

DnC ~ divide and conquer

* Merge two sorted arrays

IP : Arr1 =

2	4	6
i		

Arr 2 =

3	5	7	9	1
j				

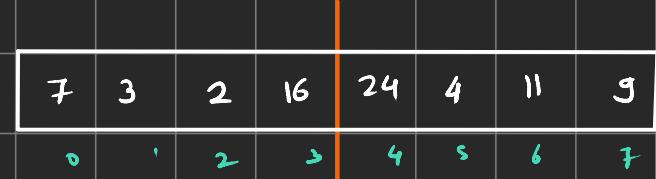
two pointer approach if ($i < j$)
then use it and
 $i++$

IF (i is out of bound or j is out of
bound)

then arrA remaining elements
add them

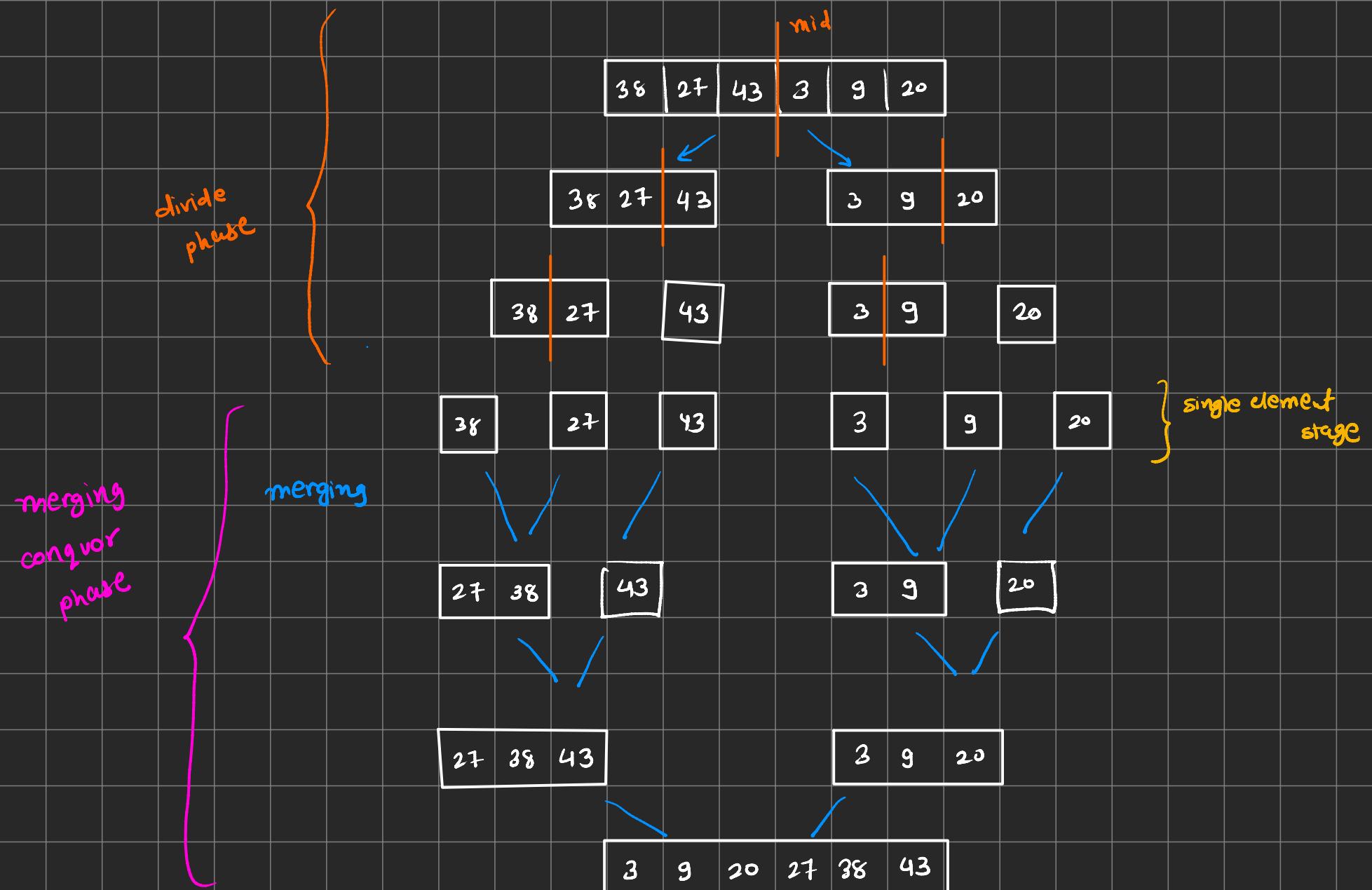
arrB remaining ele add it

* Merge sort

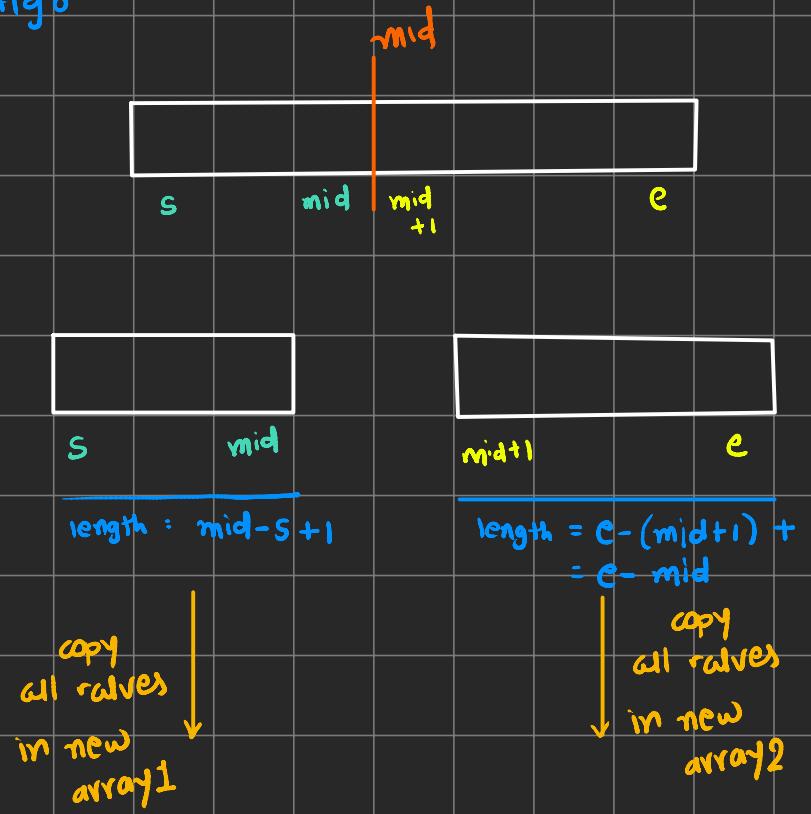


sort it
using recursion
then
merge

```
void mergeSort(int *arr, int s, int e){  
  
    // base case  
    if(s==e){  
        // single element  
        return;  
    }  
  
    // rr  
    int mid = (s+e)/2;  
    // left part sort  
    mergeSort(arr ,s, mid);  
  
    // right part sort  
    mergeSort(arr, mid+1, e);  
  
    // merge two sorted arr  
    merge(arr,s,e);  
}
```



Merging Algo



merge two sorted arrays

```
void merge(int *arr, int s, int e){  
    int mid = (s+e)/2;  
  
    int len1 = mid-s+1;  
    int len2 = e-mid;  
  
    int* leftArr = new int[len1];  
    int* rightArr = new int[len2];  
  
    // copy values  
    int k = s;  
    for(int i=0;i<len1;i++){  
        leftArr[i] = arr[k];  
        k++;  
    }  
  
    k = mid+1;  
    for(int i=0;i<len2;i++){  
        rightArr[i] = arr[k];  
        k++;  
    }  
}
```

$$TC = \underbrace{k_1}_{\substack{\text{Base} \\ \text{case}}} + \underbrace{T\left(\frac{n}{2}\right)}_{\substack{\text{left} \\ \text{sort}}} + \underbrace{T\left(\frac{n}{2}\right)}_{\substack{\text{right} \\ \text{sort}}} + \underbrace{(n * k)}_{\text{merging}}$$

$$= \underbrace{k_1}_{\substack{\text{neglect it}}} + 2 \cdot T\left(\frac{n}{2}\right) + n * k$$

$$TC = 2 \cdot T\left(\frac{n}{2}\right) + n * k$$

$$T(n) = 2T\left(\frac{n}{2}\right) + n \cdot k$$

~~$$2 \cdot T\left(\frac{n}{2}\right) = 4T\left(\frac{n}{4}\right) + 2 \frac{n \cdot k}{2} \times 2$$~~

~~$$4 \cdot T\left(\frac{n}{4}\right) = 2T\left(\frac{n}{8}\right) + 4 \frac{n \cdot k}{4} \times 4$$~~

