## Assignment No. 3

**Network Robustness** 

#### **Network:**

• Twitter Social Circles

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#### Course:

Network Analysis

#### The course is part of the below degree:

• Computer Science - Software & Security Engineering

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#### Introduction

This assignment consisted of three steps.

- 1. The first step involved investigating the impact of various attack strategies on two well-known graph models: the *Erdós-Rényi* model and the *Barabási-Albert* model. These models, previously introduced in coursework, were readily available through the *NetworkX* library. Four distinct attack methods were employed: random node attack, highest degree node attack, highest PageRank node attack, and highest betweenness node attack.
- 2. The second step focused on the significantly larger network previously utilized in Assignments 1 and 2 and attacking the mentioned methods on the network.
- 3. By Leveraging the results obtained in step 2, we further investigated the attack method that exhibited the most significant influence on network robustness in step 3. Finally, efforts were directed towards enhancing the overall robustness of the network.

The code consists of two files:

- **helper.py**: Which is used for developing the helper functions which are needed through this assignment.
- network\_robustness.ipynb: This file is used to work on the assignment itself.

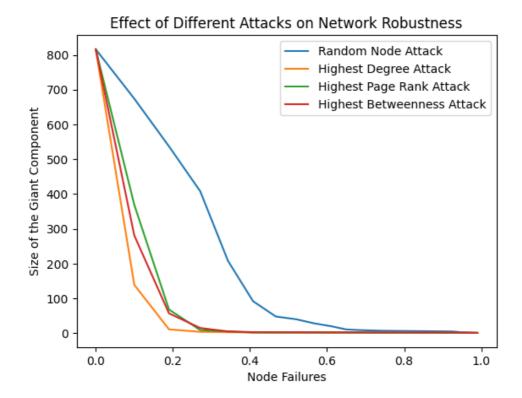
## Step 1: Attack on two famous random graphs

The four attack methods are declared in the helper.py file and they are used in "perform\_attacks" function which is declared in .ipynb file, and this function is written to handle the logic of step 1 and the visualization of attacking process effect on the graph.

## First graph: Erdos-Renyi graph

This random graph is generated using 1000 nodes and 0.002 probability of edge creation.

Our analysis revealed that the "Highest Degree Node" attack strategy had the most significant impact on the network's robustness by disrupting its giant component. This finding suggests a heightened vulnerability within the network structure. Specifically, the presence of highly connected nodes ("hubs") occupying central positions appears to be a critical factor. The removal of these hubs during the attack process resulted in a fragmentation of the giant component. Furthermore, the removal of a single high degree node can trigger a cascading effect, where the disconnected neighbors, who might themselves be crucial connections for other nodes, are subsequently isolated, leading to further fragmentation.



#### Second graph: Barabási-Albert graph

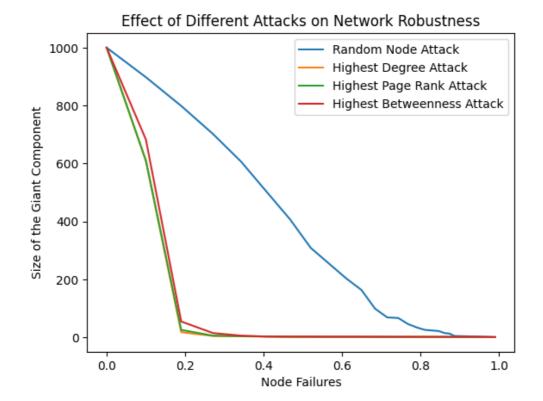
This random graph is generated using 1000 nodes and 2, as the number of edges to attach from a new node to existing nodes.

By initial analyzing of this graph, it is achievable that all the three attack methods have made the same effect on the network. As this type of graph is scale-free, meaning that it has small number of nodes have a very high number of edges while most nodes have relatively few connections. Because of this specification of the graph, we have some hubs that are acting as bridges between different parts of the network. But why these three attack methods still have shown almost the same behavior?

All the three attack methods tend to target the same nodes, which are the hubs. In the below section, it is written how each attacking method made an effect on the graph:

- Highest Degree Attack: This attack directly removes nodes with the highest number of connections, which can rapidly and easily break the network and its giant component into smaller parts.
- Highest PageRank Attack: As it was mentioned in the course, this is a centrality
  measure (which initially introduced by Google), considers both the number and
  quality of node's edges. In Barabási-Albert graph, hubs naturally have high
  PageRank due to their extensive connections with other nodes. So, this attack
  also targets hubs, just like the Highest Degree Attack.
- **Highest Betweenness Attack:** This centrality feature measures a node's importance in bridging paths between other nodes. In this graph, the hubs are

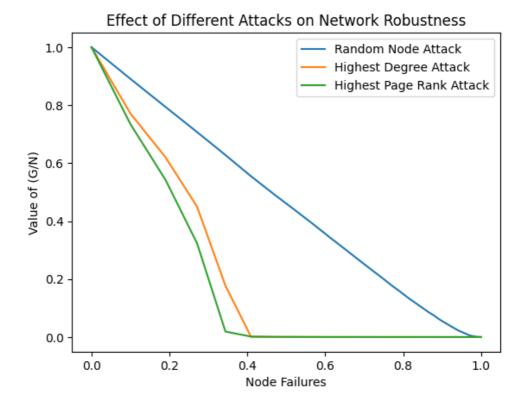
often lie on the shortest paths between many other nodes. So, this attack also tends to target hubs.



