

Topics:

- Introduction
- Types of Learning
- Features
- Training - Testing - Validation set
- Bias and Variance
- Underfitting & Overfitting
- Measuring performance
- Matrices Estimation

Day 1:

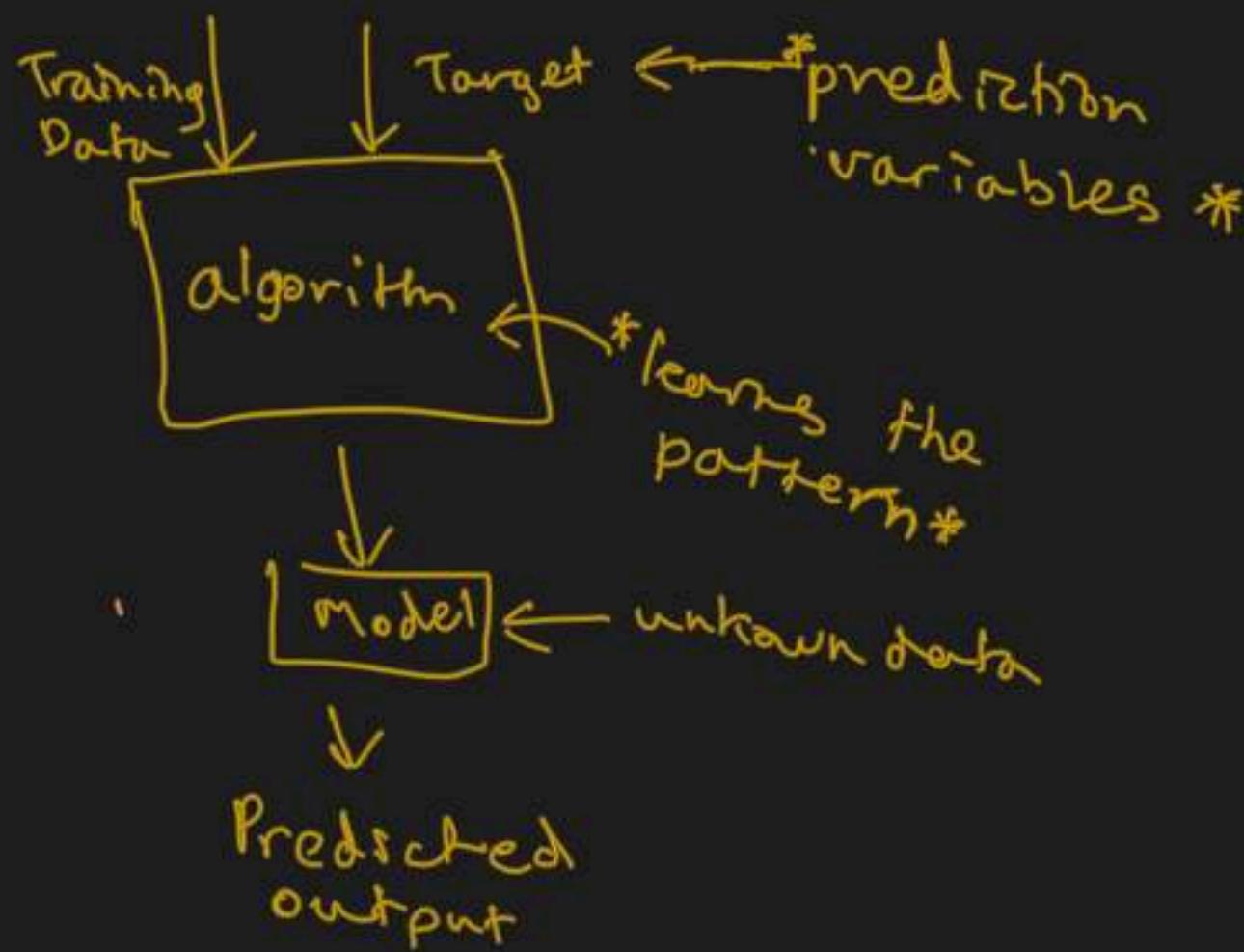
AI = ability to guess. A set of technologies
that allows computers to perform functions that
mimic human intelligence.

many subsets
like: ML, DL, RL,
genetic algorithms

Computer Program:



AI Model: (*=notes)



What is Learning?

