CB4247 Statistics & Computational Inference to Big Data for Chemical and Biomedical Engineers

Individual Project

on

Forecasting Brent Crude Oil Prices through Machine Learning

by

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1. Introduction and Literature Review

Known as the "industrial blood" and "black gold", crude oil is the basis of industrial activity in all countries and is an indispensable energy resource for the functioning of the global economy. Crude oil is a global commodity that trades in markets around the world, both as spot oil and via derivatives contracts. There are two major oil contracts that are closely watched by oil market participants. In North America, the benchmark for oil futures is West Texas Intermediate (WTI) crude, which trades on the New York Mercantile Exchange (NYMEX). In Europe, Africa, and the Middle East, the benchmark is North Sea Brent Crude, which trades on the Intercontinental Exchange (ICE) [1].

Many economists view crude oil as the single most important commodity in the world, as it is currently the primary source of energy production and hence accurate crude oil price forecasting is critical to the economy's long-term stability. Research has been conducted in a number of areas related to oil price modelling and forecasting. Research indicates that supply and demand determine the price of crude oil. Additionally, some unforeseen severe events, such natural disasters and geopolitical wars, have an impact on price movement.

Proper determination of the country's economic structure and price-influencing components is necessary for the development of an appropriate price forecasting model. The U.S. economy largely impacts the dynamics of the global oil price since it is one of the major participants in the global energy market with respect to energy supply and consumption. Any changes, news, and shocks in the U.S. economy immediately affect the global oil prices dynamics. These catalysts which are primarily determined by financial and macroeconomic variables shape the dynamics of supply and demand in the crude oil market and, as a result, affect how investors behave. To modify their investing behaviour, investors, for instance, primarily concentrate on shifting macroeconomic variables like the FED rate, industrial production, or unemployment rate. Conversely, with regard to the U.S. economy, variables like the cost of refining crude oil and the volume of oil produced impact the supply of crude oil, which in turn dictates the dynamics of the Brent crude price. The dynamics of oil prices are greatly impacted by world events, conflicts, crises, and OPEC actions. Considering all of this, the study's motivation stems from the historical crude oil prices' non-linearity, uncertainty, and dynamics, all of which make predicting challenging. The uncertain

prediction results are doomed to cause significant uncertainty in relevant investors' returns and the economic system's stable development and as a result, developing a reliable crude oil price prediction model is critical [2]. Therefore, there is an attempt to build the reliable prediction of Brent Crude Oil prices in this project which includes the factors mentioned above.

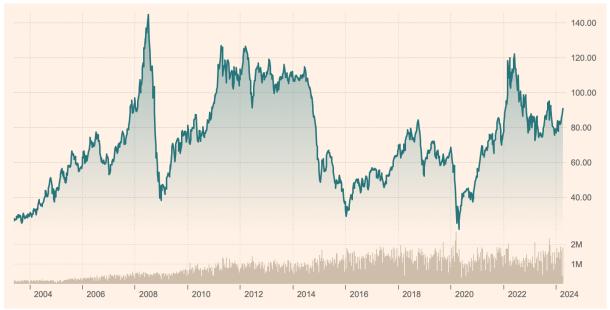


Figure 1. ICE Brent Crude Oil Front Month Prices

Oil prices fluctuate a lot over time, making it challenging to model and as Figure 1's historical graph illustrates, prices can vary significantly in a short period of time. Following the academic research over the past several years, one can observe that the study of the dynamics of oil prices has progressively evolved from linear econometric models to nonlinear ones. Recently, there is an increasing interest in research on methodologies based on machine learning (ML) and artificial intelligence (AI). [3] forecasted the crude oil indices using a Recurrent Neural Network (RNN) and [4] suggested a Neural Network model that was optimized using Genetic Algorithms to predict fluctuations in the price of crude oil. While current research have complicated neural network structures, this project aims to train simple machine learning algorithms to provide a price prediction with R-squared value larger than 0.95.

2. Data Sources

The Bloomberg terminal is used as the primary data source for this project, including the most prominently used global crude oil fundamental demand and supply, inventory and flows, refinery, utilisation data, S&P 500 to measure the optimism in the economy, US, Government 10-year bond yields to measure the interest rate and the Bloomberg Spot Index to track the performance against a basket of 10 leading global currencies. The only other source used as the Global political risk index provided by Caldara and Iacoviello which reflects automated text-search results of the electronic archives of 10 newspapers and counting the number of articles related to adverse geopolitical events in each newspaper for each month (as a share of the total number of news articles) [5]. Table 1 illustrates the category of data, ticker code and description of the feature variable used within this project.

