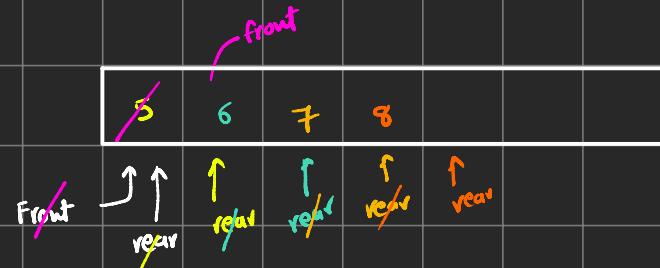


* Queue → data structure

FIFO - First In First Out



insertion from → rear

pop from → front

* Implement



(Push)

if (queue is full) → Q is full

else ↳ insert data

if (rear == size) → Q is full

else → arr[rear] = data
rear++

(Pop)

if (queue is empty) → Q is empty

else ↳ pop data

if (front == rear) → Q is empty

else ↲
arr[front] = -1
front++



Queue empty ho gega

if (front == rear)
↳ front = 0
rear = 0

(getFront)

if (queue is empty) → empty
else return front

(isEmpty)

if (front == rear) → empty
else → not empty

* circular queue



front=-1
rear=-1

(push)

if (Q is full) → Q full

else if (first Ele insert) → f=r=0 then insert

else if ↴ establish circular nature →

if (rear = n-1 && front != 0) → rear=0
and insert

else ↴ default nature → rear++

arr[rear] = Ele

```
void pop(){

    // empty check
    if(front == -1){
        cout << "q is empty cannot pop" << endl;
    }

    // single ele
    else if(front==rear){
        arr[front] = -1;
        front = -1;
        rear = -1;
    }

    // circular nature
    else if(front == size-1){
        front = 0;
    }

    // normal flow
    else{
        front++;
    }
}
```

first Element insertion } handle
single Element removed } separately

```
class CircularQueue{

public:
    int size;
    int* arr;
    int front;
    int rear;

CircularQueue(int size){
    this->size = size;
    arr = new int[size];
    front = -1;
    rear = -1;
}

void push(int data){

    // queue is full
    if( (front == 0 && rear == size-1) || (rear == (front-1)%size-1) ){
        cout << "queue is full cannot insert" << endl;
    }

    // single ele case -> first ele insert
    else if( front == -1 && rear == -1 ){
        front = 0;
        rear = 0;
        arr[rear] = data;
    }

    // circular nature
    else if( rear == size-1 && front != 0 ){
        rear = 0;
        arr[rear] = data;
    }

    // normal queue
    else{
        rear++;
        arr[rear] = data;
    }
}
```

① input restricted queue



$\text{rear} \rightarrow \text{input} (\text{push_back})$

$\text{pop} \leftarrow \text{front} (\text{pop_front})$
 $\text{pop} \rightarrow \text{rear} (\text{pop_back})$

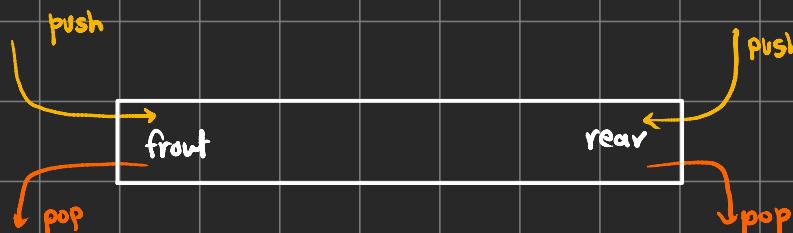
② output restricted Queue



$\text{pop} \rightarrow \text{front}$

$\text{push} \leftarrow \text{front}$
 $\text{push} \rightarrow \text{rear}$

* Doubly ended Queue (deque - dek)



