

Expt 7 - Unification & Resolution.

On Real World Problems

Aim:- Implementation of unification and resolution in real world applications.

(i) Implementation of unification (Pattern matching)

Problem Formulation:-

- * To find a mapping between the two expressions that may both contain variables.
- * Bind the variables to their values in the given expression until no bound variables remain.

Initial state:-

expression 1. = $f(x, h(x), y, g(y))$

expression 2 = $f(g(z), w, z, x)$

final state:-

$x: g(z)$

$w: h(x)$

$y: z$

expr 1. = $f(g(z), h(g(z)), z, g(z))$

expr 2 = $f(g(z), h(g(z)), z, g(z))$

Problem Solving:-

- Unify. $f(x, h(x), y, g(y))$ and $f(g(z), w, z, x)$.

- It would loop through each argument.
- Unify. $(x, g(z))$ is invoked.

x is a variable, therefore substitute.

$$x = g(z).$$

- Unify. $(h(x), w)$ is invoked

w is a variable.

\therefore Substitute. $w = h(x)$.

- The substitutions are mapped to a python dictionary and it expands as

$$\{x = g(z), w = h(x)\}$$

- Unify. (y, z) is invoked.

Both y and z are variable, hence added directly to the dictionary.

$$\{x = g(z), w = h(x), y = z\} \quad \# \quad z = y \text{ or } y = z \text{ is equivalent.}$$

- Unify $(g(x), x)$ is invoked:

x is a variable, but is already present in the dictionary.

At

- * ∴ the unify would be on the substituted value if it is not a variable, i.e., if the substituted value is not a variable.
- * unify $(g(x), g(z))$

Both the terms have g .

- * ∴ Unify $x \neq z$.

It is already present in map.

- All the variables are bounded, unification is completed successfully.

Final result: $\{x = g(z), w = h(x), y = z\}$

(ii) Implementation of Resolution (Predictive Logic)

Problem Formulation:-

By building reputation proofs, i.e. proofs by contradictions. prove a conclusion of those given statements based on the conjunctive normal form (CNF) or clausal form.

Initial State:-

- John likes all kind of food.
- Apple and vegetables are food.
- Anything anyone eats and not kills is food.
- Anil eats peanuts and still alive.
- Harry eats everything that Anil eats.

Prove by resolution:-

- John likes peanuts.

Problem Solving:-

- Conversion of facts into first order logic.
- $\forall x. \text{food}(x) \rightarrow \text{likes}(\text{John}, x)$
- $\text{food}(\text{Apples}) \wedge \text{food}(\text{Vegetable})$

- $\forall x \forall y: \text{eats}(x, y) \wedge \text{killed}(x) \rightarrow \text{food}(y)$
- $\text{eats}(\text{Anil}, \text{peanuts}) \wedge \text{alive}(\text{Anil})$
- A. $\forall x: \text{eats}(\text{Anil}, x) \rightarrow \text{eats}(\text{Harry}, x)$
- B. $\forall x: \neg \text{killed}(x) \rightarrow \text{alive}(x)$
- C. $\forall x: \text{alive}(x) \rightarrow \neg \text{killed}(x)$
- $\text{likes}(\text{John}, \text{peanuts})$

* Elimination of implication, moving negation inwards and renaming variables.

- * a. $\forall x \neg \text{food}(x) \vee \text{likes}(\text{John}, x)$
- b. $\text{food}(\text{Apple}) \wedge \text{food}(\text{Vegetables})$
- c. $\forall y \forall z: \neg \text{eats}(y, z) \vee \text{killed}(y) \vee \text{food}(z)$

- d. $\text{eats}(\text{Anil}, \text{Peanuts}) \wedge \text{alive}(\text{Anil})$
- e. $\forall w \neg \text{eats}(\text{Anil}, w) \vee \text{eats}(\text{Harry}, w)$
- f. $\forall y: \neg \text{killed}(y) \vee \text{alive}(y)$
- g. $\forall k \neg \text{alive}(k) \vee \text{killed}(k)$
- h. $\text{likes}(\text{John}, \text{peanuts})$

• Drop existential equations: $\exists x (x \text{ likes } \text{John})$

a. food (x) \vee likes (John, x)

b. food (apple).

c. food (vegetables)

d. \neg eats (y, z) \vee killed (y) \vee food (z).

e. eats (Anil, Peanuts)

f. alive (Anil).