~~$$\vdots$$~~

$$T(1) = k$$

$$T(n) = (a-1) \cdot n \cdot k + k$$

$$= (\log n - 1) \cdot n \cdot k + \frac{k}{\text{neglect}}$$

$$T(n) = \frac{n \cdot k \cdot \log n}{\text{neglect}} - \frac{n \cdot k}{\text{neglect}} = n \cdot \log n = O(n \cdot \log n)$$

```
// merge two sorted arrays
int leftIndex = 0;
int rightIndex = 0;
int mainArrIndex = s;

while(leftIndex < len1 && rightIndex < len2){
    if(leftArr[leftIndex] < rightArr[rightIndex]){
        arr[mainArrIndex] = leftArr[leftIndex];
        mainArrIndex++;
        leftIndex++;
    } else{
        arr[mainArrIndex] = rightArr[rightIndex];
        mainArrIndex++;
        rightIndex++;
    }
}

// copy logic for left arr
while(leftIndex < len1){
    arr[mainArrIndex] = leftArr[leftIndex];
    mainArrIndex++;
    leftIndex++;
}

while(rightIndex < len2){
    arr[mainArrIndex] = rightArr[rightIndex];
    mainArrIndex++;
    rightIndex++;
}

// Clean up memory
delete[] leftArr;
delete[] rightArr;
```

* Quick Sort

Pivot Index 7

8	1	3	4	20	50	30
---	---	---	---	----	----	----

s 0 1 2 3 4 5 6 e

→ Partition logic (1 element ko uski sahi Jagah rakh do)

element choose (Pivot ele)

put it at right location

chote
cles
pivot se left side
set karo

bade
ele
pivot se right side
set karo

PivotIndex = s

contno < pivotElement

count = 0, 1, 2, 3 } 8 ko 4th element hoga chalye

swap(arr[PivotIndex], arr[s+count])

for (s → e)

1 < 8, 3 < 8, 4 < 8

20 < 8 False

S is not going
to be 0 all time

4	1	3	8	20	50	30
---	---	---	---	----	----	----

0 1 2 3 4 5 6

→ Baki recursion sambhal lega

```
void quickSort(int *arr, int n, int s, int e){
    // basecase
    if(s>=e){
        return;
    }

    // partition logic
    int p = partition(arr, s, e);

    // rr
    quickSort(arr, n, s, p-1); // left
    quickSort(arr, n, p+1, e); // right
}
```

4	1	3	8	20	50	30
---	---	---	---	----	----	----

i j

left right

arrange all small
elements less than
pivot element using
two pointer approach

arrange all big
elements which are
bigger than Pivot ele
using tp method

8	1	20	30	6	5	60	5
0	1	2	3	4	5	6	7

j
s

L e

① pivotIndex = s = 0

② count = 0 for ($s \rightarrow e$)
 if (currentEle < pivotEle)
 count++

$1 < 8 \quad T$ $30 < 8 \quad F$ $5 < 8 \quad T$ $5 < 8 \quad T$
 $20 < 8 \quad F$ $6 < 8 \quad T$ $60 < 8 \quad F$

count = 4

so rightIndex = s + count = 0 + 4 = 4

pivot							
i				j			
6	1	20	30	8	5	60	5

0 1 2 3 4 5 6 7

left right

swap (pivotEle, rightIndexEle)

③ if (element > pivot) → in left part {means wrong elements
 then swap (arr[i], arr[j])
 j--

Break when
 $i = j$

if (element < pivot) → in right part
 then swap (arr[i], arr[j])
 i++

```

int partition(int *arr, int s, int e) {
    // 1) choose pivot ele
    int pivotIndex = s;
    int pivotEle = arr[s];

    // 2) find right position for pivot
    int count = 0;
    for (int i = s + 1; i <= e; i++) {
        if (arr[i] <= pivotEle) {
            count++;
        }
    }

    // jab loop se bahar aya to pivot ele ka right position index
    // ready hai
    int rightIndex = s + count;
    swap(arr[pivotIndex], arr[rightIndex]);
    pivotIndex = rightIndex;

    // 3) small in left | big in right
    int i = s;
    int j = e;

    while (i < pivotIndex && j > pivotEle) {
        while (arr[i] <= pivotEle) {
            i++;
        }

        while (arr[j] > pivotEle) {
            j--;
        }

        // two pointer method and swapping to adjust eles
        if (i < pivotIndex && j > pivotEle) {
            swap(arr[i], arr[j]);
        }
    }

    return pivotIndex;
}

```

$$TC = O(n \log n)$$

Recursive tree
try to make as
merge short type

```

vector<int> smaller, greater;

for (int i = s + 1; i <= e; i++) {
    if (arr[i] <= pivotEle) {
        smaller.push_back(arr[i]);
    } else {
        greater.push_back(arr[i]);
    }
}

// Rebuild the array with smaller, pivot, and greater elements
int index = s;
for (int num : smaller) {
    arr[index++] = num;
}

pivotIndex = index; // Correct position of pivot
arr[index++] = pivotEle;

for (int num : greater) {
    arr[index++] = num;
}

return pivotIndex;

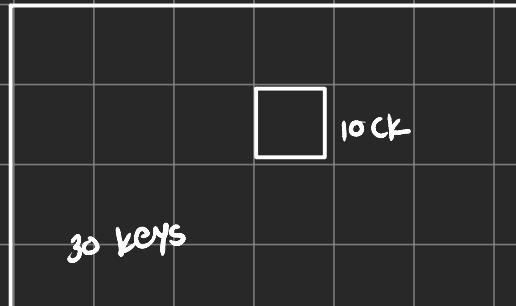
```

```

while (i < pivotIndex && j > pivotIndex) {
    if (arr[i] < pivotEle) {
        i++;
    } else if (arr[j] > pivotEle) {
        j--; // Move to the next element on the right
    } else {
        swap(arr[i], arr[j]);
        i++; // After fixing `i`, move right
        j--; // After fixing `j`, move left
    }
}

```

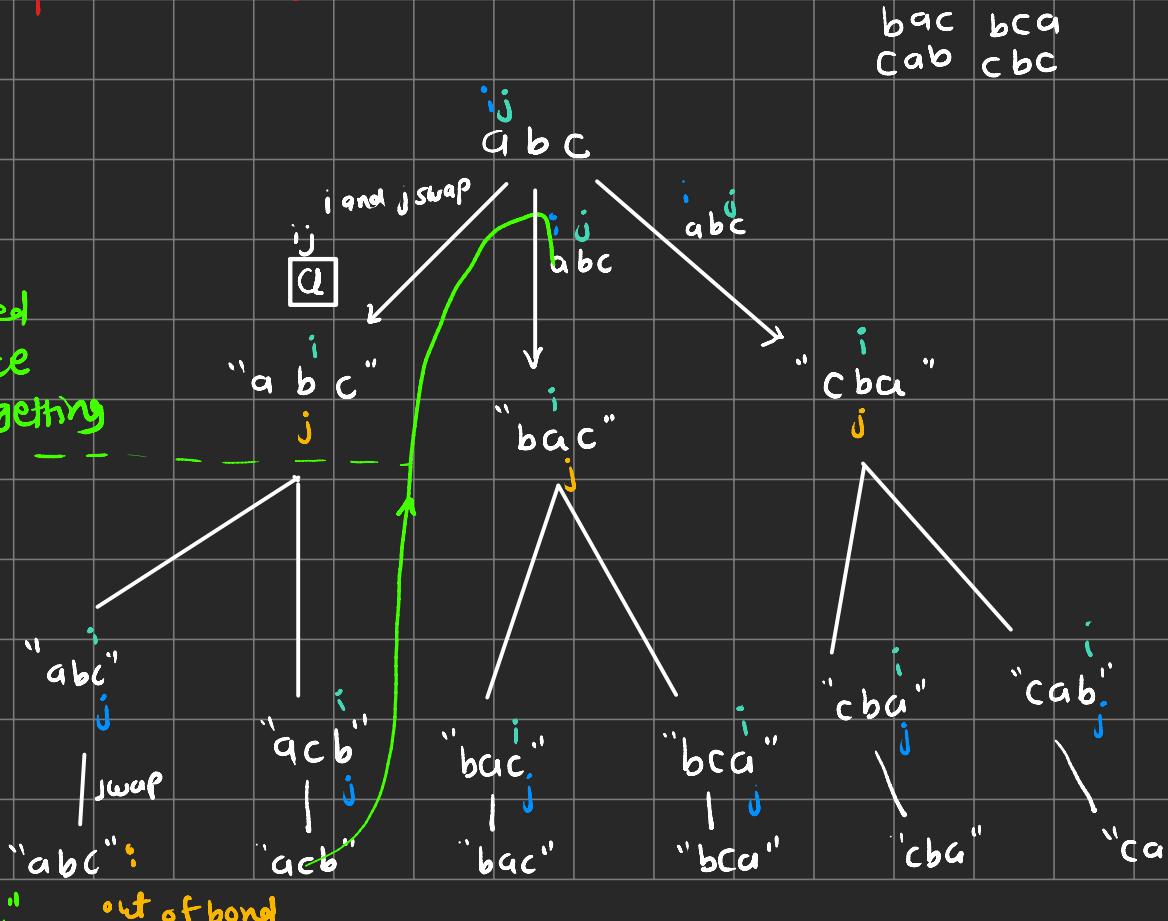
Backtracking



You have to open lock and you have to try all keys one by one to know about which key is answer

* string permutations

string passed by reference so we are getting "acb" as parameter so how to solve? using BU line by swap and make it "abc": original "abc" out of bound



