

Assignment-1

(10.15.1.9)

AI1110:Probability and Random Variables

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Question: A box contains 5 red marbles, 8 white marbles and 4 green marbles. One marble is taken out of the box at random. What is the probability that the marble taken out will be :

- (i) red ?
- (ii) white ?
- (iii) not green?

Solution :

Number of red marbles = 5
Number of white marbles = 8
Number of green marbles = 4
Total marbles = 5+8+4 = 17

X	Outcome
0	Red Marble
1	White Marble
2	Green Marble

- (i) Probability that the marble taken out is red

$$= \frac{\text{Number of red marbles}}{\text{Total number of marbles}} \quad (1)$$

Probability that the marble taken out is red:

$$\Pr(X = 0) = \frac{n(X = 0)}{\sum_{i=0}^2 n(X = i)} = \frac{5}{17} \quad (2)$$

$$\therefore \Pr(X = 0) = \frac{5}{17} \approx 0.2941 \quad (3)$$

- (ii) Probability that the marble taken out is white

$$= \frac{\text{Number of white marbles}}{\text{Total number of marbles}} \quad (4)$$

Probability that the marble taken out is white:

$$\Pr(X = 1) = \frac{n(X = 1)}{\sum_{i=0}^2 n(X = i)} = \frac{8}{17} \quad (5)$$

$$\therefore \Pr(X = 1) = \frac{8}{17} \approx 0.4706 \quad (6)$$

- (iii) Probability that the marble taken out is not green

$$= \frac{\text{Number of non green marbles}}{\text{Total number of marbles}} \quad (7)$$

Probability that the marble taken out is not green:

$$\Pr(X \neq 2) = \frac{n(X \neq 2)}{\sum_{i=0}^2 n(X = i)} = \frac{13}{17} \quad (8)$$

$$\therefore \Pr(X \neq 2) = \frac{13}{17} \approx 0.7647 \quad (9)$$