

Lab Assignment 8 (2022)

PH-566

1. According to Lanczos algorithm for nonlinear lattice, the Green function matrix element is defined as

$$G_{ii}(z) = \frac{b_1^2}{z - a_1 - \frac{b_2^2}{z - a_2 - \frac{b_3^2}{z - a_3 - \frac{b_4^2}{\ddots \frac{b_N^2}{z - a_N - b_{N+1}^2 T(z)}}}}}$$

where a_i 's, b_i 's are real numbers and z is a complex variable ($z=E+i\delta$; E is the energy). $T(z)$, which serves the purpose of terminating the continued fraction, is defined as

$$T(z) = \frac{z - a_N - \sqrt{(z - a_N)^2 - 4b_{N+1}^2}}{2b_{N+1}^2}$$

Using do-loop statement, write a code to calculate the above-mentioned Green function in the energy range $E = (-10, 10)$ in steps of 0.01 (don't worry about units) taking the imaginary part of E , i.e. $\delta = 0.001$.

Take the values of a_i and b_i from the supplied data file named "data.txt" (They are arranged in a given row as i , $a(i)$, $b(i+1)$; highest i represents termination of the continued fraction (i.e. $(i)_{\max}=N$). Also, consider $b(1)=1.0$)

Hence, calculate the basis-projected density of states $n_i(E)$, defined as

$$n_i(E) = -\frac{1}{\pi} \Im m[G_{ii}(z)]$$

Print E vs. $n(E)$ in a data file named "DOS.dat". Hence, plot this data in gnuplot.