Que - "abc"

abc
bac
cab
acb
bca
cbc

```
void printPermutation(string &str, int i){
    if(i>= str.length()){
        cout << str << " ";
        return;
    }

    for(int j=i; j<str.length(); j++){
        swap(str[i], str[j]); // swap
        printPermutation(str, i+1); // rr
        swap(str[i], str[j]); // BACKTRACKING
    }
}
```

without this line of

abc acb cab cba abc acb
after BU:
abc acb bac bca cba cab

Rat in a Maze

	0	1	2	3
0	start	0	0	0
1	↓	↓ →	0	0
2	↓	↓ →	0	0
3	0	↓ →	end	

0 → Rats blocked way
 1 → Rats open way
 - find all solution to reach destination
 - do not find blocker ways

- rat can move



like

(0,0) → X | L | R | U

↓

(1,0) → X | X | X | U

↓

(1,1) → X | L | R | U

↓

(2,1) → X | L | R | U

↓

(3,1) → X | X | X | U

↓

(3,2) → X | L | R | U

then } Here has just infinite loop me } if visited
 (3,1) } (3,2) ← (3,1) like this } then marking it
 in visited2Darray

start	0	1	0
1	1	1	1
0	1	1	0
0	1	1	0
0	0	1	end

3ways only

maze ^o	1	2	3
0	start	0	0
1	1	1	1
2	0	1	1
3	0	1	1 end

o	1	2	3	visited
0	1	0	0	0
1	1	0	1	0
2	0	1	0	0
3	0	1	1	1

(0,0) → D | L | R | U

↓ visited mark [1][0] = true

(1,0) → X | * | R | U

↓ visited [1][1] = true

(1,1) → D | L | R | U

↓ visited [2][1] = true

(2,1) → D | L | R | U

↓ visited [3][1] = true

(3,1) → X | X | R | U

check down is possible?

— index inside array

— that index value should be 1

— not visited hona chahiye

if you are on (i,j) then

D = (i+1, j)

L = (i, j-1)

R = (i, j+1)

U = (i-1, j)

mark unvisited

mark unvisited

mark unvisited

mark unvisited
mark unvisited to all
that we did before

while coming BACK

visited [3][2] = true

(3,2) X | X | R | U
visited already

visited [2][3]

→ Base condition
destination pahunch gaya

(3,3) D | L | R | U

```

int main() {
    // Initialize the maze
    int maze[3][3] = {
        {1, 0, 0},
        {1, 1, 0},
        {1, 1, 1}
    };

    int row = 3;
    int col = 3;

    // Create a visited array and mark the source as visited
    vector<vector<bool>> visited(row, vector<bool>(col, false));
    visited[0][0] = true; // Mark the source value as true

    // Prepare to store paths
    vector<string> path;
    string output = "";

    // Solve the maze
    solveMaze(maze, row, col, 0, 0, visited, path, output);

    // Print all possible paths
    for (auto i : path) {
        cout << i << " ";
    }

    return 0;
}

```

```

void solveMaze(int arr[3][3], int row, int col, int i, int j, vector<vector<bool>> &visited, vector<string> &path, string output) {
    // base case
    if (i == row - 1 && j == col - 1) {
        path.push_back(output);
        return;
    }

    // down -> i+1, j
    if (isSafe(i + 1, j, row, col, arr, visited)) {
        visited[i + 1][j] = true;
        solveMaze(arr, row, col, i + 1, j, visited, path, output + 'D');
        visited[i + 1][j] = false; // BACKTRACK
    }

    // left -> i, j-1
    if (isSafe(i, j - 1, row, col, arr, visited)) {
        visited[i][j - 1] = true;
        solveMaze(arr, row, col, i, j - 1, visited, path, output + 'L');
        visited[i][j - 1] = false; // BACKTRACK
    }

    // right -> i, j+1
    if (isSafe(i, j + 1, row, col, arr, visited)) {
        visited[i][j + 1] = true;
        solveMaze(arr, row, col, i, j + 1, visited, path, output + 'R');
        visited[i][j + 1] = false; // BACKTRACK
    }

    // up -> i-1, j
    if (isSafe(i - 1, j, row, col, arr, visited)) {
        visited[i - 1][j] = true;
        solveMaze(arr, row, col, i - 1, j, visited, path, output + 'U');
        visited[i - 1][j] = false; // BACKTRACK
    }
}

```

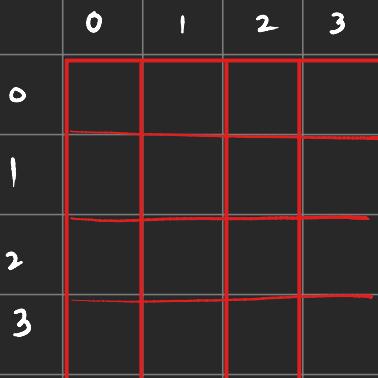
```

bool isSafe(int i, int j, int row, int col, int arr[][3], vector<vector<bool>> &visited) {
    if ((i >= 0 && i < row) && (j >= 0 && j < col) && (arr[i][j] == 1) && (visited[i][j] == false)) {
        return true;
    }
    return false;
}

```

TC \Rightarrow Exponential (4 calls DLRU)

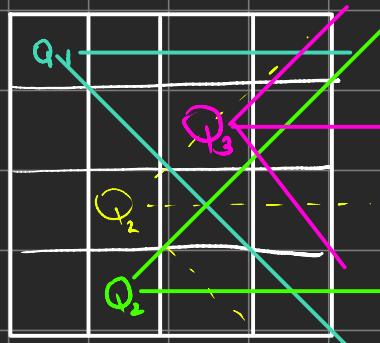
N queen



$n \times n$
so place n queens

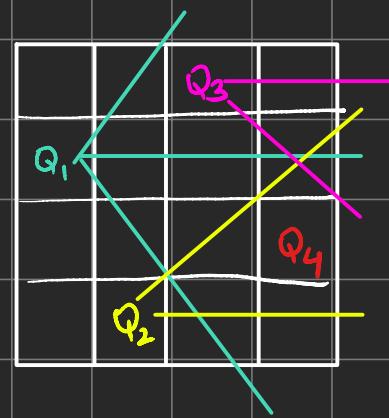


set N-queen in such a way so that no queen can attack the other queen

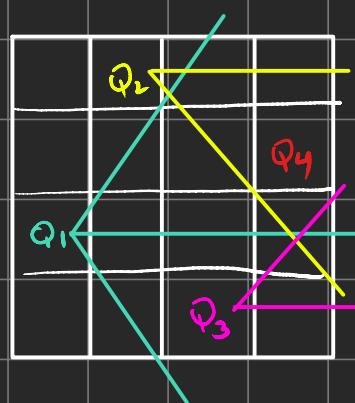


if I place Q_2 there
then for Q_3 all ways
are blocked So go down
for Q_2

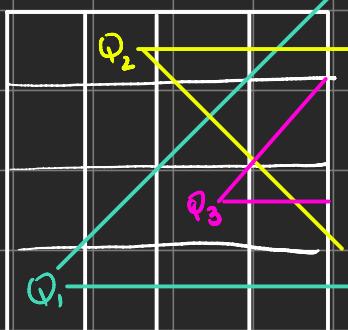
not possible



all placed



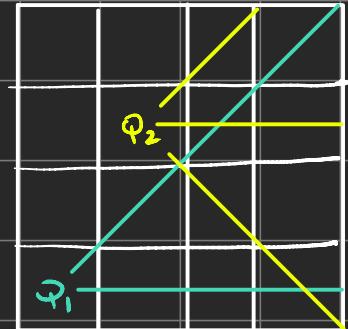
all placed



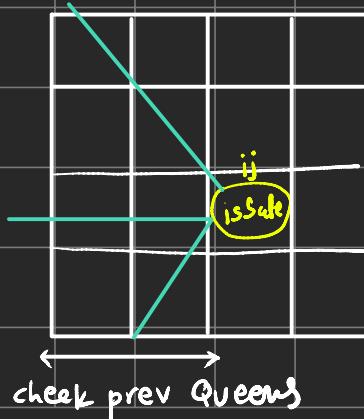
with this not possible

so think that we did
some mistake while
organizing Q_3, Q_2 in past
for Q_3 only one place was there
for Q_2 there was two place so change

Explained more in last case



Gab Q3 ke liye jagah nahi so
pichli placement mei galti hai
for Q2 we tried both but not
working for Both ways
so piche jao aur Q1 we tried all
before so leve it.



```
void solve(vector<vector<int>> &board, int col, int n) {  
    // Base case  
    if (col >= n) {  
        printSolution(board, n);  
        return;  
    }  
  
    // Place queen in each row of the current column  
    for (int row = 0; row < n; row++) {  
        if (isSafe(row, col, board, n)) {  
            board[row][col] = 1; // Place queen  
            solve(board, col + 1, n); // Recur for next column  
            board[row][col] = 0; // Backtrack  
        }  
    }  
}  
  
void printSolution(vector<vector<int>> &board, int n) {  
    for (int i = 0; i < n; i++) {  
        for (int j = 0; j < n; j++) {  
            // cout << board[i][j] << " ";  
            cout << (board[i][j] == 1 ? "Q " : ". ");  
        }  
        cout << endl;  
    }  
    cout << endl;  
}
```

```
bool isSafe(int row, int col, vector<vector<int>> &board, int n) {  
    // check current cell [i][j] par queen rakh saka hoon  
    int i = row, j = col;  
  
    // Check row on left  
    while (j >= 0) {  
        if (board[i][j] == 1)  
            return false;  
        j--;  
    }  
  
    // Check upper left diagonal  
    i = row, j = col;  
    while (i >= 0 && j >= 0) {  
        if (board[i][j] == 1)  
            return false;  
        i--;  
        j--;  
    }  
  
    // Check lower left diagonal  
    i = row, j = col;  
    while (i < n && j >= 0) {  
        if (board[i][j] == 1)  
            return false;  
        i++;  
        j--;  
    }  
  
    return true;  
}
```

optimization issafer \rightarrow TC $O(n)$ \rightsquigarrow how to make it $O(1)$

by using Map \rightarrow DS. that stores key value pair and It has TC $O(1)$

while adding Queen

do like $\text{map}[\text{rowNo}] = \text{true}$

so In issafer we can check

for row like If ($\text{map}[i] == \text{true}$)

its True means that row has Queen

map < string, int > m ;
key value

	0	1	2	3
0	0	1	2	3
1	1	2	3	4
2	2	3	4	5
3	3	4	5	6

no = row + col

For bottomleft diagonal,

make another new map with pattern of no.

check like IF ($\text{map}[i+j] == \text{true}$)

its True means that row has Queen

INPUT : m ["love"] = 98 love \rightarrow 98

m ["babbar"] = 36 babbar \rightarrow 36

Access : cout << m ["love"]

	0	1	2	3
0	4	5	6	7
1	3	4	5	6
2	2	3	4	5
3	1	2	3	4

n=4
no = (n-1) + col - row

For uppleft diagonal,

make another new map with pattern of no.