g. \neg eats (Anil, w) \vee eats (Harry, w).

h. killed (y) \vee alive (y).

i. \neg alive (k) \vee \neg killed (k)

j. likes (John, Peanuts)

• Negate the statement to be proved.

j: \neg likes (John, Peanuts)

\neg likes (John, Peanuts) \neg food (x) \vee likes (John, x)

\neg food (Peanuts)

\neg eats (y, z) \vee killed (y)

\vee food (z) (Peanuts/z)

\neg eats (y, Peanuts) \vee killed (y)

killed (y)

eats (Anil, Peanuts)

{Anil, y}

\neg alive (Anil)

\neg alive (k) \vee \neg killed (k)

{Anil, k}

$\neg \text{alive}(Ani)$

$\text{alive}(Ani)$

$\{ \}$

Hence, proved

Unification (Pattern matching):

ALGORITHM:-

Step-1: Start

Step-2: Declare a Python dict mapping variable names to terms

Step-3: When either side is a variable, it calls `unify_variable`.

Step-4: Otherwise, if both sides are function applications, it ensures they apply the same

function (otherwise there's no match) and then unifies their arguments one by one, carefully

carrying the updated substitution throughout the process.

Step-5: If `v` is bound in the substitution, we try to unify its definition with `x` to guarantee consistency throughout the unification process (and vice versa when `x` is a variable).

Step-6: `occurs_check`, is to guarantee that we don't have self-referential variable bindings

like `X=f(X)` that would lead to potentially infinite unifiers.