dequeue → pop
 enqueue → push

```
class Deque{
public:
    int* arr;
    int size;
    int front;
    int rear;

    Deque(int size){
        this->size = size;
        arr = new int[size];
        rear = -1;
        front = -1;
    }

    void pushRear(int data){
        // queue is full
        if( (front == 0 && rear == size-1) || (rear == (front-1)%size-1) ){
            cout << "queue is full cannot insert" << endl;
        }
        // single ele case -> first ele insert
        else if( front == -1 && rear == -1 ){
            front = 0;
            rear = 0;
            arr[rear] = data;
        }
        // circular nature
        else if( rear == size-1 && front != 0 ){
            rear = 0;
            arr[rear] = data;
        }
        // normal queue
        else{
            rear++;
            arr[rear] = data;
        }
    }
}
```

```

void pushFront(int data){
    // queue is full
    if( (front == 0 && rear == size-1) || (rear == (front-1)%size-1) ){
        cout << "queue is full cannot insert" << endl;
    }

    // single ele case -> first ele insert
    else if( front== -1 && rear== -1 ){
        front = 0;
        rear = 0;
        arr[front] = data;
    }

    // circular nature
    else if( rear != size-1 && front == 0 ){
        front = size-1;
        arr[front] = data;
    }

    // normal queue
    else{
        front--;
        arr[front] = data;
    }
}

```

```

void popFront(){
    // empty check
    if(front == -1){
        cout << "q is empty cannot pop" << endl;
    }

    // single ele
    else if(front==rear){
        arr[front] = -1;
        front = -1;
        rear = -1;
    }

    // circular nature
    else if(front == size-1){
        front = 0;
    }

    // normal flow
    else{
        front++;
    }
}

void popRear(){
    // empty check
    if(front == -1){
        cout << "q is empty cannot pop" << endl;
    }

    // single ele
    else if(front==rear){
        arr[front] = -1;
        front = -1;
        rear = -1;
    }

    // circular nature
    else if(rear == 0){
        rear = size - 1;
    }

    // normal flow
    else{
        rear--;
    }
}

```

Queue Reverse

ip [3 | 6 | 9 | 2 | 8]

op [8 | 2 | 9 | 6 | 3]

put in stack



[8 | 2 | 9 | 6 | 3]

Tc. $O(2n) = O(n)$
Sc. $O(n)$ (stack)

Stack se
kar sakte hain to
recursion se bhi
kar sakte hain

[3 | 6 | 9 | 2 | 8]

1st step

pee will
take care

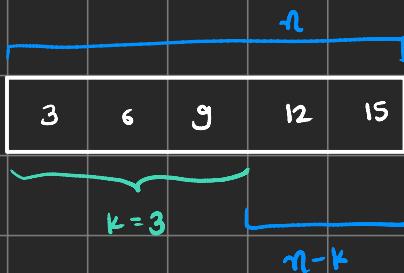
→ 3 ko nikal lo
Recursion de do
3 ko piche daal do

- ① { int temp = q.front();
 q.pop();
- ② { Recursion(2)
- ③ { q.push(temp);

[3 | 6 | 9 | 2 | 8]

[6 | 9 | 2 | 8 | 3]

* Reverse first k elements



$k=3$



→ k element → stack

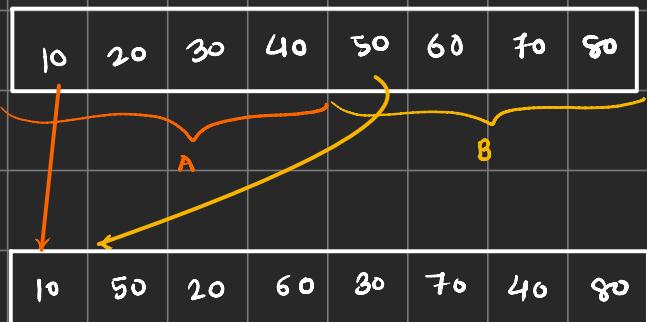
→ stack → queue

→ $(n-k)$ ele \rightsquigarrow pop then push

* Interleave first and second half of queue

→ Transfer $n/2$ elems from queue to another queue

This is
called
interleave



Then push 1 ele

* Sliding Window

* First -ve integer in every window of size k

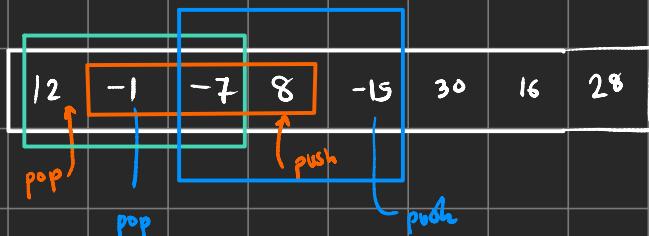
Array.