Just as the first graph (Erdos-Renyi), this attacks on the Barabási-Albert also might have cascading effect that whenever a hub is removed, it might affect other connected nodes and make them also isolated components that will be ignored in the second attack (if the giant component is considered in the attack algorithm).

## Step 2: Attack on the network of Twitter's Circles

This stage of the analysis excluded the highest betweenness centrality attack due to its computational demands associated with betweenness calculations. Consequently, only three alternative attack scenarios were simulated on the network. As previously observed, the random node attack exhibited the minimal disruptive impact on network robustness compared to attacks targeting nodes with the highest degree centrality and PageRank centrality.



As random node attack has the least impact, it suggests the network has some level of robustness. Even if random users are removed, the core functionality might not be significantly affected. The consideration of alternative attack scenarios targeting nodes with high degree centrality and PageRank centrality suggests the presence of critical nodes within the Twitter Circles network. Nodes exhibiting high degree centrality likely possess a significant number of connections to other users, functioning as hubs within the information flow. Conversely, nodes with high PageRank centrality, while potentially possessing fewer connections, exert a strong influence due to the prominence of users connecting to them. Targeted attacks on these critical nodes would demonstrably disrupt network functionality to a greater extent compared to attacks on randomly chosen nodes.

# Step 3: Building robustness on the network of Twitter's Circles

In the final step, as we understood that the highest PageRank attack is the most effective one on the disruption of the network, we will work on this area to make the network more robust against this type of attack.

### Algorithm

This algorithm designed to improve the resilience of complex networks by strategically connecting highly influential nodes. The core principle lies in leveraging the PageRank

metric to identify critical nodes within the network and subsequently augmenting their connectivity. This approach aims to bolster the network's robustness against potential disruptions, such as highest PageRank targeted attack, which had the most influence on the network robustness.

The algorithm commences by calculating the PageRank score for each node within the network. Subsequently, these scores are compiled and arranged in descending order, effectively forming a ranked list that prioritizes nodes based on their influence. The average degree of the network is then computed, which serves as a parameter for the critical threshold calculation (denoted as  $f_{\rm c}$ ).

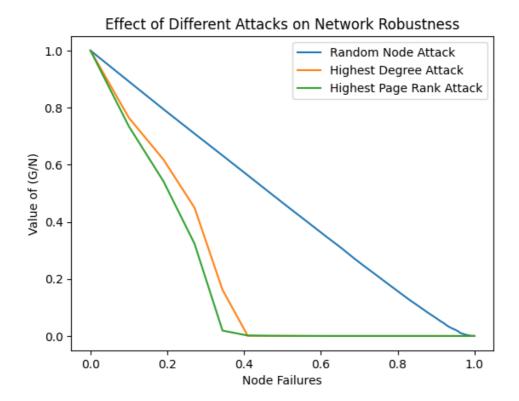
The **critical threshold**, a pre-defined value representing the network's susceptibility to disruptions before the robustness enhancement (**0.9706** in this instance), serves as a benchmark for evaluating the effectiveness of the algorithm.

Following the identification of critical nodes based on the top 'f' fraction of the ranked PageRank list (f = 0.1 in this specific case), the algorithm establishes connections between these influential nodes and a maximum of five non-connected nodes within the network. This targeted edge creation aims to strategically increase the connectivity of these critical nodes, potentially enhancing the network's overall robustness. However, the selection of five connections remains a limitation of the current implementation, as it relies on a pre-determined value rather than a dynamically determined threshold based on network properties. Future iterations of the algorithm should incorporate a more data-driven approach for selecting the optimal number of connections.

The **critical threshold** is then recalculated after implementing the network modifications (**0.9714**).

Finally, the algorithm returns the modified network structure, enabling visualization of the changes. However, the minimal improvement observed in this specific case highlights the need for further refinement to ensure a more visually discernible enhancement in network robustness.

The visualization is illustrated in the below section:



## Conclusion

This assignment provided valuable insights into the impact of diverse network attacks, encompassing both random and targeted variants, on network structures. The observations demonstrate a strong correlation between network vulnerability and its underlying architecture. Furthermore, the assignment explored mitigation strategies, equipping us with methodologies to enhance network robustness against specific attack types that demonstrably inflict significant disruption.