Step-7: Stop

CODE:-

```
def get_index_comma(string):
    index_list = list()
    par_count = 0

    for i in range(len(string)):
        if string[i] == ',' and par_count == 0:
            index_list.append(i)
        elif string[i] == '(':
            par_count += 1
        elif string[i] == ')':
            par_count -= 1

    return index_list

def is_variable(expr):
    for i in expr:
        if i == '(' or i == ')':
            return False
```



```
return True
```

```
def process_expression(expr):  
    expr = expr.replace(' ', '')  
    index = None  
    for i in range(len(expr)):  
        if expr[i] == '(':  
            index = i  
            break  
    predicate_symbol = expr[:index]  
    expr = expr.replace(predicate_symbol, '')  
    expr = expr[1:len(expr) - 1]  
    arg_list = list()  
    indices = get_index_comma(expr)  
  
    if len(indices) == 0:  
        arg_list.append(expr)  
    else:  
        arg_list.append(expr[:indices[0]])  
        for i, j in zip(indices, indices[1:]):  
            arg_list.append(expr[i + 1:j])  
        arg_list.append(expr[indices[len(indices) - 1] + 1:])  
  
    return predicate_symbol, arg_list
```

```
def get_arg_list(expr):  
    _, arg_list = process_expression(expr)  
  
    flag = True  
    while flag:  
        flag = False  
  
        for i in arg_list:  
            if not is_variable(i):  
                flag = True  
                _, tmp = process_expression(i)  
                for j in tmp:  
                    if j not in arg_list:  
                        arg_list.append(j)  
                arg_list.remove(i)  
  
    return arg_list
```

```
def check_occurs(var, expr):  
    arg_list = get_arg_list(expr)  
    if var in arg_list:  
        return True
```

```
return False
```

```
def unify(expr1, expr2):
```

```
    if is_variable(expr1) and is_variable(expr2):
```

```
        if expr1 == expr2:
```

```
            return 'Null'
```

```
        else:
```

```
            return False
```

```
    elif is_variable(expr1) and not is_variable(expr2):
```

```
        if check_occurs(expr1, expr2):
```

```
            return False
```

```
        else:
```

```
            tmp = str(expr2) + '/' + str(expr1)
```

```
            return tmp
```

```
    elif not is_variable(expr1) and is_variable(expr2):
```

```
        if check_occurs(expr2, expr1):
```

```
            return False
```

```
        else:
```

```
            tmp = str(expr1) + '/' + str(expr2)
```

```
            return tmp
```

```
    else:
```

```
        predicate_symbol_1, arg_list_1 = process_expression(expr1)
```

```
        predicate_symbol_2, arg_list_2 = process_expression(expr2)
```

```
        # Step 2
```

```
        if predicate_symbol_1 != predicate_symbol_2:
```

```
            return False
```

```
        # Step 3
```

```
        elif len(arg_list_1) != len(arg_list_2):
```

```
            return False
```

```
        else:
```

```
            # Step 4: Create substitution list
```

```
            sub_list = list()
```

```
            # Step 5:
```

```
            for i in range(len(arg_list_1)):
```

```
                tmp = unify(arg_list_1[i], arg_list_2[i])
```

```
            if not tmp:
```

```
                return False
```

```
            elif tmp == 'Null':
```

```
                pass
```

```
            else:
```

```
                if type(tmp) == list:
```

```
                    for j in tmp:
```

```
                        sub_list.append(j)
```

```
            else:
```

```

        sub_list.append(tmp)

    # Step 6
    return sub_list

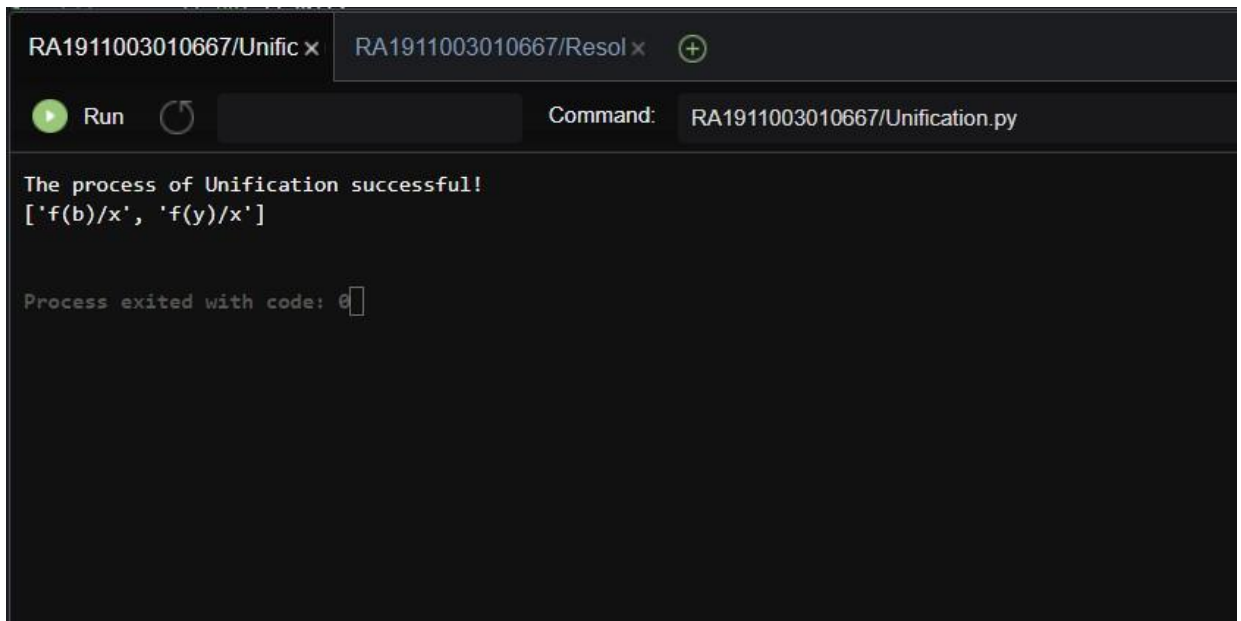
if __name__ == '__main__':

    f1 = 'Q(a, g(x, a), f(y))'
    f2 = 'Q(a, g(f(b), a), x)'
    # f1 = input('f1 : ')
    # f2 = input('f2 : ')

    result = unify(f1, f2)
    if not result:
        print("The process of Unification failed!")
    else:
        print("The process of Unification successful!")
        print(result)

```

OUTPUT:-



```

RA1911003010667/Unific x RA1911003010667/Resol x
Run Command: RA1911003010667/Unification.py

The process of Unification successful!
['f(b)/x', 'f(y)/x']

Process exited with code: 0

```

RESULT:-

Hence, the Implementation of unification algorithm for Pattern Matching is done successfully.

Resolution (Predicate logic):

Algorithm:-

Step-1: Start

Step-2: if L1 or L2 is an atom part of same thing do

(a) if L1 or L2 are identical then return NIL

(b) else if L1 is a variable then do

(i) if L1 occurs in L2 then return F else return (L2/L1)

else if L2 is a variable then do

(i) if L2 occurs in L1 then return F else return (L1/L2)

else return F.