IF ($\text{map}[(n-1)+\text{col}-\text{row}] == \text{true}$)

n=4

Generate Parentheses

$n=1$ $()$ $) ($
 no of Brackets ✓ X (not parenthesis)

$n=2$ $(())$ $(())$
 $(\rightarrow 1$ $) \rightarrow 1$

$n=3$ $(((()))$ $(((()))$ $(((()))$ $(((()))$ $(((()))$ 5

1

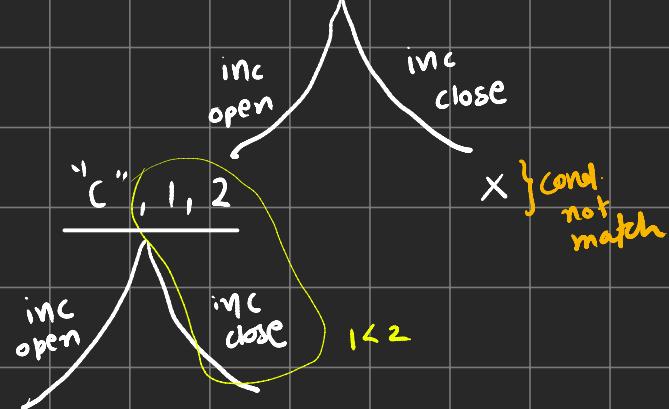
2

If $(open > 0)$
 then include
 open bracket

output "", 2, 2 — closing brackets

open bracket

2, 2 — closing brackets

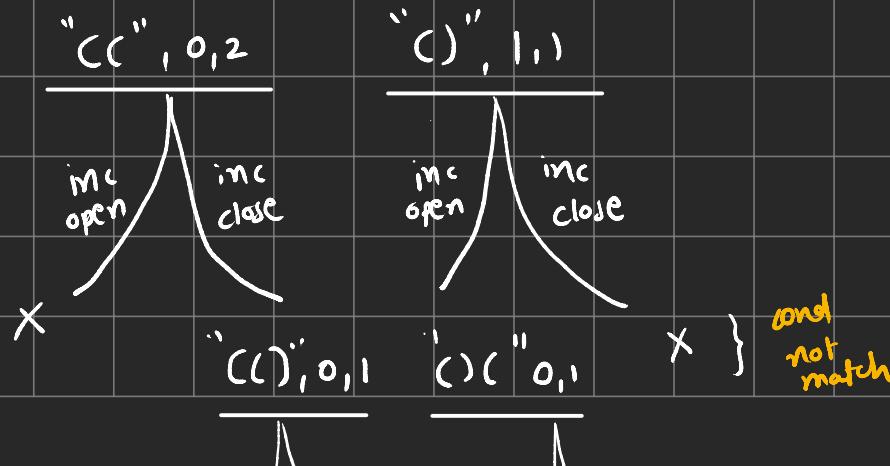


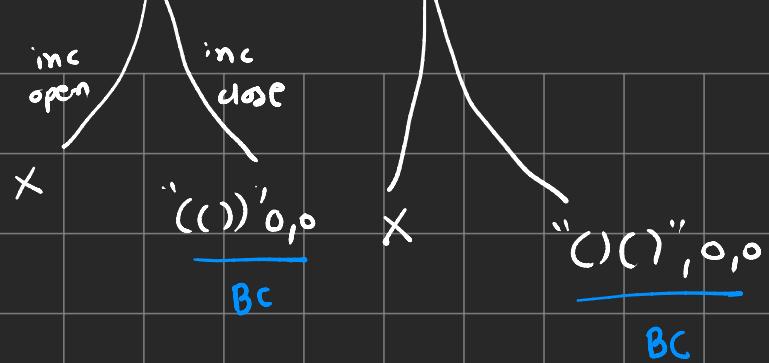
condition to include closing bracket

_____)
 left

open close
 brackets brackets

for upcoming
 _____ brackets
 right part remaining
 open < close } brackets





```

void solve(vector<string> &ans, int n, int open, int close, string output){
    // base case
    if( open<=0 && close<=0 ){
        ans.push_back(output);
        return;
    }

    // rr
    // include open bracket
    if(open>0){
        // output.push_back('(');
        // solve(ans, n, open-1, close, output);
        // output.pop_back(); // backtracking

        solve(ans, n, open-1, close, output + '(');

        // include close bracket
        if(open<close){
            // output.push_back(')');
            // solve(ans, n, open, close-1, output);
            // output.pop_back(); // backtracking

            solve(ans, n, open, close-1, output + ')' );
        }
    }
}

```

Letter combination of Phone number

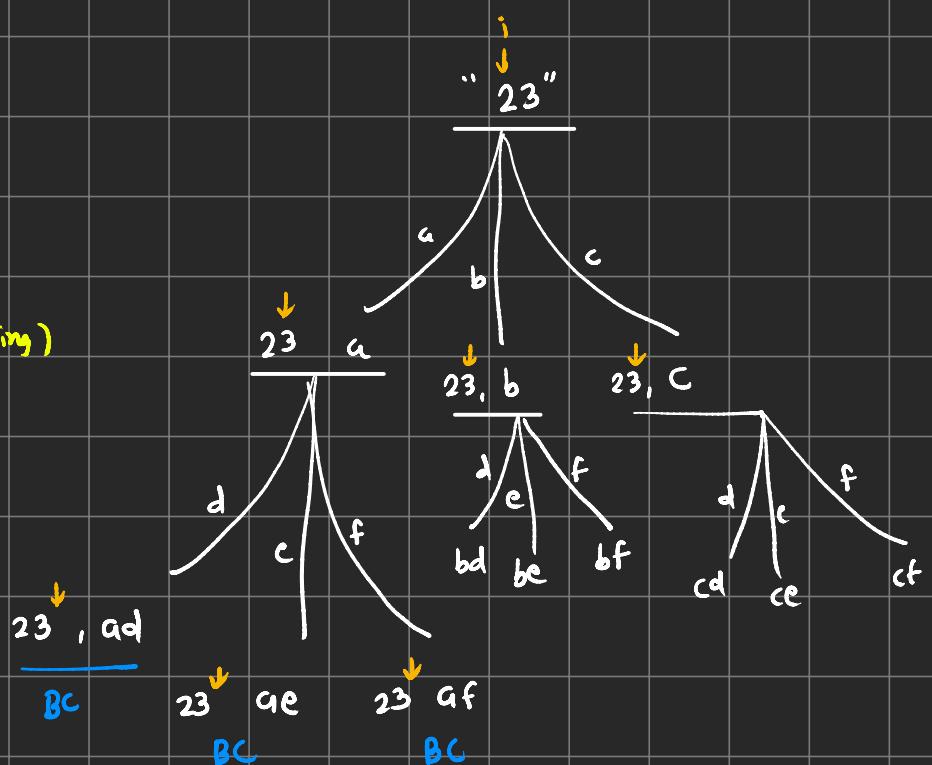
```

void solve(vector<string> &ans, int index, string output, string digits, vector<string> mapping) {
    // base case
    if (index >= digits.length()) {
        ans.push_back(output);
        return;
    }

    // rr
    int digit = digits[index] - '0'; // int convert
    string value = mapping[digit];
    for (int i = 0; i < value.length(); i++) {
        char ch = value[i];
        output.push_back(ch);
        solve(ans, index + 1, output + ch, digits, mapping);
        output.pop_back(); // backtracking
    }
}

```

} solve (ans, i+1, output + ch, digits, mapping)
without BK



```

vector<string> letterCombinations(string digits) {
    vector<string> ans;
    if (digits.length() == 0) {
        return ans;
    }

    int index = 0;
    string output = "";

    vector<string> mapping(10);
    mapping[2] = "abc";
    mapping[3] = "def";
    mapping[4] = "ghi";
    mapping[5] = "jkl";
    mapping[6] = "mno";
    mapping[7] = "pqrs";
    mapping[8] = "tuv";
    mapping[9] = "wxyz";

    solve(ans, index, output, digits, mapping);

    return ans;
}

