

Name : Km Parshvi Sahu

Uni. Rollno : 1918035

Sec : D4

DAA  
Tutorial 1

Ans1:- → Asymptotic notation are used to tell the complexity of an algorithm when the I/p is very large.

→ Asymptotic Notation are language to express the required time & space by an algorithm to solve a given problem or It is a function to describe the performance of an algorithm

<u>Eg.</u> Time Complexity ( $n^2$ )	Space Complexity
approx. no. of instructions	( $n$ ) extra space that an algorithm takes except input

Ans2:- for ( $i=1$  to  $n$ )  
{  
     $i = i * 2$ ;  
}

1, 2, 4, . . . . n

$a = 1, r = 2$

$$t_k = ar^{k-1} = 1 \cdot 2^{k-1} \rightarrow n = \frac{2^k}{2}$$

$$2^k = 2n \rightarrow k = \log_2(2n)$$

$$k = \log_2(2n) + 1$$

$$\text{Time Complexity} = \log_2(n)$$

Ans3:-  $T(n) = \{ 3T(n-1) \text{ if } n > 0; \text{ otherwise } 1 \}$   
using substitution method

$$\begin{aligned} T(n) &= 3T(n-1) \\ &= 3(3T(n-2)) \\ &= 3^2 T(n-2) \\ &= 3^3 T(n-3) \\ &\vdots \end{aligned}$$

$$\begin{aligned}
 &= 3^n + (n-n) \\
 &= 3^n + T(0) \\
 &= 3^n
 \end{aligned}$$

$$T.C. = O(3^n)$$

Ans 4:-  $T(n) = \{ 2T(n-1) - 1 \text{ if } n > 0, 0 \text{ otherwise} \}$   
Using substitution method:-

$$\begin{aligned}
 T(n) &= 2T(n-1) - 1 \\
 &= 2T(2T(n-1-1) - 1) - 1 \\
 &= 2^2(T(n-2)) - 2 - 1 \\
 &= 2^2(2T(n-3) - 1) - 2 - 1 \\
 &= 2^3T(n-3) - 2^2 - 2^1 - 2^0 \\
 &\dots \\
 &= 2^n \cdot T(n-n) - 2^{n-1} - 2^{n-2} - 2^{n-3} \dots - 2^0 \\
 &= 2^n - (2^n - 1) \\
 &= 1
 \end{aligned}$$

$$T.C. = O(1)$$

Ans 5:-

```

int i = 1, s = 1;
while (s <= n) {
    i++;
    s = s + i;
    printf("%d\n", i);
}
    
```

We can define the term 's' a/c to relation  $s_i = s_{i-1} + i$ .  
The value of 'i' increases by one for each iteration. The

value contained in 's' at the  $i^{th}$  relation is the sum of the  $i^{th}$  first 'i' the integers. If K is total no. of iterations taken by the program then while



loop terminates if: -

$$1+2+3+\dots K = \frac{K(K+1)}{2} > n$$

$$K = O(\sqrt{n})$$

$$T.C = \underline{O(\sqrt{n})}$$

Ans6:

```
void function(int n) {
    int i, count = 0;
    for(i=1, i*i <= n; i++)
        count++;
}
```

loop ends if  $i^2 > n$   
 $\Rightarrow T(n) = O(\sqrt{n})$

Ans7:

```
void function(int n) {
    int i, j, k, count = 0;
    for(i=n/2; i <= n; i++) ... n
        for(j=1; j <= n; j=j*2)
            for(k=1; k <= n; k=k*2) ] execute log n
                                    time
        count++;
}
```

Time Complexity =  $O(n \log^2 n)$

Ans8:

```
void function(int n)
{
    if(n==1) return; → constant time
    for(i=1 to n) { → n times
        for(j=1 to n) { → n times
            printf("%*"),
        }
    }
    function(n-3);
}
```

Page: \_\_\_\_\_  
Date: \_\_\_\_\_

Recurrence sol<sup>n</sup>:  $T(n) = T(n-3) + n^2$   
 $\Rightarrow T(n) = O(n^3)$

Ans 3:- Void function (int n) {  
 for (i=1 to n) {  $\rightarrow$  This loop execute n times  
 for (j=1; j<=n; j=j+i)  $\rightarrow$  This execute j-  
 printf ("\*"); times with i increase  
 } by the value of i  
 }  
 }

$\Rightarrow$  Inner loop executes  $n/i$  times for each value of i  
 Its running times is  $n \times \left( \sum_{i=1}^n n/i \right)$   
 $= O(n \log n)$

Ans 4:- The asymptotic relationship b/w the functions  $n^k$  and  $a^n$  is  
 $n^k = O(a^n)$   $k \geq 1, a > 1$   
 $n^k \leq c \cdot a^n \quad \forall n \geq n_0$   
 $\Rightarrow \frac{n^k}{a^n} \leq c$