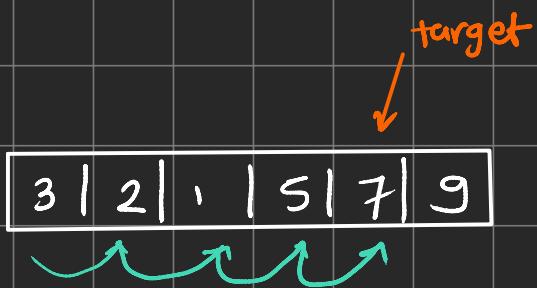


SEARCHING

* Linear search

Tc $O(n)$



* Binary search

→ condition = element should be in monotonic order

(sorted → increasing
decreasing)

target = 15



→ start = 0-th index

→ mid = 9 value

→ end = $(n-1)$ th index

and target = 15 go

→ mid = $\left(\frac{\text{start} + \text{end}}{2} \right)$ index

9 ≠ 15 and

9 < 15

→ go to right side
while searching



→ here $\text{mid} = 13$ and $13 \neq 15$

and $13 < 15$



neglect left side
search on right

15 | 19

6 7

start || end

mid

→ if value does not
exist so return (-1)
($\text{start} \leq \text{end}$)
condition

→ here $\text{mid} = 15$ and

15 = 15

got index = 6

$$\text{mid} = \frac{s+e}{2} \quad \left\{ \text{issue of INT overflow} \xrightarrow{\text{sol}} \text{mid} = s + \frac{e-s}{2} \right.$$

→ Tc

$$\begin{aligned} &\boxed{n} \\ &\boxed{\frac{n}{2}} = \frac{n}{2^1} \\ &\boxed{\frac{n}{4}} = \frac{n}{2^2} \\ &\boxed{\frac{n}{8}} = \frac{n}{2^3} \\ &\vdots \\ &\boxed{\frac{n}{2^k}} \end{aligned} \quad \left\{ k^{\text{th}} \text{ iteration} \right.$$

$$\frac{n}{2^k} = 1 \text{ element}$$

$$n = 2^k$$

$$\log(n) = k$$

$$O(\log n) = O(k)$$

at this point
there is only one →
element present
in array

```
// #include <algorithm>
// on vector -----
std::vector<int> v{1,2,3,4,5,6};

if (binary_search(v.begin(), v.end(), 3)) {
    cout << "3 is found in the vector." << endl;
} else {
    cout << "3 is not found in the vector." << endl;
}
```



```
// on array -----
int arry[] = {1,2,3,4,5,6};
int sizeOfarry = 6;

// binary_search(initialAddress, lastElementAddress, target)
if (binary_search(arry, arry+sizeOfarry, 3)) {
    cout << "3 is found in the vector." << endl;
} else {
    cout << "3 is not found in the vector." << endl;
}
```

→ Find First occurrence

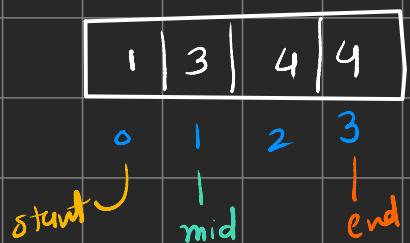
target = 4



→ $\text{mid} = 4 = \text{target}$

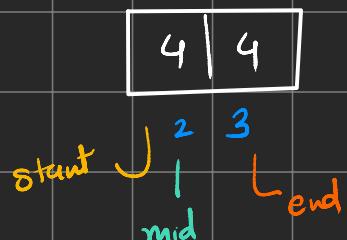
→ ans store

→ search in left



→ here $\text{mid} \rightarrow 3 < 4$

→ search in right



→ here $\text{mid} \rightarrow 4 = 4$

→ store ans
→ search left

stop condition { start = 2 and end = 1
($s < e$)

→ Find Last occurrence

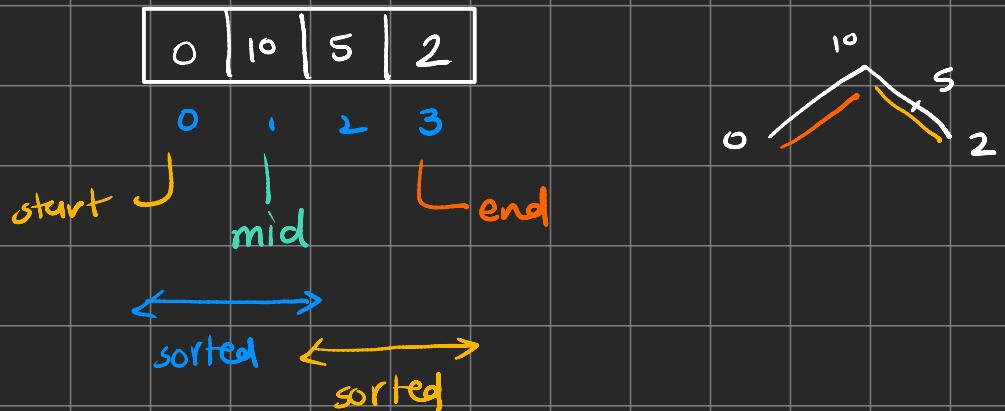
→ $\text{mid} = 4 = \text{target}$

→ ans store

→ search in right

→ Total number of occurrence = lastOcc - firstOcc + 1

→ Find peak element



while ($s < e$)

{ if ($mid < mid + 1$) → right search

} else → $e = mid$

update mid.

return s

* Find Sqrt using Binary Search

$$n = 25 \rightarrow \sqrt{25} = 5$$

$$n = 30 \rightarrow \sqrt{30} = 5\dots = 5$$

$$n = 35 \rightarrow \sqrt{35} = 5\dots = 5$$

$$\rightarrow n = 10$$

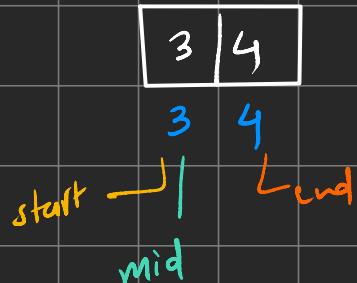


$$25 \neq 10, 5 \times 5 = 25 > 10$$

0	1	2	3	4
---	---	---	---	---



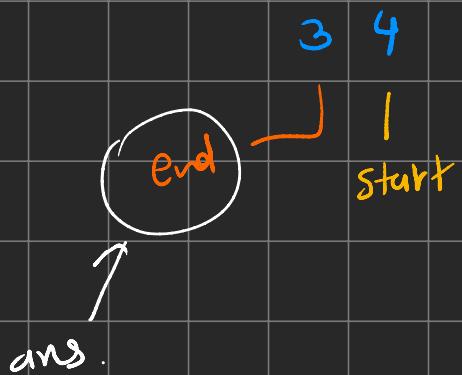
$$2 \times 2 = 4 \neq 10, \quad 4 < 10 \rightarrow \text{right}$$



$$3 \times 3 = 9 \neq 10, \quad 9 < 10 \rightarrow \text{right}$$



$$4 \times 4 = 16 \neq 10, \quad 16 > 10 \rightarrow \text{left.}$$



→ BS in 2D array

	0	1	2	3	/ $m=4$
0	1	2	3	4	
1	5	6	7	8	
2	9	10	11	12	
3	13	14	15	16	
4	17	18	19	20	

element = arr [rowIndex] [colIndex]

$\frac{mid}{totalCol}$ $\frac{mid \%}{totalCol}$

$n=5$

end = $n \times m - 1$

→ as we know underthehood, 2D stores as form of 1D Array so we can apply method that we are doing on 1D Array's BS.