Step-3: If length (L1) is not equal to length (L2) then return F.

Step-4: Set SUBST to NIL

(at the end of this procedure , SUBST will contain all the substitutions used

to unify L1 and L2).

Step-5: For I = 1 to number of elements in L1 do

i) call UNIFY with the i th element of L1 and I'th element of L2, putting the

result in S

ii) if S = F then return F

iii) if S is not equal to NIL then do

(A) apply S to the remainder of both L1 and L2

(B) SUBST := APPEND (S, SUBST) return SUBST.

Step-6: Stop

CODE:-

```
import copy
```

```
import time
```

```
class Parameter:
```

```
    variable_count = 1
```

```
    def __init__(self, name=None):
```

```
        if name:
```

```
            self.type = "Constant"
```

```

        self.name = name
    else:
        self.type = "Variable"
        self.name = "v" + str(Parameter.variable_count)
        Parameter.variable_count += 1

def isConstant(self):
    return self.type == "Constant"

def unify(self, type_, name):
    self.type = type_
    self.name = name

def __eq__(self, other):
    return self.name == other.name

def __str__(self):
    return self.name

class Predicate:
    def __init__(self, name, params):
        self.name = name
        self.params = params

    def __eq__(self, other):
        return self.name == other.name and all(a == b for a, b in
zip(self.params, other.params))

    def __str__(self):
        return self.name + "(" + ",".join(str(x) for x in self.params) + ")"

    def getNegatedPredicate(self):
        return Predicate(negatePredicate(self.name), self.params)

class Sentence:
    sentence_count = 0

    def __init__(self, string):
        self.sentence_index = Sentence.sentence_count
        Sentence.sentence_count += 1
        self.predicates = []

```

```

self.variable_map = {}
local = {}

for predicate in string.split("|"):
    name = predicate[:predicate.find("(")]
    params = []

    for param in predicate[predicate.find("(") + 1:
predicate.find(")")]
.split(","):
        if param[0].islower():
            if param not in local: # Variable
                local[param] = Parameter()
                self.variable_map[local[param].name] = local[param]
                new_param = local[param]
            else:
                new_param = Parameter(param)
                self.variable_map[param] = new_param

        params.append(new_param)

    self.predicates.append(Predicate(name, params))

def getPredicates(self):
    return [predicate.name for predicate in self.predicates]

def findPredicates(self, name):
    return [predicate for predicate in self.predicates if predicate.name ==
name]

def removePredicate(self, predicate):
    self.predicates.remove(predicate)
    for key, val in self.variable_map.items():
        if not val:
            self.variable_map.pop(key)

def containsVariable(self):
    return any(not param.isConstant() for param in
self.variable_map.values())

def __eq__(self, other):
    if len(self.predicates) == 1 and self.predicates[0] == other:
        return True
    return False

```

```

def __str__(self):
    return "".join([str(predicate) for predicate in self.predicates])

class KB:
    def __init__(self, inputSentences):
        self.inputSentences = [x.replace(" ", "") for x in inputSentences]
        self.sentences = []
        self.sentence_map = { }

    def prepareKB(self):
        self.convertSentencesToCNF()
        for sentence_string in self.inputSentences:
            sentence = Sentence(sentence_string)
            for predicate in sentence.getPredicates():
                self.sentence_map[predicate] = self.sentence_map.get(
                    predicate, []) + [sentence]

    def convertSentencesToCNF(self):
        for sentenceIdx in range(len(self.inputSentences)):
            # Do negation of the Premise and add them as literal
            if "=>" in self.inputSentences[sentenceIdx]:
                self.inputSentences[sentenceIdx] = negateAntecedent(
                    self.inputSentences[sentenceIdx])

    def askQueries(self, queryList):
        results = []

        for query in queryList:
            negatedQuery = Sentence(negatePredicate(query.replace(" ", "")))
            negatedPredicate = negatedQuery.predicates[0]
            prev_sentence_map = copy.deepcopy(self.sentence_map)
            self.sentence_map[negatedPredicate.name] =
self.sentence_map.get(
            negatedPredicate.name, []) + [negatedQuery]
            self.timeLimit = time.time() + 40

            try:
                result = self.resolve([negatedPredicate], [
                    False]*(len(self.inputSentences) + 1))
            except:
                result = False