Table 1: Key Characteristics of the Dataset

Category	Description				
	DOE Crude Oil Total Inventory Data (excluding Strategic Petroleum Reserve)				
	DOE Total Change in Crude Oil Inventories Data				
	DOE Strategic Petroleum Reserve (SPR) Total Inventory Data				
Inventory	DOE Cushing Oklahoma Crude Oil Total Stocks Data				
	United States DOE Crude Oil Total Production Data				
	Baker Hughes United States Crude Oil Rotary Rig Count Data				
	Baker Hughes Total World Oil And Gas Rotary Rig Count Data				
	US DOE Crude Oil Supply Adjustment				
	DOE Crude Oil Lower 48 States Production Data				
	Bloomberg Total OPEC Crude Oil Production Output Data				
	DOE EIA US Crude Oil Production (MBPD)				
	Bloomberg OPEC Crude Oil Production Output Data/Saudi Arabia				
	DOE Russia Crude Oil Production Data				
	World Crude Oil & Liquid Fuels Production Total World Supply				
	DOE World Crude Oil Production Data				
	Bloomberg OPEC Crude Oil Production Output Data/Nigeria				
	China Industrial Output - Crude Oil Processed				
	Bloomberg OPEC Crude Oil Production Angola Output Data				
	Bloomberg OPEC Crude Oil Production Output Data/Iran				
	Bloomberg OPEC Crude Oil Production Output Data/Venezuela				
	Bloomberg OPEC Total Crude Oil Production Quota/OPEC				
	DOE Saudi Arabia Crude Oil Production Data				
	DOE PSM US Field Production of Crude Oil				
	Bloomberg OPEC Crude Oil Production Output Data/Iraq				
	DOE Brazil Crude Oil Production Data				
	DOE Canada Crude Oil Production Data				
Production	DOE Nigeria Crude Oil Production Data				

	Canada Crude Oil Oil Sands Total Production Monthly				
	Bloomberg OPEC Crude Oil Production Output Data/Libya				
	Bloomberg OPEC Crude Oil Production Output Data/Kuwait				
	DOE Angola Crude Oil Production Data				
	World Crude Oil & Liquid Fuels Consumption Total World Consumption				
	China Supertanker Crude Imports				
	World Crude Oil & Liquid Fuels Consumption Total World Consumption				
	World Crude Oil & Liquid Fuels Consumption OECD				
	China Import Commodity Volume Crude Petroleum Oil				
	India Crude Oil Imports Quantity Monthly				
	South Korea Crude Oil Imports Total				
Demand	Japan Crude Oil Import Data/Total				
	DOE Percent Utilization Refinery Operable Capacity Data				
	DOE PSM Total US Operable Refinery Utilization Rate Monthly				
	India Refineries Crude Runs Monthly				
	China Shandong Local Refineries Utilization Rate Weekly				
	DOE Crude Oil Refinery Input Data/PADD 3				
	DOE Crude Oil Refinery Input Data/PADD 2				
	DOE Crude Oil Refinery Input Data/PADD 1				
Refinery	DOE Crude Oil Total Refinery Input Data				
· ·	Iraq Crude Oil Total Exports				
	Iran Crude Oil Total Exports				
	Qua Iboe Crude Oil Loading				
	Nigeria Crude Oil Loading				
	Nigeria Crude Oil Exports				
	Venezuela Crude Exports				
	Primorsk Diesel Loading				
	ESPO Crude Oil Loading				
	Libya Crude Oil Loading Total				
	Iraq Total Crude Oil Exports to China				
	Global Crude Oil Floating Storage				
	Global Crude Oil on Water				
Flows	Global Crude Oil in Transit				
	US Government 10 year yields				
	S&P 500 Index				
	Bloomberg Dollar Spot Index				
Economy	S&P 500 Integrated Oil & Gas Sub Industry				
Geopolitical Risk Index	7 day average				
THE HIGH	CO1 Comdty - Brent Crude Oil Futures Front Month Price price				
Price	Crude Oil 60 Day Volatility				
11100	Crace on to Day Tolumity				

These feature variables were divided into two different data sets depending on how many years' worth of data is available for the particular feature and modelling was run separately on each dataset. The first data set contained 14 years of data, including 54 feature variables and 3615 observations. Meanwhile, the second data set contained seven years' worth of data, 69 features and 1808 observations. This was due to data collection of some features having begun more recently starting in 2017. The correlation coefficient between the oil price and the feature variable are demonstrated, in Figure 1. and Figure 2.

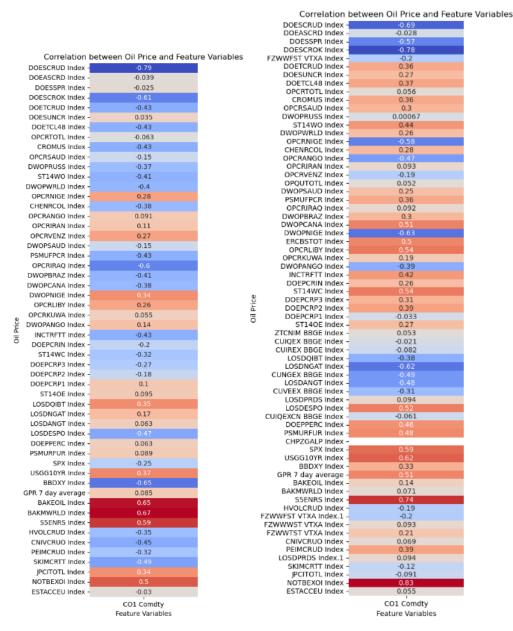


Figure 2. (left) demonstrates correlation coefficients between 54 features and oil prices used for historical data used from 2010-2023 and **Figure 3.** (right) demonstrates correlation coefficients 69 features and oil prices used for historical data from 2017-2023.

3. Data Cleaning and Pre-processing

The data was cleaned and pre-processed within Microsoft Excel since Bloomberg Excel add-in was used to import raw data using the tickers. Since several features of the data were updated on a weekly or on a monthly basis, to ensure the array integrity, the observation was repeated for days until the next observation was available for that particular feature. At the same time, a column containing the price CO1 COMDTY was altered to reflect the next day prices are as a result of current day observations that is, the column was moved by one cell upward. The features and prices were then stored in a .csv file for use in regression and modelling analysis within Python.

4. Regression and Modelling Algorithms

Given that the each dataset has more than 50 feature variables and 1 output variable (oil price) with 1500 observations, below is an analysis of the suitability of each model and why it is selected:

Table 2. Machine Learning Methods' Suitability and Selection

Method	Suitability	Selected?	
Linear Least-Squares	This model is a good starting point due to	Yes, for starting point.	
Regression	its simplicity and interpretability.		
	However, it assumes a linear relationship		
	between features and the target variable,		
	which may not capture complex nonlinear		
	relationships within the data.		
Weighted Least Squares	This method is useful when there is	No	
Regression	heteroscedasticity in the data, meaning the		
	variance of the errors is not constant		
	across observations. If the variance of		
	errors changes with different feature		
	values, this method might be beneficial.		
Nonlinear Regression	If the relationship between features and	Yes, since a non-linear	
	the target is nonlinear, consider nonlinear	relationship has been	
	regression techniques such as polynomial	expected between features	
	regression or regression with basic	and oil prices	
	functions. These models can capture more		

	complex relationships compared to linear	
	regression.	
Principal Component	PCA is useful for dimensionality	No, since it cannot help to
Analysis (PCA) based	reduction if there is multicollinearity	interpret the relationship
Regression	among your features or there is need to	between individual
	reduce the number of features while	features and the oil price.
	preserving most of the variance in the	
	data. However, it is not be the best choice	
	to interpret the relationship between	
	individual features and the target variable.	
Partial Least Squares	Suitable with large number of predictors	No, dimensionality
(PLS)	and multicollinearity among them. It is a	reduction methods are not
	dimensionality reduction technique that	suitable for use with the
	aims to find the directions in the feature	current dataset.
	space that explain the maximum variance	
	in both the predictors and the response	
	variable and can help improve prediction	
	accuracy.	
Kernel Ridge	Extends Ridge regression by using kernel	Yes
Regression	methods to capture nonlinear relationships	
	between features and the target variable.	
Gaussian Process	Suitable for modelling complex nonlinear	Yes
Regression	relationships and can provide uncertainty	
	estimates along with predictions.	
Feedforward Neural	Powerful for capturing complex patterns	Yes, commonly used
Networks	in data, but they require careful tuning and	Feedforward Neural
	may be prone to overfitting with a small	Network is chosen.
	dataset.	

5. Modelling Process

Two separate coding algorithms are used for each dataset, first of which applies Linear Regression, Nonlinear Regression (using statsmodels), Kernel Ridge Regression, and Gaussian Process Regression models together and another which applies the Feedforward Neural Networks respectively.

 Table 3. The modelling process for the first coding algorithm (Also see Appendix)

Step	Function
Loading the Dataset	The pd.read_csv() function loads the dataset from a CSV file into a
	DataFrame called data.
Splitting the Data	The train_test_split() function splits the dataset into training and
	validation sets. Here, 80% of the data is used for training, and 20% for
	validation.
Model Training and	We train the Linear Regression, Nonlinear Regression (using
Prediction	statsmodels), Kernel Ridge Regression, and Gaussian Process
	Regression models on the training data.
Model Evaluation	We evaluate the models using Mean Squared Error (MSE), R-squared,
	Adjusted R-squared, and Sum Squared Error.
Visualization	We visualize the predictions versus the actual values for each model
	on the validation set using scatter plots.

Table 4. The modelling process for the second coding algorithm (Also see Appendix)

Step	Function		
Loading the Dataset	The pd.read_csv() function loads the dataset from a CSV file into a		
	DataFrame called data.		
Splitting the Data	The train_test_split() function splits the dataset into training and		
	validation sets. Here, 80% of the data is used for training, and 20% for		
	validation.		
Define the Neural	5 hidden layers using the ReLu activation functions and 1 output layer		
Network Architecture	have been specified.		
Choosing a loss function	MSE Loss and Adam optimizer were chosen for the model		
and an optimizer for			
training the model			
Model Training and	Loop through the dataset for a number of epochs, perform forward and		
Prediction	backward passes, and update the model parameters.		
Model Evaluation	By evaluating the trained model on the test set, we calculate the test		
	loss and find Mean Squared Error (MSE), Mean Absolute Error		
	(MAE) and R-squared.		
Visualization	We visualize the predictions versus the actual values for each model		
	on the validation set using scatter plots.		

