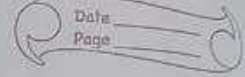


PR. 2 Expectation Decider



Q1. what is probability?

⇒ probability is a measure of how likely an event is to occur expressed as a number between 0 and 1 (or 0% to 100%)

Formula:

$$P(\text{event}) = \frac{\text{number of favorable outcomes}}{\text{total number of possible outcomes}}$$

Q2. key probability Terminology.

⇒ 1) experiment:- A process or action whose outcome is uncertain (e.g. selecting a student)

2) ~~outcome~~ outcome:-

2) sample space:- the set of all possible outcomes of an experiment (e.g. the set of all 200 students)

3) event:- A subset of the sample space (e.g. the event that a student passed the exam)

4) mutually Exclusive event:- events that cannot occur at the same time

5) independent Events:- Events where the occurrence of one does not affect the probability of the other

Q3. Give at least three probability event? Examples from the dataset?

1) probability of passing the exam

$$\text{probability} = \frac{104}{200} = 0.52$$

2) probability of High Attendance:

$$\text{probability} = \frac{85}{200} = 0.425$$

Attendance Above ~~80~~ 80%

3) probability of high study Hours:

$$\text{probability} = \frac{\text{Study Hours}}{\text{Sample Space}}$$

Study Hours more than 20 hours :- 71

$$\text{probability} = \frac{71}{200} = 0.355$$

Q4. Types of probability

1) Empirical probability :- Empirical probability is the calculated based on actual observations or experiments, not theory.

Formula

$$\text{Empirical probability} = \frac{\text{All pass student}}{\text{sample space}}$$

All pass student = 104
Sample space = 200

$$\text{empirical probability} = \frac{104}{200} = 0.52$$

empirical probability is 0.52

2) Theoretical probability :- Theoretical probability is based on reasoning about the possible outcomes of an event assuming they are equally likely.

~~theori~~ theoretical probability of getting a heads on a single coin toss.

$$\text{Theoretical probability} = 0.5$$

Q 5) Random variable and probability distribution

1) Define a random variable for the event "Number of students passing the 'final exam' out of 3 randomly selected student".

- * A list of student is created with their pass/fail status.
- * From that list, we first filter only those students who passed the exam.
- * Then we use random sample(s) to randomly select 5 students from the pass group.

* Finally, we print the name of the 5 randomly selected passed students.

2) mean and variance.

n = total number of ~~selected~~ randomly selected student.

p = probability of randomly selected student of passing.

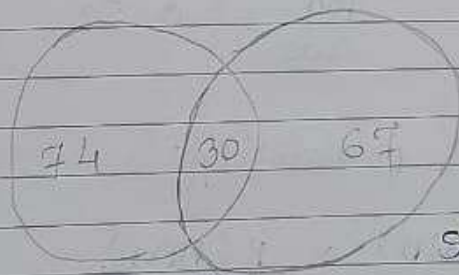
$$\text{mean} = n \times p$$

$$\text{variance} = n \times p \times (1 - p)$$

Q6 Venn diagram in probability.

Student pass the exam = 104

Student participates in group discussions = 97



Student pass the exam

Student participates in group discussion.

Q7 probability calculations:

1) Joint probability of participates in group discussion and pass exam.

$$\text{Joint probability} = P(A \text{ and } B)$$

$$\text{Joint probability} = (48.5 \text{ and } 52)$$

$$\frac{97}{200} = 0.485 \quad \frac{104}{200} = 0.52$$

2) marginal probability of "pass exam"

$$P(\text{Pass exam}) = 52$$

$$\frac{104}{200} = 0.52$$

3) conditional probability of pass exam given participation in group discussion.

$$P(A|B) = \frac{P(A \cap B)}{P(B)}$$

number of students with high study Hours = 71

number of students ~~with~~ who passed and had High study Hours = 68

$$P(A|B) = \frac{\cancel{51}}{\cancel{68}} = \frac{68}{71} \approx 0.9577$$

conclusion

The analysis of the synthetic student dataset provides valuable insight for the "Expectation Decider" model. Key findings include:

- * The overall passing rate in the sample is 52%.
- * Study hours show the strongest ~~cor~~ correlation with passing, with a conditional probability of 95.77% for students with high study hours.
- * Group discussion participation is dependent event with passing suggesting it is a beneficial factor.
- * A Venn diagram is a useful tool to understand the relationship between students who passed the exam and those who participated in the group discussion
 - 1) student who only pass = 74
 - 2) student who only participated = 67
 - 3) students who did both = 30
- * This insights confirm that study hours attendance and group discussion participation are all statically significant factors that should be heavily weighted in the final predictive model