{ -1, -1, -7, -15, -15, 0 }

when you
do not get any
-ve then

$k=3$



$k=2$

first window deque<int> dq

① First k sized (first window) \leadsto -ve index
window process inside push dq.

dq.



answer = dq.front()

② Processing remaining window



\rightarrow Removal

\rightarrow for ($k \rightarrow <n$) \rightarrow Removal if ($dq.front() - i \geq k$) \rightarrow dq.pop_front()
 \rightarrow Addition if ($arr[i] < 0$) \rightarrow dq.push_back(i)

```

● ● ●

void solve(int arr[], int size, int k)
{
    vector<int> ans;
    // Create a deque
    deque<int> q;
    // Process first window of size = k
    for (int i = 0; i < k; i++)
    {
        // If negative number found, then simply insert index in queue
        if (arr[i] < 0)
        {
            q.push_back(i);
        }
    }
    // Process the remaining windows
    for (int i = k; i < size; i++)
    {
        // First store answer of previous window
        if (q.empty())
        {
            ans.push_back(0);
        }
        else
        {
            int temp = arr[q.front()];
            ans.push_back(temp);
        }
        // Out of window element to be removed
        while (!q.empty() && (i - q.front()) >= k)
        {
            q.pop_front();
        }
        // Check current element whether negative or not. If negative then push index in queue
        if (arr[i] < 0)
        {
            q.push_back(i);
        }
        // For last window (as last window was not processed)
        if (q.empty())
        {
            ans.push_back(0);
        }
        else
        {
            int temp = arr[q.front()];
            ans.push_back(temp);
        }
        // Printing ans vector
        for (int i = 0; i < ans.size(); i++)
        {
            cout << ans[i] << " ";
        }
    }
}

```

→ Answer

$dq.size() \rightarrow 7$

$ans \rightarrow dq.front()$

$size = 0$

```

deque<long long int> dq;
vector<long long> ans;
int negative = -1;

//process first window
for(int i=0; i<k; i++) {
    if(A[i] < 0) {
        dq.push_back(i);
    }
}

//push ans for FIRST window
if(dq.size() > 0) {
    ans.push_back(A[dq.front()]);
}
else
{
    ans.push_back(0);
}

//now process for remaining windows
for(int i = k; i<n; i++) {
    //first pop out of window element

    if(!dq.empty() && (i - dq.front())>=k ) {
        dq.pop_front();
    }

    //then push current element
    if(A[i] < 0)
        dq.push_back(i);

    // put in ans
    if(dq.size() > 0) {
        ans.push_back(A[dq.front()]);
    }
    else
    {
        ans.push_back(0);
    }
}

return ans;

```

easyest

```

vector<int> firstNegInt(vector<int>& arr, int k) {
    queue<int> q;           // store indices of negative numbers
    vector<int> ans;

    int n = arr.size();

    // process first window
    for(int i = 0; i < k; i++) {
        if(arr[i] < 0) q.push(i);
    }
    ans.push_back(q.empty() ? 0 : arr[q.front()]);

    // process remaining windows
    for(int i = k; i < n; i++) {
        // remove elements out of window
        while(!q.empty() && q.front() <= i - k) {
            q.pop();
        }

        // add current element if negative
        if(arr[i] < 0) q.push(i);

        // answer for this window
        ans.push_back(q.empty() ? 0 : arr[q.front()]);
    }

    return ans;
}

