

Codeforces 455B – A lot of Games:

Andrew, Fedor and Alex are inventive guys. Now they invent the game with strings for two players.

Given a group of n non-empty strings. During the game two players build the word together, initially the word is empty. The players move in turns. On his step player must add a single letter in the end of the word, the resulting word must be prefix of at least one string from the group. A player loses if he cannot move.

Andrew and Alex decided to play this game k times. The player who is the loser of the i -th game makes the first move in the $(i + 1)$ -th game. Guys decided that the winner of all games is the player who wins the last (k -th) game. Andrew and Alex already started the game. Fedor wants to know who wins the game if both players will play optimally. Help him.

Input

The first line contains two integers, n and k ($1 \leq n \leq 10^5$; $1 \leq k \leq 10^9$).

Each of the next n lines contains a single non-empty string from the given group. The total length of all strings from the group doesn't exceed 10^5 . Each string of the group consists only of lowercase English letters.

Output

If the player who moves first wins, print "First", otherwise print "Second".

Idea:

To solve this problem we need the prefix tree(trie), which will have all the strings from the group. Next we will calculate the two DP:

$\text{win}[u]$ — Can player win if he makes a move now (players have word equal to prefix u in the prefix tree(trie)).

$\text{lose}[u]$ — Can player lose if he makes a move now (players have word equal to prefix u in the prefix tree(trie)).

if u is leaf of trie, then $\text{win}[u] = \text{false}$; $\text{lose}[u] = \text{true}$;

Else $\text{win}[u] = (\text{win}[u] \text{ or } (\text{not win}[v]))$; $\text{lose}[u] = (\text{lose}[u] \text{ or } (\text{not lose}[v]))$,
such v — children of vertex u .

Let's look at a few cases:

If $\text{win}[u] = \text{false}$, then second player win (first player lose all games).

If $\text{win}[u] = \text{true}$ and $\text{lose}[u] = \text{true}$, then first player win (he can change the state of the game in his favor).

If $\text{win}[u] = \text{true}$ and $\text{lose}[u] = \text{false}$, then if k is odd, then first player win, else second player win.