* BS in nearly sorted array

← nearly sorted

target =

arr

10	3	40	20	50	80	70
0	1	2	3	4	5	6

i th index

sorted arr

3	10	20	40	50	70	80
0	1	2	3	4	5	6

i-1 i i+1

→ in sorted array, 3 → 0th index



→ on these index 3 will be there in array

→ 20 → 2 index

→ 40 → 3 index

→ 70 → 5 index



① linear search = n

② sort + BS

$$n \log n + \log n = \log(n+1), (n+1) \approx n \\ = n \log n$$

③

$i-1$ i $i+1$

3	10	20	40	50	70	80
---	----	----	----	----	----	----



10	3	40	20	50	80	70
----	---	----	----	----	----	----



→ If ($mid == target$)

 ↳ return mid

→ IF ($mid == target$)

 ↳ return mid

→ else if ($mid < target$)

 ↳ right search

$s = mid + 1$

ELSE IF ($mid - 1 == target$)

 ↳ return ($mid - 1$)

→ else

 ↳ left search

$e = mid - 1$

→ else if ($mid < target$)

 ↳ right search

$s = mid + 2$

→ else

 ↳ left search

$e = mid - 2$

$O(\log n)$



Divide 2 numbers using BS

dividend = 10, divisor = 2, quotient = ?

$$\begin{array}{r} 5 \\ \hline 2 \overline{) 10} \\ \underline{-10} \\ 00 \end{array}$$

- * Here quotient can be relay between
 - \rightarrow dividend
- * $\text{quotient} * \text{divisor} + \text{remainder} = \text{dividend}$
- \xrightarrow{x}
- quotient * divisor \leq dividend

→ $0 \rightarrow 10$

0	1	2	3	4	5	6	7	8	9	10
---	---	---	---	---	---	---	---	---	---	----



$$\rightarrow 5 * 2 \leq \text{div}$$

$$10 \leq \text{div}$$

$$\underbrace{10 \leq 10}$$

True.

→ $\frac{22}{7}$

$$7 * \text{ans} \leq 22$$

$$\rightarrow \frac{0}{s} \quad \frac{11}{\text{mid}} \quad \frac{22}{e}$$

$$\rightarrow 7 * 11 \leq 22$$

$$77 \leq 22$$

$$77 < 22$$

← left search

$$\rightarrow \frac{0}{s} \quad \frac{5}{m} \quad \frac{10}{e}$$

$$\rightarrow 7 * 5 \leq 22$$

$$35 \leq 22$$

$$35 < 22$$

← left search

$$\rightarrow \frac{0}{s} \quad \frac{2}{m} \quad \frac{4}{e}$$

$$\rightarrow 7 * 2 \leq 22$$

$$14 < 22$$

→ right search

store this ans = 2

$$\rightarrow \frac{3}{s} \quad \frac{4}{e}$$

\downarrow

m

$$\rightarrow 7 * 3 \leq 22$$

$$21 \leq 22$$

store ans

$$21 < 22$$

→ right search

$$\rightarrow \frac{4}{s}$$

\downarrow

m

mid

$$\rightarrow 7 * 4 \leq 22$$

$$28 < 22$$

← left search

$$\rightarrow \frac{3}{s}$$

e

\downarrow

m

mid

$e > s \Rightarrow$ break in this case

Here end = 3
ans = 3
mid = 3

$$\rightarrow \text{For negative numbers} \rightarrow \begin{array}{c|c|c|c} \text{tve} & \text{-ve} & \text{tve} & \text{-ve} \\ \hline \text{tve} & -ve & -ve & +ve \\ \downarrow & \downarrow & \downarrow & \downarrow \\ + & + & - & - \end{array}$$

do all things with tve and in end according to above just change ans's sign.

* Find odd occurring element in array

1	1	2	2	3	3	4	4	3	600	600	4	4
0	1	2	3	4	5	6	7	8	9	10	11	12

→ all elements occurs even no of times ($2n$), except one element

→ all repeating occurrence of elements exists in pair

and pair are not adjacent (ਜਾਨ ਸਮੇਂ ਵੱਡੇ ਪਾਸ ਪਾਸ ਨਹੀਂ ਪੜ੍ਹੇ)

(there cannot be more than 2 consecutive occurrence of any element)

→ Find the element that appeared odd no of times

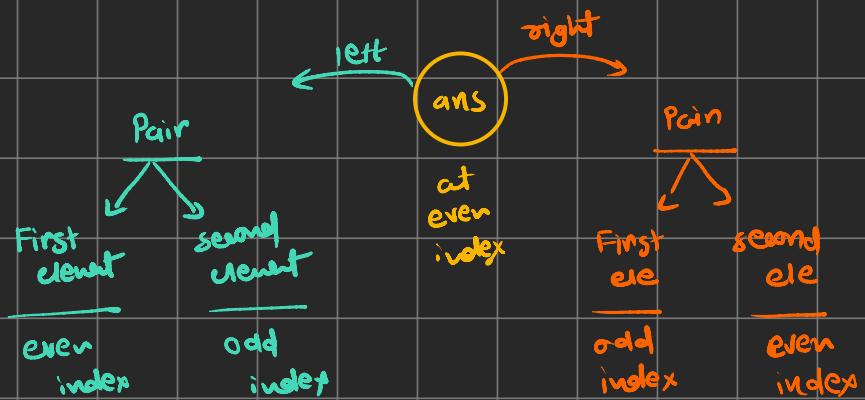
$$1 \rightarrow 2, 2 \rightarrow 2, 3 \rightarrow \underline{3}, 4 \rightarrow 4, 600 \rightarrow 2$$

① XOR approach $\rightarrow 1^{\wedge} 1^{\wedge} 2^{\wedge} 2^{\wedge} 3^{\wedge} 3^{\wedge} 4^{\wedge} 4^{\wedge} 3^{\wedge} 600^{\wedge} 600^{\wedge} 4^{\wedge} 4^{\wedge} 4 \rightarrow 3$