Residual Analysis	Analysing the distribution of residuals (the differences between
	predicted and actual values) to check for any patterns or systematic
	errors.

6. Modelling Outcomes and Results

Dataset 1 (14 years)

First coding algorithm

Linear Regression Metrics: {'MSE': 26.5001901743684, 'R-squared': 0.9585994959414958, 'Adjusted R-squared': 0.9552527486074252, 'Sum Squared Error': 19159.637496068353}

Nonlinear Regression Metrics: {'MSE': 37.15587148212258, 'R-squared': 0.9419524238138968, 'Adjuste d R-squared': 0.9372599550802896, 'Sum Squared Error': 26863.695081574624}

Kernel Ridge Regression Metrics: {'MSE': 5472.17784348724, 'R-squared': -7.54903000799124, 'Adjuste d R-squared': -8.240119260134245, 'Sum Squared Error': 3956384.580841275}

Gaussian Process Regression Metrics: {'MSE': 1034.871906299114, 'R-squared': -0.616751361966011, 'A djusted R-squared': -0.7474468313464968, 'Sum Squared Error': 748212.3882542595}

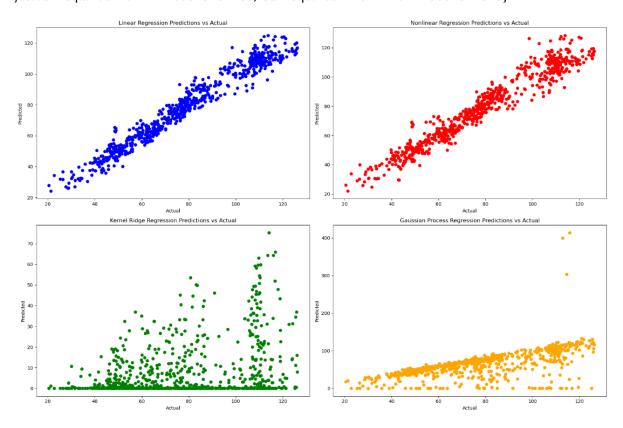


Figure 4. Predictions vs Actual Scatter Plots for Algorithm 1 for Dataset 1

Second coding algorithm

Mean Squared Error (MSE): 7.0591 Mean Absolute Error (MAE): 2.0495

R-squared: 0.9890

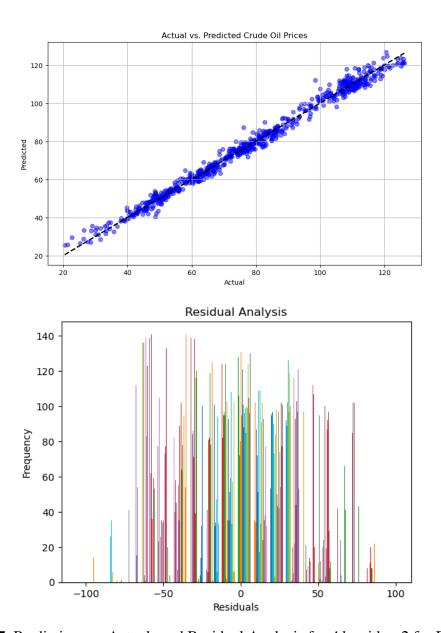


Figure 5. Predictions vs Actuals and Residual Analysis for Algorithm 2 for Dataset 1

Dataset 2 (7 years)

First coding algorithm

Linear Regression Metrics: {'MSE': 9.889596404157938, 'R-squared': 0.9720599423979265, 'Adjusted R-squared': 0.965457668512505, 'Sum Squared Error': 3580.0338983051734}
Nonlinear Regression Metrics: {'MSE': 12.097638254918929, 'R-squared': 0.9658217892947207, 'Adjust ed R-squared': 0.9577454312855965, 'Sum Squared Error': 4379.345048280652}
Kernel Ridge Regression Metrics: {'MSE': 4963.73866189401, 'R-squared': -13.02353933034606, 'Adjust ed R-squared': -16.337320884434686, 'Sum Squared Error': 1796873.3956056316}
Gaussian Process Regression Metrics: {'MSE': 702.0787827086218, 'R-squared': -0.9835108358744764, 'Adjusted R-squared': -1.4522171635297467, 'Sum Squared Error': 254152.5193405211}

