

* Signed and Unsigned Numbers:

An n bit signed binary number consists of two parts:

- (1) Denoting the sign of the number and
- (2) Denoting the magnitude of the number.

The MSB is always a sign bit.

0, 1
↓
denotes '+', '-'

smallest eight-bit number 0000 0000

largest eight bit number 1111 1111

Range: 0 to 255

Binary Number

The 1st complement: +ve are same but we need to define the negative number in system

Unsigned number 000 1 1 0 1 1 0 All -ve no.s have the
1s complement 1 0 1 1 0 0 1 0 0 1 Binary MSB = 1

Complement of Number = -ve numbers convert as +ve

-ve Binary Numbers - The 2s complement: (for -ve Binary no.)
do not put 1 in MSB of a Binary number to make it negative.

We must take the 2s complement of the number.
Taking the 2s complement of the number will cause the MSB to become 1.

Unsigned Number 0 0 1 1 0 1 1 0

1s complement 1 1 0 0 1 0 0 1

2s complement + 1

1 1 0 0 1 0 1 0

If we are using signed Binary numbers and MSB is already logic 1, it means the value is the 2s complement of the number.

Representation of signed numbers Using 2s complement

$+(12)_{10}$ in 2s complement form.

Binary number	1	1	0	0	
1s complement	0	0	1	1	
2s complement	0	1	0	0	
With sign bit	0	0	1	0	0

+

$-(10)_{10}$ in 2s complement form.

Binary Number	1	0	0	1	0
1s complement	0	1	1	0	1
2s complement	1	0	0	0	1
with sign bit	1	1	0	0	0

* Addition- subtraction of Signed Numbers Using 2s complement Addition:

Ex' Add $(27)_{10}$ and $(-11)_{10}$ using complementary representation for the -ve value.

$$(27)_{10} = (011011)_2$$

$$(11)_{10} = (001011)_2$$

Get the 2s complement of $(001011)_2 = \overline{001011}$

$$1s \text{ com. } 110100$$

$$1s \text{ com. } 110100$$

$$+ 1$$

$$\text{for } 2s \text{ } + 1$$

$$2s \text{ comple. } 110101$$

$$110101$$

$$(27)_{10} \quad \begin{array}{r} 0 \ 1 \ 1 \ 0 \ 1 \ 1 \\ + \ 1 \ 1 \ 0 \ 1 \ 0 \ 1 \\ \hline 1 \ 0 \ 1 \ 0 \ 0 \ 0 \end{array}$$

$$2s \text{ com. } + 1 \ 1 \ 0 \ 1 \ 0 \ 1$$

$$\boxed{1} \ 0 \ 1 \ 0 \ 0 \ 0 \ 0$$

IF 1 carry occur in solution ignore it from the result to obtain correct solution."

Note: Here, carry 1 is ignored and solution is $(010000)_2$

Ex' Subtract $(25)_{10}$ From $(42)_{10}$

$$(25)_{10} = (011001)_2$$

$$(42)_{10} = (101010)_2$$

42

-25

x17

Get the 2s complement of $(011001)_2 = \overline{011001}$

$$1s \text{ comp. } 100110$$

$$1s \text{ comp. } 100110$$

$$+ 1$$

$$\text{for } 2s \text{ } + 1$$

$$2s \text{ comp. } 100111$$

$$100111$$

$$(42)_{10} \quad \begin{array}{r} 1 \ 0 \ 1 \ 0 \ 1 \ 0 \\ + \ 1 \ 0 \ 0 \ 1 \ 1 \ 1 \\ \hline 1 \ 0 \ 1 \ 0 \ 0 \ 1 \end{array}$$

$$+ (-25)_{10} + 1 \ 0 \ 0 \ 1 \ 1 \ 1$$

$$\boxed{1} \ 0 \ 1 \ 0 \ 0 \ 0 \ 1$$

result is $(010001)_2$

* Binary Coding:-

- Numerical data (0,1..9) is not the only form of data which is handled by the computer. Alphanumeric data (A,B,C..Z) and some special characters such as =, -, +, * - also required.

* BCD

- Binary coded decimal is a method of using binary digits to represent the decimal digits 0-9.
- A decimal digit is represented by Four Binary Digits.
- The BCD coding is the binary equivalent of the decimal digit.

$$(5319)_{10} = (?)_{BCD}$$

$$5319 = \underline{0101} \underline{0011} \underline{0001} \underline{1001}$$

Devim

* ASCII - 8 bit "code"

- American Standard Code for Information Interchange
- This code was originally designed by as a seven bit code. $ASCII = 2^7 = 128$ characters codes.

Later on IBM developed a new version of ASCII called ASCII-8, which made use of all eight bits providing $2^8 = 256$ symbols.

- ASCII coding contains upper case, lower case, 0-9.