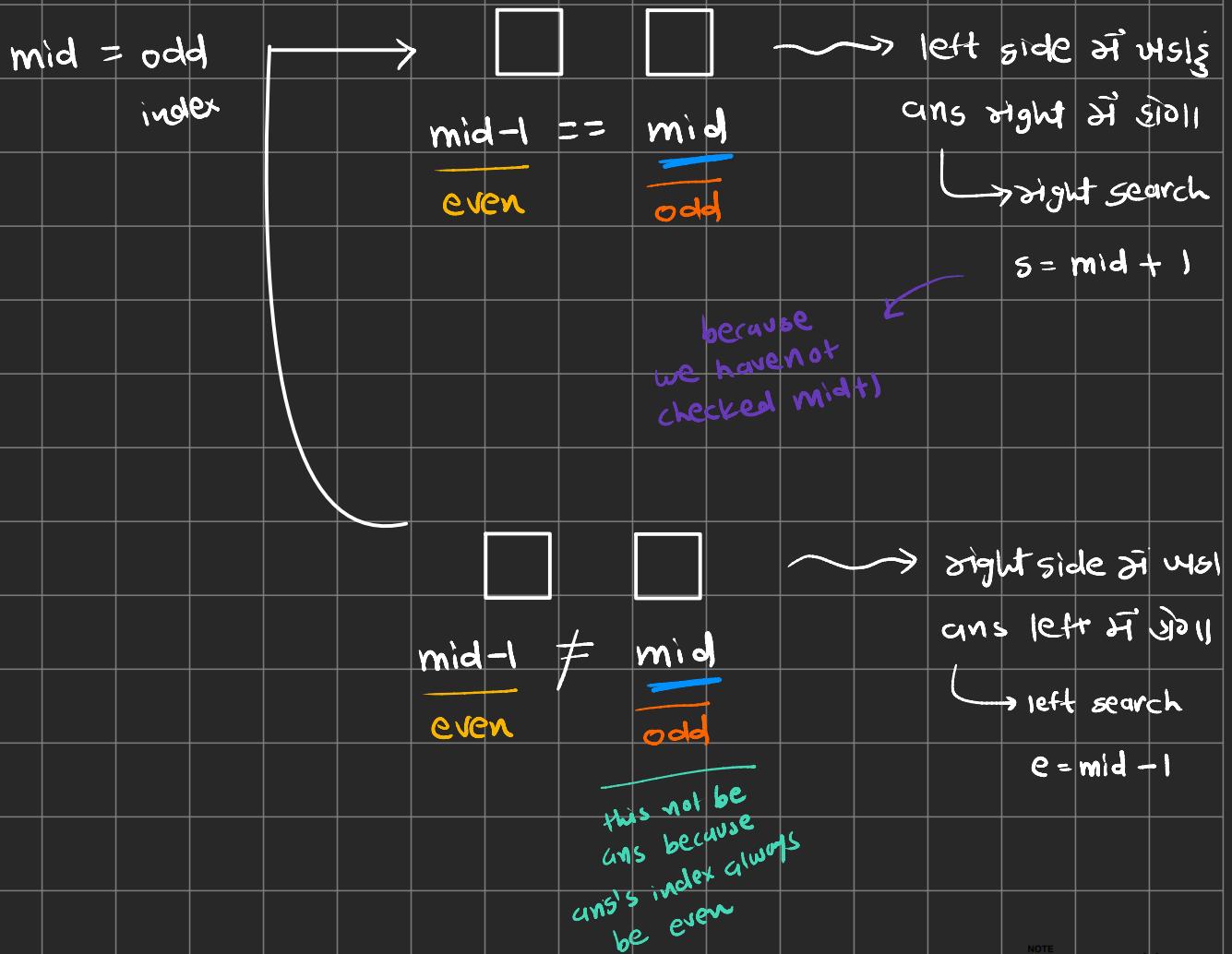
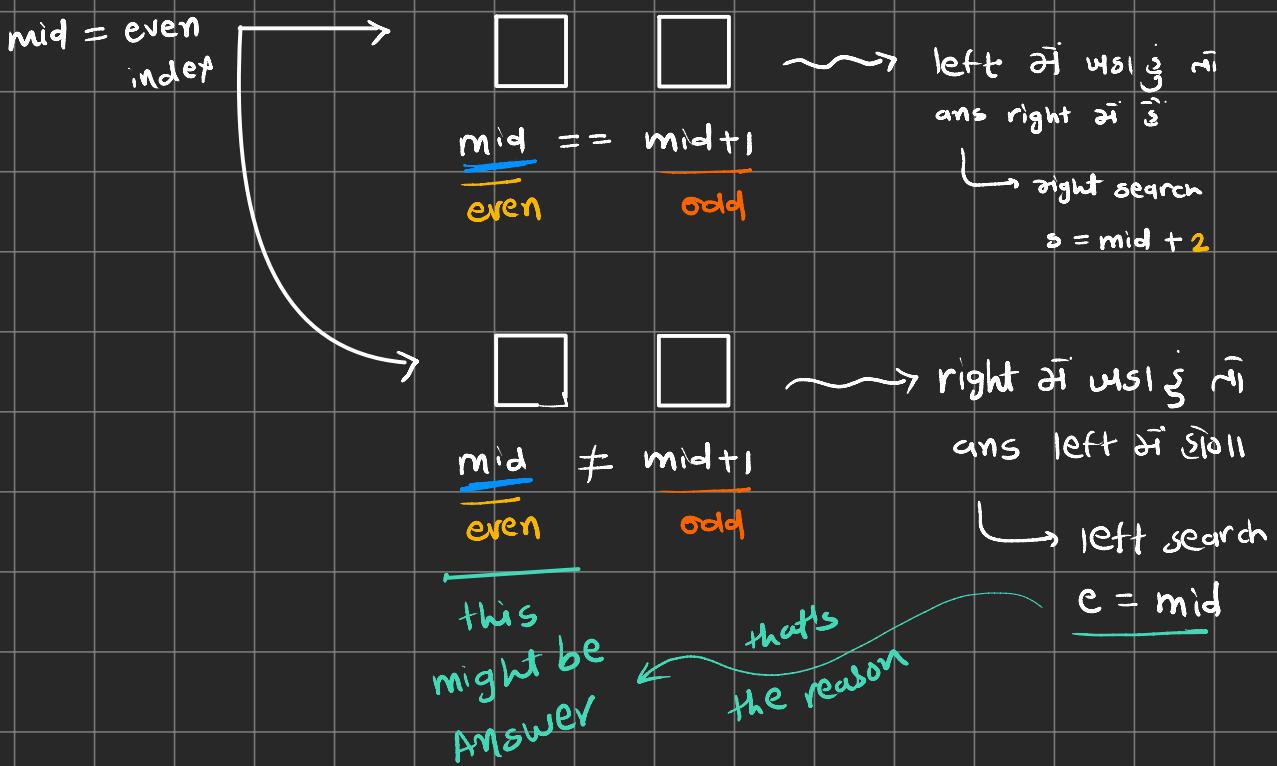
②