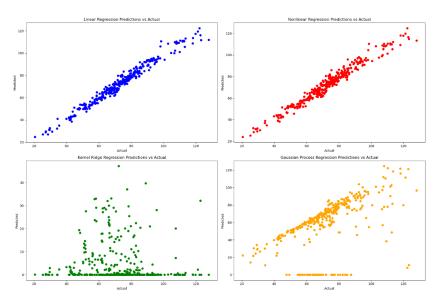


Figure 6. Predictions vs Actual Scatter Plots for Algorithm 1 for Dataset 2

Second coding algorithm

Mean Squared Error (MSE): 7.1623 Mean Absolute Error (MAE): 1.9763

R-squared: 0.9798

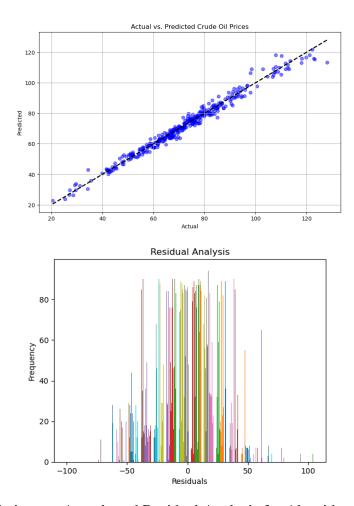


Figure 7. Predictions vs Actuals and Residual Analysis for Algorithm 2 for Dataset 2

7. Discussion of Results

Dataset 1

	Linear	Nonlinear	Kernel	Gaussian	Feedforward
	Regression	Regression	Ridge	Process	Neural
			Regression	Regression	Network
MSE	26.5002	37.1559	5472.1778	1034.8719	7.0591
R-squared	0.9586	0.9420	-7.5490	-0.6168	0.9890

Table 5. Model Evaluation Metric Summary for Dataset 1

Dataset 2

Model/Metric	Linear	Nonlinear	Kernel	Gaussian	Feedforward
	Regression	Regression	Ridge	Process	Neural
			Regression	Regression	Network
MSE	9.8896	12.0976	4963.7387	702.0788	7.1623
R-squared	0.9721	0.9658	-13.0235	-0.9835	0.9798

Table 6. Model Evaluation Metric Summary for Dataset 2

As seen in Table 5 and Table 6 results, it is clear that using feedforward neural networks to forecast Brent crude oil prices for the next day using feature variables from the previous day is the most accurate model applied with the highest R-squared value and lowest MSE value, thus meeting a better level of accuracy than the linear regression and non-linear methods applied. Feedforward neural networks are often considered better than traditional regression techniques like Linear Regression, Nonlinear Regression, Kernel Ridge Regression, and Gaussian Process Regression for certain types of datasets due to their ability to capture complex temporal dependencies and nonlinear relationships. Kernel Ridge regression and Gaussian ridge regression on the other hand, resulted in large MSE value and negative R-squared value which make it infeasible for predictions. Dataset 1 which includes more observations than Dataset 2, which has more features than Dataset 1, has performed better across all metrics. Nonetheless, as seen in Figure 5 and 7, from the residual analysis, it is clear that Dataset 1 has higher variance in terms of residuals compared to Dataset 2.

There are several reasons why neural networks are preferred since they are designed to capture temporal dependencies in sequential data, learn from past observations and make

predictions based on the sequence of historical data points. Neural networks also have the ability to automatically learn relevant features from the data, whereas traditional regression techniques often require manual feature engineering. This is advantageous when dealing with high-dimensional datasets or when the relationships between features and the target variable are not well understood [6].

Improving the accuracy of the neural network model involves a combination of various techniques, including hyperparameter tuning and model evaluation. By iteratively applying the techniques and carefully evaluating the model's performance, it is possible to improve accuracy and reduce bias, leading to a more effective and reliable model. Below are three techniques to improve the model:

- 1. Hyperparameter Tuning: Parameters such as learning rate, batch size, number of epochs and optimizer choice can significantly impact model performance [7].
- 2. Bias-Variance Tradeoff Analysis: Analysing the bias and variance of the model to understand its generalization performance and identify areas for improvement.
- 3. Feature Importance: Investigating which features have the most impact on predictions and focus on improving the quality of those features.

This model may still not however meet requirements of commercial use within a commodity trading company since it predicts the absolute price of the next day, instead of change in price from today to tomorrow. Further Analysis (Figure 8, Figure 9) has been conducted using a new column CO1 Comdty Delta = Tomorrow's price – Today's price and as we can see the current R-squared value is negative across all models tested on. To explain how measurements of predicted price are still largely inaccurate, due to real time pricing of feature variables into the CO1 Comdty price rather than each day. Therefore, to make the model powerful for commercial use, not only do we need thousands of intra-day observations for each feature variable, but the model needs to be trained continuously in real-time, for it to increase the R-squared value and reduce the MSE value in order to identify inefficiencies and make profitable trades.