```

```

self.sentence_map = prev_sentence_map

if result:
    results.append("TRUE")
else:
    results.append("FALSE")

return results

def resolve(self, queryStack, visited, depth=0):
    if time.time() > self.timeLimit:
        raise Exception
    if queryStack:
        query = queryStack.pop(-1)
        negatedQuery = query.getNegatedPredicate()
        queryPredicateName = negatedQuery.name
        if queryPredicateName not in self.sentence_map:
            return False
        else:
            queryPredicate = negatedQuery
            for kb_sentence in self.sentence_map[queryPredicateName]:
                if not visited[kb_sentence.sentence_index]:
                    for kbPredicate in
kb_sentence.findPredicates(queryPredicateName):

                        canUnify, substitution = performUnification(
                            copy.deepcopy(queryPredicate),
copy.deepcopy(kbPredicate))

            if canUnify:
                newSentence = copy.deepcopy(kb_sentence)
                newSentence.removePredicate(kbPredicate)
                newQueryStack = copy.deepcopy(queryStack)

            if substitution:
                for old, new in substitution.items():
                    if old in newSentence.variable_map:
                        parameter = newSentence.variable_map[old]
                        newSentence.variable_map.pop(old)
                        parameter.unify(
                            "Variable" if new[0].islower() else
"Constant", new)

```



```

        newSentence.variable_map[new] = parameter

    for predicate in newQueryStack:
        for index, param in enumerate(predicate.params):
            if param.name in substitution:
                new = substitution[param.name]
                predicate.params[index].unify(
                    "Variable" if new[0].islower() else
"Constant", new)

```

```

        for predicate in newSentence.predicates:
            newQueryStack.append(predicate)

        new_visited = copy.deepcopy(visited)
        if kb_sentence.containsVariable() and
len(kb_sentence.predicates) > 1:
            new_visited[kb_sentence.sentence_index] = True

        if self.resolve(newQueryStack, new_visited, depth +
1):
            return True
        return False
    return True

```

```

def performUnification(queryPredicate, kbPredicate):
    substitution = {}
    if queryPredicate == kbPredicate:
        return True, {}
    else:
        for query, kb in zip(queryPredicate.params, kbPredicate.params):
            if query == kb:
                continue
            if kb.isConstant():
                if not query.isConstant():
                    if query.name not in substitution:
                        substitution[query.name] = kb.name
                    elif substitution[query.name] != kb.name:
                        return False, {}
                query.unify("Constant", kb.name)
            else:
                return False, {}
    else:

```

```

    if not query.isConstant():
        if kb.name not in substitution:
            substitution[kb.name] = query.name
        elif substitution[kb.name] != query.name:
            return False, { }
        kb.unify("Variable", query.name)
    else:
        if kb.name not in substitution:
            substitution[kb.name] = query.name
        elif substitution[kb.name] != query.name:
            return False, { }
    return True, substitution

```

```

def negatePredicate(predicate):
    return predicate[1:] if predicate[0] == "~" else "~" + predicate

```

```

def negateAntecedent(sentence):
    antecedent = sentence[:sentence.find("=>")]
    premise = []

    for predicate in antecedent.split("&"):
        premise.append(negatePredicate(predicate))

    premise.append(sentence[sentence.find("=>") + 2:])
    return "|".join(premise)

```

```

def getInput(filename):
    with open(filename, "r") as file:
        noOfQueries = int(file.readline().strip())
        inputQueries = [file.readline().strip() for _ in range(noOfQueries)]
        noOfSentences = int(file.readline().strip())
        inputSentences = [file.readline().strip()
                           for _ in range(noOfSentences)]
    return inputQueries, inputSentences

```

```

def printOutput(filename, results):
    print(results)
    with open(filename, "w") as file:
        for line in results:

```

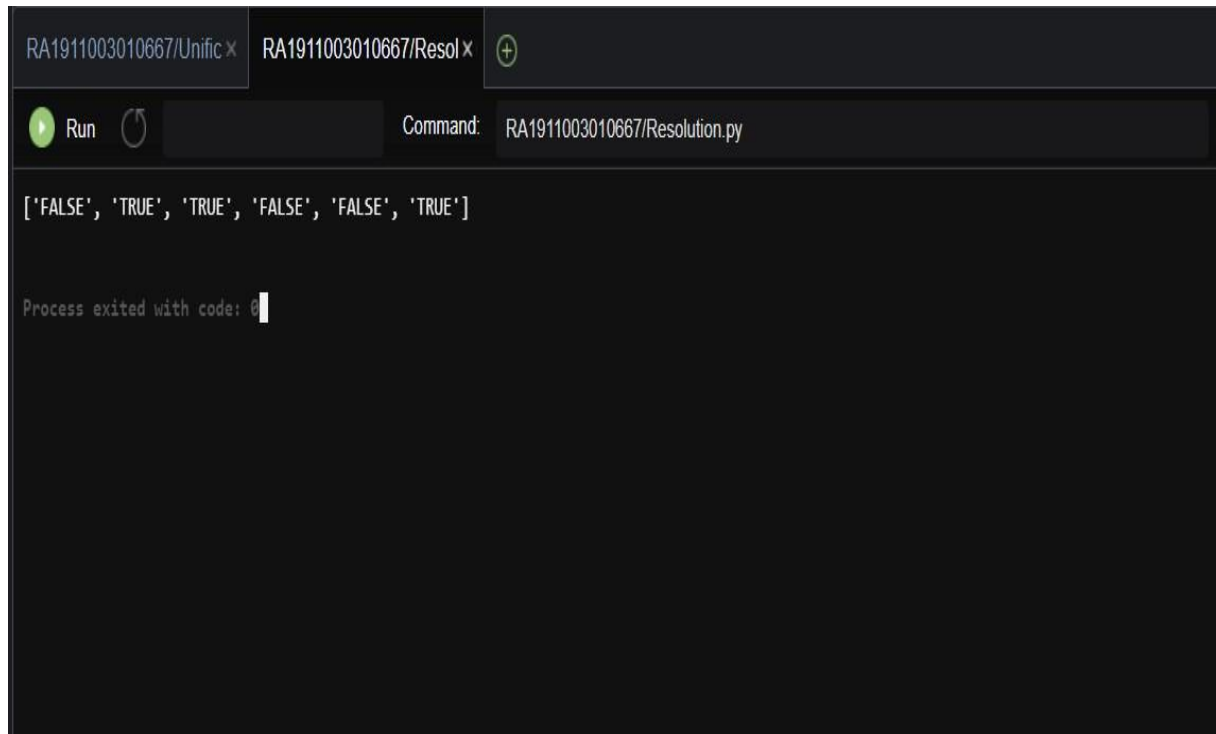
```
        file.write(line)
        file.write("\n")
    file.close()
```

```
if __name__ == '__main__':
    inputQueries_, inputSentences_ =
    getInput("RA1911003010667/Input.txt")
    knowledgeBase = KB(inputSentences_)
    knowledgeBase.prepareKB()
    results_ = knowledgeBase.askQueries(inputQueries_)
    printOutput("RA1911003010667/output.txt", results_)
```

INPUT:-

```
6
F(Joe)
H(John)
~H(Alice)
~H(John)
G(Joe)
G(Tom)
14
~F(x) | G(x)
~G(x) | H(x)
~H(x) | F(x)
~R(x) | H(x)
~A(x) | H(x)
~D(x,y) | ~H(y)
~B(x,y) | ~C(x,y) | A(x)
B(John,Alice)
B(John,Joe)
~D(x,y) | ~Q(y) | C(x,y)
D(John,Alice)
Q(Joe)
D(John,Joe)
R(Tom)
```

OUTPUT:-



The screenshot shows a code editor with two tabs: 'RA1911003010667/Unific x' and 'RA1911003010667/Resol x'. The 'Resol x' tab is active. Below the tabs, there is a 'Run' button with a green play icon and a refresh icon. To the right of the 'Run' button, the command 'RA1911003010667/Resolution.py' is displayed. The main area of the editor shows the output of the script: a list of six boolean values: ['FALSE', 'TRUE', 'TRUE', 'FALSE', 'FALSE', 'TRUE']. Below this output, it says 'Process exited with code: 0'.

```
RA1911003010667/Unific x RA1911003010667/Resol x (+)  
Run [refresh] Command: RA1911003010667/Resolution.py  
['FALSE', 'TRUE', 'TRUE', 'FALSE', 'FALSE', 'TRUE']  
Process exited with code: 0
```

RESULT:-

Hence, the Implementation of resolution algorithm for Predicate logic is done successfully.