1	1	2	2	3	3	4	4	3	600	600	4	4
0	1	2	3	4	5	6	7	8	9	10	11	12

even odd even odd even odd even odd Ans odd even odd even even



$$\rightarrow s = 0, e = n-1, \text{mid} = \frac{s+e}{2}$$



* Pivot Element

→ rotated and sorted array
→ no duplicate element

2	4	6	8	10
---	---	---	---	----

→ ascending (sorted)

10	2	4	6	8
----	---	---	---	---

rotated

6	8	10	2	4
---	---	----	---	---

rotated

pivotal ele. { max element }
↓
order break

9	10	2	4	6	8
---	----	---	---	---	---

start

mid	1
10	2

→ IF ($\text{arr}[\text{mid}] > \text{arr}[\text{mid}+1]$)
└ return mid

mid	1
10	2

→ IF ($\text{arr}[\text{mid}-1] > \text{arr}[\text{mid}]$)
└ return ($\text{mid}-1$)

↗

9	10	2	4	6	8
---	----	---	---	---	---

0 1 2 3 4 5

→ → line B

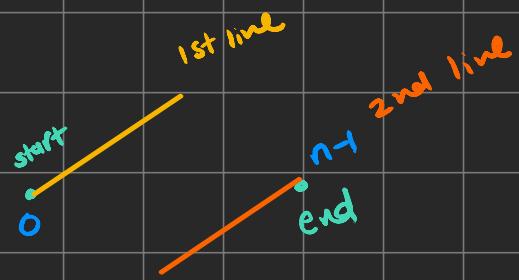
IF ($\text{arr}[s] > \text{arr}[\text{mid}]$)

└ so mid is in line B

left search

e = mid - 1

00



ELSE

↳ right search
 $s = mid + 1$

$\text{arr}[mid] \geq \text{arr}[0]$

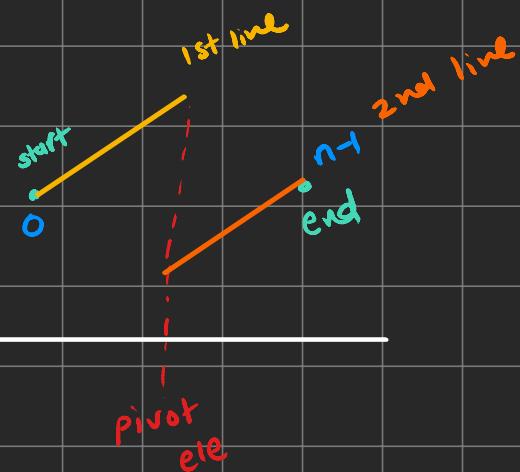
↳ shows first line
so move to right side

→ Search in rotated and sorted array

target =

9	10	2	4	6	8
0	1	2	3	4	5

10 is
pivot
element



IF $(\text{arr}[\text{pivot}] \leq \text{target} \leq \text{arr}[n-1])$

↳ use BS on
second line

$s = \text{pivot index}$
 $e = n - 1$

then do regular BS.

else

↳ use BS on First line

$s = 0$
 $e = \text{pivot index}$

Q8 K-diff pairs in array

difference

3	1	4	1	5
0	1	2	3	4

$\rightarrow 0 \leq i < j \leq \text{nums.length}$

$\rightarrow i \neq j$

$\rightarrow \text{abs}(\text{nums}[i] - \text{nums}[j]) = k$

① Brute Force

② two pointer approach (sorted and then 2pointer app)

1	1	1	3	4	5
0	1	2	3	4	
i	j				

① IF ($i - j = \text{target}$)

$\hookrightarrow i++$, $j++$

② $i - j < \text{target}$

$\hookrightarrow j++$

③ else

$\hookrightarrow i++$

$i - j > \text{target}$

④ BS (sorted + BS)

1	1	1	3	4	5
0	1	2	3	4	
	i				

$k = 2$

$\rightarrow a[i:j] = 1$, $k + a[i:j] = 3$ \rightarrow now search on right side that

is there 3 available?

(1,3)

$\rightarrow a[i:j] = 1$, \dots

$\rightarrow a[i:j] = 3$, $2+3 = 5$ \rightarrow search 5 on right side.

(3,5)

* Find K closest Element

$k=4 \rightarrow$ elements to return
 $\alpha=3$

1	2	3	4	5
0	1	2	3	4

$$\rightarrow k=4, \alpha=35$$

12	16	22	30	35	39	42	45	48	50	53	55	56
0	1	2	3	4	5	6	7	8	9	10	11	12

$$\text{diff} = |x - u[i]|$$

22 < 48

when drift is same
take small \rightarrow
big

① sort according to diff like

35 39 30 42 45 22 48

کے ۴ جو کیا

two pointer

2

12	16	22	30	35	39	42	45	48	50	53	55	56
2	1	2	3	4	5	6	7	8	9	10	11	12

$$\text{diff} = |x - u[i]|$$

$\lambda \dashv \dashv \gamma$

r ← - - / - < - < - h ↓

IF (diff at low > diff at high)

Litt

$$N \xrightarrow{k} O(n^{-k})$$

ELSE

L h --

$$h - 1 \geq k \rightarrow \text{break condition}$$

$$\begin{aligned}x - 57 &= 4 \\27 &= 4\end{aligned}$$

③ BS + 2 pointer

12	16	22	30	35	39	42	45	48	50	53	55	56
0	1	2	3	4	5	6	7	8	9	10	11	12
23	19	13	5	0	4	7	10	13	15	18	20	21

① Find smallest ele. in array which is $>= \alpha$

- lower bound
- closest ele to α

② $H \rightarrow$ index of closest's element

$$L \rightarrow H - 1$$

③ $[L, H]$ window form, size $\rightarrow K$

↳ expand window to K

if $(x - arr[low] > arr[high] - x)$

↳ $h++$

else

↳ $l--$

12	16	22	30	35	39	42	45	48	50	53	55	56
0	1	2	3	4	5	6	7	8	9	10	11	12
23	19	13	5	0	4	7	10	13	15	18	20	21

↓ ↓ ↴ ↴ ↴ ↴ ↴

l x h k h

→ $diff_{low} > diff_{high} \rightsquigarrow h++$

else $\rightsquigarrow l++$

$\rightarrow S > 0 \rightsquigarrow \text{light} +$
 $\rightarrow S > 4 \rightsquigarrow \text{light} +$
 $\rightarrow S < 7 \rightsquigarrow \text{low} ++$
 $\rightarrow 13 > 7 \rightsquigarrow \text{light} +$

