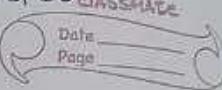


PR. 2 Expectation Decider



Q1 what is probability?

→ Probability is a measure of how likely an event is to occur expressed as a number between 0 and 1 (or 0% to 100%)

Formula:

$$P(\text{event}) = \frac{\text{number of favorable outcomes}}{\text{Total number of possible outcomes}}$$

Q2. Key probability Terminology.

→ Experiment :- A process or action whose outcome is uncertain (e.g. selecting a student)

2) outcome :-

3) sample space :- the set of all possible outcomes of an experiment (e.g. the set of all 200 students)

4) event :- A subset of the sample space (e.g. the event that a student passed the exam)

4) mutually Exclusive events :- events that cannot occur at the same time

5) independent Events :- Events where the occurrence of one does not affect the probability of the other

- Q3. Give at least three probability events examples from the dataset?
- ⇒ 1) Probability of passing the exam

$$\text{Probability} = \frac{104}{200} = 0.52$$

- 2) Probability of High Attendance:

$$\text{Probability} = \frac{85}{200} = 0.425$$

Attendance Above ~~80~~ 80 %

- 3) Probability of high study hours:

$$\text{Probability} = \frac{\text{Study Hours}}{\text{Sample Space}}$$

Study hours more than 20 hours :- 71

$$\text{Probability} = \frac{71}{200} = 0.355$$

- Q4. Types of probability

⇒ Empirical probability : Empirical probability is the calculated based on actual observations or experiments, not theory

Formula

$$\text{Empirical probability} = \frac{\text{All pass student}}{\text{Sample Space}}$$

All pass student = 104
Sample space = 200

$$\text{empirical probability} = \frac{104}{200} = 0.52$$

empirical probability is 0.52

2) Theoretical probability :- Theoretical probability is based on reasoning about the possible outcomes of an event assuming they are equally likely.

Theoretical probability of getting a heads on a single coin toss.

$$\text{Theoretical probability} = 0.5$$

Q5) Random variable and probability distribution

→ Define a random variable for the event Number of students passing the "final exam out of 3 randomly selected student".

* A list of student is created with their pass/fail status.

* From that list, we first filter only those students who passed the exam.

* Then we use random sample(s) to randomly select 5 students from the pass group.

* Finally, we print the name of the 5 randomly selected passed students.

ii) mean and variance.

n = total number of selected of randomly Selected Student.

p = probability of randomly selected student of passing.

$$\text{mean} = n \times p.$$

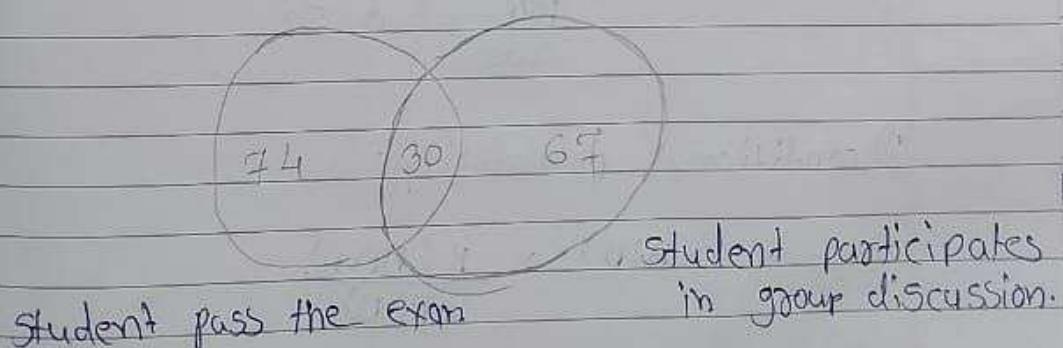
mean

$$\text{variance} = n \times p \times (1 - p)$$

Q6 Venn diagram in probability.

student pass the exam = 104

student participates in group discussions = 97



Q7 probability calculations:

b) joint probability of participates in group discussion and pass exam.

$$\text{Joint probability} = P(A \text{ and } B)$$

$$\begin{aligned}\text{Joint probability} &= (48.5 \text{ and } 52) \\ \frac{97}{200} &= 0.485 \quad \frac{104}{200} = 0.52\end{aligned}$$

c) marginal probability of "pass exam"

$$P(\text{Pass exam}) = 52$$

$$\frac{104}{200} = 0.52$$

d) conditional probability of pass exam given participation in group discussion.

$$P(A|B) = \frac{P(A \cap B)}{P(B)}$$

number of students with high study hours = 71

number of students who passed and had high study hours = 68

$$P(A|B) = \frac{\cancel{68}}{\cancel{71}} = \frac{68}{71} \approx 0.9591$$

Conclusion

The analysis of the synthetic student dataset provides valuable insight for the "Expectation Decider" model. Key finding include:

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- * The overall passing rate in the sample is 52%.
- * Study hours show the strongest ~~core~~ correlation with passing, with a conditional probability of 95.77% for students with high study hours.
- * Group discussion participation is dependent event with passing suggesting it is a beneficial factor.
- * A Venn diagram is a useful tool to understand the relationship between students who passed the exam and those who participated in the group discussion.
 - 1) Student who only pass = 74
 - 2) Student who only participated = 67
 - 3) Students who did both = 30
- * This insights confirm that study hours attendance and group discussion participation are all statistically significant factors that should be heavily weighted in the final predictive model.