



BRAC University  
Department of Mathematics and Natural Sciences  
**MAT215: Complex Variables & Laplace Transform**  
**Assignment-01**

Section: 12

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Submission Date:

Summer 2025

Total Marks: 15

**Use this page as the cover page of your assignment**

1. Using the definition **5×5=25**

a) Find the derivative of  $f(z) = \frac{aQ1a - a@z - @Q1a - b@}{@Q1a - c@z + @Q1a - d@i}$  at  $z = i$ .

b) Find the derivative of  $f(z) = \frac{@Q1b - k@}{@Q1b - a@z + @Q1b - b@}$  at  $z = z_0$ .

c) Show that  $f(z) = @Q1c - a@z^2 + @Q1c - b@z - @Q1c - c@$  is differentiable at all points.

d) Show that  $f(z) = @Q1d - a@z\bar{z} - @Q1d - b@z + @Q1d - c@\bar{z}$  is not differentiable at  $z = 0$ .

e) Find the derivative of  $f(z) = \frac{@Q1e - k@}{z^2}$  at  $z = @Q1e - a@ + @Q1e - b@i$ .

2. Using C-R equatins determine whether the functions are analytic or not. **5×5=25**

a)  $f(z) = @Q2a - a@ \sinh (@Q2a - b@z)$

b)  $f(z) = @Q2b - a@ \cos (@Q2b - b@z)$

c)  $f(z) = @Q2c - a@|z|^2 + @Q2c - b@z - @Q2c - c@\bar{z}$

d)  $f(z) = \frac{@Q2d - k@}{z + @Q2d - a@ - @Q2d - b@i}$

e)  $f(z) = @Q2e - a@z^2 e^{@Q2e - b@z}$

3. Show that the given function  $U$  (or  $V$ ) is harmonic. Determine the harmonic conjugate  $V$  (or  $U$ ) such that  $\mathbf{U+iV}$  becomes analytic. **5×10=50**

a) Given  $V = @Q3a - k@ \ln ((x - @Q3a - a@)^2 + (y - @Q3a - b@)^2)$ , show that  $V$  is harmonic and find  $U$ .

b) Given  $U = @Q3b - 3a@x^2y - @Q3b - b@x^2 - @Q3b - a@y^3 + @Q3b - b@y^2$ , show that  $U$  is harmonic and find  $V$ .

c) Given  $V = @Q3c - p@e^{-@Q3c - a@x} \cos (@Q3c - a@y) - @Q3c - q@e^{@Q3c - b@y} \sin (@Q3c - b@x)$ , show that  $V$  is harmonic and find  $U$ .

d) Given  $U = @Q3d - k@ \sin (@Q3d - a@x) \cosh (@Q3d - a@y)$ , show that  $U$  is harmonic and find  $V$ .

e) Given  $V = @Q3e - a@xe^{-@Q3e - b@x} \cos (@Q3e - b@y) + @Q3e - a@ye^{-@Q3e - b@x} \sin (@Q3e - b@y)$ , show that  $V$  is harmonic and find  $U$ .