} 4 movements

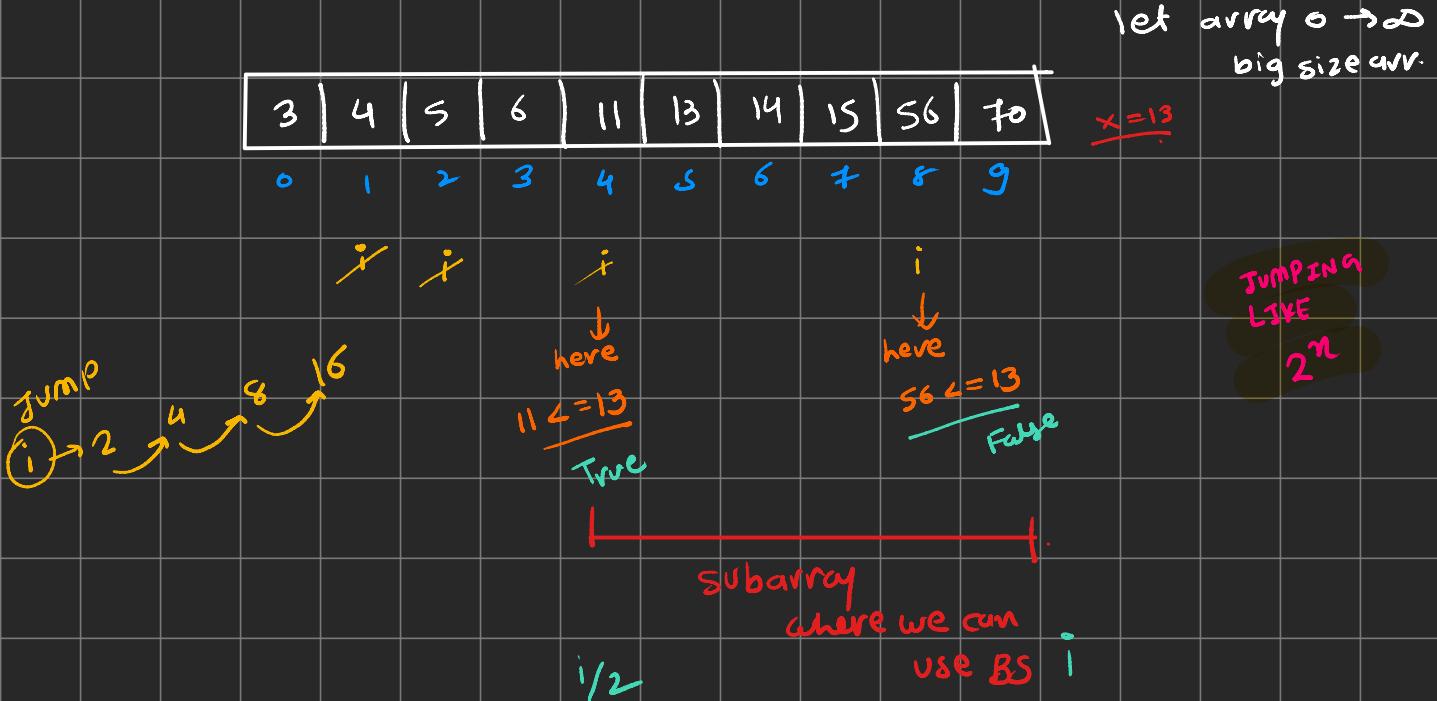


* Exponential Search

\rightarrow Array should be sorted

↳ doubling / galloping / strazic search

\rightarrow Application : when u have a too long array so during that time just think like u have array from $0 \rightarrow \infty$ something so during that time TC becomes $O(n)$ even if u are using BS to solve this and to reduce TC we are using this method



```

if (a[0] == x) → return 0;

int i = 1;

while (i < n && a[i] <= x)
{
    i = i * 2
}

return BS(a, i/2, min(i, n-1), x)

```

TC. $\log(2^{\log m - 1})$

while loop { $\log 16 \rightarrow \log(i) \rightarrow \log_2 2^4 \rightarrow 4$ steps $O(\log m)$

$$\begin{aligned}
&\text{BS in subarray} \rightarrow 2^4 - 2^3 \rightarrow 16 - 8 = 8 \\
&\rightarrow 2^{\log m} \rightarrow 2^{\log_2 16} \rightarrow 2^{\log_2 2^4} \rightarrow 2^4 \\
&\rightarrow 2^{\log m} - 2^{\log m - 1} \\
&\rightarrow 2^{\log m} - 2^{\log m - 1} \cdot 2^1 \\
&\rightarrow 2^{\log m} (1 - 2^{-1}) \\
&\rightarrow 2^{\log m} \quad \rightarrow \frac{2^{\log m}}{2} \quad \text{Application}
\end{aligned}$$

$$\begin{aligned}
m = 16 \\
&\rightarrow 2^{\log 16 + 1} \\
&\rightarrow 2^{n-1} \\
&\rightarrow 2^3 \\
&\rightarrow 2^3 \text{ steps} \\
&\rightarrow 8 \text{ steps}
\end{aligned}$$

→ search in ∞ array
 unbounded array ↙
 → Better than binary search
 when x is near beginning

→ Unbounded search

find the element in ∞ array sorted $1, 2, 3, \dots, \infty$

```
i = 0  
while (1) {
```

```
    if (a[i] > x) → break
```

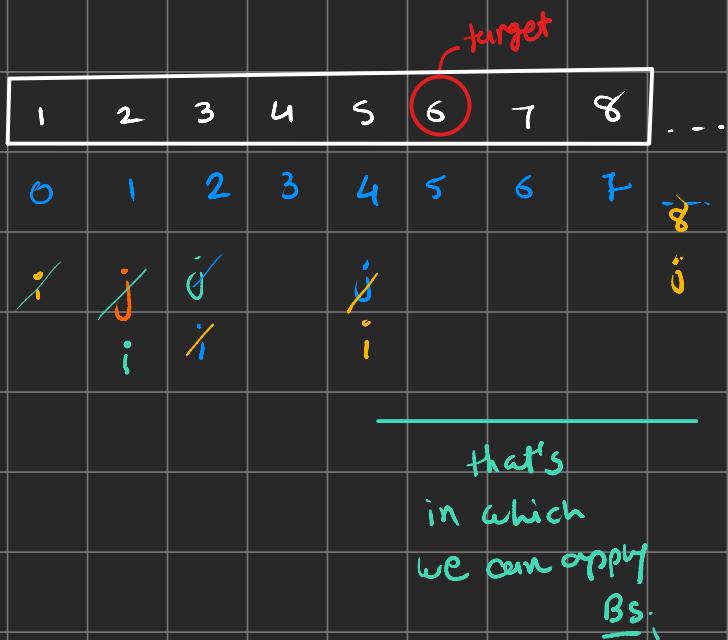
```
    if (a[i] == x) → ans = i
```

```
    i++
```

```
}
```

Brute Force
approach

→ Exponential search is optimized



Book Allocation Problem

$book = 4 \quad m = 2$
 $10, 20, 30, 40 \rightarrow \text{Pages}$

Allocate books in such a way that:

1. Each student gets at least one book.
2. Each book should be allocated to only one student.
3. Book allocation should be in a contiguous manner.

\max

10	20	30	40
0	1	2	3

\min

10	20	30	40
10	20	30	40
10	20	30	40
10	20	30	40

You have to allocate the book to ' m ' students such that the maximum number of pages assigned to a student is minimum.

