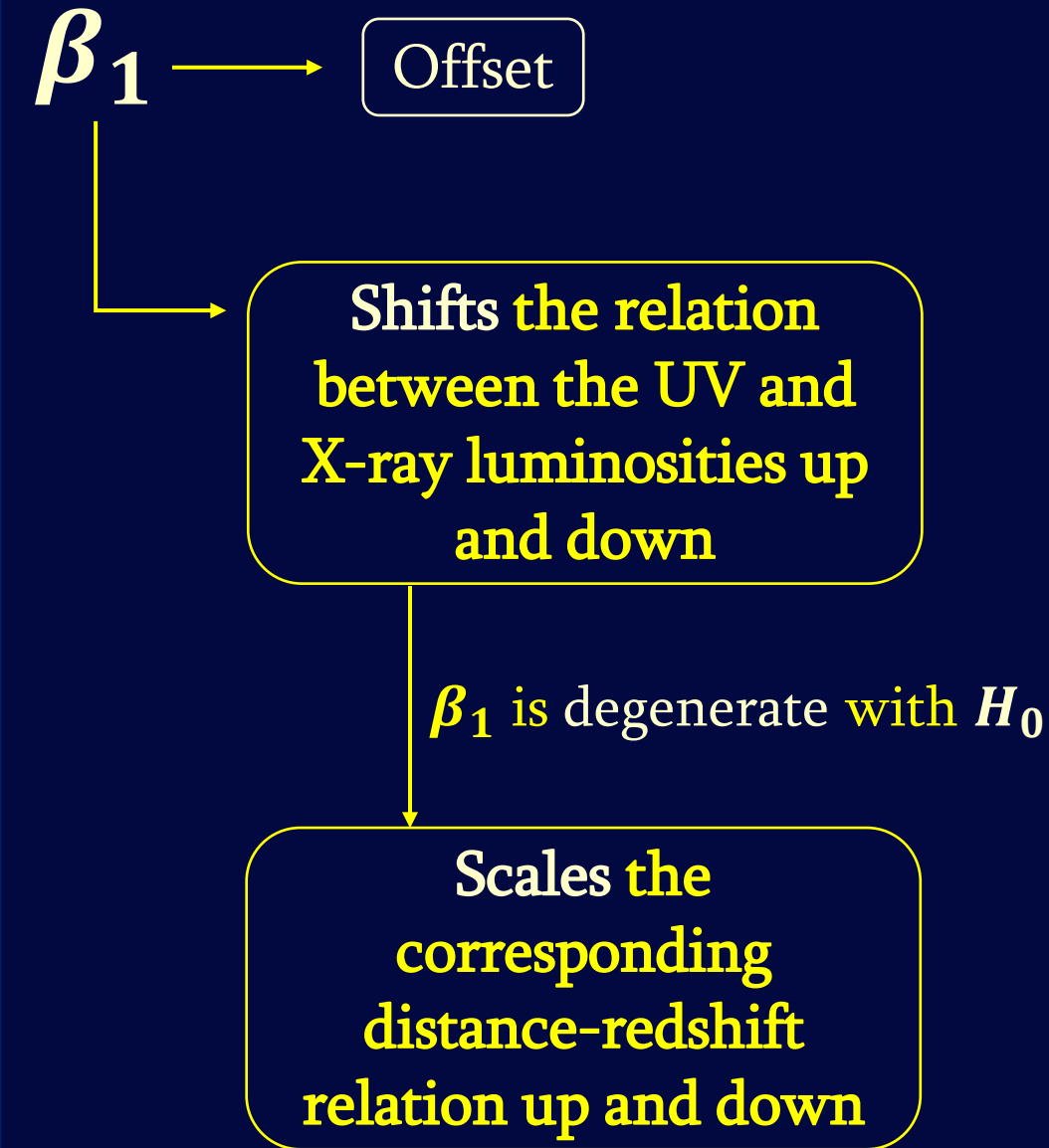
rest-frame luminosities

Slope

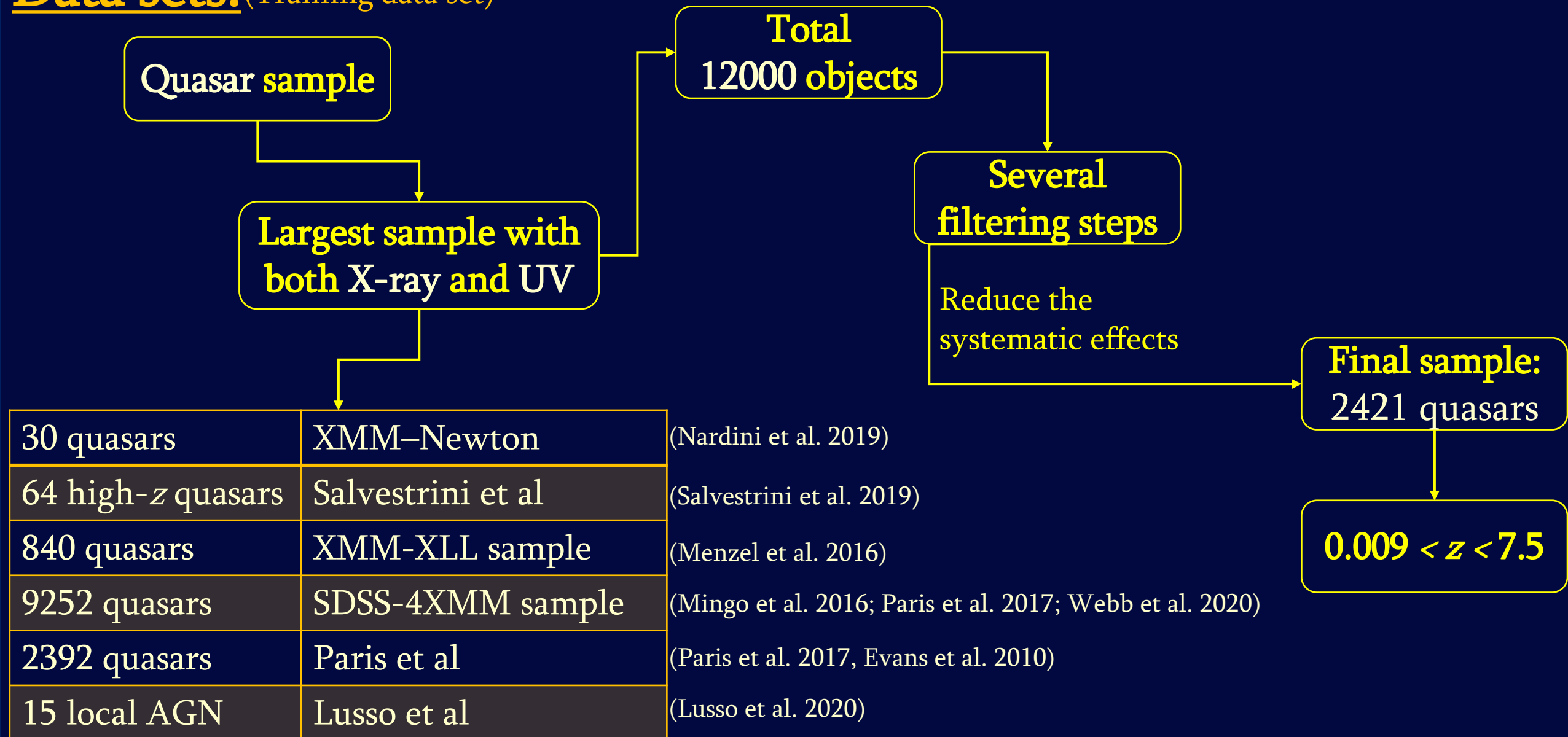
Offset



