

Step 1

find $\|x_1 - z_1\|_2 \dots \|x_1 - z_k\|_2$
for all $x_1, x_2 \dots x_N \in \mathbb{R}^n$
Then find minimum

subtraction $\rightarrow \cancel{O(n)} n$

norm $\rightarrow 2n$

Minimum $\rightarrow k$

\Rightarrow Total operations Per x_i for $i \in 1, 2, \dots, N$

$$= 3n \times k$$

\Rightarrow Total ~~time~~ complexity = $O(nkN)$
computation

(b) Step 2 for all $i \in 1, 2, \dots, k$

$$z_{i^*} = \frac{1}{|S_{i^*}|} \sum x_{j^*} [C_j = i^*]$$

summation = nN

Divisions = $k \times n$

Total complexity = $nN + kn$
 $\approx O(nN)$ ~~if~~ $N > k$

iii Total No. of computations

$$= 3nKN + nN + Kn$$

\Rightarrow for 10 iterations computations are

$$= 10(3nKN + nN + Kn)$$

$$\approx 30nKN + 10nN + 10Kn$$