①

25	46	28	48	24
----	----	----	----	----

$\text{students} = 4$

$$\text{low} = \max(\text{arr}) / \text{os}$$

49
0

$$\text{high} = \sum(\text{arr})$$

171

mid (maximum allowed pages)

for ($\text{pages} = \text{low} \rightarrow \text{high}$)

{

$\text{countStudent} = \text{funct}(\text{arr}, \text{pages})$

if ($\text{countStudent} == m$)

 └ return pages

}

$\text{fun}(\text{arr}, \text{pages})$

{

$\text{stu} = 1, \text{pageStudent} = 0$

for ($i = 0 \rightarrow n - 1$)

{
 if ($\text{pageStudent} + \text{arr}[i] \leq \text{pages}$)

$\text{pageStudent} = \text{pageStudent} + \text{arr}[i]$

else

$\text{stu}++$

$\text{pageStudent} = \text{arr}[i]$

}

return stu

→ pages = 49

25	46	28	48	24
1	2	3	4	5 → students

$$i=0 \rightarrow 0 + 25 \leq 49 \rightarrow ps = 0 + 25 = 25$$

$$i=1 \rightarrow 25 + 46 \leq 49 \times$$

$$\left. \begin{array}{l} stu = 1, \\ ps = 46 \end{array} \right\}$$

$$i=2 \rightarrow 25 + 46 + 28 \leq 49 \times$$

$$\left. \begin{array}{l} stu = 2, \\ ps = 28 \end{array} \right\}$$

$$i=3 \rightarrow 25 + 46 + 28 + 49 \leq 49 \times$$

$$\left. \begin{array}{l} stu = 3, \\ ps = 49 \end{array} \right\}$$

$$i=4 \rightarrow 25 + 46 + 28 + 49 + 24 \leq 49 \times$$

$$\left. \begin{array}{l} stu = 4, \\ ps = 24 \end{array} \right\}$$

$$\underline{\text{total students}} = 5$$

→ pages = 71

25	46	28	48	24
1	2	3	4	

$$i=0 \rightarrow 0 + 25 \leq 71 \rightarrow ps = 25$$

$$i=1 \rightarrow 25 + 46 \leq 71 \rightarrow ps = 46$$

$$i=2 \rightarrow 25 + 46 + 28 \leq 71 \times \left. \begin{array}{l} stu = 1, \\ ps = 28 \end{array} \right\}$$

$$i=3 \rightarrow 25 + 46 + 28 + 49 \leq 71 \times \left. \begin{array}{l} stu = 2, \\ ps = 49 \end{array} \right\}$$

$$i=4 \rightarrow 25 + 46 + 28 + 49 + 24 \leq 71 \times \left. \begin{array}{l} stu = 3, \\ ps = 24 \end{array} \right\}$$

Tc → $O(\sum - \max + 1) \times n$

total stu = 4 done

NOTE

IN

Created by Notein

WHY BS ? MAX-MIN ઓન એંથી હોવા દળ અપ્પુણી માત્રા

and linear search TC લોકાર માટે ચુંગાપે

(2)

s
49

m
110
↓

e
172

Func (arr, 110) \rightarrow student = 2

we need more students

$2 < 4$

move to left
search

s
49

m
78
109

↳ 3 students

$3 < 4$
again
left search

s
49
m
63
77



s
64
m
69
77

↓

students $5 < 4 \times$
right search

↓
s student

→
right
student

s m e
f0 f3 f7

store f3

4 student

$4 < 4$

← left search

try to reduce it because we need
min'num

s m e
f0 f1 f2

4 student

$4 < 4$

← left search

s m e
f0 f0 f0

5 student

last store ans = f1.

s c } break here
f1 f0

* Painter's partition

Split array - largest sum

→ split the array into k subarrays such that the max subarray sum is minimum



ans: [10 20 30] [40]

same as
book allocation

$$0 \quad \frac{m}{10} \quad e \quad \text{sum(curr)} = 20$$

$$\begin{aligned} I \rightarrow & \quad 5 \leq 10 \\ & 5+5 \leq 10 \\ & 5+5+5 \leq 10 \times \end{aligned}$$

$$\begin{aligned} II \rightarrow & \quad 5 \leq 10 \\ & 5+5 \leq 10 \end{aligned}$$

$$0 \quad \frac{4}{m} \quad 9$$

$$I \rightarrow 5 \leq 4 \times \times$$

cannot do
right search

$$\begin{array}{c} s \\ \hline s \end{array} \quad \begin{array}{c} m \\ \hline x \end{array} \quad \begin{array}{c} g \\ \hline e \end{array}$$

I \rightarrow $5L7$, $s+5L=7X$

II \rightarrow $sL7$

III \rightarrow X no solution

$$\begin{array}{c} s \\ \hline s \end{array}) \quad \begin{array}{c} g \\ \hline e \end{array}$$

mid

I \rightarrow $5L8$, $10L=8X$

II \rightarrow

III \rightarrow X no sol.

$$\underbrace{\begin{array}{c} g \\ s \\ e \\ m \end{array}}_{} \quad \left. \right\} \text{break}$$

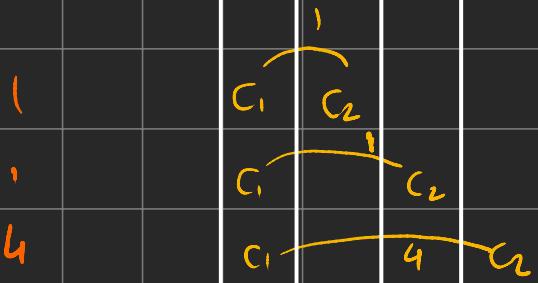
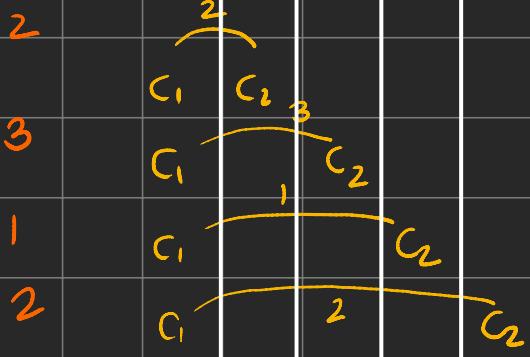
★ Aggressive cows

min

4	2	1	3	6
---	---	---	---	---

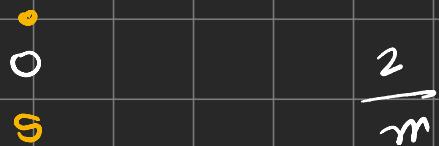
still position

$k = 2$ cows



$\max = 5$

search space



$5 = \max - \min \text{ in arr}$
e



$\text{mid} = 2$

$3-1 \geq \text{mid}$
 ≥ 2
} 2012 2 0121 2 distance variable GL
 अद्य दी गयी निम्नों से distance का
 जो एकीकरण होगा

right search now

minimum allowed distance

isPossible
(stalls, mid, n)

cowCount = 1
lastPos = stalls[0]

for (i = 0 → n)
if (stalls[i] - lastPos
 $\geq \text{mid}$)

{ cowCount++

if (cowCount == k)
return true

lastPos = stalls[i]

}

return false



Sort the array
that given in que.