```

that's why storing index

* First non repeating chars in string

ip → a a b c
 ↓
 ↘ ↗
 ↘ ↗
 ↘ ↗

op → a # b b

in string "aa" "aab" "aabc"
 a first non repeating char not available because a is repeating
 first non repeating char not available because a is repeating
 first non repeating char is b because a is repeating
 first non repeating char is b because a is repeating
 first non repeating char is c because a is repeating
 first non repeating char is c because a is repeating

ip = q a c
 ↓
 ↗ ↘

op = a # c

ip : z a b c z a
 ↓
 ↗ ↗ ↗ ↗

op = z z l l a #

ip = a a b c
 —

→ frequency count

→ q.push(ch)

→ q.front → character

q.empty
 ↙

Repeating

pop

non repeating
 print

① a ② a ③ b ④ c
 a → 1 a → 2 a → 2
 b → 1 b → 1 b → 1
 c → 1 c → 1

[a] [a|a] [b] [b|c]
 a a(repeating) b b

$$\begin{aligned} SC &= O(26) \\ &\quad + \text{queue } O(n) \\ &= O(n) \end{aligned}$$

$$\begin{aligned} TC &= O(n) \\ &\quad \text{for } (0 \rightarrow n) \\ &\quad \text{neglect } \rightarrow \text{while } (\text{!empty}) \end{aligned}$$

```
string str = "aabc";
int freq[26] = {0};
queue<char> q;
string ans = "";

for(int i=0; i<str.length(); i++){
    char ch = str[i];

    // increment frequency
    freq[ch-'a']++;

    q.push(ch);

    while(!q.empty()){
        if(freq[q.front()]-'a' > 1){
            // repeating char
            q.pop();
        } else{
            ans.push_back(q.front());
            break;
        }
    }

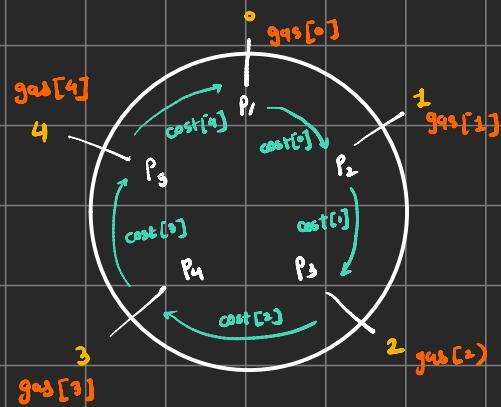
    if(q.empty()){
        ans.push_back('#');
    }
}

cout << ans << endl;
```

fact

* Circular Tour / Gas station

assume 1 gas (liter) \rightarrow cost (distance)



gas	1	2	3	4	5
index	0	1	2	3	4

cost	3	4	5	1	2
------	---	---	---	---	---

1 liter = 1 km distance

0th index : $gas = 1$
 $dist = 3$

1 liter se 3 km nahi chal paae
X

1st index : $gas = 2$
 $dist = 4$

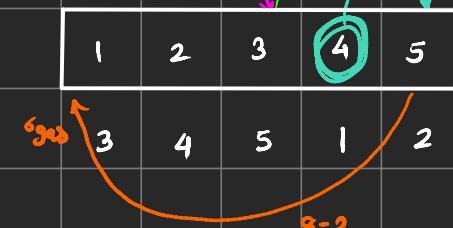
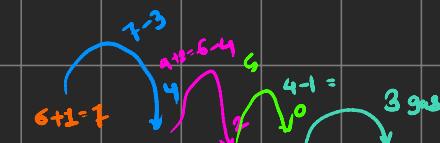
2 liter \rightarrow 4 km X

2nd index : $gas = 3$
 $dist = 5$

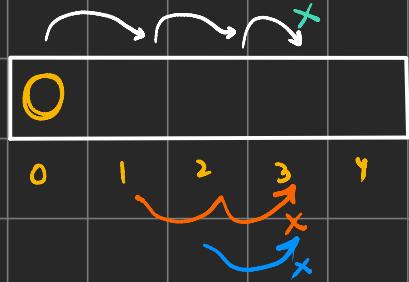
3 liter \rightarrow 5 km X

3 index : $gas = 4$
 $dist = 1$

4 liter \rightarrow 1 km ✓



This Approach (two loops) $\Rightarrow O(n^2)$



just think that started from 0th index and then go to $1 \rightarrow 2 \rightarrow 3 (X)$ 3rd is not able to go bcz of cost

and now you are again going to try from 1st index

to try from 2nd index

optimization.