A computer program is said to learn from experience (E) with respect to tasks (T) and measure performance (P)

If its performance at task (T) as measured by performance (P) improves with the experience (E).

(TEP model of Learning)

What is a Model?

A model is the output of the learning process.

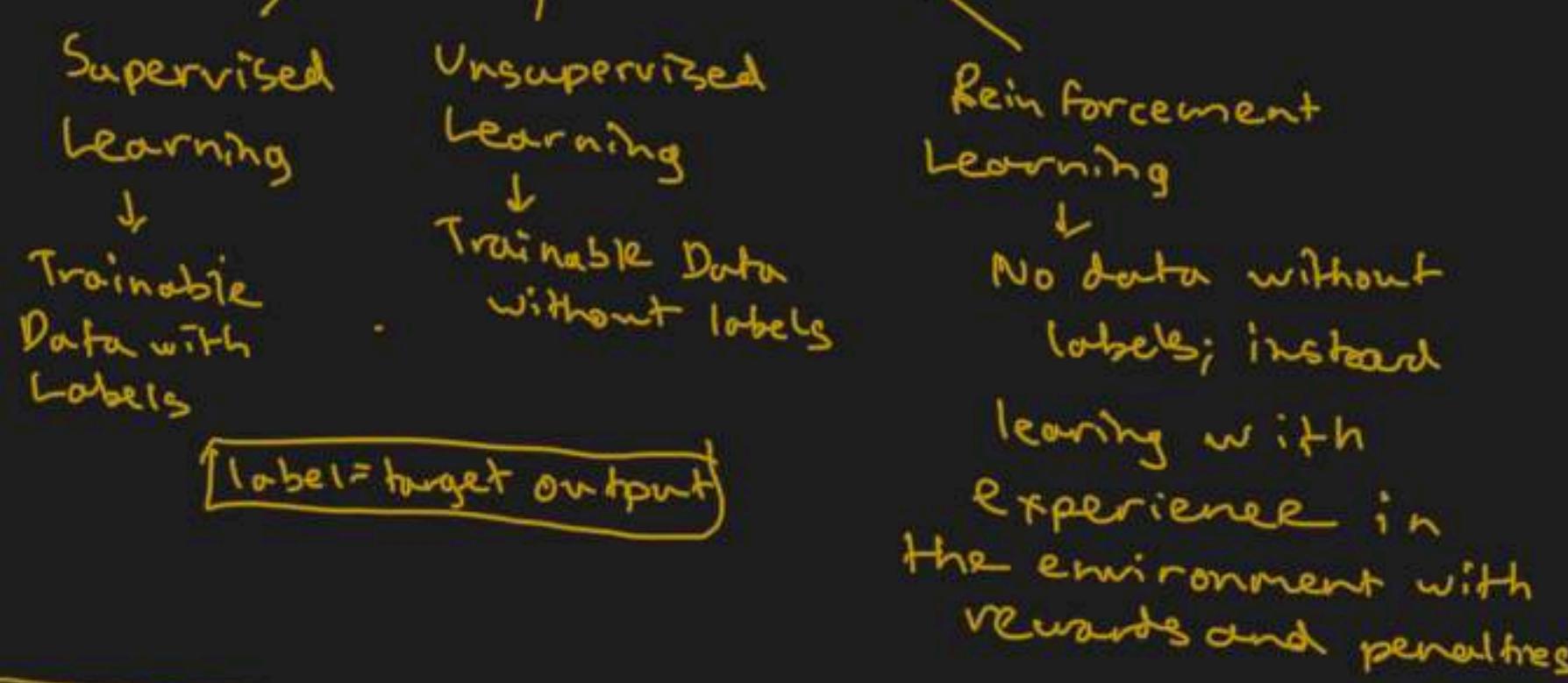
It is also a mathematical representation of the relationship within the data.