CO1 Comdty Delta Modelling Outcomes and Results

First coding algorithm

Linear Regression Metrics: {'MSE': 2.4864199695754006, 'R-squared': -0.025126705598896404, 'Adjust ed R-squared': -0.10799622970419653, 'Sum Squared Error': 1797.6816380030145}

Nonlinear Regression Metrics: {'MSE': 2.504354478409105, 'R-squared': -0.03252092869161438, 'Adjusted R-squared': -0.11598818939422983, 'Sum Squared Error': 1810.6482878897828}

Kernel Ridge Regression Metrics: {'MSE': 2.4792998487640907, 'R-squared': -0.022191149224640494, 'Adjusted R-squared': -0.10482336787453672, 'Sum Squared Error': 1792.5337906564375}

Gaussian Process Regression Metrics: {'MSE': 2.4257980636237897, 'R-squared': -0.0001328849669322 0075, 'Adjusted R-squared': -0.08098195051815127, 'Sum Squared Error': 1753.8519999999999}

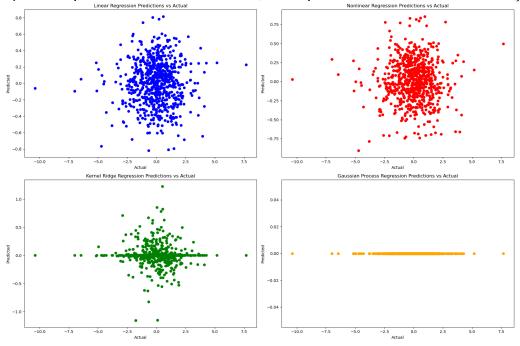


Figure 8. Predictions vs Actual Scatter Plots for Algorithm 1 for CO1 Comdty Delta dataset

Second coding algorithm

Mean Squared Error (MSE): 4.3662 Mean Absolute Error (MAE): 1.4282 R-squared: -0.8001

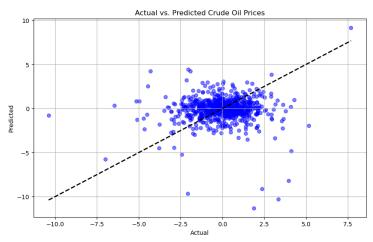


Figure 9. Predictions vs Actuals for Algorithm 2 for CO1 Comdty Delta dataset

8. Conclusion

Crude oil, known as "black gold," is vital for global economic activity and its price, influenced by supply, demand, and unpredictable events like conflicts or disasters, all affect the economy's stability. Forecasting crude oil prices accurately is crucial but challenging due to non-linearity and uncertainty nonetheless, recent research has shifted from linear econometric models to AI and ML-based approaches like Recurrent Neural Networks (RNN). For this project, a dataset with an array of relevant variables is acquired from Bloomberg. Following this, the dataset is partitioned into training and validation sets, facilitating model building and cross-validation. Various regression algorithms, encompassing both linear and nonlinear options were then deployed to model the relationships between the independent and dependent variables. Through use of evaluation metrics like sum squared error and Rsquared, the performance of the models was then scrutinized. This project achieved to develop a reliable crude oil price prediction model using Feedforward neural network method on Dataset 1 with an R-squared value exceeding 0.95, at 0.989. Finally, the pitfalls of using this algorithm and dataset in commercial applications was explained using price delta dataset, showcasing the need for thousands of intra-day observations for each feature variable that the model will need and for it to be trained continuously in real-time, for it to increase the Rsquared value and reduce the MSE value of the delta.

9. References

- [1] What Is Crude Oil, and Why Is It Important to Investors? https://www.investopedia.com/terms/c/crude-oil.asp
- [2] H. Guliyev and E. Mustafayev, "Predicting the changes in the WTI crude oil price dynamics using machine learning models," Resources policy, vol. 77, pp. 102664-, 2022, doi: 10.1016/j.resourpol.2022.102664.
- [3] J. Wang, J. Wang, Forecasting energy market indices with recurrent neural networks: Case study of crude oil price fluctuations, Energy 102 (2016) 365–374.
- [4] H. Chiroma, S. Abdulkareem, T. Herawan, Evolutionary neural network model for west texas intermediate crude oil price prediction, Applied Energy 142 (2015) 266 273.
- [5] Caldara, Dario and Matteo Iacoviello (2022), "Measuring Geopolitical Risk," American Economic Review, April, 112(4), pp.1194-1225. https://www.matteoiacoviello.com/gpr.htm
- [6] Why Deep Learning over Traditional Machine Learning? https://towardsdatascience.com/the-advantages-of-neural-networks-over-traditional-machine-learning-algorithms-7f594464d716
- [7] How to Grid Search Hyperparameters for Deep Learning Models in Python with Keras https://machinelearningmastery.com/grid-search-hyperparameters-deep-learning-models-python-keras/

