

**Solution Idea:**

This problem is a nice example of segment tree with lazy propagation. All you need to solve this kind of problem is to do some experiment with the formula and convert them into a suitable form. From which we can drive the segment tree solution.

In this problem given an integer array  $A=[a_1, a_2, a_3, a_4, \dots]$ . You need to perform 3 kinds of operation on it.

type 0: Set all the element in the interval  $l$  to  $r$  to  $x$ .

type 1: Increase all the element in the interval  $l$  to  $r$  by  $x$ .

type 2: Print the value of square sum of the interval  $l$  to  $r$ . For example let  $l=1$  and  $r=3$ . then you need to print  $a_1^2 + a_2^2 + a_3^2$ .

At first think we have a pre-calculated square sum array. Then if we perform type 1 operation which is increase it by  $x$  then what scenario will happen?

Our sum now become  $(a_1+x)^2 + (a_2+x)^2 + (a_3+x)^2$ . Let expand this equation-

$$\begin{aligned} & (a_1+x)^2 + (a_2+x)^2 + (a_3+x)^2 \\ &= a_1^2 + 2*a_1*x + x^2 + a_2^2 + 2*a_2*x + x^2 + a_3^2 + 2*a_3*x + x^2 \\ &= (a_1^2 + a_2^2 + a_3^2) + 3*x^2 + 2*x*(a_1 + a_2 + a_3) \end{aligned}$$

for a range  $l$  to  $r$  the generalized equation is –

$$(a_l^2 + a_{l+1}^2 + \dots + a_r^2) + (r-l+1)*x^2 + 2*x*(a_l + a_{l+1} + \dots + a_r)$$

We can store the information about sum, square\_sum, type\_0 lazy and type\_1 lazy of an interval in each segment tree node. And perform type 1 operation then we can calculate then sum value for a node over a range by multiplication and square sum value by above equation.

For every type 0 operation we can simply put the value of sum and square sum by using some basic calculation and arithmetic multiplication operation.

And for every type 2 operation we just need to get the sum of square sum value over a range  $l$  to  $r$ .

So we can perform each of 3 operation using a segment tree with lazy propagation.