What is a Learning Algorithm?

It is a method/procedure to train a model from data.

In simple words: Learning Algorithm builds the model and that model is used to predict unknown data.

Types of Learning:



Features

Features, are the individual measurable properties or characteristic of the data used as an input to the model.

	Training				Output
	c ₁	c ₂	c ₃	c ₄	
v ₁	1	2	3	4	
v ₂	1	6	7	8	
v ₃	10	9	7	6	

features

Types of Features

1. Categorical features: Represents category/group
Ex. Blood group, Spam classification, multi-class classification.
2. Ordinal features: Represents category without intervals (thresholds) in ranked based.
Ex. Good, bad, large, medium, small
3. Numerical features: Represents number
Ex. height, weight, temperature
4. Boolean Features: True/False

Splitting data into training, testing and validation sets

- Training set: The data used to train and teach about pattern to the model
 - The training data should not be imbalanced that is the data should not contain only one type of value, it should be the combination of all types of values.
- Validation set: Testing during training is known as validation
 - The validation set helps fine-tune the model after each epoch (iteration)
- Testing set: Set of data, used to test the model after completing training.
 - Provides a final model performance in terms of accuracy and precision

Training data > validation data

Training data > testing data

Normally # testing data = # validation data

Ex. T: 60% V: 20%, Te: 20%

Features	Out
~60% Train	
20% validation	
20% test	

Similar objects sometimes not there
thus test being 40%.

Types of learning (detailed)

Supervised learning: data with labels. This means that, each training example consists of input-output pairs, where the input is the data that we need to be analyzed and the output is the corresponding label or target value you want to predict.

- 2 types of learning tasks:

- Regression: Type of predictive modeling technique used to predict continuous values. (There can be an infinite amount of numerical values between 0 and 1.)
The main objective is to establish a relationship between independent variables (features) and a dependent variable (target), to predict a future value. E.g. Linear regression.
- Classification: A task where model predicts the discrete labels (variables) or categories for given input data.
The goal is to assign each input sample to one of several pre-defined classes based on its feature.
E.g. Logistic regression.

Bias and Variance

- Bias

Bias is the difference between the actual value and the predicted value.

High bias can not capture the important features of the data.

- Variance

This can be described as the model sensitivity to fluctuations in the data. More specifically, variance

is the variability of the model, that is how much it can adjust to the new subset of the training data.

Variance should be minimum and closer to average set for some class of data.

Variance should be more for different class of data.

High variance is the signal to change the algorithm.

$$\text{Variance representation} = E[(\hat{Y} - E(\hat{Y}))^2]$$

$E(\hat{Y})$ = Expectation/mean of the predicted value

\hat{Y} = predicted value of the target variable

Over fitting & Under Fitting

over fitting: when model is over trained and tries to learn the details and noise in the training data resulting in high error rates

is known as over fitting.

- Noise here is outliers or irrelevant/meaningless data, missing values,
- Low bias & High variance
- Low training error & High testing error
- Can also arise due to class imbalance

Under fitting: Our model is too simple and has very few variables on data points that it considers each of them as a separate class, which results into high bias, and low variance.

- High training error & high testing error

a = actual value

b = predicted value

$$\text{bias} = b - a$$

$$\{\gamma - \gamma\}$$

Measuring Performance

↓ [performance metrics]

Sum² error (also known as residual sum of square error)

$$SSE = \sum_{i=0}^n e_i = \sum_{i=0}^n (y - \hat{y})^2$$

Ex.

i=0	x	y	\hat{y}	$(y - \hat{y})^2$
0	1	2	1	1
1	3	1	4	9
2	2	0	4	16
3	5	4	1	9
4	7	6	1	25