Analys: if you are not able to make it from 0th index where you already have some gas and the another gas is going to add when you visit station and failed in between so in this situation,

1st } X
2nd } for both this is not going to work



additional kaam bach gaya idhar
because 1st and 2nd index ko
skip karoge

movement possible \rightarrow rear ++
movement not possible \rightarrow front = rear + 1
rear = front

movement possible $P_a \rightarrow P_j$
(gas - dist $>= 0$)

gas	1	2	3	4	5
cost	3	4	5	1	2

0th index = $P=1 \rightarrow P-D = -2 > 0 \times$

1 index = $P=2 \rightarrow 2-4 = -2 \times$

2 index = $P=3 \rightarrow 3-5 = -2 \times$

3 index = $P=4 \rightarrow 4-1 = 3 \checkmark \rightarrow P=3+5=8 \left. \begin{array}{l} \\ \end{array} \right\} = 8-2 = 6 \checkmark \rightarrow P=6+1 \left. \begin{array}{l} \\ \end{array} \right\} = 7-3 = 4 \checkmark$

$D=1$

go back to
back so
optimization
showed above

$D=2$

$P=4+2 \left. \begin{array}{l} \\ \end{array} \right\} = 6 \rightarrow P=2+3 \left. \begin{array}{l} \\ \end{array} \right\} = 5-2 = 3 \checkmark$

\downarrow

now reached
to index 3
circle complete

The diagram shows a grid-based solution for the gas station problem. The top row represents gas stations and the bottom row represents costs. The first column is labeled "gas" and the last column is labeled "cost".

gas	4	6	3	4	8
cost	3	6	7	1	3

Arrows indicate the flow of the dynamic programming algorithm:

- A green arrow starts at the value 4 in the first station and points to the value 6 in the second station.
- A green arrow starts at the value 6 in the second station and points to the value 3 in the third station.
- A green arrow starts at the value 3 in the third station and points to the value 4 in the fourth station.
- An orange arrow starts at the value 4 in the fourth station and points to the value 8 in the fifth station.
- A yellow star is placed above the value 8 in the fifth station, indicating it is the maximum value found.

0th index : $P=4$ $\nearrow 1$ $\rightarrow 7 \nearrow 1$ $\rightarrow 4 \rightarrow -3$
 $D=3$ $\quad\quad\quad 6$ $\quad\quad\quad 7$ X deficit = -3

3rd index : $P = 4 \rightarrow 3 \rightarrow 11 \rightarrow 8 \rightarrow$
 $D = 1 \quad \quad \quad 3 \quad \quad \quad$ remaining
 $\text{balance} = 8$

if (`balance >= deficit`)
 ↳ circle complete
 no page

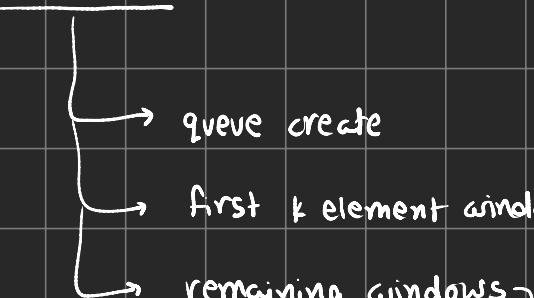
$$\left\{ \begin{array}{l} o(n) \\ o(1) \end{array} \right.$$

```
int canCompleteCircuit(vector<int>& gas, vector<int>& cost) {
    int deficit = 0; // kitna gas kam pad raha he
    int balance = 0; // kitna gas bacha hua he
    int start = 0; // starting index

    for(int i=0; i<gas.size(); i++){
        balance = balance + gas[i] - cost[i]; // updated balance
        if(balance<0){
            deficit = deficit+balance; ← galti logi
            start = i+1;
            balance = 0;
        }
    }

    if(deficit+balance>=0){
        return start;
    }else{
        return -1;
    }
}
```