```

count Inversion

{ 8, 4, 2, 1 }
i j

Inversion kab hoga?

i < j

$a[i] > a[j]$

{ 8, 4, 2, 1 } → descending sorted array hai so main to ye sorted nahi hai

(8,4) (4,2) (2,1)
(8,2) (4,1)
(8,1)

(8,4) { 8, 4, 2, 1 }

(8,2) { 4, 8, 2, 1 }

(8,1) { 4, 2, 8, 1 }

{ 4, 2, 1, 8 } → this array
more close
to sorted array

{ 4, 2, 1, 8 } (4,2)

{ 2, 4, 1, 8 } (4,1)

{ 2, 1, 4, 8 } (2,1)

{ 1, 2, 4, 8 } → sorted
after all
inversions

so isko sorted
karne k liye kitne
inversions
(swapping)
chiye honge

Simple approach

{ 8, 4, 2, 1 }

i j

TC = O(n²)

SC = O(1)

for (i=0 → end) {

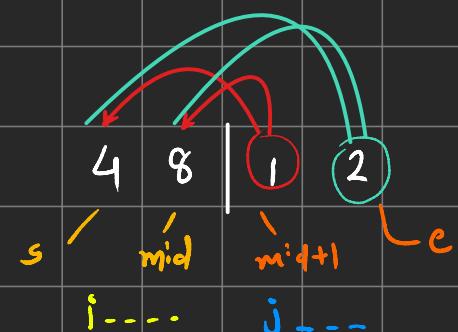
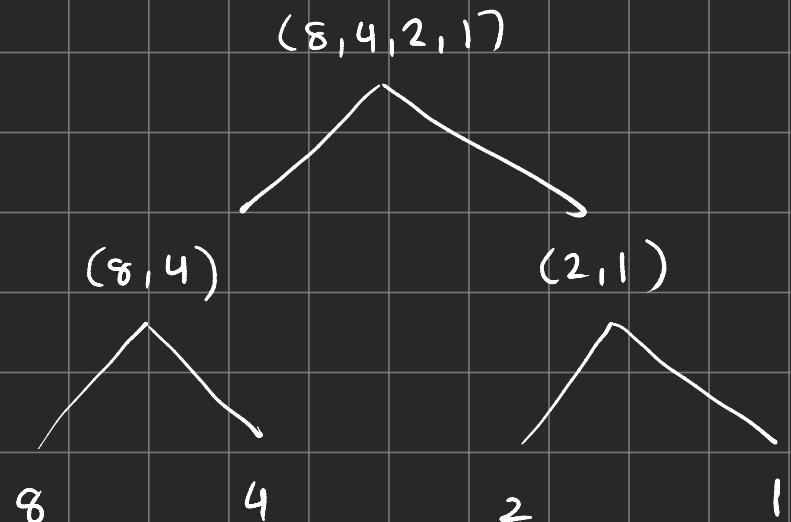
for (j=i+1 → end) {

if (i < j && arr[i] > arr[j]) → count++

}

}

In MergeSort

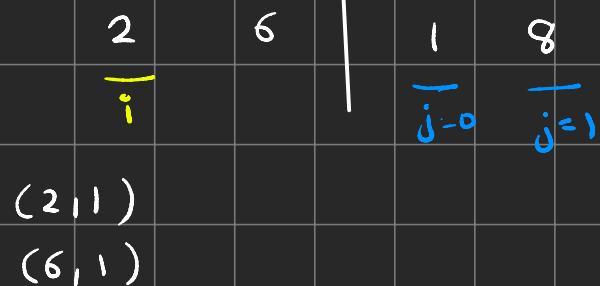


if (arr[i] > arr[j])

(4,1) (4,2)

(8,1) (8,2)

count = mid - i + 1



```

long merge(vector<int> &arr, vector<int> &temp, int s, int mid, int e){
    int i = s, j = mid + 1, k = s;

    long count = 0;

    while( i <= mid && j <= e ){
        if( arr[i] <= arr[j]){
            temp[k++] = arr[i++];
        }
        else{ // arr[j] > arr[i] // INVERSION COUNT CASE
            temp[k++] = arr[j++];
            count = count + (mid - i + 1);
        }
    }

    while (i <= mid){
        temp[k++] = arr[i++];
    }

    while(j <= e){
        temp[k++] = arr[j++];
    }

    // copy temp array to original array
    while(s <= e){
        arr[s] = temp[s];
        s++;
    }

    return count;
}

```

when $j=0 \rightarrow a[i] > a[j] = \text{True}$
and during this left array is going to
be sorted every time so all combinations
on left side are counted as inversion

(2,1)
(6,1)

when $j=1 \rightarrow a[i] > a[j] = \text{False}$

```

long mergeSort(vector <int> &arr, vector <int> &temp, int s, int e){
    long count = 0;
    if(s == e){
        return 0;
    }

    int mid = s + (e - s) / 2;

    count += mergeSort(arr, temp, s, mid);
    count += mergeSort(arr, temp, mid + 1, e);

    count += merge(arr, temp, s, mid, e);

    return count;
}

```

In Place Merge Sort \rightarrow In merge sort we are using temp array that creates space complexity of $O(n)$
so how to do it with $O(1)$

Method ①

$i \quad i \quad i$

1 2 8 9 12 13 \rightarrow arr1

0 \swarrow swap

3 4 7 10 \rightarrow arr2

if ($a[i] < a[j]$) then nothing

else {

swap ($a[i], a[j]$)

i

1 2 3 9 12 13 \rightarrow arr1

8 4 7 10 \rightarrow arr2 }

} this array is not sorted bcz of 8

so use PARTITION METHOD from quicksort.

.

i

1 2 3 9 12 13 \rightarrow arr1

4 7 8 10 \rightarrow arr2

1 2 3 4 12 13

9 7 8 10

1 2 3 4 12 13
 7 8 9 10

i
 1 2 3 4 7 13
 8 9 10 12

1 2 3 4 7 8
 9 10 12 13

totalLength

$$\left(\frac{(n+m)}{2} \right) + \left(\frac{(n+m)}{2} \cdot 0.2 \right)$$

or

Method ② GAP method

$$\text{gap} = \lceil \text{ceil} \left(\frac{(n+m)}{2} \right) \rceil$$

$$\text{ceil do } 2 \cdot 7 \approx 3$$

1 2 8 9 12 13 $\rightarrow n=6$

3 4 7 10 $\rightarrow n=4$



if ($a[i] > a[j]$)
 ↳ do swap

$$\text{gap} = \frac{4+5}{2} = 5$$

$$\text{index } j = i + \text{gap} = 0 + 5 = 5$$

$i > j$ False $i++$
 $j++$



$i > j$ False $i++$
 $j++$

$8 > 4$ True swap
 $i++$
 $j++$

$9 > 7$ True swap
 $i++$
 $j++$

$12 > 10$ True swap
 $i++$
 $j++$

$$\text{updated GAP} = \text{ceil} \left(\frac{\text{gap}}{2} \right) = \frac{5}{2} = 2.5 \approx 3$$

$$j = i + \text{gap}$$

$$= 0 + 2$$



same
 $i > j$ F

$7 > 3$ T swap

$$\text{updated Gap} = \lceil \text{ceil}(gap/2) \rceil = \lceil 3/2 \rceil = 1.5 \approx 2$$

do same
again

1	2	4	3	8	9	7	10	13	12
0	1	2	3	4	5	6	7	8	9

$$\text{updated Gap} = \text{ceil}(gap/2) = (2/2) = 1$$

1	2	4	3	8	9	7	10	13	12
---	---	---	---	---	---	---	----	----	----

do same
again

```

void mergeInPlace(int *arr, int s, int e){

    int totalLength = (e-s) + 1;
    int gap = (totalLength/2) + (totalLength%2);

    while (gap>0)
    {
        int i = s;
        int j = s+gap;

        while(j<=e){
            if(arr[i]>arr[j]){
                swap(arr[i],arr[j]);
            }
            i++;
            j++;
        }

        // gap agar 1 hai to usko break karne k liye 0 de diya
        gap = gap<=1 ? 0 : ((gap/2) + (gap%2));
    }
}

```

$$\text{updated Gap} = \text{ceil}(gap/2) = \lceil 1/2 \rceil = 0.5 = \underline{\underline{1}}$$

again 1 so
stop at 1

Merge two arrays

```
void merge(vector<int> &a, vector<int> &b) {  
    int n = a.size();  
    int m = b.size();  
    int total_len = n + m;  
    int gap = (total_len / 2) + (total_len % 2);  
  
    while (gap > 0) {  
        int i = 0, j = gap;  
  
        while (j < total_len) {  
            // Compare elements in the first array  
            if (j < n && a[i] > a[j]) {  
                swap(a[i], a[j]);  
            }  
            // Compare elements across both arrays  
            else if (j >= n && i < n && a[i] > b[j - n]) {  
                swap(a[i], b[j - n]);  
            }  
            // Compare elements in the second array  
            else if (j >= n && i >= n && b[i - n] > b[j - n]) {  
                swap(b[i - n], b[j - n]);  
            }  
  
            i++;  
            j++;  
        }  
        gap = gap <= 1 ? 0 : (gap / 2) + (gap % 2);  
    }  
  
    int main() {  
        vector<int> arrA = {1, 2, 8, 9, 12, 13};  
        vector<int> arrB = {3, 4, 7, 10};  
  
        merge(arrA, arrB);  
  
        cout << "Merged arrays: ";  
        for (int num : arrA) {  
            cout << num << " ";  
        }  
        for (int num : arrB) {  
            cout << num << " ";  
        }  
    }  
}
```