Math ex. 1+2+3+4+5

$$\sum(5) = \frac{5(5+1)}{2}$$

→ 15

Mean Absolute error

MAE represents the average of the absolute difference between the actual and predicted value, and it is shown as:

$$MAE = \frac{1}{N} \sum_{i=1}^N |y - \hat{y}| \quad \left\{ \begin{array}{l} N = \# \text{ of data points} \\ \frac{1}{N} = \text{mean} \end{array} \right.$$

x	y	\hat{y}	$ y - \hat{y} $
0	1	2	1
1	3	1	2
2	2	0	2
3	5	4	1
4	7	6	1

*Unlike MSE, it measures the average of the residuals

$$\sum = 7 \rightarrow \frac{7}{5} = 1.4$$

Each data is having an average error of 1.4

* SSE limitation: only measures the variability of the data and doesn't provide information about the goodness of the fit of the model, doesn't generalize model well
 SSE always provides a non-negative value which turns rewards into penalties ~prone to under-fitting

Mean² Err.

Mean² Error

MSE represents the average of the squared diff. between the original and predicted values.

* Measures the variance of the residuals.

$$MSE = \frac{1}{N} \sum_{i=0}^N (y - \hat{y})^2$$

\hat{y} diff.
gotten

x	y	\hat{y}	$(y - \hat{y})^2$
0	1	2	1
1	3	1	4
2	2	0	4
3	5	4	1
4	7	6	1

$$\sum = 11 \rightarrow \frac{11}{5} = 2.2$$

* lower the error , the more accuracy,

Always: $MAE \leq RMSE \leq MSE \leq SSE$

Root mean² error

$RMSE = \sqrt{\frac{1}{N} \sum_{i=0}^N (y - \hat{y})^2}$ indicates how close the predicted value are to the actual value

$$RMSE \approx \sqrt{\frac{1}{N} \sum_{i=0}^N (y - \hat{y})^2}$$

$$\sqrt{2.2} \approx 1.48$$

From MSE ex.

* shows closeness to the actual value.

Hw: Understand - Matrix inverse, and how to find it

- Transpose

- Matrix multiplication

- Variance & co-variance
↳ STD

- x and \hat{y}

→

x	y	\hat{y}	Calculate all errors
10	1	2	
20	3	1	
30	2	0	
40	5	4	
50	7	6	
60	8	5	
70	8	7	

x	y	\hat{y}	calculate all errors
10	1	2	-1
20	3	1	2
30	2	0	2
40	5	4	-1
50	7	6	-1
60	8	5	3
70	8	7	1

$$SSE = 1 + 4 + 4 + 1 + 1 + 9 + 1 = \underline{\underline{21}}$$

$$MAE = 1 + 2 + 2 + 1 + 1 + 3 + 1 = \frac{11}{7} \approx \underline{\underline{1.57}}$$

$$MSE = \frac{21}{7} \rightarrow \frac{21}{7} = \underline{\underline{3}}$$

$$RMSE = \sqrt{3} \approx \underline{\underline{1.73}}$$

Matrices

Inverse $\begin{bmatrix} a & b \\ c & d \end{bmatrix}$

$$\hookrightarrow \frac{1}{ad-bc} \begin{bmatrix} \dots \end{bmatrix}^{-1} \rightarrow \begin{bmatrix} a & b \\ c & d \end{bmatrix}^{-1} = \begin{bmatrix} d & -b \\ -c & a \end{bmatrix}$$

Ex. $\begin{bmatrix} ? & ? \\ ? & ? \end{bmatrix}$

$$\hookrightarrow \frac{1}{7-9} = -\frac{1}{2}$$

$$\hookrightarrow -\frac{1}{2} \begin{bmatrix} 1 & -9 \\ -1 & 7 \end{bmatrix}$$

$$\hookrightarrow \begin{bmatrix} -\frac{1}{2} & \frac{9}{2} \\ \frac{1}{2} & -\frac{7}{2} \end{bmatrix}$$

Transpose: $\begin{bmatrix} a & b & c \\ d & e & f \end{bmatrix} \rightarrow \begin{bmatrix} a & d \\ b & e \\ c & f \end{bmatrix}$