* Sliding window maximum



nums: 

$k=3$

①



② First k ele process $(\underline{1}, \underline{3}, \underline{-1})$



- assume 0th index biggest ele

- for 1st index $\text{arr}[0] < \text{arr}[1]$ → so remove 1 and put 3

$$1 < 3$$

- for 2nd index $3 > -1$ → -1 wo 3 ko nahi hata sakte

but ho sakte hain ki upcoming queues mei wo cms ho sakte hain

→ actually index storing

③



+ Answer → $q.\text{front} = \text{arr}[1]$

3

→ out of window
(nothing here)

→ Add new ele -3 → logic



{3, 3}

1	3	-1	-3	5	3	6	7
---	---	----	----	---	---	---	---

0 1 2 3 4 5 6 7

i



- out of window

Here 1 (3)

- Inserting new ele

Here 5 → logic → 5 se chote sub ko remove kardo

{3, 3, 5}

1	3	-1	-3	5	3	6	7
---	---	----	----	---	---	---	---

0 1 2 3 4 5 6 7

i



→ remove out of Bound
Here nothing

→ Add new Ele Here 3 → 3 se chota koi nahi

3 se buda 5 hai
So 3 ko push kardo

{3, 3, 5, 5}

--- do for all windows

```

vector<int> maxSlidingWindow(vector<int>& nums, int k) {
    deque<int> dq;
    vector<int> ans;

    // first window
    for(int i=0; i<k; i++){
        // chote element delete kar do
        while(!dq.empty() && nums[i]>=nums[dq.back()]){
            dq.pop_back();
        }
        // inserting index so we can check out of window element
        dq.push_back(i);
    }

    // store ans of first window
    ans.push_back(nums[dq.front()]);

    // remaining windows process
    for(int i=k; i<nums.size(); i++){
        // out of window ele ko remove
        if(!dq.empty() && i-dq.front() >= k){
            dq.pop_front();
        }

        // ab firse current ele k liye chote ele ko remove karna h
        while(!dq.empty() && nums[i]>=nums[dq.back()]){
            dq.pop_back();
        }

        // inserting index so we can check out of window element
        dq.push_back(i);

        // current window ka ans store karna
        ans.push_back(nums[dq.front()]);
    }

    return ans;
}

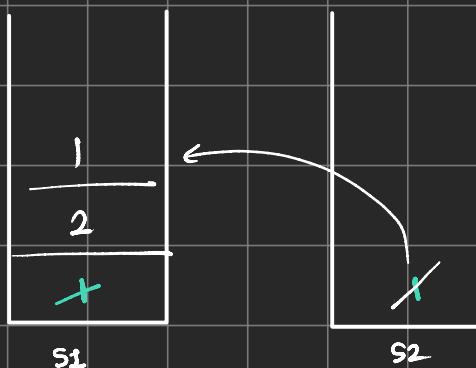
```

* Queue using Stack

FIFO

LIFO

(M1) Push $\rightarrow O(1)$



push(1)
push(2)

① $S_1 \rightarrow S_2$ (push)

② add α to S_1

③ $S_2 \rightarrow S_1$ (push)

* $q.\text{front}() = s_1.\text{top}()$ $\rightarrow O(1)$

* $q.\text{pop}() = s_1.\text{pop}()$ $\rightarrow O(1)$



(M2) $\text{push}(\alpha) \rightarrow O(1)$

$\text{push}(\alpha) \rightarrow S_1$

$\text{pop}() \rightarrow O(n)$

if (S_2 not empty) $\rightarrow S_2.\text{pop}()$

else $S_1 \rightarrow S_2$
 $S_2.\text{pop}()$

(S_1 empty ho
jagega isbar)