Here arrA and arrB both are different

(inplace merge has single array that we cut into two parts using mid)

1,2,3,4,7,8,9,10,12,13

Maximum Subarray Sum → find the subarray with the largest sum and return its sum

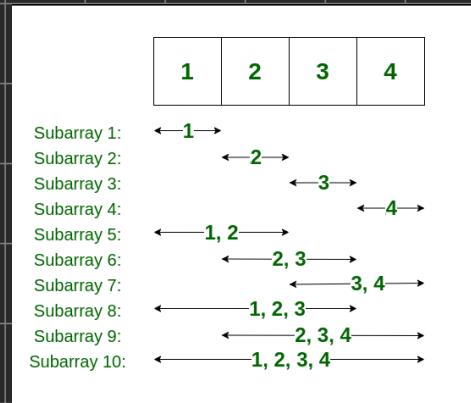
if all elements are positive in array so → the sum of all element is ans

But here in que also negative els are there in array

Method ① → find all subarrays
→ find max of them

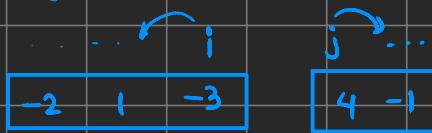
```
for (i=0 → len)
    for (j=0 → len)
        for (k=i → j) }
```

$O(n^3)$



Method ②

CSS finding



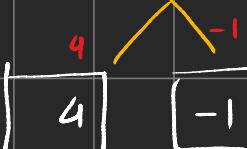
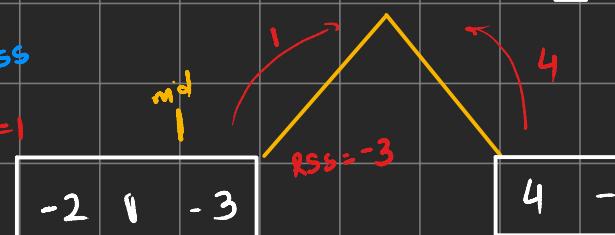
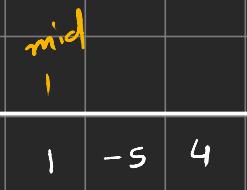
$$\begin{aligned} -3 &= 4 \\ -3+1 &= -2 \\ -3+1-2 &= -4 \end{aligned}$$

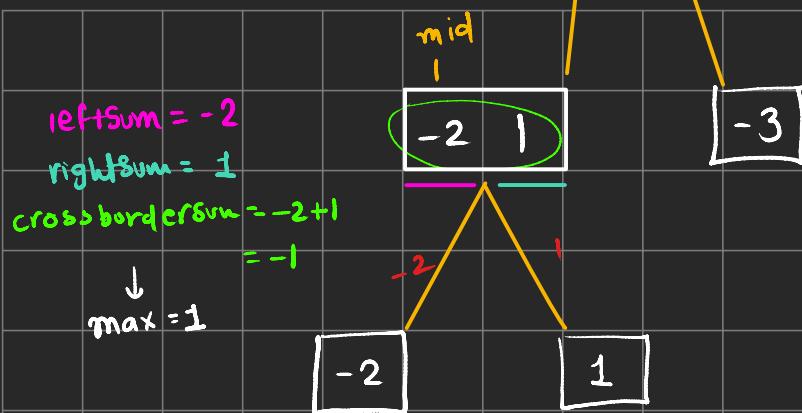
$\max(-2)$

$$\begin{aligned} = 4 & \\ = 4-1 &= 3 \end{aligned}$$

$\max(4)$

$$\begin{aligned} -2, 1 \rightarrow \max & \\ \text{is } 1 & \end{aligned}$$





```

int maxSubArray(vector<int> &arr, int s, int e) {
    // Base case: single element
    if (s == e) {
        return arr[s];
    }

    int maxOfLeftBorderSum = INT_MIN;
    int maxOfRightBorderSum = INT_MIN;

    int mid = (s + e) / 2;

    // Recursively find the maximum sum in the left and right halves
    int maxLeftSum = maxSubArray(arr, s, mid);
    int maxRightSum = maxSubArray(arr, mid + 1, e);

    // Calculate maximum cross-border sum
    int leftBorderSum = 0;
    for (int i = mid; i >= s; i--) {
        leftBorderSum += arr[i];
        maxOfLeftBorderSum = max(maxOfLeftBorderSum, leftBorderSum);
    }

    int rightBorderSum = 0;
    for (int i = mid + 1; i <= e; i++) {
        rightBorderSum += arr[i];
        maxOfRightBorderSum = max(maxOfRightBorderSum, rightBorderSum);
    }

    int crossBorderSum = maxOfLeftBorderSum + maxOfRightBorderSum;

    // Return the maximum of the three cases
    return max(maxLeftSum, max(maxRightSum, crossBorderSum));
}

```

Quick Sort (end element as pivot)

→ Partitioning

→ pivot = end

pivot = 7

→ i = s - 1

j = s

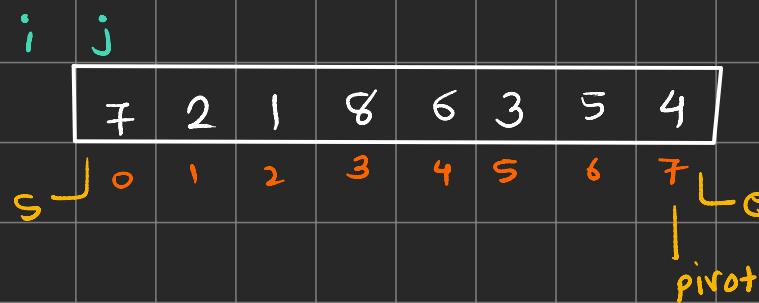
→ set smaller ele left of pivot and bigger to right of pivot

if ($a[j] \geq a[\text{pivot}]$) → j++

else → i++

→ swap($a[i], a[j]$)

→ j++



here i is right
position of pi

```
void quickSort(int a[], int start, int end)
{
    if(start >= end) return;
    int pivot = end;
    int i = start - 1;
    int j = start;

    while(j < pivot){
        if(a[j] < a[pivot]){
            ++i;
            swap(a[i], a[j]);
        }
        ++j;
    }
    ++i;
    swap(a[i], a[pivot]);
    quickSort(a, start, i - 1);
    quickSort(a, i + 1, end);
}
```

while ($j < \text{pivot}$)

{

if ($a[j] < a[\text{pivot}]$)

{

i++

swap($a[i], a[j]$)

}

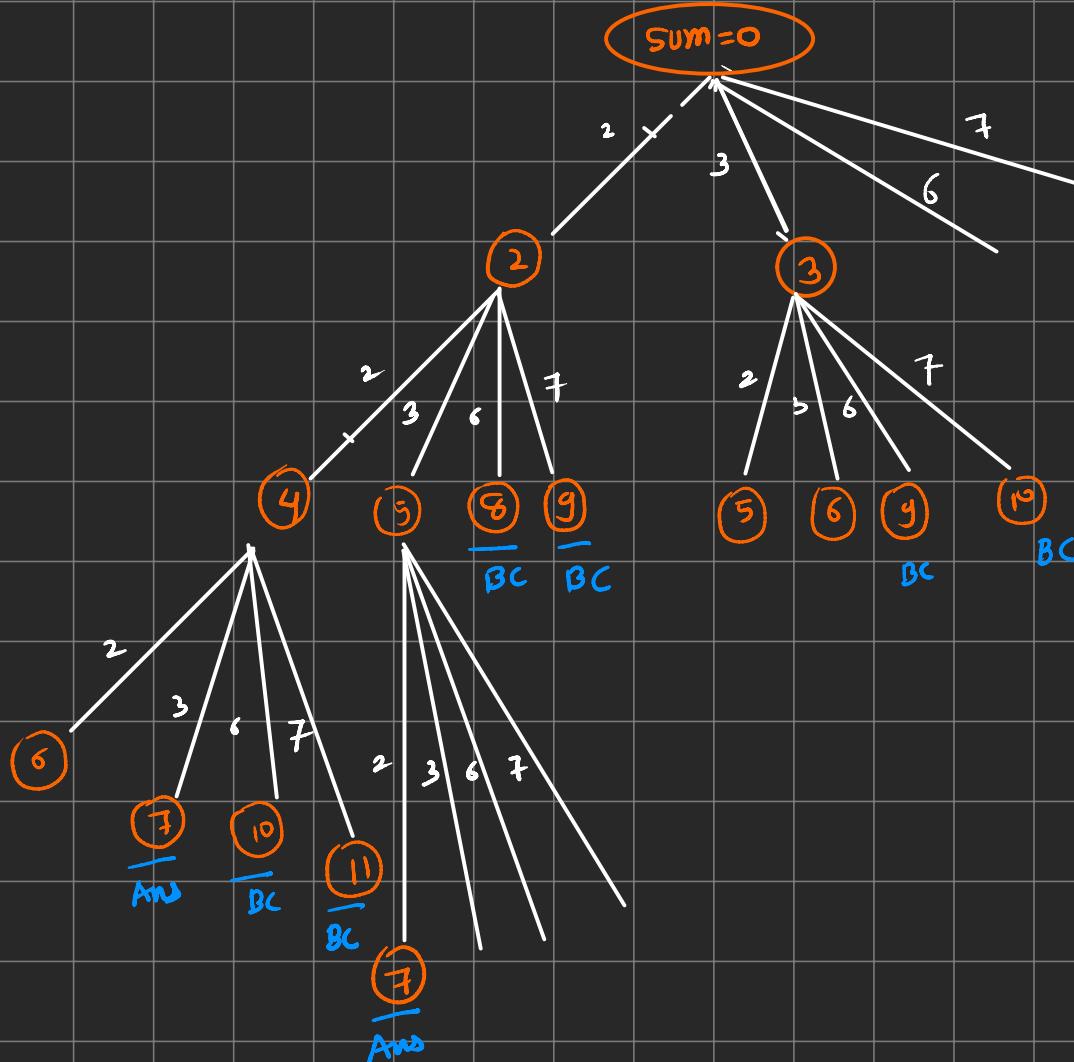
i++

swap($a[i], a[\text{pivot}]$)

