

GSS1 - Can you answer these queries I & GSS3 - Can you answer these queries III:

Problem: You are given a sequence $A[1], A[2], \dots, A[N]$. ($|A[i]| \leq 15007, 1 \leq N \leq 50000$).

A query is defined as follows:

Query(x,y) = Max { $a[i] + a[i+1] + \dots + a[j]$; $x \leq i \leq j \leq y$ }.

Given M queries, your program must output the results of these queries.

Solution: Lets analyze this query.

Query(x, y) is the maximum of below values where $\text{sum}(i, j) = a[i] + a[i+1] + \dots + a[j]$.

Left Sum: Where the range starts at 'x' but ends at anywhere in $[x, y]$.

Right Sum: Where the range starts at somewhere in $[x, y]$ and ends at 'y'.

Sum: Simply sum of all elements in interval $[x, y]$.

Best Sum: Maximum possible sum in range $[x, y]$.

Lets maintain 4 values.

bestLeftSum - Best of all the Left Sums, **bestRightSum** - Best of all the Right Sums

Sum - Sum of all the elements, **bestSum** - need to store resultSum of each query.

Logically, $\text{Query}(x, y).\text{resultSum} = \max(\text{bestLeftSum}, \text{bestRightSum}, \text{sum}, \text{Query}(x+1, y-1).\text{bestSum})$;

Lets call the above info {bestLeftSum, bestRightSum, Sum, bestSum} as QueryNode. and given information about QueryNode(L, M) and QueryNode(M+1, R).

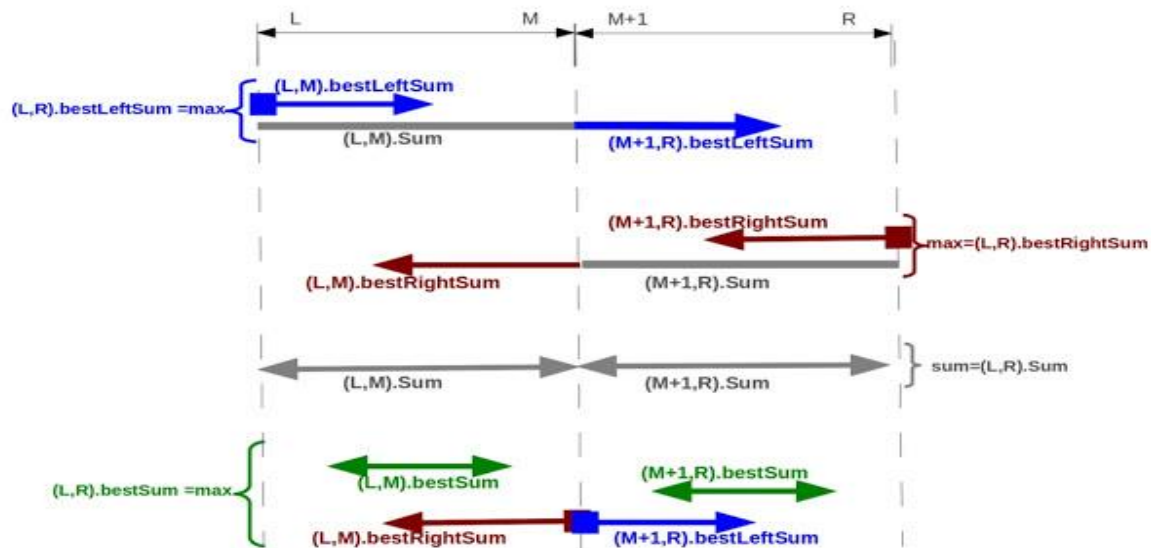
QueryNode(L, M) \rightarrow l and QueryNode(M+1, R) \rightarrow r. Then For QueryNode(L, R),

bestLeftSum = max (l.bestLeftSum, l.Sum + r.bestLeftSum);

bestRightSum = max (l.bestRightSum + r.Sum, r.bestRightSum);

Sum = l.Sum + r.Sum;

bestSum = max(l.bestSum, r.bestSum, l.bestRightSum + r.bestLeftSum)



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1  /* SPOJ - GSS3 - Can you answer these queries III
2  Given a sequence A of N(N<=50000) integers between -10000 and 10000.
3  On this sequence you have to apply M (M <= 50000) operations:
4  Modify the i-th element in the sequence or
5  For given x y print max{Ai + Ai+1 + .. + Aj | x<=i<=j<=y }.
6  */
7  #include<bits/stdc++.h>
8  using namespace std;
9  #define ll long long
10 #define MAXN 50005
11 #define lf nd<<1
12 #define rg (nd<<1)+1
13 #define m (int)((b+e)>>1)
14 #define N tree[nd]
15 #define L tree[lf]
16 #define R tree[rg]
17
18 int a[MAXN];
19 struct data{
20     ll prefix,suffix,bestSum,sum;
21 }tree[4*MAXN];
22
23 data maxData(data x, data y){
24     data z;
25     z.prefix = max(x.prefix, x.sum + y.prefix);
26     z.suffix = max(y.suffix, y.sum + x.suffix);
27     z.bestSum = max(max(x.bestSum, y.bestSum), x.suffix + y.prefix);
28     z.sum = x.sum + y.sum;
29     return z;
30 }
31 void build(int nd,int b,int e){
32     if(b==e){ N.prefix = N.suffix = N.bestSum = N.sum = a[b]; return; }
33     build(lf,b,m);
34     build(rg,m+1,e);
35     N = maxData(L,R);
36 }
37 void update(int nd,int b,int e,int x,int v){
38     if(b==e && b==x){ N.prefix = N.suffix = N.bestSum = N.sum = a[b] = v; return; }
39     if(x<=m)update(lf,b,m,x,v);
40     else update(rg,m+1,e,x,v);
41     N = maxData(L,R);
42 }
43 data query(int nd,int b,int e,int x,int y){
44     if(b>y || e<x){ data INF; INF.prefix=INF.suffix=INF.bestSum=INF.sum=-1000000000; return INF; }
45     if(b>=x && e<=y) return tree[nd];
46     return maxData(query(lf,b,m,x,y), query(rg,m+1,e,x,y));
47 }
48 int main(){
49     int n; scanf("%d",&n);
50     for(int i=1; i<=n; i++) scanf("%d",&a[i]);
51
52     build(1,1,n);
53
54     int q; scanf("%d",&q);
55     while(q--){
56         int t,x,y; scanf("%d%d%d",&t,&x,&y);
57         if(t==0){
58             update(1,1,n,x,y);
59         }else{
60             data ans = query(1,1,n,x,y);
61             ll res = max(max(ans.prefix,ans.suffix), max(ans.bestSum,ans.sum));
62             printf("%lld\n",res);
63         }
64     }
65 }

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