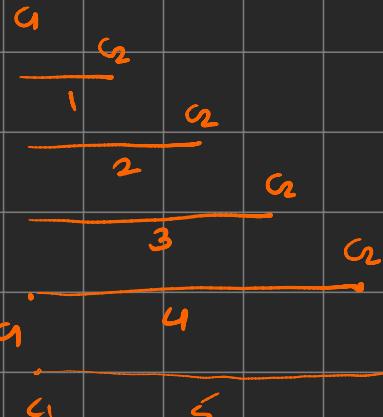


$$1-5 \geq \text{mid}$$

$$7 = 4$$

right search

s
s, e
mid



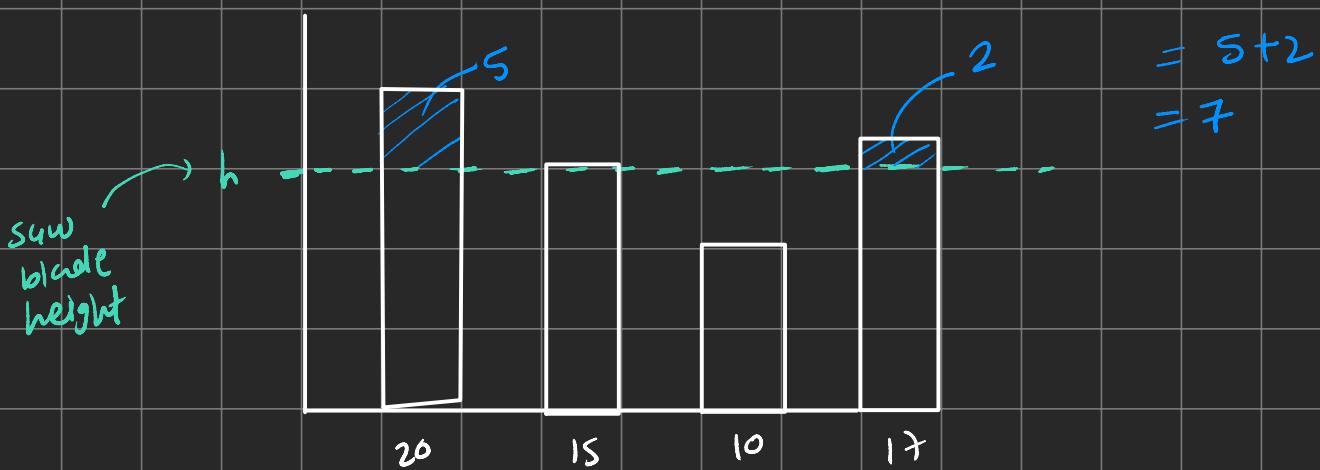
$a[n] = 5$

$$1-6 = 5$$

EKO SPOJ

$$M = 7 \text{ meter (min)}$$

20	15	10	17
----	----	----	----



→ so when blade height is 15 meter we can get 7 meter of total wood

① BruteForce ($i=0 \rightarrow i = \max(\text{avr}) = 20$)

$$i=1 \rightarrow 19 + 14 + 9 + 16 =$$

$$i=2 \rightarrow 18 + 13 + 8 + 15 =$$

$$\vdots$$

$$i=10 \rightarrow 10 + 5 + 0 + 7 =$$

$$i=15 \rightarrow 7 \text{ meter} \rightarrow \text{got ans}$$

(2)



$$h = 10 \rightarrow 10 + 5 + 0 + 7 = 22$$

$22 > \text{target}$

$22 > 7 \rightarrow$ move right search

store ans

11 m 20
 | |
 s 15 e

$h = 15 \rightarrow 7 >= \text{target}$

$7 == 7 \rightarrow \underline{\text{got ans}}$

store ans

right search

16 . 20
 | |
 s 18 e
 m

$h = 18 \rightarrow 2 >= \text{target}$

(not) \rightarrow left search

s 17
 | |
 16 e
 m

$h = 16 \rightarrow 5 >= \text{target}$

(not) \rightarrow left search

e s } break
 15 16

* Parata - rotiparata spoj



total Parata = 10

min time to
make order = ?

junks

$R \rightarrow 1 \text{ parata in } R \text{ min}$

$2R \rightarrow 2 \text{ parata in } 2 * R \text{ min}$

$3R \rightarrow 3 \text{ parata in } 3 * R \text{ min}$

:

1

6 °
 S - m
 0 ° max

$$\rightarrow C_1 = 1 + 2 \times 1 + \dots + 10 \times 1 \\ = 55 \text{ min}$$

is Possible to make \rightarrow Yes



left search

to decrease time
for cook

e 220 \rightarrow time taken by cook
with highest rank
when all purathas are
given to him to make

here \rightarrow 4 rank

$$\begin{aligned} &= 4 + 2 \times 4 + 3 \times 4 \\ &+ \dots + 10 \times 4 \\ &= 4 \times [1 + 2 + 3 \dots \\ &\quad + 10] \\ &= 4 \times \frac{n \times (n+1)}{2} \\ &= 220 \end{aligned}$$

° °
 S - m e
 0 54 109

work \downarrow
 common work
 parallel

$\rightarrow C_1 \rightarrow 45 \text{ min for } 9 \text{ puratha}$

$\rightarrow C_2 \rightarrow 2 \text{ min for } \frac{1 \text{ puratha}}{10 \text{ puratha}}$

is Possible to make \rightarrow Yes

left search

0 °
 S - m e
 . 26 53

$$\rightarrow C_1 = 1 + 2 + 3 + 4 + 5 + 6 + 7 \rightarrow 6 \text{ purathas}$$

$\underbrace{\qquad\qquad\qquad}_{21 \text{ min}}$

$28 >= \text{mid}$
 $>= 26$

$$\rightarrow C_2 = \underbrace{2 + 4 + 6 + 8}_{20 \text{ min}}$$

$\rightarrow 4$ parathas

is possible to make \rightarrow yes
left search

0 m 25
| |
s 12 e

$$\rightarrow C_1 = \underbrace{1 + 2 + 3 + 4 + 5}_{10 \text{ min}} \rightarrow 4 \text{ parathas}$$

$$15 \geq \text{mid}$$

$$7 = 12$$

$$\rightarrow C_2 = \underbrace{2 + 4 + 6}_{12 \text{ min}} \rightarrow 3 \text{ parathas}$$

$$12 \geq \text{mid}$$

$$12 \geq 12$$

$$\rightarrow C_3 = \underbrace{3 + 6}_{9 \text{ min}} \rightarrow 2 \text{ parathas}$$