* combination Sum

ex. 2 | 3 | 6 | 7 , target = 7

(2,2,3) → 7
(7) → 7



```
void findCombinations(int sum, vector<int>& candidates, int target, vector<int>& current, vector<vector<int>>& result) {
    // bc
    if( sum == target ){
        cout << " matched target" << endl;
        result.push_back(current);
        return ;
    }

    if( sum > target ){
        return;
    }

    // rr
    for( int i=0; i<candidates.size(); i++ ){
        current.push_back(candidates[i]);
        findCombinations(sum+candidates[i], candidates, target, current, result);
        current.pop_back();
    }
}

vector<vector<int>> combinationSum(vector<int>& candidates, int target) {
    vector<vector<int>> result;
    vector<int> current;

    // Start backtracking
    findCombinations(0, candidates, target, current, result);

    return result;
}
```

Combinations that sum to 7 are:

- [2 2 3]
- [2 3 2]
- [3 2 2]
- [7]

How to avoid this?

```
void findCombinations(int sum, vector<int>& candidates, int target, vector<int>& current, vector<vector<int>>& result, int indexNow) {  
    // bc  
    if( sum == target ){  
        cout << " matched target" << endl;  
        result.push_back(current);  
        return ;  
    }  
  
    if( sum > target ){  
        return;  
    }  
  
    // rr  
    for( int i=indexNow; i<candidates.size(); i++ ){  
        current.push_back(candidates[i]);  
        findCombinations(sum+candidates[i], candidates, target, current, result, i);  
        current.pop_back();  
    }  
  
}  
  
vector<vector<int>> combinationSum(vector<int>& candidates, int target) {  
    vector<vector<int>> result;  
    vector<int> current;  
  
    // Start backtracking  
    findCombinations(0, candidates, target, current, result, 0);  
  
    return result;  
}
```

```
Combinations that sum to 7 are:  
[ 2 2 3 ]  
[ 7 ]
```

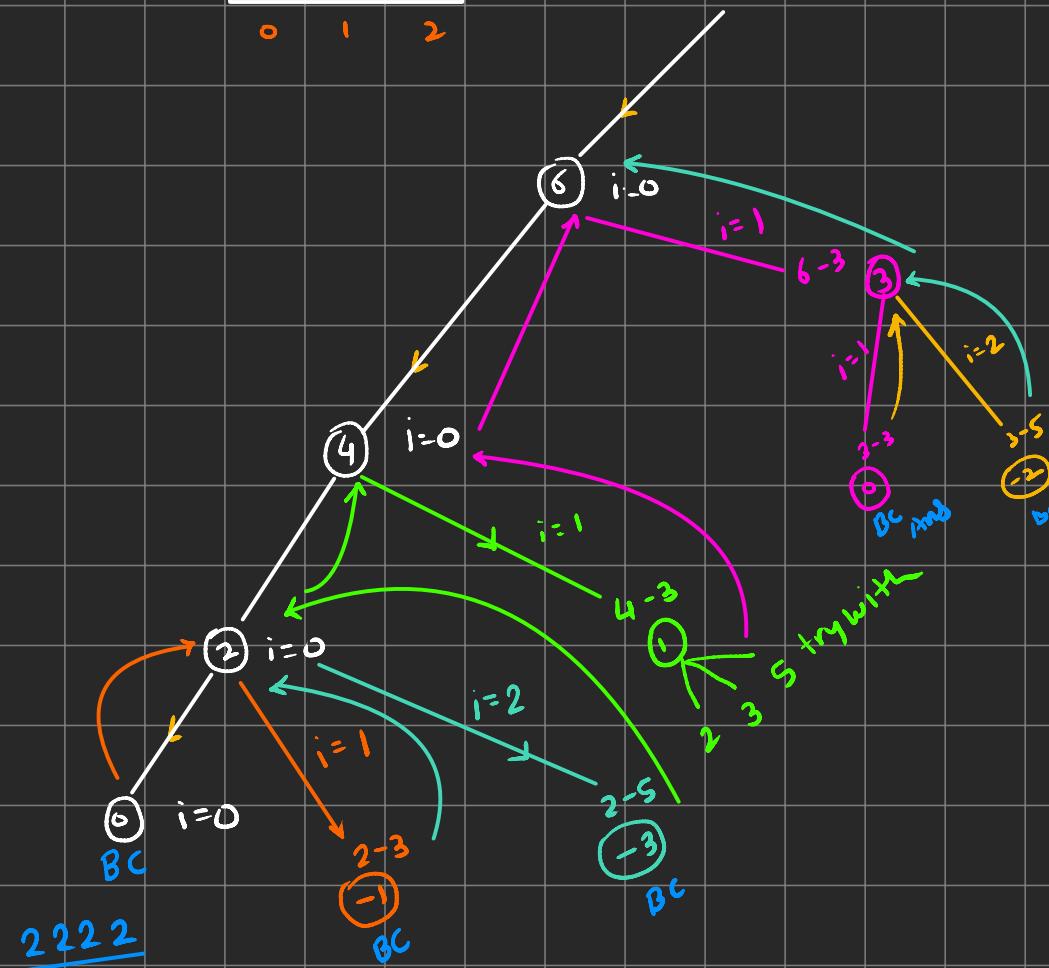
so every time that stops
from coming with that
index again like

consider that same num
again

loop starts from Index
not 0 everytime

2 | 3 | 5

$$\text{target} = 8, \quad i = 0$$



Combination Sum II

→ Each candidate only be picked / used once
 → no duplicates combination

```
void findCombinations(int sum, vector<int>& candidates, int target, vector<int>& current, vector<vector<int>>& result, int indexNow) {
    // bc
    if( sum == target ){
        cout << " matched target" << endl;
        result.push_back(current);
        return ;
    }

    if( sum > target ){
        return;
    }

    // rr
    for( int i=indexNow; i<candidates.size(); i++ ){
        current.push_back(candidates[i]);
        findCombinations(sum+candidates[i], candidates, target, current, result, i+1); // i+1
        current.pop_back();
    }
}

vector<vector<int>> combinationSum(vector<int>& candidates, int target) {
    vector<vector<int>> result;
    vector<int> current;

    // Start backtracking
    findCombinations(0, candidates, target, current, result, 0);

    return result;
}
```

→ Each candidate only be used once

target=5

2 5 2 1 2



After using go to next element by i+1

↓ getting

① 2 2 1

→ sort the give array so we got all outputs in some order

② 2 1 2

use SET map

③ 5

④ 2 1 2

→ }

use SET map

```

vector<int> candidates = {2, 5, 2, 1, 2};
int target = 5;

// to get unique ans ✓
sort(candidates.begin(), candidates.end());

vector<vector<int>> result = combinationSum(candidates, target);

// using SET map to get unique ans ✓
set<vector<int>> st;
for(auto e: result){
    st.insert(e);
}

result.clear();

for(auto ele: st){
    result.push_back(ele);
}

```

} gives TLE

In sorted que

1	2	2	2	5
---	---	---	---	---

i-1 i



when we are here it is going to give same ans as that (i-1) if i = i-1 same element

```

for(int i=index;i<candidates.size();i++){
    if(i > index && candidates[i] == candidates[i - 1]){
        continue;
    }
    v.push_back(candidates[i]);
    combinationSum_helper(candidates,target-candidates[i],v,ans,i + 1);
    v.pop_back();
}

```

* Permutation - II

→ no duplicates allowed

→ can use set method as above but taking long time

```
void permuteUniqueHelper(vector<int>& nums, vector<vector<int>>& ans, int start){  
    //base  
    if(start == nums.size()) {  
        ans.push_back(nums);  
        return;  
    }  
  
    unordered_map<int, bool> visited;  
    for(int i = start; i < nums.size(); i++) {  
        if(visited.find(nums[i]) != visited.end()) {  
            continue;  
        }  
        visited[nums[i]] = true;  
        swap(nums[i], nums[start]);  
        permuteUniqueHelper(nums, ans, start + 1);  
        swap(nums[i], nums[start]);  
    }  
}
```

} means → num[i] ko ekbaar start & saath swap
kiya hai to dubara nahi karunga to avoid
duplicates