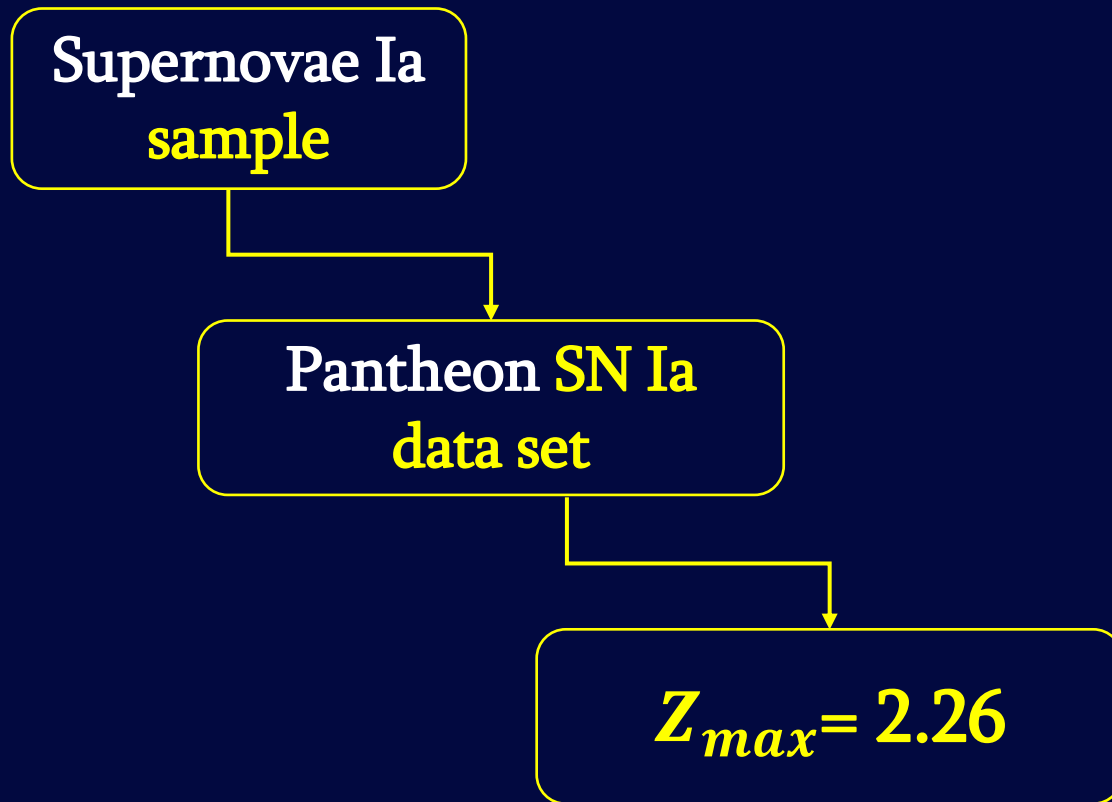
Hyperparameters:



Data sets: (Training data set)

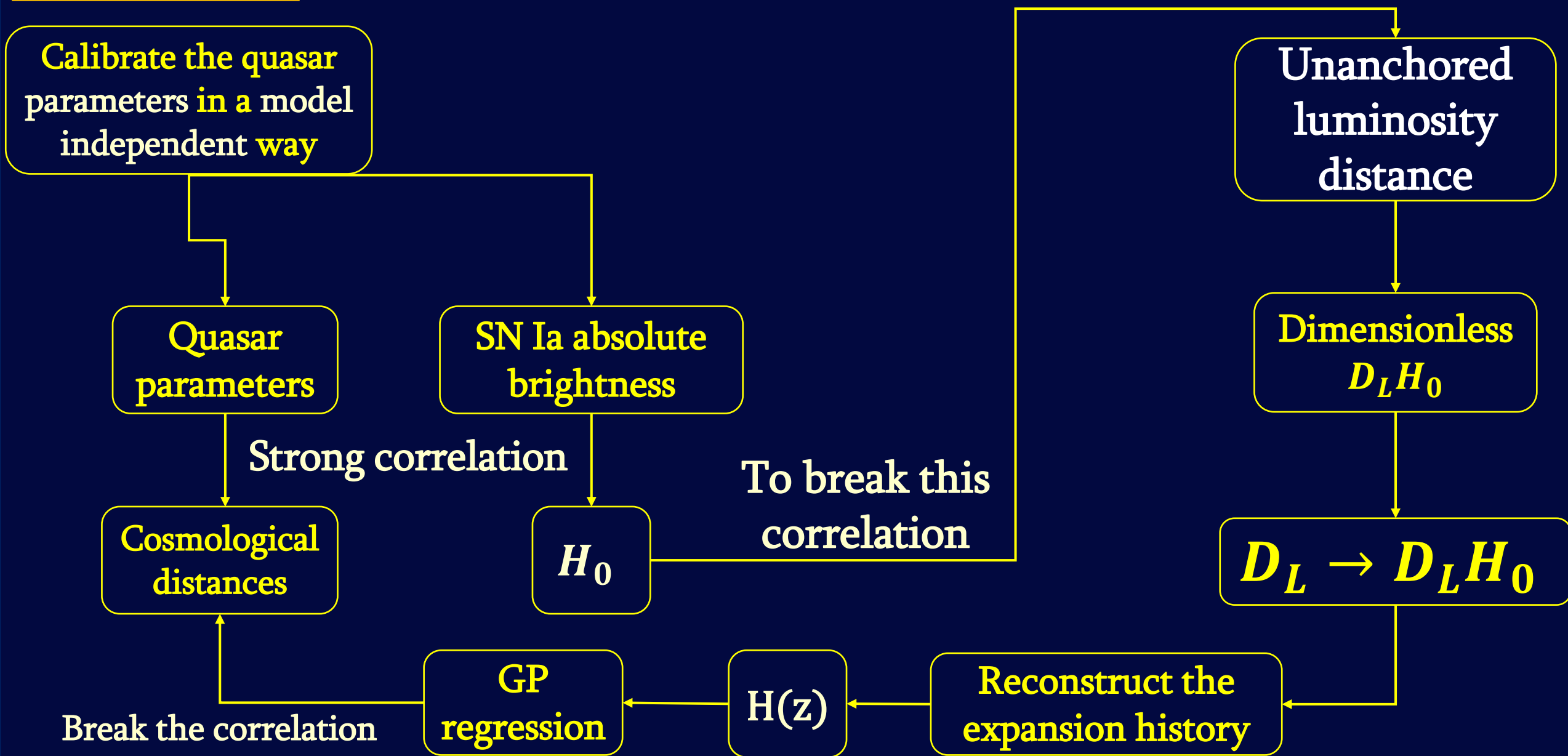


Data sets: (Test data set)