10. Appendix

First Coding Algorithm

```
import numpy as np
import pandas as pd
from sklearn.model selection import train test split
from sklearn.linear_model import LinearRegression, Ridge
from sklearn.kernel_ridge import KernelRidge
from sklearn.gaussian process import GaussianProcessRegressor
from sklearn.gaussian_process.kernels import RBF
from sklearn.metrics import mean_squared_error, r2_score
import statsmodels.api as sm
import matplotlib.pyplot as plt
import seaborn as sns
# Load the dataset
file_path = 'crudeoil8 (1).csv' # Change this to the path of your dataset
data = pd.read csv(file path)
# Calculate correlations
correlation_matrix = data.corr()
# Extract correlations with the oil price
oil_price_correlation = correlation_matrix.iloc[:, -1]
# Plot heatmap
plt.figure(figsize=(3, 15))
sns.heatmap(oil_price_correlation[:-1].to_frame(), annot=True, cmap='coolwarm', cbar=False)
plt.title('Correlation between Oil Price and Feature Variables')
plt.xlabel('Feature Variables')
plt.ylabel('Oil Price')
plt.show()
# Load the dataset.
# Load the dataset
file_path = 'crudeoil8 (1).csv' # Change this to the path of your dataset
data = pd.read_csv(file_path)
y_index = -1 # Assuming oil price is in the last column
X = data.iloc[:, :-1] # Features
y = data.iloc[:, y_index] # Target variable (oil prices)
# Finding the dimensions of X and y
num_samples, num_features = X.shape
num_samples_y = y.shape[0]
print("Dimension of X:", num_samples, "samples x", num_features, "features")
print("Dimension of y:", num_samples_y, "samples")
# Split the data into training and validation sets
def split data(X, y):
 return train_test_split(X, y, test_size=0.2, random_state=42)
# Linear Least-Squares Regression
def linear_regression(X_train, X_val, y_train):
 linear_model = LinearRegression()
 linear_model.fit(X_train, y_train)
```

```
linear_preds = linear_model.predict(X_val)
 return linear_preds
# Nonlinear Regression (Polynomial of degree 2)
def nonlinear_regression(X_train, X_val, y_train):
 X_train_poly = sm.add_constant(X_train)
 X_val_poly = sm.add_constant(X_val)
 poly_reg = sm.OLS(y_train, sm.add_constant(X_train_poly**2))
 polv result = polv reg.fit()
 poly_preds = poly_result.predict(X_val_poly**2)
 return poly_preds
# Kernel Ridge Regression
def kernel_ridge_regression(X_train, X_val, y_train):
  kernel_ridge_model = KernelRidge(kernel='rbf')
  kernel_ridge_model.fit(X_train, y_train)
 kernel_ridge_preds = kernel_ridge_model.predict(X_val)
 return kernel_ridge_preds
# Gaussian Process Regression
def gaussian_process_regression(X_train, X_val, y_train):
 gaussian_kernel = RBF(length_scale=1.0)
 gaussian_process_model = GaussianProcessRegressor(kernel=gaussian_kernel)
 gaussian_process_model.fit(X_train, y_train)
 gaussian_process_preds, _ = gaussian_process_model.predict(X_val, return_std=True)
 return gaussian process preds
# Evaluate the models
def evaluate_model(y_true, y_pred):
 mse = mean_squared_error(y_true, y_pred)
 r2 = r2_score(y_true, y_pred)
 adj_r^2 = 1 - (1 - r^2) * (len(y_true) - 1) / (len(y_true) - X.shape[1] - 1)
 sse = np.sum((y_true - y_pred)**2)
 return {'MSE': mse, 'R-squared': r2, 'Adjusted R-squared': adj_r2, 'Sum Squared Error': sse}
  # Split the data into training and validation sets
 X_train, X_val, y_train, y_val = split_data(X, y)
  # Perform linear least-squares regression
 linear_preds = linear_regression(X_train, X_val, y_train)
  # Perform nonlinear regression
 poly_preds = nonlinear_regression(X_train, X_val, y_train)
  # Perform kernel ridge regression
 kernel_ridge_preds = kernel_ridge_regression(X_train, X_val, y_train)
  # Perform Gaussian process regression
 gaussian_process_preds = gaussian_process_regression(X_train, X_val, y_train)
#Evaluate the models
 linear_metrics = evaluate_model(y_val, linear_preds)
  poly_metrics = evaluate_model(y_val, poly_preds)
  kernel_ridge_metrics = evaluate_model(y_val, kernel_ridge_preds)
 gaussian process metrics = evaluate model(y val, gaussian process preds)
# Print evaluation metrics
  print("Linear Regression Metrics:", linear_metrics)
 print("Nonlinear Regression Metrics:", poly_metrics)
```

```
print("Kernel Ridge Regression Metrics:", kernel_ridge_metrics)
 print("Gaussian Process Regression Metrics:", gaussian_process_metrics)
# Visualize predictions vs actual values for each model
 plt.figure(figsize=(18, 12))