$$\rightarrow C_4 = 4 \rightarrow 1 \text{ paratha}$$

is possible to make \rightarrow yes
left search

0 m 24
| |
s 5 e

$$\rightarrow C_1 = \underbrace{1 + 2}_{3 \text{ min}} = 2P$$

$$\rightarrow C_2 = 1P$$

$$\rightarrow C_3 = 1P$$

$$\rightarrow C_4 = 1P$$

$$\rightarrow C_5 = 1P$$

6 p ≤ 10 parata \rightarrow not Possible

→ right search



$$\rightarrow C_1 = 3P$$

$$\rightarrow C_2 = 2P$$

$$\rightarrow C_3 = 1P$$

$$\rightarrow C_4 = 1P$$

$$\rightarrow C_5 = 1P$$

8 P \rightarrow not possible



$$\rightarrow C_1 = 4P \quad 1+2+3+4$$

$$\rightarrow C_2 = 2P$$

$$\rightarrow C_3 = 2P$$

$$\rightarrow C_4 = 1P$$

$$\rightarrow C_5 = 1P$$

g

#

Selection sort

→ different Rounds / passes

smallest element take, usko right jagah par place kar de
hai

0	1	2	3	4	
i	64	25	12	22	11

Round ①

64	25	12	22	11
<i>i=0</i>	swap			

Round ②

11	25	12	22	64
<i>i=1</i>	swap			

Round ③

11	12	25	22	64
<i>i=2</i>	swap			

Round ④

11	12	22	25	64
<i>i=3</i>	swap			

total

last element is already sorted

$$= N - 1$$

$$= 5 - 1$$

$$= 4$$

```
void selectionSort(vector<int>& arr, int n){
```

```
    for(int i=0; i<n-1; i++){
```

```
        int minIndex = i;
```

```
        for(int j=i+1; j<n-1; j++){
            if(arr[j]<arr[minIndex]){
                minIndex = j;
            }
        }
```

```
        swap(arr[minIndex], arr[i]);
    }
```

```
}
```

$n-1$

$(n-1), (n-2), \dots, 1$

$$= 1 + 2 + 3 + \dots + (n-1) + (n-2)$$

$$= \frac{n(n-1)}{2}$$

$$= \frac{n^2-n}{2} = O(n^2)$$

Best case / worst case = $O(n^2)$

Use case

↳ small size arr

Bubble Sort

Round ①

10 1 7 6 14 9

$a > b \rightarrow \text{swap}$
 $10 > 1 \rightarrow \text{swap}$

1 10 7 6 14 9

$10 > 7 \rightarrow \text{swap}$

1 7 10 6 14 9

$10 > 6 \rightarrow \text{swap}$

1 7 6 10 14 9

$10 > 14 \rightarrow \text{False}$

do not swap

1 7 6 10 14 9

$14 > 9 \rightarrow \text{swap}$

1 7 6 10 9 14

sorted

→ After Round ① first largest element comes on right place , here 14 comes on right place

Round ②

1 7 6 10 9 14

sorted

1 7 6 10 9

s

1 6 7 10 9

1 6 7 10 9

1 6 7 9 10

→ After this , second largest element comes on right place

1 6 7 9 10 14

sorted Already sorted

Round ③

1 6 7 9 10 14

sorted

1 6 7 9



1 6 7 9



1 6 7 9



1 6 7 9 10 14

sorted

→ third largest ele from array on 8th place

Round ④

1 6 7 9 10 14

sorted

1 6 7



1 6 7 9 10 14

sorted

Round ⑤

1 6



1 6 7 9 10 14

sorted

1 6 7 9 10 14



in end
automatic
sorted bcz
all others are
sorted

```
void bubbleSort(vector<int>& arr, int n){  
  
    for(int i=0; i<n; i++){  
  
        bool swapped = false;  
  
        for(int j=0; j<n-i; j++){  
            // process ele till n-i element  
            if(arr[j]>arr[j+1]){  
                swap(arr[j],arr[j+1] );  
                swapped = true;  
            }  
        }  
  
        if(swapped==false){  
            cout << "here swapped false hitted" << endl;  
            break;  
        }  
    }  
}
```

use case :

ith round mei ith
largest element ko
uske 8th place par
phuchha de do

Tc	comparisons	$Sc = O(1)$
1	$\rightarrow (n-1)$	
2	$\rightarrow (n-2)$	
3	$\rightarrow (n-3)$	
4		$= 1 + 2 + 3 + \dots + (n-2) + (n-1)$
\vdots		$= O(n^2)$
$(n-1)^{th}$	$\rightarrow 1$	n is size of arr

→ optimised → in any round, when there is no swapping it means array is already sorted
 due to
 Best case : $O(n)$, worst case : $O(n^2)$

Insertion Sort → card example

$arr[] = \{ 4 \ 12 \ 11 \ 20 \}$ → compare ele which is in Last

0 1 2 3 4 5 6

10	1	7	4	8	2	11
----	---	---	---	---	---	----

10	1	7	4	8	2	11
----	---	---	---	---	---	----

↑

Round ①

$i < 10$

← left me dada

$i=1$

so we need space of one index in left side

10 8 1 space aur 1 left side
 0th index yr 1 copy seki

1	10	7	4	8	2	11
---	----	---	---	---	---	----

sorted i

Round ②

$7 < 10 \rightarrow$ left side go

$i = 2$

$7 > 1 \rightarrow$ so right side of 1

10 8 7 4 11 2 11

1	7	10	4	8	2	11
sorted						i

Round ③

$4 < 10 \rightarrow$ left side

$4 < 7 \rightarrow$ left

$4 > 1 \rightarrow$ right

7, 10 ടി ഓഫ space right ദി സീരേജ്യാമി

1	4	7	10	8	2	11
sorted						i

Round ④

$8 < 10 \rightarrow$ left side

$8 > 7 \rightarrow$ right side

10 8 1 space shift ബാി

1	4	7	8	10	2	11
sorted						i

Round ⑤

$2 < 10 \rightarrow$ left

$2 < 8$

$2 < 7$

$2 < 4 \rightarrow$ left

$2 > 1 \rightarrow$ right

4, 7, 8, 10 shift all to 1 space right side

1	2	4	7	8	10	11
---	---	---	---	---	----	----

Round 6

 $11 > 10 \rightarrow \text{right side}$

1	2	4	7	8	10	11
---	---	---	---	---	----	----

```
void insertionSort(vector<int>& arr, int n){  
    for(int i=1; i<n; i++){  
        int temp = arr[i];  
        int j=i-1;  
        for(; j>=0; j--){  
            if(arr[j]>temp){  
                // shift  
                arr[j+1] = arr[j];  
            }  
            else{ // ruk jao  
                break;  
            }  
        }  
        arr[j+1] = temp;  
    }  
}
```

use case

→ adaptable

→ stable

→ n small so good performance

→ partially sorted array then good

 $Tc = O(n^2)$ Best case = $O(n)$, worst = $O(n^2)$