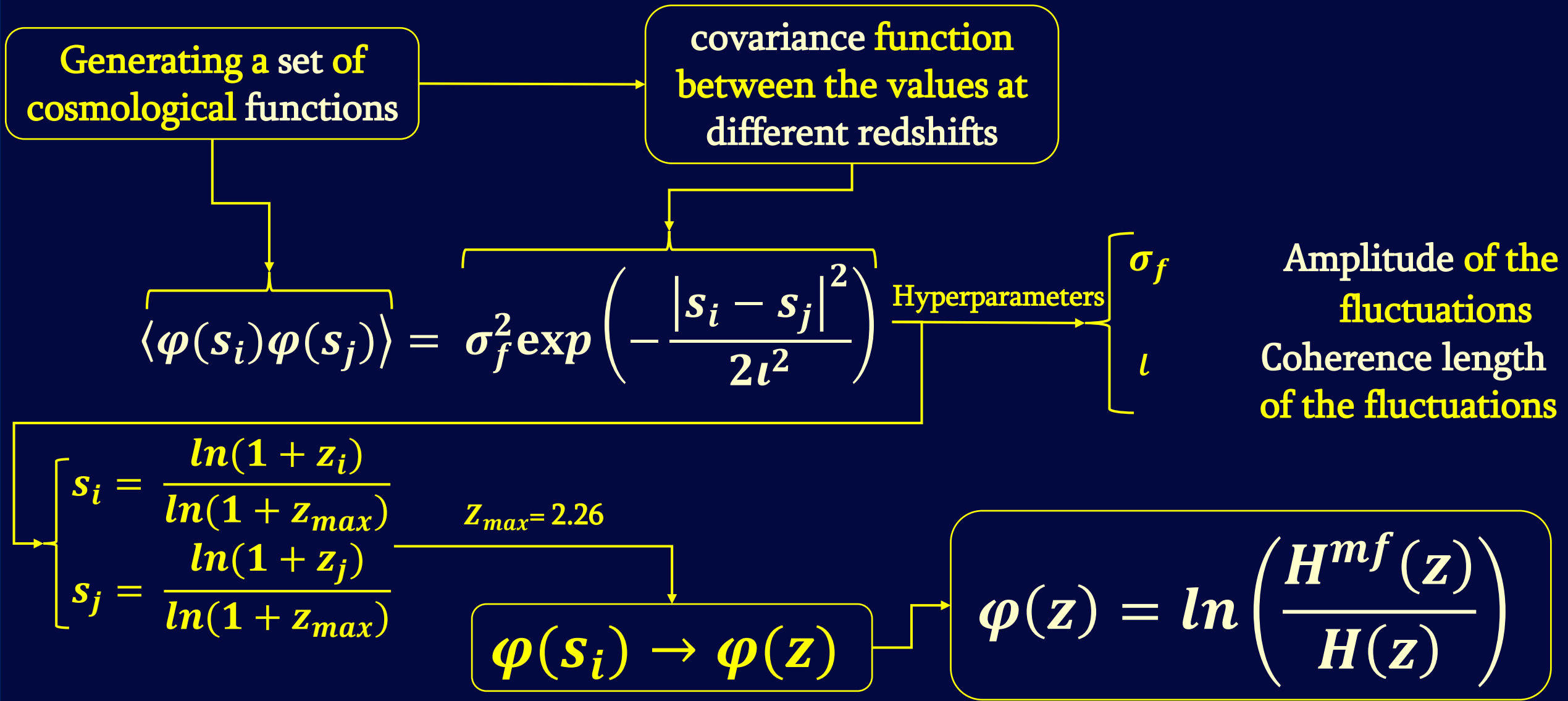


(Scolnic et al. 2017; Liao et al. 2019, 2020; Rasmussen & Williams 2006, Holsclaw et al. 2010a, b, 2011, Shafieloo, Kim & Linder 2012, Joudaki et al. 2018, Keeley et al. 2019, 2020, 2021

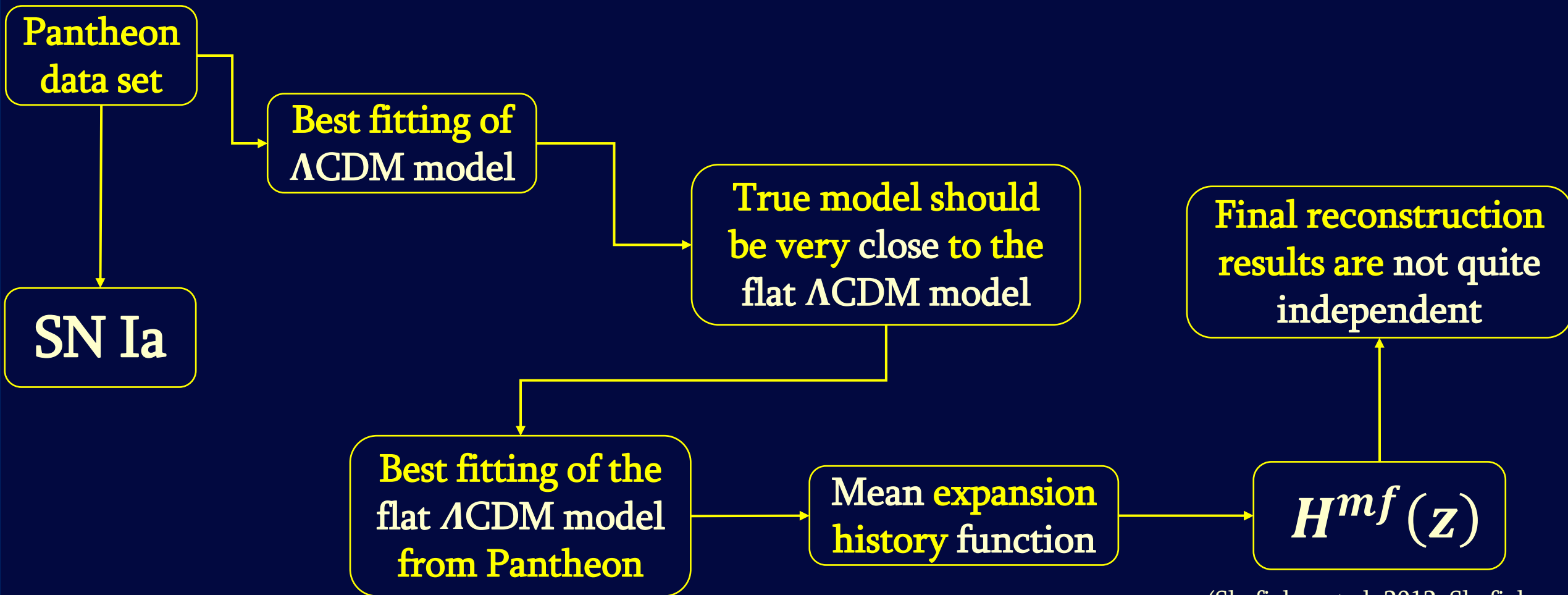
Calibration:



GP regression: (Gaussian Process regression)



GP regression: (Gaussian Process regression)



(Shafieloo et al. 2012; Shafieloo, Kim & Linder 2013; Aghamousa, Hamann & Shafieloo 2017)

GP regression: (Gaussian Process regression)

Unanchored
luminosity
distance

Dimensionless
 $D_L H_0$

$D_L \rightarrow D_L H_0$

$$\varphi(z) = \ln \left(\frac{H^{mf}(z)}{H(z)} \right)$$

$$\varphi(z) \leftrightarrow H(z)$$

Integrate this function
to get the unanchored
luminosity distance

$$D_L H_0(z) = (1 + z) \int_0^z \frac{c}{h(z)} dz$$

$$h(z) = \frac{H(z)}{H_0}$$

**This function is
directly constrained by
the SN Ia data set and
can be reconstructed**

GP regression: (Gaussian Process regression)

GP calculates a posterior for $D_L H_0$ function

Posterior probability

Revised or Updated probability

Updating the prior probability using Bayes' theorem

$$P(A|B) = \frac{P(B|A)P(A)}{P(B)}$$

$$D_L H_0(z) = (1 + z) \int_0^z \frac{c}{h(z)} dz$$

Posterior

$$P(D_L H_0 | D_L) = \int \frac{\mathcal{L}(D_L H_0(\varphi)) P(\varphi)}{P(D_L)}$$

$$\mathcal{L}(D_L H_0(\varphi))$$

Likelihood of the data

$$P(\varphi)$$

Consequence using a flat prior on the GP hyperparameters

Calibration:

Draw 1000 unanchored luminosity distances reconstructed from the SN Ia data

$$P(D_L H_0 | D_L) = \int \frac{\mathcal{L}(D_L H_0(\varphi)) P(\varphi)}{P(D_L)}$$

$D_L H_0$

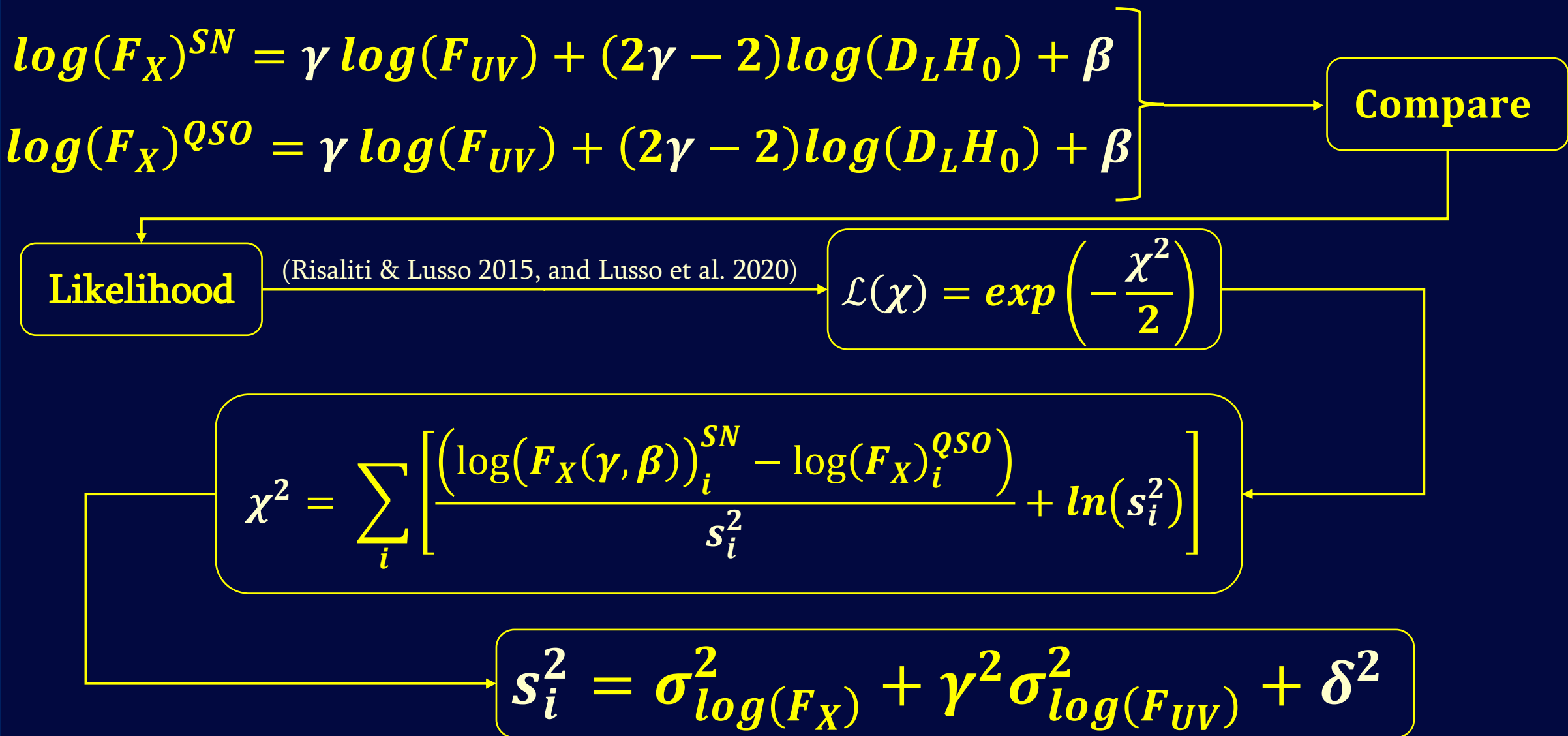
Calculate the predicted quasar X-ray flux corresponding to these unanchored luminosity

