

## REPORT

### 1. Theory:

- a. Linearization: It is achieved by differentiating (Jacobian) around the equilibrium points since nonlinear systems act like linear systems near the equilibrium points.
- b. State Feedback Control: SFC relies on current states to decide the input to the system. It can be achieved by:
  - i.  $U = -Kx$

### 2. Step Results:

- a.  $\begin{bmatrix} 0 & \pi & 0 \\ 0 & 0 & 0 \\ 0 & 0 & \pi \\ 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} \pi \\ 0 \\ \pi \\ 0 \end{bmatrix} \rightarrow \text{This eqn. pos.}^n \text{ was not provided by MATLAB}$
- b.  $\text{linear\_A} = 4 \times 4$ 

0	1.0000	0	0
12.5769	0	-11.9611	0
0	0	0	1.0000
-16.9227	0	46.1565	0

  
 $\text{linear\_B} = 4 \times 2$ 

0	0
1.7250	-4.4345
0	0
-4.4345	14.8902
- c. System is unstable
- d.  $C = 4 \times 8$ 

0	0	1.7250	-4.4345	0	0	74.7378	-233.8759
1.7250	-4.4345	0	0	74.7378	-233.8759	0	0
0	0	-4.4345	14.8902	0	0	-233.8759	762.3251
-4.4345	14.8902	0	0	-233.8759	762.3251	0	0

System is controllable
- e.  $\text{poles} = 1 \times 4 \text{ complex}$ 

-1.0000 + 0.0000i -2.0000 + 0.0000i -1.0000 - 1.0000i -1.0000 + 1.0000i

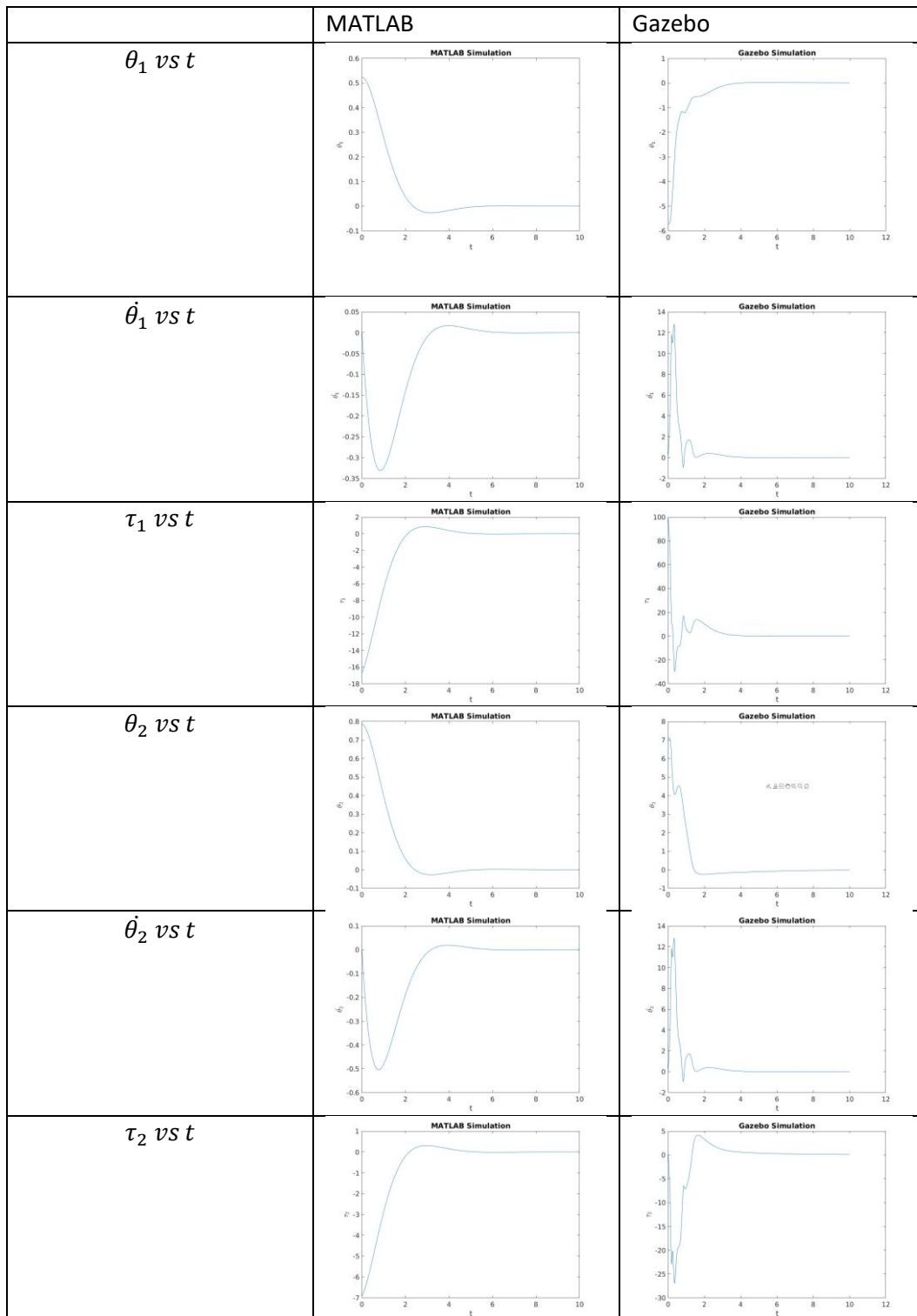
$K = 2 \times 4$

23.9371	6.4042	5.2636	0.1559
6.0097	1.8868	4.7955	0.2022

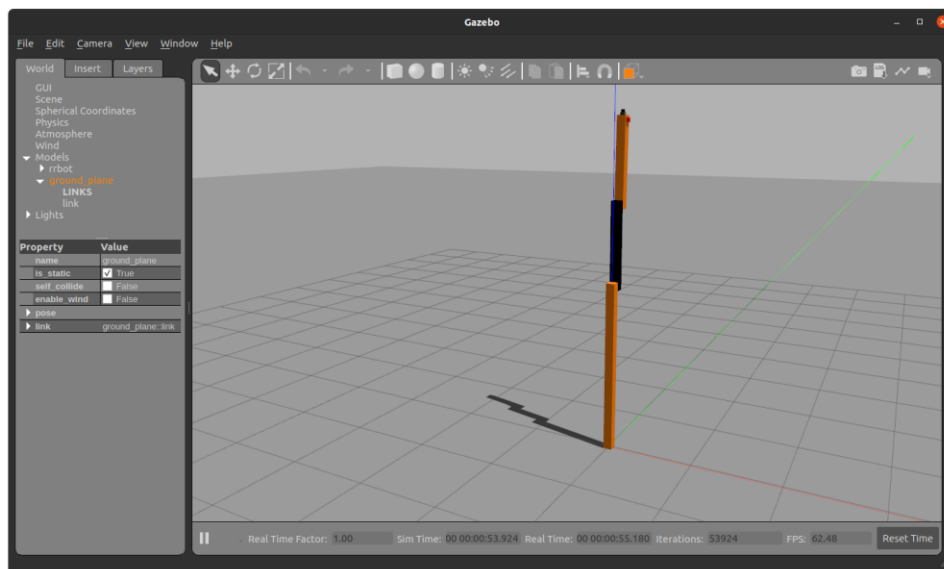
$A_{\text{SF}} = 4 \times 4$

0	1.0000	0	0
-2.0655	-2.6804	0.2250	0.6277
0	0	0	1.0000
-0.2582	0.3049	-1.9085	-2.3196

### 3. Trajectory Plots



4. From Gazebo results I found that due to absence of friction, the torque on motor is significantly different and much smoother in MATLAB simulations than Gazebo Simulation.



5.