Multiplication:

$$A = \begin{bmatrix} 3 & 1 & 4 \end{bmatrix} \quad B = \begin{bmatrix} 4 & 3 \\ 2 & 5 \\ 6 & 8 \end{bmatrix}$$

$AB?$

$(1 \times 3) \leftarrow$ have to be equal $\rightarrow (3 \times 2)$
 result will be (1×2)

$$3(4) + 1(2) + 4(6) \leftarrow * A by first col of B \\ = 38 \\ 9 + 5 + 32 = \leftarrow \text{second col} \\ 46$$

Result: $[38 \ 46]$

* Multiply all rows by each column one by one:

1st row $\begin{bmatrix} 1 & 2 & 3 \end{bmatrix}$
 2nd $\begin{bmatrix} 1 & 2 & 3 \end{bmatrix}$
 3rd $\begin{bmatrix} 1 & 2 & 3 \end{bmatrix}$

cols of A (sums)

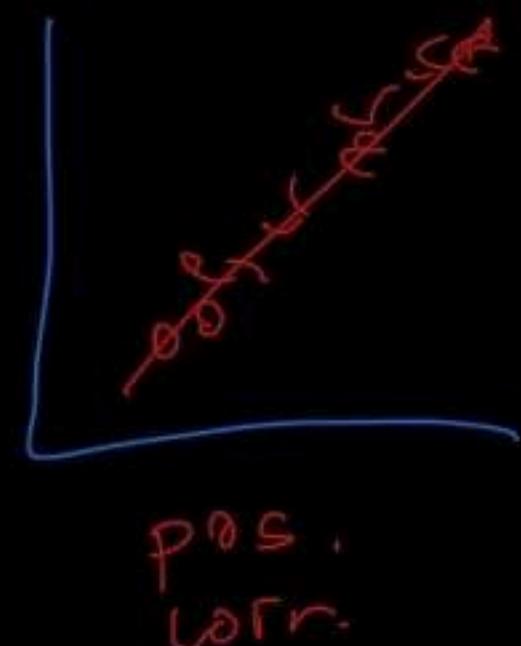
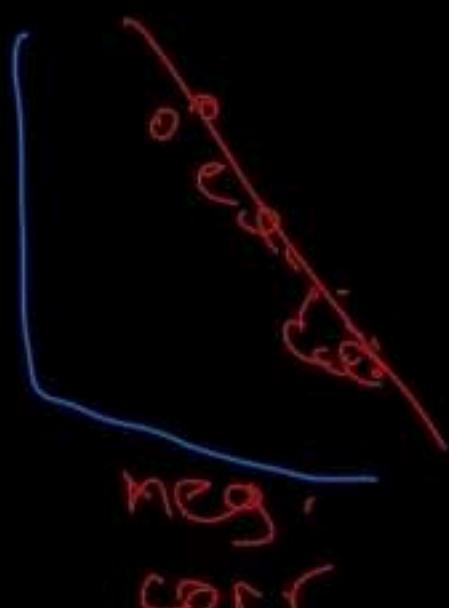
Co-variance: how related variables X and Y are related

$$\text{Co-var} = \frac{\sum (x - \text{mean } x) * (y - \text{mean } y)}{N - 1}$$

positive = both var's change in same dir.

inverse = opp. dir
no relation:

corr coefficient
 \rightarrow (same thing but between -1 and 1)