$$\log(L_X) = \gamma \log(L_{UV}) + \beta_1$$

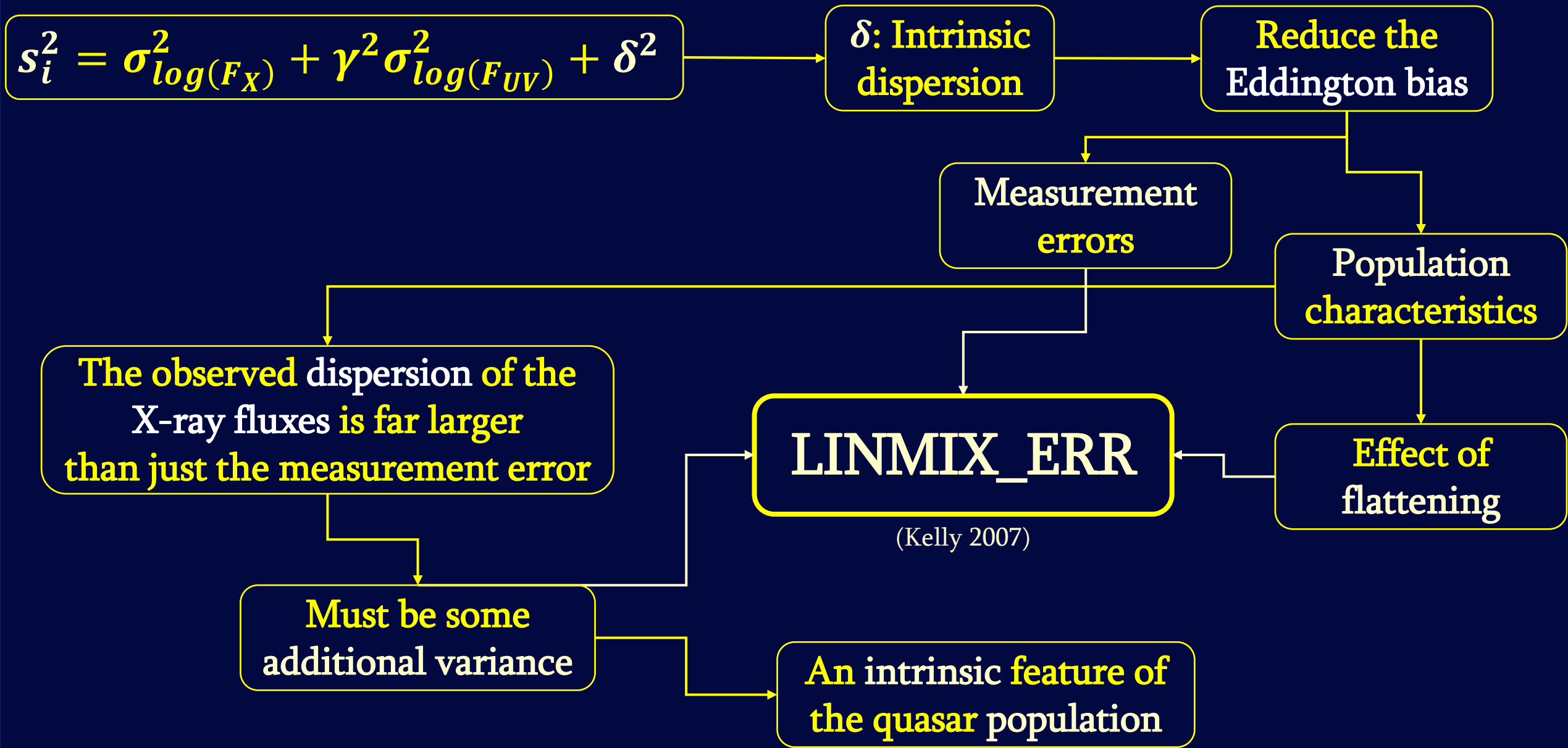
$$\begin{aligned} \log(F_X) &= \gamma \log(F_{UV}) + (2\gamma - 2) \log(D_L) + \beta_2 \\ \beta_2 &= \gamma \log(4\pi) - \log(4\pi) + \beta_1 \end{aligned}$$

$$\begin{aligned} \log(F_X)^{SN} &= \gamma \log(F_{UV}) + (2\gamma - 2) \log(D_L H_0) + \beta \\ \beta &= \beta_2 - (2\gamma - 2) \log(H_0) \end{aligned}$$

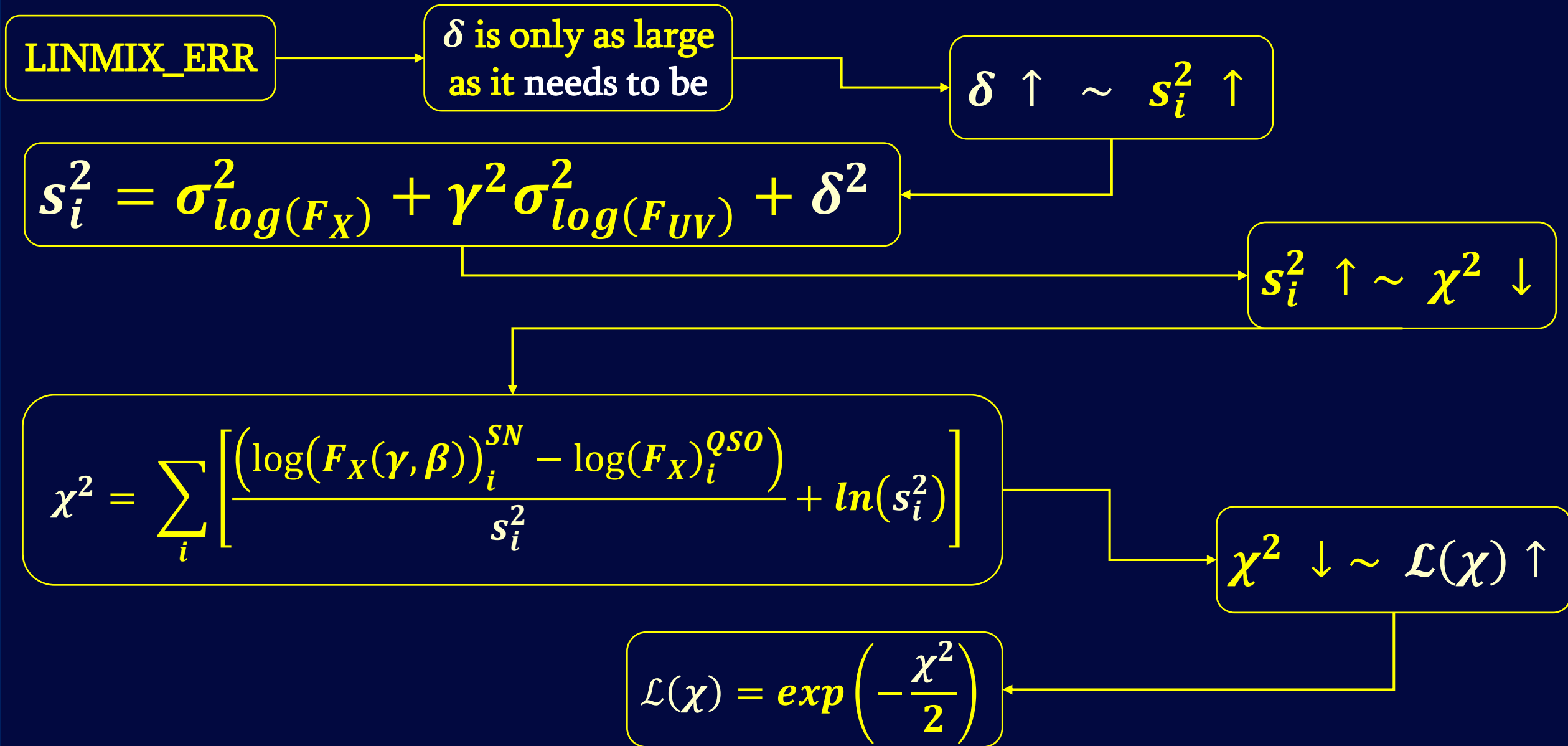
Calibration:



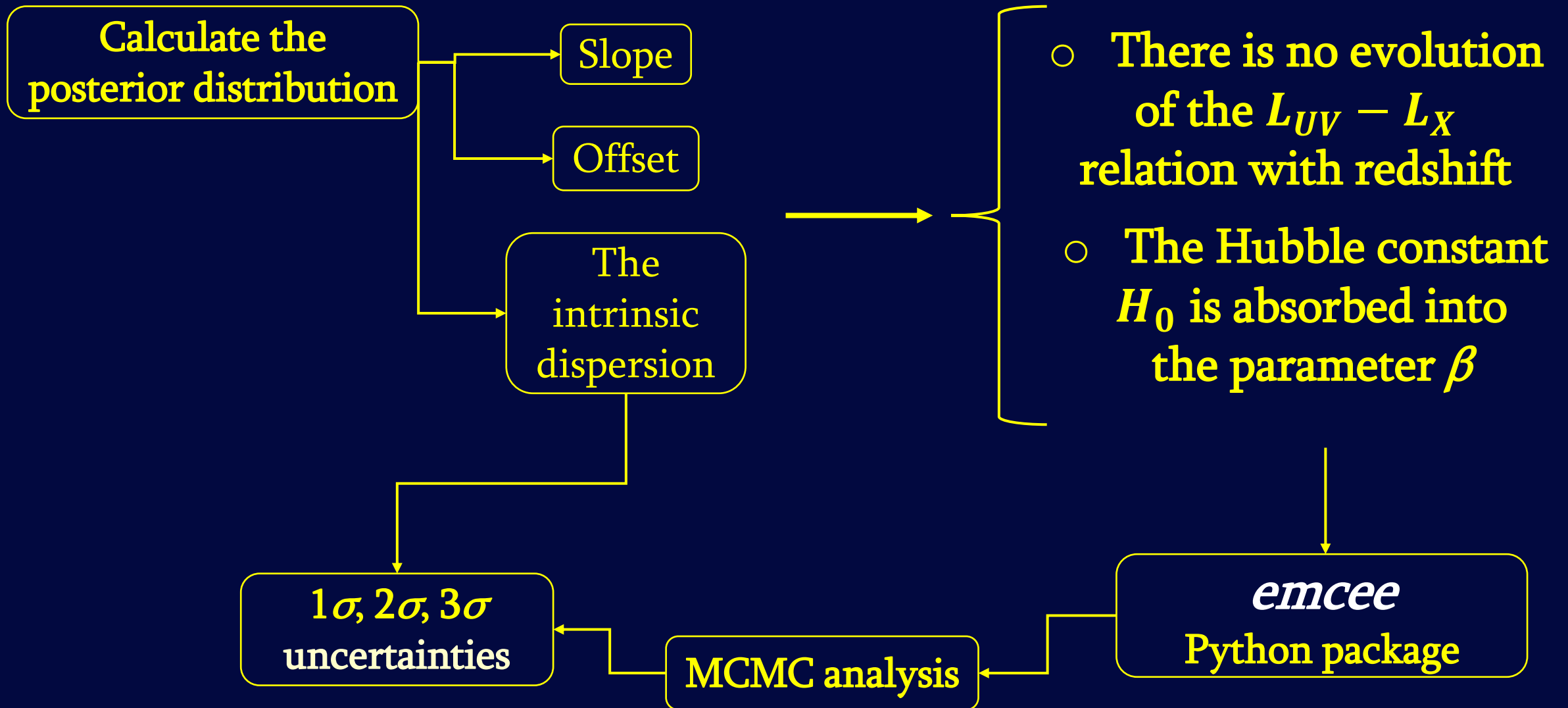
Calibration:



Calibration:



Calibration:



Calibration:

- i. Draw 1000 unanchored luminosity distances from supernovae data
- ii. Calculate the predicted quasar X-ray flux corresponding to these unanchored luminosity distances
- iii. Define the likelihood of the quasar parameters
- iv. Calculate the posterior distribution of the quasar parameters