 plt.subplot(2, 2, 1)
 plt.scatter(y_val, linear_preds, color='blue')
 plt.xlabel('Actual')
 plt.ylabel('Predicted')
 plt.title('Linear Regression Predictions vs Actual')
 plt.subplot(2, 2, 2)
 plt.scatter(y_val, poly_preds, color='red')
 plt.xlabel('Actual')
 plt.ylabel('Predicted')
 plt.title('Nonlinear Regression Predictions vs Actual')
 plt.subplot(2, 2, 3)
 plt.scatter(y_val, kernel_ridge_preds, color='green')
 plt.xlabel('Actual')
 plt.ylabel('Predicted')
 plt.title('Kernel Ridge Regression Predictions vs Actual')
 plt.subplot(2, 2, 4)
 plt.scatter(y_val, gaussian_process_preds, color='orange')
 plt.xlabel('Actual')
 plt.ylabel('Predicted')
 plt.title('Gaussian Process Regression Predictions vs Actual')
 plt.tight_layout()
 plt.show()
Second Coding Algorithm
import pandas as pd
# Load data from CSV file
data = pd.read_csv("crudeoil8 (1).csv")
# Assuming 'crude oil price' is the column name for crude oil prices
# and other columns are feature variables
X = data.drop(columns=['CO1 Comdty']).values
y = data['CO1 Comdty'].values
X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.2, random_state=42)
scaler = StandardScaler()
X_train_scaled = scaler.fit_transform(X_train)
X_test_scaled = scaler.transform(X_test)
X_train_tensor = torch.tensor(X_train_scaled, dtype=torch.float32)
y_train_tensor = torch.tensor(y_train, dtype=torch.float32)
X_test_tensor = torch.tensor(X_test_scaled, dtype=torch.float32)
v_test_tensor = torch.tensor(v_test, dtype=torch.float32)
class NeuralNet(nn.Module):
 def __init__(self, input_size):
    super(NeuralNet, self).__init__()
```

```
self.fc1 = nn.Linear(input_size, 256) # Input layer to first hidden layer
    self.fc2 = nn.Linear(256, 128)
    self.fc3 = nn.Linear(128, 64)
    self.fc4 = nn.Linear(64, 32)
    self.fc5 = nn.Linear(32, 16)
    self.fc6 = nn.Linear(16, 1)
  def forward(self. x):
    x = torch.relu(self.fc1(x)) # ReLU activation function for first hidden layer
    x = torch.relu(self.fc2(x))
    x = torch.relu(self.fc3(x))
    x = torch.relu(self.fc4(x))
    x = torch.relu(self.fc5(x))
    x = self.fc6(x)
                         # Output layer, no activation function
    return x
input_size = X_train.shape[1]
model = NeuralNet(input_size)
criterion = nn.MSELoss()
optimizer = torch.optim.Adam(model.parameters(), lr=0.001)
num epochs = 1000
for epoch in range(num_epochs):
  # Forward pass
 outputs = model(X train tensor)
 loss = criterion(outputs, y train tensor.unsqueeze(1)) # Unsqueezing y train tensor to match shape
  # Backward pass and optimization
 optimizer.zero_grad()
 loss.backward()
 optimizer.step()
 if (epoch+1) \% 100 == 0:
    print(f'Epoch [{epoch+1}/{num_epochs}], Loss: {loss.item():.4f}')
with torch.no grad():
  model.eval()
 v pred = model(X test tensor)
 test_loss = criterion(y_pred, y_test_tensor.unsqueeze(1))
 print(f'Test Loss: {test_loss.item():.4f}')
# Convert predictions back to a numpy array for further analysis
y_pred_numpy = y_pred.detach().numpy()
from sklearn.metrics import mean_squared_error, mean_absolute_error, r2_score
# Compute evaluation metrics
mse = mean_squared_error(y_test, y_pred_numpy)
mae = mean_absolute_error(y_test, y_pred_numpy)
r2 = r2_score(y_test, y_pred_numpy)
print(f'Mean Squared Error (MSE): {mse:.4f}')
print(f'Mean Absolute Error (MAE): {mae:.4f}')
print(f'R-squared: {r2:.4f}')
plt.figure(figsize=(10, 6))
plt.scatter(y_test, y_pred_numpy, color='blue', alpha=0.5)
plt.plot([y_test.min(), y_test.max()], [y_test.min(), y_test.max()], 'k--', lw=2)
```

```
plt.xlabel('Actual')
plt.ylabel('Predicted')
plt.title('Actual vs. Predicted Crude Oil Prices')
plt.grid(True)
plt.show()
def mean_absolute_percentage_error(y_true, y_pred):
  return np.mean(np.abs((y_true - y_pred) / y_true)) * 100
mape = mean_absolute_percentage_error(y_test, y_pred_numpy)
print(f'Mean Absolute Percentage Error (MAPE): {mape:.4f}%')
rmse = np.sqrt(mean_squared_error(y_test, y_pred_numpy))
print(f'Root Mean Squared Error (RMSE): {rmse:.4f}')
mae = mean_absolute_error(y_test, y_pred_numpy)
print(f'Mean Absolute Error (MAE): {mae:.4f}')
r2 = r2_score(y_test, y_pred_numpy)
print(f'R-squared: {r2:.4f}')
residuals = y_test - y_pred_numpy
plt.hist(residuals, bins=20)
plt.xlabel('Residuals')
plt.ylabel('Frequency')
plt.title('Residual Analysis')
plt.show()
```