Beautiful Arrangement

$1 \leq i \leq n$ means — one indexed array

→ $\text{perm}[i]$ is divisible by $i \rightarrow \text{perm}[i] \% i == 0$

or i is divisible by $\text{perm}[i] \rightarrow i \% \text{perm}[i] == 0$

Brute Force

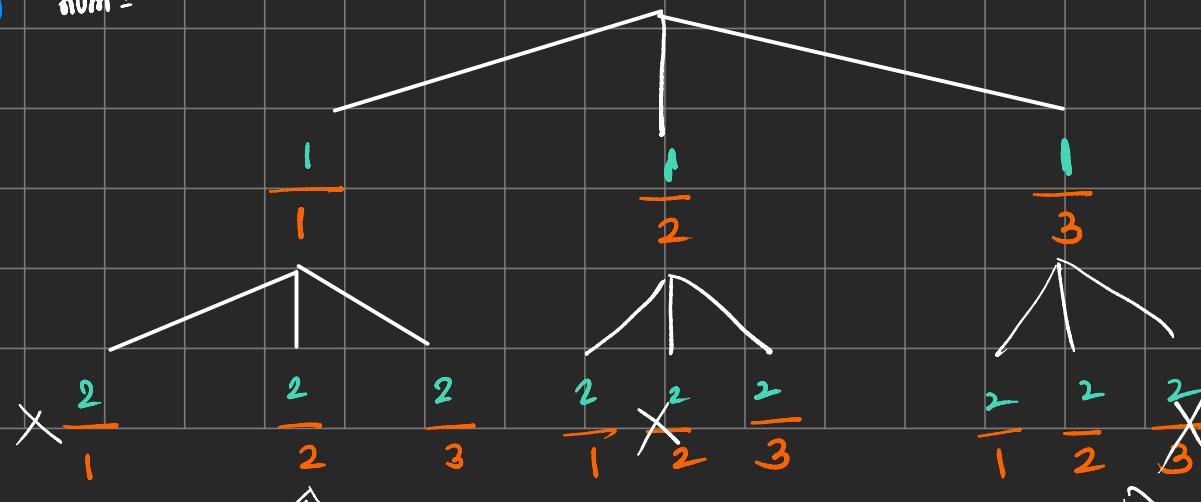
$$\rightarrow \begin{matrix} 1 & 3 & 2 \\ \text{Index} & 1 & 2 & 3 \end{matrix} \quad \begin{array}{c|c} 1 \% 1 == 0 & \checkmark \\ \hline 3 \% 2 \neq 0 & \times \end{array} \quad \begin{array}{c|c} 1 \% 1 == 0 & \checkmark \\ \hline 2 \% 3 \neq 0 & \times \end{array}$$

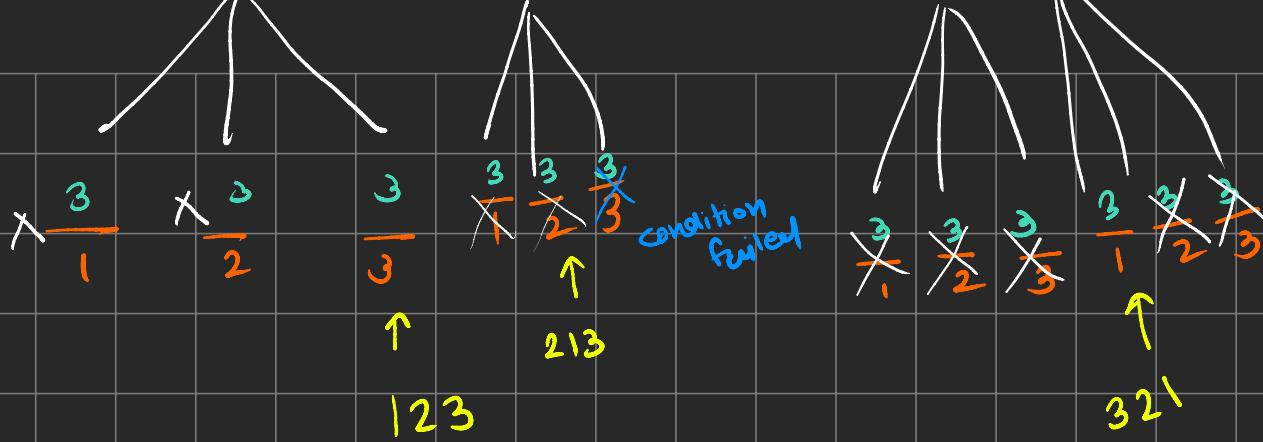
→ not beautiful arrangement

$$\rightarrow \begin{matrix} 3 & 2 & 1 \\ 1 & 2 & 5 \end{matrix} \quad \begin{array}{c|c} 3 \% 1 == 0 & \checkmark \\ \hline 2 \% 2 == 0 & \checkmark \\ \hline 1 \% 3 \neq 0 & \times \end{array} \quad \begin{array}{c|c} 1 \% 3 \neq 0 & \times \\ \hline 2 \% 1 == 0 & \checkmark \\ \hline 3 \% 5 \neq 0 & \times \end{array}$$

so, Yes BA.

Optimal (BK) num =





Ans = 3 Beautiful Arrangements

```

void counterHelper(vector<int>& v, int& n, int& ans, int currNum) {
    // Base case
    if (currNum == n + 1) {
        ans++;
        for (int i = 1; i <= n; i++) {
            cout << v[i] << " ";
        }
        cout << endl;
        return;
    }

    // Try placing `currNum` in each valid position
    for (int i = 1; i <= n; i++) {
        if (v[i] == 0 && (currNum % i == 0 || i % currNum == 0)) {
            v[i] = currNum; // Place `currNum`
            counterHelper(v, n, ans, currNum + 1); // Recurse for the next number
            v[i] = 0; // Backtrack
        }
    }
}

int countArrangement(int n) {
    vector<int> v(n + 1, 0); // Vector to track used positions (1-based indexing)
    int ans = 0; // To count valid arrangements
    counterHelper(v, n, ans, 1);
    return ans;
}

```

Distributing Repeating Integer

1	1	2	2
0	1	2	3

→ nums

2	2
0	1

→ quantity

customer0 wants 2 int and that should be same everytime → so I am allocating 1, 1
 mean total two integers / nums

1 2
 this both should be same

customer1 wants 2 int and that should be same everytime → so 2, 2

1	1	2	2	2	2	3	3
cus0	cus1			↓		↓	

cannot allocate to cus2
 cannot allocate to cus2

2	2	3
0	1	2

→ quantity

cus0 →

1	1
---	---

cus1 →

2	2
---	---

cus2 → needs three nums (cannot allocate)

BackTrack Here

so again with new allocation order

cus0 → [1 1]

cus1 → [3 3]

cus2 → [2 2 2]

[1 1 2 2 2 3 3]

cus0

cus2

cus1

↳ done

[1 1 2 2 2 3 3]



num howmany

1 → 2

2 → 4

3 → 2

counts [1 2 3]
 [2 4 2]
 [0 1 2]

quantity

[2 2 3]
[0 1 2]

index of
quantity
↓
(0, 0)
index of
counts
↓
(1, 1)

→ quantity[0] wants two nums that can be satisfied with counts[0] which has 2 num

0
[2 4 2]

(1, 1)

(1, 2)

0
[4 2]

False
Bk

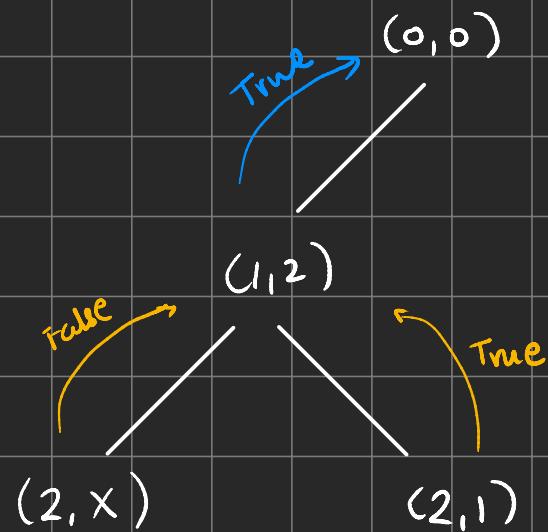
2
[0 4 2]

0	2	2
---	---	---

(2,)

→ we need three nums that are not have in counts arr.

so try with different order here we need to do Backtrack



optimized

sort quantity array in decreasing order

3	2	2
---	---	---

because subse highest quantity he satisfied nahi hogi to jaldi false nikal paunge

```
bool canDistributeHelper(vector<int> &counts, vector<int> &quantity, int ithCustomer) {
    // Base case: all customers are satisfied
    if (ithCustomer == quantity.size()) {
        return true;
    }

    // Try to satisfy the ith customer
    for (int i = 0; i < counts.size(); i++) {
        if (counts[i] >= quantity[ithCustomer]) {
            counts[i] -= quantity[ithCustomer]; // Deduct quantity for the current customer

            if (canDistributeHelper(counts, quantity, ithCustomer + 1)) {
                return true;
            }

            counts[i] += quantity[ithCustomer]; // Backtrack
        }
    }

    return false;
}

bool canDistribute(vector<int> &nums, vector<int> &quantity) {
    unordered_map<int, int> countMap;

    // Count frequency of each number in nums
    for (int num : nums) {
        countMap[num]++;
    }

    // Convert frequency map to a vector
    vector<int> counts;
    for (auto it : countMap) {
        counts.push_back(it.second);
    }

    // Sort quantities in descending order to optimize backtracking
    sort(quantity.rbegin(), quantity.rend());

    return canDistributeHelper(counts, quantity, 0);
}
```