$$D_L H_0$$

$$F_X^{QSO}$$

$$\mathcal{L}(\chi)$$

MCMC

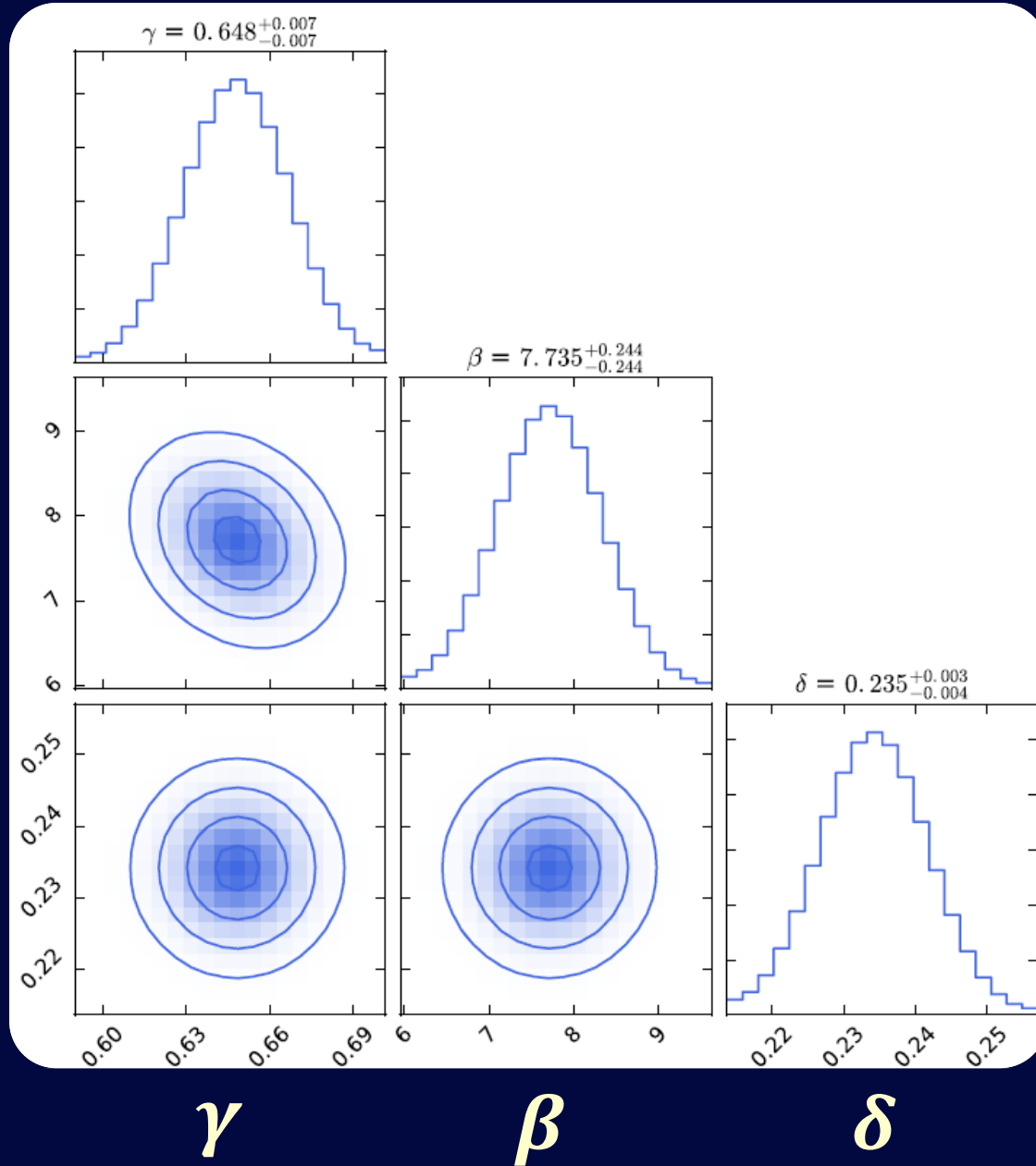
$$\gamma, \beta_1, \delta, 1\sigma, 2\sigma, 3\sigma$$

Results:

γ

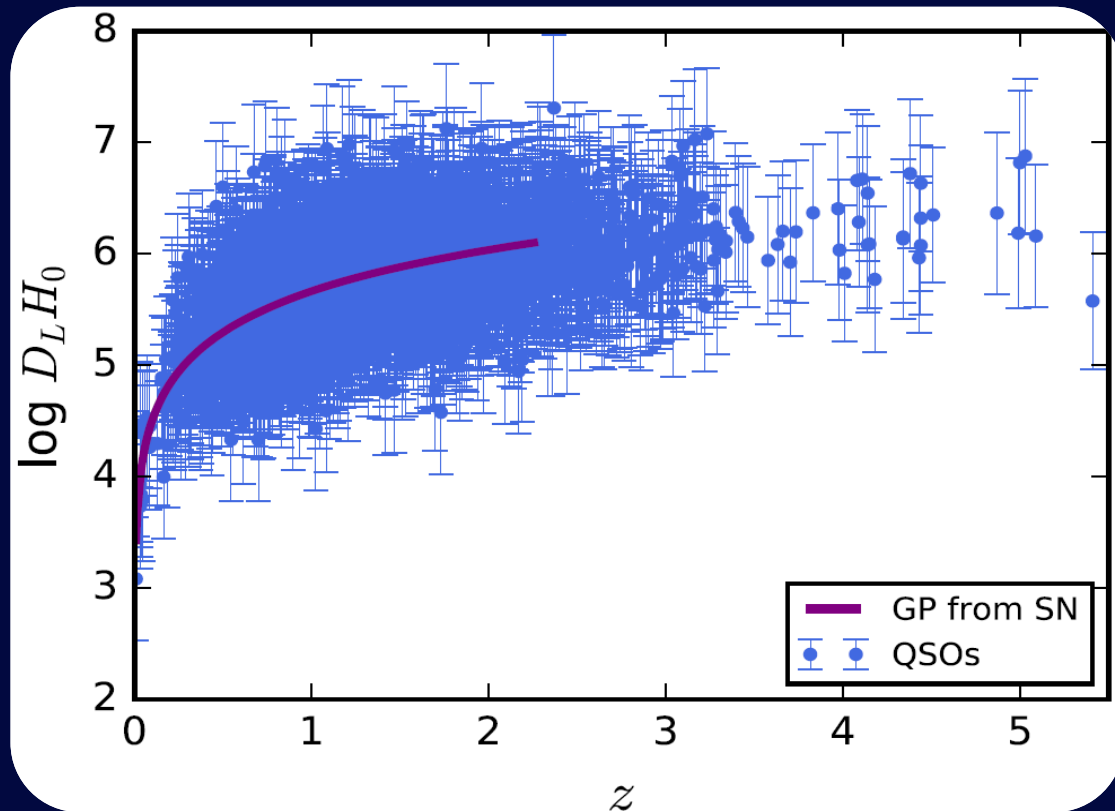
β

δ

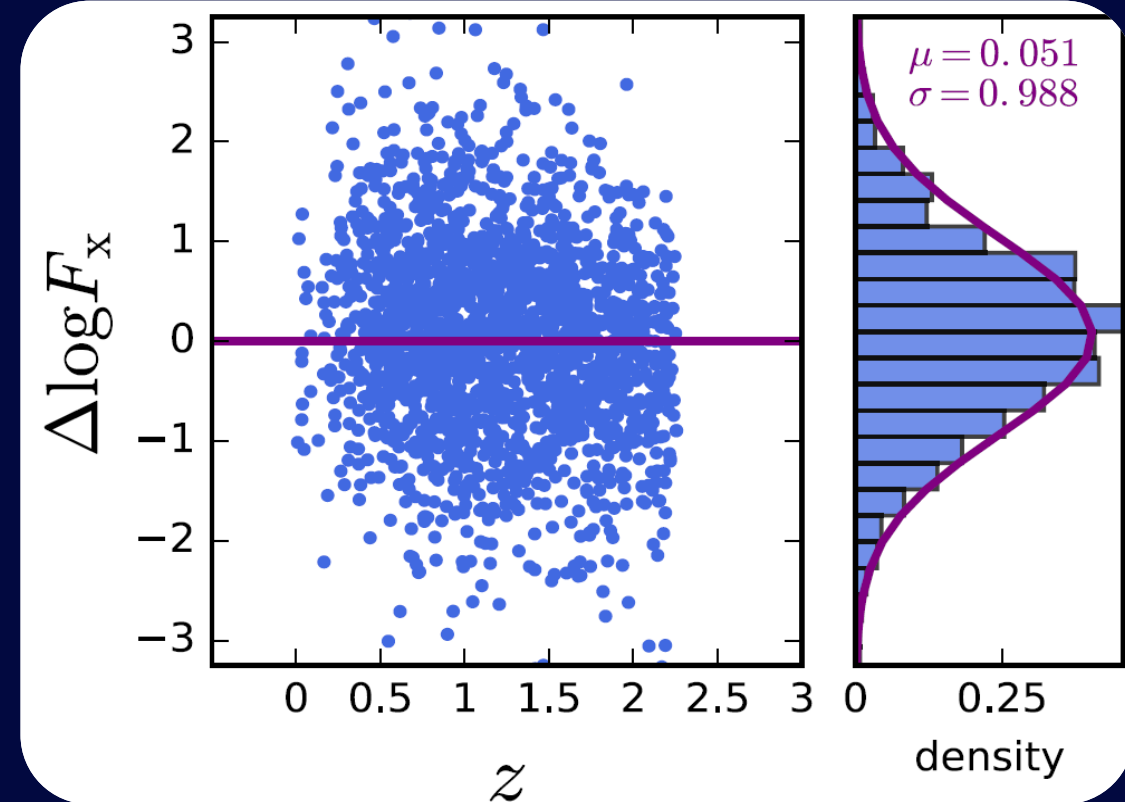


Model independent calibration results for the quasar parameters. GP regression reconstructions of $D_L H_0$ based on the Pantheon SN Ia compilation were used. The contours represent the 1 σ , 2 σ , and 3 σ uncertainties for γ , β , and δ .

Results:

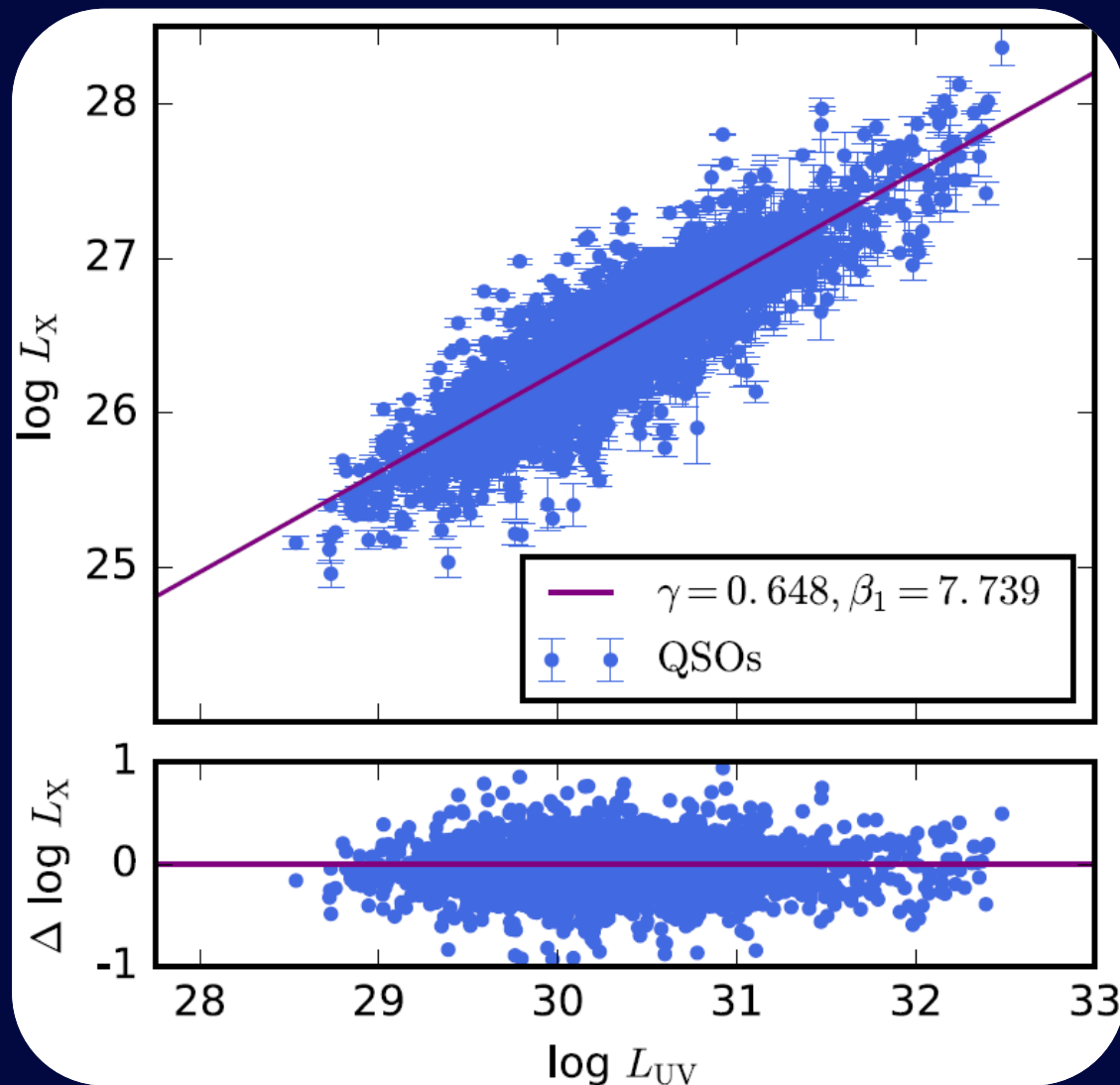


$\log(D_L H_0)$ -redshift relation for the 2421 calibrated quasars. The error bars of $\log(D_L H_0)$ are obtained through error propagation and the purple solid line shows $\log(D_L H_0)$ drawn from the posterior of the Pantheon compilation calculated with GP.



Residuals of the observed $\log(F_X)$ values with respect to the predicted $\log(F_X)$ values derived from the GP reconstructions of the Pantheon SN Ia compilation, normalized to the calibrated errors. The right plot shows the histogram for $\log(F_X)$ and the purple line shows the best Gaussian fit with $\mu = -0.051$ and $\sigma = 0.988$.

Results:



The linear relation between $\log(L_{UV})$ and $\log(L_X)$ for the 2421 quasar sample we used. The purple solid line presents the best fit from our calibration results with slope $\gamma = 0.648$. The lower panel shows the residual of $\log(L_X)$ with respect to the best fitting results.