$\text{front}() \rightarrow O(n)$

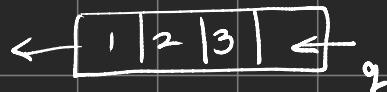
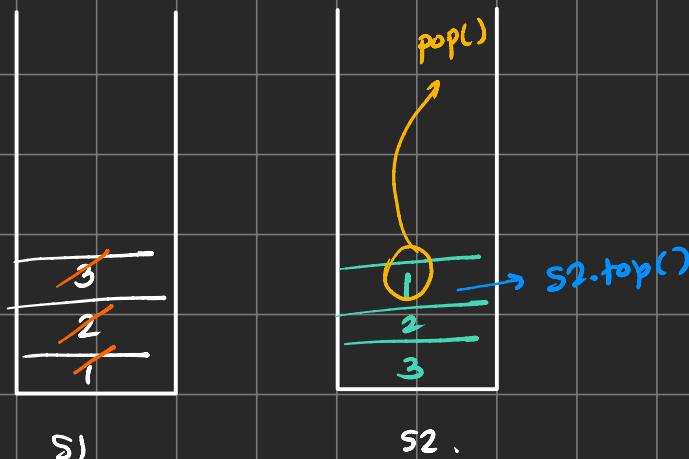
if (S_2 not empty) $\rightarrow S_2.\text{top}()$

else $S_1 \rightarrow S_2$
 $S_2.\text{top}()$

push(1)
push(2)
push(3)

push() \rightarrow 1, 2, 3 \rightarrow s1

front() \rightarrow s1 \rightarrow s2
s2.top



pop() \rightarrow s2 is not empty now \rightarrow s2.pop()

```
class MyQueue {  
    stack<int> s1, s2;  
public:  
    MyQueue() {}  
  
    void push(int x) {  
        s1.push(x);  
    }  
  
    int pop() {  
        int pop = -1;  
        if(!s2.empty()){  
            pop = s2.top();  
        }else{  
            while(!s1.empty()){  
                s2.push(s1.top());  
                s1.pop();  
            }  
            pop = s2.top();  
        }  
        s2.pop();  
        return pop;  
    }  
  
    int peek() {  
        int front = -1;  
        if(!s2.empty()){  
            front = s2.top();  
        }else{  
            while(!s1.empty()){  
                s2.push(s1.top());  
                s1.pop();  
            }  
            front = s2.top();  
        }  
        return front;  
    }  
  
    bool empty() {  
        return s1.empty() && s2.empty();  
    }  
};
```

* Stacks using queues

(M1) push(x)



\rightarrow push x to Q_2
 $\rightarrow Q_1 \rightarrow Q_2$
 $\rightarrow Q_2 \rightarrow Q_1$

$pop()$ $\rightarrow q_1.front()$ will give you top of stack



$\rightarrow 1 \rightarrow Q_2$
 $\rightarrow Q_1 \rightarrow Q_2$ (not here)
 $\rightarrow Q_2 \rightarrow Q_1$

$\rightarrow 2 \rightarrow Q_2$
 $\rightarrow Q_1 \rightarrow Q_2$
 $\rightarrow Q_2 \rightarrow Q_1$

$top() \rightarrow$

(M2) Stack using only one queue

push(1)

push(2)

push(3)



push(1)



push(2)



push(3)



- push into queue

- loop (size-1) $\rightarrow x = q.pop()$
 \downarrow
 $\rightarrow q.push(x)$

```
class MyStack {
    queue<int> q;
public:
    MyStack() {

    }

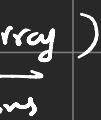
    void push(int x) {
        q.push(x);
        for(int i=0; i<q.size()-1; i++){
            int front = q.front();
            q.pop();
            q.push(front);
        }
    }

    int pop() {
        int top = q.front();
        q.pop();
        return top;
    }

    int top() {
        int top = q.front();
        return top;
    }

    bool empty() {
        return q.empty();
    }
};
```

170 → remaining

(+) K stacks in array 

171 →