STD: How spread out the values are

1. Find mean of values

2. Find diffs from mean (value-mean)

3. Find all deviation²

4. Sum of Squares Σ

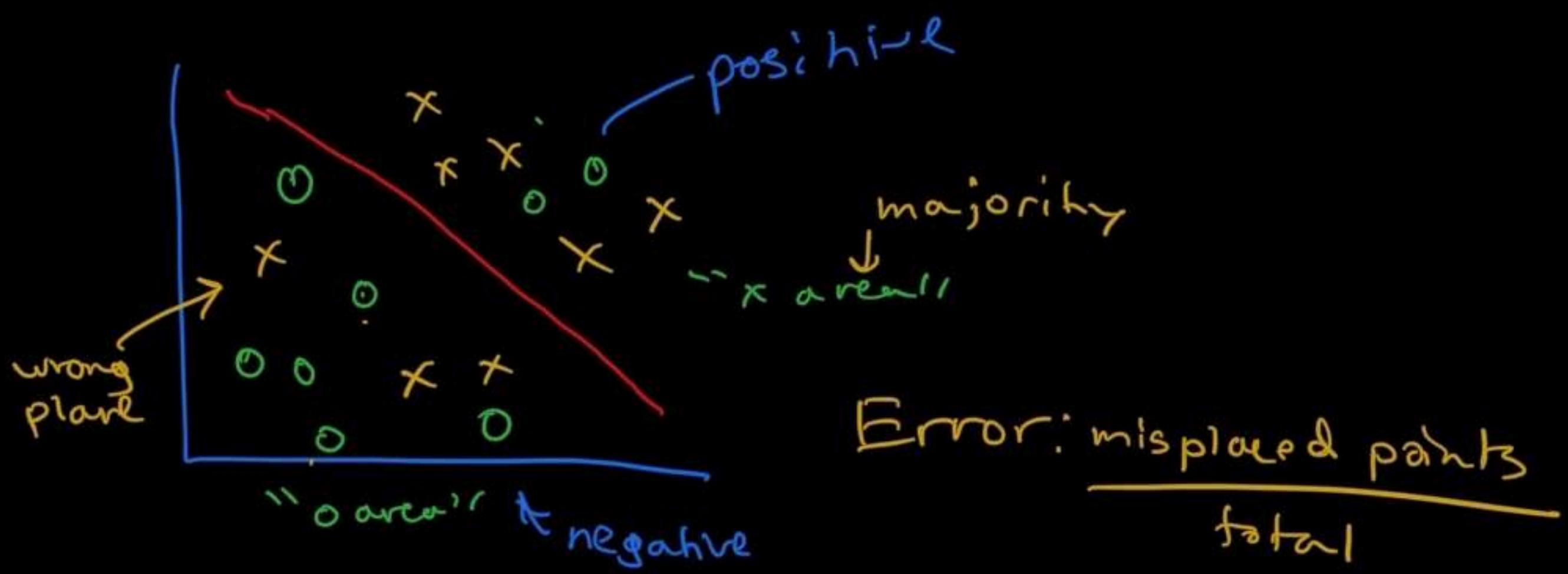
5. $\frac{\text{sum}}{n-1}$] variance
 \uparrow sample size (n)

6. $\sqrt{\text{variance}}$

deviation
how to find variance
 $\text{Var} = \frac{\sum y^2}{n}$

Classification Performance

Evaluation



Error: $\frac{\text{misplaced points}}{\text{total}}$

$$= \frac{4}{16}$$

$$\text{ACC} = \frac{\text{correctly classified points}}{\text{total}} = \frac{11}{16}$$

$$\text{Error} = 1 - \text{ACC}$$

Pos = Plane #1(x):

True Pos = 5

False Pos = 2

Neg \Rightarrow Plane #2(o):

True neg: 6

False neg: 3

True Positive = proportion of all actual positive that are correctly classified

False Positive = proportion of all actual negative that are incorrectly classified as positive

True Negative = proportion of all actual neg. that are correctly classified

False Neg = proportion of all actual pos. that are incorrectly classified as neg.

Confusion Matrix: a table used to evaluate the performance of a classification model

	Actual pos.	Actual neg.	
Pred. Pos.	TP	FP	
Pred. Neg.	FN	TN	

Truthness

Ex.

5	2
3	6

Precision =

$$\frac{TP}{TP + FP}$$

the proportion of all the model's pos. classification that are actually pos. to everything classified as pos.

Recall = true pos. rate =
ratio between true pos rate to all pos. samples

$$\frac{TP}{TP + FN}$$

* The dimension of the confusion matrix can change as per the number of classes defined