Ex: 01110111 01101111

W O r d s

119 111 114 100 115 115

01110111

W

119

d

01101111

O

113

s

01110010

r

114

* Floating Point representation:

- (a) Mantissa
- (b) Base
- (c) Exponent

Number

Base

Exponent

 4×10^6

04

10

06

 1160×2^8

1160

2

08

 1537.379

1537379

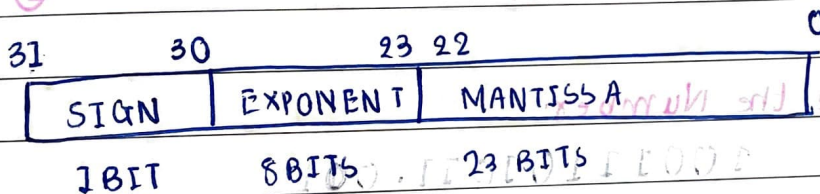
10

-3

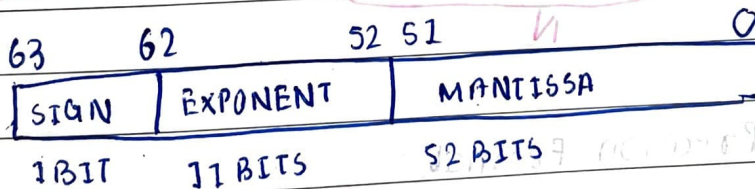
Example:

IEEE 754 Floating point number representation:

(a) Single Precision Format



(b) Double Precision Format



* Represent $(1259.125)_{10}$ in single and double precision format

① Convert Decimal to Binary.

$$(1259)_{10} = 10011101011_2$$

$$(0.125)_{10} = 0.125 \times 2 = 0.250$$

$$0.250 \times 2 = 0.500$$

$$0.50 \times 2 = 1.000$$

$$\begin{array}{r} 0 \\ 0 \\ 1 \end{array} \downarrow = (001)_2$$

$$1259.125 = (10011101011.001)_2$$

② Normalize the Number

$$\text{Single Precision: } (1.N) 2^{E-127}$$

$$\text{Double Precision: } (1.N) 2^{E-1023}$$

Normalize the Number:

$$10011101011.001$$

$$= 1. \underbrace{0011101011001}_N \times 2^{10}$$

③ Single Precision Format

$$(1.N) 2^{E-127}$$

$$\text{Normalized Number: } 1.0011101011001 \times 2^{10}$$

compare with eq (1)

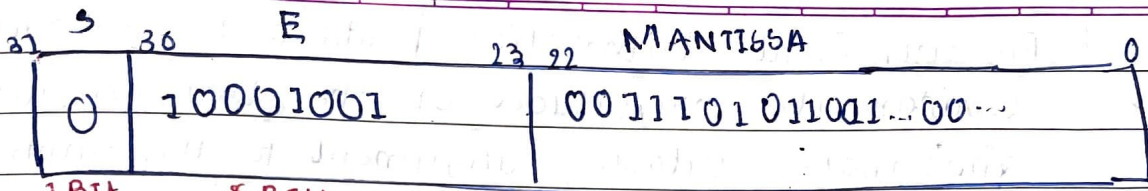
$$E = 127 + 10$$

$$E = 137$$

convert in Binary Numbers...

$$(137)_{10} = (10001001)_2$$

128 Bit



1 Bit Number is
 8 Bits Exponent in
 23 Bits Fraction Part
 +ve so put
 0 otherwise Binary

1

(4) Double Precision Format

$$(1.N)_2 \times 2^{E-1023}$$

Normalized the

Number: $1.0011101011001 \times 2^{10}$

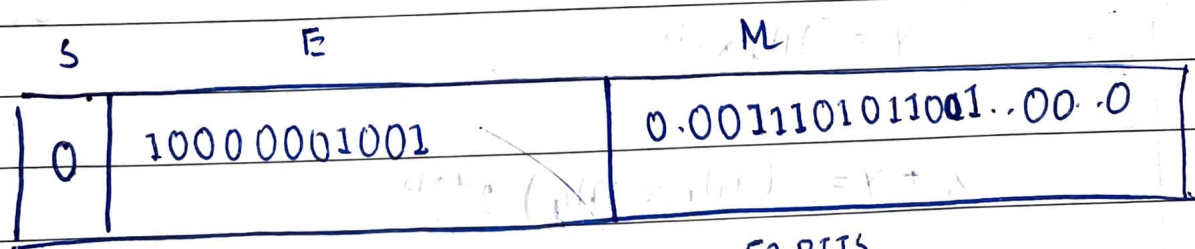
Compare with eqⁿ ②.

$$E - 1023 = 10$$

$$E = 1033$$

Convert in Binary No.

$$(1033)_2 = (10000001001)_2$$



1 Bit
 11 Bits
 52 Bits