



# **BRAC University**

Department of Mathematics and Natural Sciences

**Total Points: 15**

 **Assignment-01**

**Course Code: MAT215**  
Complex

 **Name: TAHSIN MOHAMMAD MUNIF**


 **Student ID: 24301136**

 **Section: 12**

 **Semester: FALL 2025**

 **Submission Date: \_\_\_\_\_**

*Assigned by*


 **Partho Sutra Dhor**  
Lecturer, Department of MNS  
BRAC University

### Question 1

Find all possible values of  $z$  such that

$$z^{10} - 1 = 16\sqrt{2}(1 + i)$$

Locate them in the complex plane. Show that they are contained in a circle and find the radius of that circle. Also find the angular distance between two adjacent roots.

 **Solution:**

## Question 2

Consider the equation

$$\left| \frac{z + 9i}{z - 9i} \right| = 2$$

Describe the above locus in the complex plane.


 **Solution:**

### Question 3

Consider the inequality

$$|z - 6| - |z + 6| \geq 8$$

Describe the above locus in the complex plane.


 Solution:

### Question 4

Solve the following equation for  $z$ :

$$e^{3z} = -6$$

Express  $z$  as  $x + iy$  where  $x, y \in \mathbb{R}$ .

 Solution:

### Question 5

Prove that


$$\coth^{-1} z = \frac{1}{2} \ln \left( \frac{z+1}{z-1} \right).$$

 Solution:

## Question 6

Solve for  $z$ :

$$\sin^{-1} z = 4 + bi$$

 Solution: